TROPHIC CLASSIFICATION OF LAKES USING LANDSAT-1 (ERTS-1) MULTISPECTRAL SCANNER DATA



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TROPHIC CLASSIFICATION OF LAKES USING LANDSAT-1 (ERTS-1) MULTISPECTRAL SCANNER DATA

Ву

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PREFACE

In this report the satellite under scrutiny is referred to as LANDSAT-1, an acronym for Land Satellite One. It was the first space observatory launched under the National Aeronautics and Space Administration's Earth Resources Technology Satellite Program and originally carried the designation Earth Resources Technology Satellite One (ERTS-1). The series name change was accomplished with the launch of ERTS-2 (<u>i.e.</u>, LANDSAT-2) in January 1975.

Both LANDSAT-1 and LANDSAT-2 are still operational at this point in time (November 1975). The third satellite of the series, LANDSAT-3, is tentatively scheduled for launch in February 1977. While this report was of necessity limited to LANDSAT-1, the successful launch of LANDSAT-2, the decision to proceed with LANDSAT-3, and the forthcoming Space Shuttle Program will provide many opportunities to further define the role of orbital-level remote sensors in surveying the earth's lacustrine resource.

ABSTRACT

This study evaluates the Earth Resources Technology Satellite One (ERTS-1; <u>i.e.</u>, LANDSAT-1) multispectral scanner (MSS) as a means of estimating lacustrine trophic state and the magnitude of two trophic state indicators.

Numerical classificatory methods are employed to ascertain the trophic character of 100 lakes in Minnesota, Wisconsin, Michigan, and New York using the trophic indicators: chlorophyll a, total organic nitrogen, inverse of Secchi disc transparency, conductivity, total phosphorus, and an algal assay yield. A complete linkage clustering algorithm is first used to examine the lakes for natural clusters. The resultant clusters are not readily interpretable in terms of the three classic states of trophy (oligotrophic, mesotrophic, eutrophic). The hyper-dimensional cloud of data points is then reduced in dimensionality through the ordination technique of principal components analysis. A multivariate trophic state index (PCI) is derived from the principal component analysis.

A binary masking technique is used to extract lake-related MSS data from computer-compatible tapes. Data products are in the form of descriptive statistics and photographic concatenations of lake images.

MSS color ratio regression models are developed which are of practical value for estimating lake Secchi disc transparency and chlorophyll a levels for one date of LANDSAT-1 coverage. The trophic state of lakes, as defined by lake position on the first principal component axis (PC1 value), is predicted using MSS color ratio regression models. Each date of LANDSAT-1 coverage has its unique regression models for the prediction of the trophic indicators and the trophic index; the models for different dates vary greatly in their practical applicability.

The mean infrared-one band intensity levels for several "hypereutrophic" lakes exceed their mean red band intensity levels and effectively isolate them from other lakes in three-dimensional MSS color models.

A Bayes Maximum Likelihood Multispectral Classifier is employed to classify a group of Wisconsin lakes using MSS colors in conjunction with the lakes' trophic state index values. The results are depicted in the form of both gray-scale and color-coded photographic concatenations.

The utility of the LANDSAT-1 MSS is most apparent when the seasonal contrasts between lakes at different points on the trophic scale are at a maximum. Periods of excessive cloud cover, frames with faulty or missing MSS data, and the need for some ground truth, impair, but do not preclude its use in lake monitoring and classification. The use of computer-compatible tapes in conjunction with digital image processing techniques is essential if the maximum benefits are to be derived from the LANDSAT-1 MSS in lake-orientated studies.

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SECTION I

CONCLUSIONS

Based on the ground truth and the multispectral scanner frames selected for analysis, the image extraction and enhancement techniques and data reduction methods employed, it is concluded that:

- The LANDSAT-1 MSS is an effective tool for lake enumeration and for the estimation of lake surface area.
- 2. Estimates of lake Secchi disc transparency and chlorophyll a levels having practical significance can be achieved through the incorporation of lake MSS color ratios in regression models. Each trophic indicator has a model which is unique to the specific date of LANDSAT-1 coverage.
- 3. MSS color ratios can be used to estimate lake position on a multivariate trophic scale. However, each date of LANDSAT-I coverage has its unique model. The models for different dates vary greatly in their predictive capabilities. The standard error of the models tends to decrease as the growing season progresses and the manifestations of eutrophication become more evident.
- 4. While information relating to lacustrine trophic state can be extracted from LANDSAT-1 MSS imagery, either by visual inspection or through microdensitometry and optical density slicing, the maximum benefits in water-based studies can be derived only through the use of the digital data contained on the computer-compatible tapes in conjunction with automatic image processing techniques.
- 5. Although LANDSAT-1 provides 18-day repetitive coverage, systematic times-series are difficult, if not impossible, to obtain due to excessive cloud cover on many dates of satellite coverage.
- 6. The LANDSAT-1 MSS has utility as a supplemental data source in lake survey and monitoring programs. Its value is most apparent in situations involving large lakes and/or large numbers of lakes.

SECTION II

RECOMMENDATIONS

In January 1975, NASA inserted its second Earth Resources Technology Satellite (ERTS-2, i.e., LANDSAT-2) into a sun-synchronous near-polar orbit. The orbital parameters of LANDSAT-2 and its still operational predecessor, LANDSAT-1, have resulted in 9-day repetitive coverage. The tandem combination of satellites has effectively doubled the amount of imagery and digital data available to investigators. The increased coverage should be of great value in lake monitoring and survey programs. Lakes are by their very nature dynamic and the more frequent satellite coverage should increase the accuracy of the trophic state estimates.

NASA has been authorized to launch a third Earth Resources Technology Satellite (ERTS-3, i.e., LANDSAT-3) into orbit; the tentative launch date is February 1977. The instrumentation will include an improved multispectral scanner having greater spatial resolution and capabilities in the thermal region of the spectrum. It is anticipated that the improvements will increase the utility of the satellite-borne sensor as a means of classifying lakes.

As of September 1975, the LANDSAT series of earth resources satellites has amassed an inventory numbering in excess of 150,000 frames (scenes) of the United States. The collection is expanding at an average rate of about 190 frames per day. It is maintained by the EROS Data Center at Sioux Falls, South Dakota.

A magnetic tape library has been established at JPL's Image Processing Laboratory for the lakes examined during the course of this investigation. The lake images have been extracted from their terrestrial matrix and are readily available for additional statistical analyses using automatic digital image processing techniques. The enlargement of this library through continued acquisition of MSS data for NES-sampled lakes will give researchers the opportunity to study long-term changes in the lakes.

In light of the preceding information and the conclusions drawn from this investigation, it is recommended that additional effort be expended to refine the predictive capabilities of the LANDSAT MSS. Several problem areas which merit additional consideration have been identified.

The development of a more representative trophic state index may well be in order. Although automatic data processing techniques (such as cluster analysis) have a role in the classification of lakes, the kinds and number of trophic indicators, the types of data transformations, and the methodologies employed can produce significant differences in the

resulting classifications, Very little work has been done in this area using the techniques commonly employed in numerical taxonomy. ADP techniques are well suited for the reduction of the large data masses generated by lake survey programs.

Although atmospheric and solar angle effects were disregarded, it is apparent that they can degrade the lake color signal received by the multispectral scanner. The development of radiometric calibration techniques to account for the peripheral effects would greatly increase the utility of the MSS. An increase in instrument gain (this is possible in the RED and GRN bands) would aid the water-based investigator, possibly at the expense of terrestrial studies.

The need exists to study in greater detail the relationships between the magnitude of trophic state indicators and MSS data under both laboratory and field conditions. This study suffered in part from the lack of concurrent data; it is imperative that concurrent satellite-ground truth sampling be conducted to further elucidate the relationships.

Bottom effects were assumed to be insignificant in this study because Secchi disc transparency was much less than water depth. However, in some lakes the bottom can be seen by the sensor. A better knowledge of bottom effects may be of value in refining the predictive capabilities of the MSS in the aquatic environment.

With the exception of some lakes in the New York frames, the remote sensing aspects of this investigation have been heavily weighted with lakes that are often referred to as "eutrophic". The need exists to examine more lakes, particularly those possessing high water quality. The sensitivity limits of the MSS have yet to be established for trophic state indicators as well as the trophic state index. The examination of lakes from other geographic regions should be undertaken to determine whether the relationships found in the study area extend to other regions.

SECTION III

INTRODUCTION

Homo sapiens has developed the burgeoning population and the technological level necessary to effect significant alterations in the biosphere. His impact on environment is accelerating in variety, magnitude, and geographic extent. He has failed, either through gross ignorance or a lack of concern, to give adequate consideration to the interrelatedness of the biotic and abiotic elements which compose the environment. Man-induced environmental alterations generally result in a chain of consequences, both direct and indirect, short-term and long-term, and varying in magnitude. Many of the consequences (e.g., air pollution, water pollution) adversely affect his health, his economic well-being, and the pristine qualities of environment.

Man's strategies for using the earth's lacustrine resources have usually been predicated on immediate short-term economic gains with little consideration of long range environmental ramifications. It is becoming increasingly apparent that man has adversely affected many lakes, particularly those located in countries with large population densities and/or which are technologically advanced. The United States of America can serve as a prime example.

STATEMENT OF PURPOSE

Rational management of the lacustrine resource dictates, as the first step, an assessment of each lentic body's trophic status. Data collection for the determination of trophic status is a costly, time-consuming process, especially when thousands of lakes are to be evaluated. The need exists to find a means of rapidly assessing the trophic state of water bodies which would make it economically feasible to operate extensive systematic surveillance programs. Stewart and Rohlich (1967) have urged investigators to develop remote sensing techniques and evaluate their potential for eutrophication surveillance.

Satellite-borne sensors show promise as a means of monitoring and classifying lakes and reservoirs. The successful orbiting of the Earth Resources Techology Satellite (ERTS-1; <u>i.e.</u>, LANDSAT-1) affords the opportunity to investigate the potential of one type of satellite-borne sensor.

The purpose of this report is the evaluation of LANDSAT-1 remotely sensed multispectral scanner data as a means of determining the

trophic state of a selected group of lakes located in the northern part of the conterminous United States. Specific objectives include: the development and application of a multivariate trophic ranking system to a selected group of lakes; the formulation of empirical models for the estimation of selected trophic state indicators; and the development of empirical models for the prediction of lacustrine trophic state using LANDSAT-1 data.

FORMAT OF REPORT

The remainder of this section is devoted to a description of the Earth Resources Technology Satellite, its orbital characteristics, instrumentation, and products. In addition, the study area is described along with the criteria used in the selection of the lakes and the techniques used in the collection of the ground ($\underline{i} \cdot \underline{e} \cdot$, water) truth.

Section IV discusses lakes as natural resources, the concept of eutrophication, trophic state indicators, and demonstrates the use of multivariate techniques in the classification of a large group of lakes on the basis of selected ground truth parameters.

Section V is devoted to a detailed description of the methodology used in the extraction and transformation of LANDSAT-1 multispectral scanner (MSS) data into forms and products which can then be used in the study of hypothesized ground truth-MSS data relationships.

Correlations between lake parameters (surface area, chlorophyll \underline{a} , Secchi disc transparency) and MSS data are explored in Section VI. Regression models are developed to predict the magnitude of selected trophic state indicators.

Section VII includes the prediction of lake trophic state using MSS color ratios in regression models. Three-dimensional models are used to illustrate qualitative differences among the lakes on the basis of MSS color ratios. An automatic image processing technique is employed to generate enhanced photographic products depicting the trophic state of selected lakes.

Section VIII is devoted to a brief discussion and summation of the potential applications and limitations of the LANDSAT-1 MSS in lake monitoring and classification.

THE EARTH RESOURCES TECHNOLOGY SATELLITE

The Earth Resources Technology Satellite Program, under the sponsorship of the National Aeronautics and Space Administration, is a concerted effort to merge space and remote sensing technologies into a system which will demonstrate techniques for efficient management of the earth's natural resources. To explore the feasibility of applying earth resource data collected from satellite altitudes to resource

management problems, NASA inserted an experimental satellite (ERTS-A) into a circular earth orbit. Another satellite (ERTS-B) is scheduled for launch when ERTS-A, officially designated ERTS-1 (i.e., LANDSAT-1) ceases to function. Detailed information regarding the Earth Resources Technology Program is found in the <u>Data Users Handbook</u> (NASA, 1972).

ERTS-1 Orbit Parameters and Earth Coverage

LANDSAT-1 was placed into a nominal sun-synchronous near-polar orbit by a Delta launch vehicle on 23 July 1972 (Freden, 1973). Orbital parameters are listed in Table 1.

TABLE 1. LANDSAT-1 ORBITAL PARAMETERS^a

Orbit Parameter	Actual Orbit
Semi-major axis	7285.82 kilometers
Inclination	99.114 degrees
Period	103.267 minutes
Eccentricity	0.0006
Time at descending node (southbound equatorial crossing)	9:42 a.m.
Coverage cycle duration	18 days (251 revolutions)
Distance between adjacent ground tracks (at equator)	159.38 kilometers

^aAdapted from <u>Data Users Handbook</u> (NASA, 1972).

The earth coverage pattern is shown in Figure 1 for two orbits on two consecutive days. Orbital parameters result in a 1.43 degree westward migration of the daily coverage swath, equivalent to a distance of 159 kilometers at the equator. The westward progression of the satellite revolutions continues, exposing all of the area between orbit N and orbit N+1 to the satellite sensors by day M. This constitutes one complete coverage cycle and consists of 251 revolutions. The cycle takes exactly 18 days and results in total global coverage between 81°N and 81°S latitude. Fourteen orbits (i.e., revolutions) are completed during each of 17 days in a cycle with 13 revolutions during one day (NASA, 1972). Approximately 188 scenes are acquired on an average day (Nordberg, 1972).

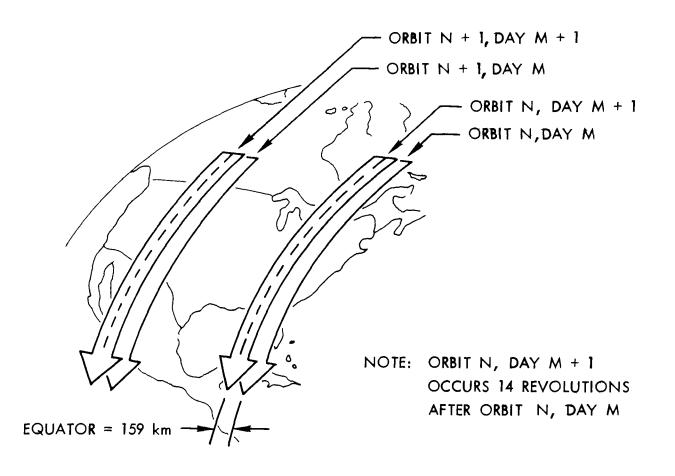


Figure 1. LANDSAT-1 ground coverage pattern. Adapted from Data Users Handbook (NASA, 1972).

LANDSAT-1 Instrumentation

The LANDSAT-1 payload consists of a Return Beam Vidicon (RBV) Camera Subsystem, a Multispectral Scanner Subsystem (MSS), and a Data Collection System (DCS). The RBV and MSS are designed to provide multispectral imagery of the earth beneath the observatory (i.e., satellite). A malfunction occurred on 6 August 1972 (orbit 198) in the RBV power switching circuit and the RBV cameras were turned off as only one sensor system can be used in conjunction with the one functioning video tape recorder. The second recorder aboard the observatory malfunctioned between orbits 148 and 181 (Freden, 1973). The DCS serves to relay environmental information from geographically remote ground-based sensors to LANDSAT ground stations for processing and delivery to users. The RBV and DCS aspects of the satellite need not concern us.

The MSS is a line-scanning radiometer which collects data by creating images of the earth's surface in four spectral bands simultaneously through the same optical system. The instrument operates in the solar-reflected spectral band region from 500 to 1,100 nanometers. Scanner characteristics are listed in Table 2. The MSS scans cross-track swaths 185 kilometers in width, simultaneously imaging six scan lines for each of the four bands. The object plane is scanned by an oscillating flat mirror positioned between the scene and a double reflector telescopetype of optical chain. An 11.5 degree (Horan, Schwartz, and Love, 1974) cross-track field of view is produced by the mirror oscillating ±2.89 degrees about its nominal position (Figure 2).

A nominal orbital velocity of 6.47 kilometers per second, neglecting observatory perturbations and earth rotation effects, produces the requisite along-track scan. The subsatellite point moves 474 meters along the track during the 73.42 millisecond active scan-retrace cycle which is itself a consequence of the 13.62 hz mirror oscillation rate. The track distance of 474 meters synchronizes with the 474 meter along-track field of view of each set of six detectors. The line scanned by the first detector in one cycle of the active scan is in juxtaposition to the line scanned by the sixth detector of the previous scan (Figure 3).

Twenty-four glass optical fibers, arranged in a four by six (4x6) matrix in the focused area of the telescope, intercept the light from the earth scene. Light impinging on the square input end of each optical fiber is conducted to an individual detector through an optical filter unique to the respective spectral band under consideration. Photomultiplier tubes (PMT) serve as detectors for Bands Four through Six; Band Seven uses silicon photodiodes. A video signal is produced at the scanner electronics output as the image of a line across the swath is swept across the fiber during active scan. The signal is sampled at 9.95 microsecond (µsec) intervals which correspond to a 56 meter crosstrack motion of the instantaneous field of view. The sampled signal is digitized and arranged into a serial digit data stream for transmission

TABLE 2. LANDSAT-1 MSS CHARACTERISTICS^a

Item	Characteristics		
Telescope optics	22 cm (aperture diameter), f/3.6 Ritchey-Chretien		
Scanning method	Flat mirror oscillating ± 2.9 degrees at 13.62 Hz		
Scan (Swath) width	11.5 degrees (185 kilometers at 917 kilometers altitude)		
Scan duty cycle	44%		
Instantaneous field of view (IFOV)	86 microradians		
Number of bands	Four		
Number of lines (detectors) scanned per band	Six		
Limiting ground resolution from 917 kilometers altitude	40 meters		
Spectral band wavelength: NDPF Band Code Band 4 (Green) Band 5 (Red) Band 6 (Near-infrared One) Band 7 (Near-infrared Two)	500-600 nanometers 600-700 nanometers 700-800 nanometers 800-1,100 nanometers		
Sensor response: Detector Nominal input for 4 V Scanner Output (10 ⁻⁴ W cm ⁻² sr ⁻¹)	Band 4 Band 5 Band 6 Band 7 PMT PMT Photodiode 24.8 20.0 17.6 46.0		
Scanner and multiplexer weight	50 kilograms		
Signal channels	24		
Telemetry channels	97		
Command capability	72		
Scanner size	Approximately 36 x 38 x 89 cm		

^aAdapted from Horan, <u>et al</u>. (1974). photomultiplier tube.

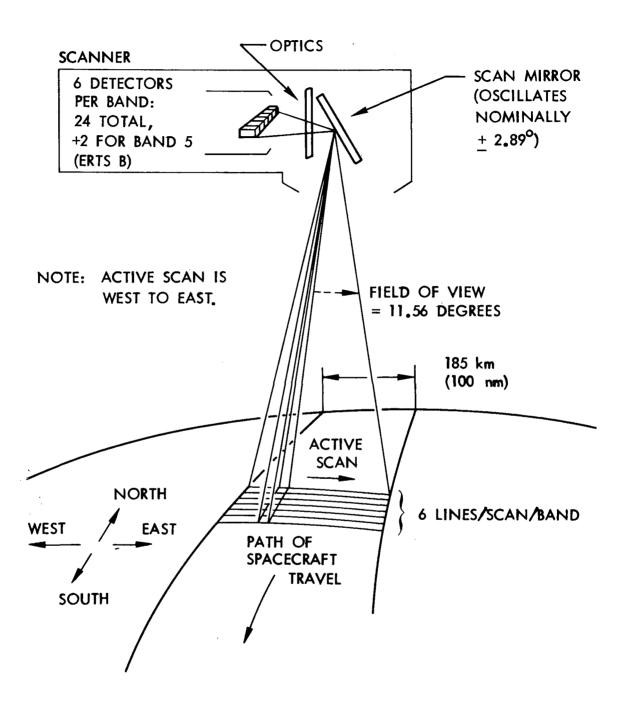


Figure 2. Schematic diagram of the LANDSAT-1 MSS scanning arrangement. Adapted from the <u>Data Users Handbook</u> (NASA, 1972).

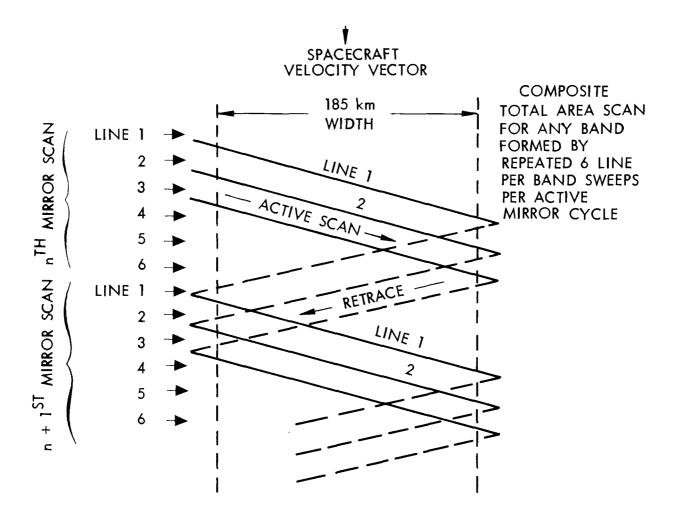


Figure 3. Ground scan pattern for a single MSS detector. Adapted from the <u>Data Users Handbook</u> (NASA, 1972).

to ground stations. Individual signals are derived from light passing through each fiber, resulting in 24 channels of output.

LANDSAT-1 Products

The electronic signals from the observatory's MSS are converted into photographic and computer products at the Goddard Space Flight Center, Greenbelt, Maryland. Third and fourth generation photographic products are available in the form of prints, positive and negative transparencies, and come in several scales including: 1:3,369,000; 1:1,000,000; 1:500,000; and 1:250,000 with the transparencies being limited to the two smaller scales. Color products are available for a relatively small number of scenes. Computer-compatible magnetic digital tapes (CCT's) may be requested in either a 7-track or a 9-track format. Four CCT's are required for the MSS data corresponding to one scene.

Copies of the CCT's and the photographic products are placed in the public domain at the Department of the Interior's Earth Resources Observations Systems (EROS) Data Center located in Sioux Falls, South Dakota.

LANDSAT-1 Lake Monitoring Potential

The advantages of using remote sensing imagery systems are threefold: they afford an overall (synoptic) view, they can give a time record, and they expand the spectral limits of the human eye (Scherz, et al., 1969; Scherz, 1971a; Scherz, 1971b). Multispectral satellite-borne imagery systems show promise as a means of monitoring and classifying the earth's lacustrine resources. This is partially due to the repetitive nature of a satellite and the tremendous synoptic view offered from orbital altitudes.

Visual examination of select frames of LANDSAT-1 MSS imagery from Wisconsin, Minnesota, and Florida suggest that good correlations may exist between the trophic status of lakes and their tonal characteristics. MSS Frame 1017-16093, recorded at an altitude of approximately 917 kilometers over southeastern Wisconsin and northeastern Illinois on 9 August 1972, will serve to illustrate this point.

Figure 4 is a reproduction of an EROS Data Center photograph of the scene as recorded in the near-infrared (IR2; 800 to 1,100 nanometers) spectral band. Water bodies, including the larger streams, stand out boldly against the lighter tones of the land features. The labelled lakes, excluding Lake Michigan, were sampled by the U.S. Environmental Protection Agency's National Eutrophication Survey (NES) during the 1972 open water season. Gray tone differences are not evident among the lakes nor are tonal patterns visible on any of the lakes. IR2 is, however, a good spectral band for the location and demarcation of water bodies. Some caution is necessary when conducting a lake enumeration

on the photograph because some of the "lakes" are in reality shadows cast by cumulus clouds.

Figure 5 is the same scene recorded in near-infrared one (IR1; 700 to 800 nanometers). Tonal differences are apparent, at least in the original photographic print, among the lakes, and patterns are evident on some of the lakes ($\underline{e}.\underline{g}$., Lake Koshkonong). Lakes are readily located and their boundaries delimited in this band.

Figure 6 is a red light (RED; 600 to 700 nanometers) MSS photograph of the scene. Marked gray tone differences are apparent among the lakes. Lakes commonly recognized as eutrophic (e.g., Lake Como) tend to appear light in tone and meld in with the land features. Lakes with relatively good water quality (e.g., Lake Geneva) are characterized by darker tones. Lotic bodies are not readily apparent in the photograph.

The green light (GRN; 500 to 600 nanometers) sensed by the MSS was used to construct the Figure 7 photograph. Although the lakes are difficult to discern, a result of low contrast among the scene elements, differences among the lakes can be detected with the unaided eye.

It is apparent, from the visual examination of LANDSAT-1 MSS Frame 1017-16093 and other frames from several additional states, that the satellite-borne multispectral scanner is collecting data which may be of value in the classification and monitoring of lentic bodies. The results of the examination suggest that GRN, RED, and IR1 contain most of the information relative to trophic status assessment.

DESCRIPTION OF THE STUDY AREA

Many current efforts to determine the feasibility of using LANDSAT-1 MSS data in water quality monitoring tend to be intensive in nature, near-real time, and oriented toward the dymanics of pollution or eutrophication (e.g., Chase and Smith, 1973; Lind and Henson, 1973; Lind, 1973). The investigations are very limited in geographic scope, typically involving fewer than six water bodies.

Another approach, the one used in this report, involves the examination of a relatively large number of lakes over a more extensive geographic area. Although it is not uncommon to find lakes of different trophic state within the same lake region (e.g., Southeastern Lake District of Wisconsin), the selection of a larger study area affords the opportunity to include lakes exhibiting a greater trophic range. In addition, assuming that lakes have characteristic multispectral signatures at particular points on the trophic scale, the use of a larger and more diverse lake population permits a more extensive evaluation of the LANDSAT-1 MSS's capabilities in the realm of lake monitoring and classification.

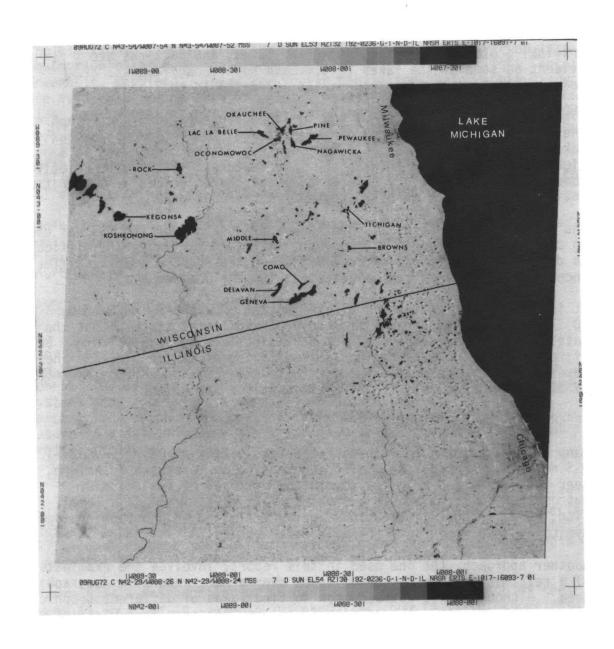


Figure 4. Reproduction of an EROS Data Center IR2 print of Frame 1017-16093 (9 August 1972). Water bodies stand out in stark contrast to the lighter-toned land features. The labelled lakes, excluding Lake Michigan, were sampled by the National Eutrophication Survey during 1972. The reproduction, originally printed at a scale of 1:1,000,000, has a scale of approximately 1:1,415,000.



Figure 5. Reproduction of EROS IR1 print of Frame 1017-16093 (9 August 1972). Surface patterns are evident on some of the lakes (e.g., Lake Koshkonong). Each edge of the picture is equivalent to a ground distance of approximately 185 kilometers. The reproduction is printed at a scale approximating 1:1,415,000.



Figure 6. Reproduction of EROS RED (MSS Band 5) print of Frame 1017-16093 (9 August 1972). Variations in gray tone are readily apparent among the lakes and suggest differences in water quality. Lake Geneva, characterized by relatively high water quality, is dark in tone compared with, for example, eutrophic Lake Koshkonong. The small ball-like white objects between Milwaukee and Chicago are cumulus clouds. The reproduction is printed at a scale of approximately 1:1,415,-000.

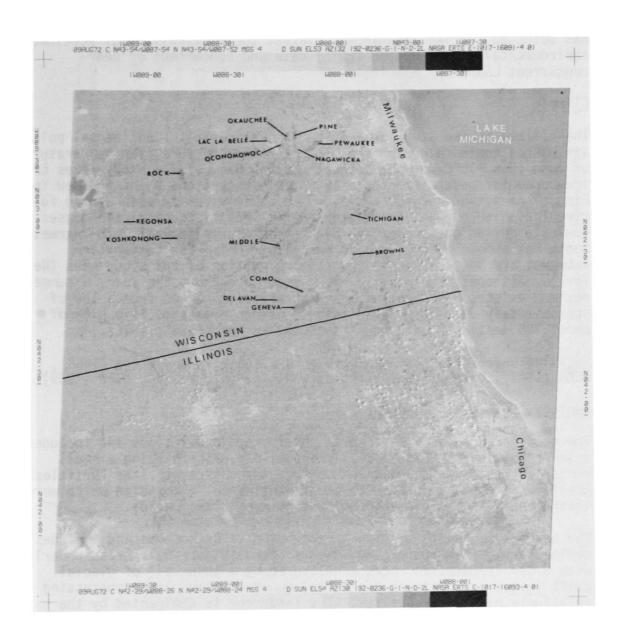


Figure 7. Reproduction of EROS GRN (MSS Band 4) print of Frame 1017-16093 (9 August 1972). Scenes recorded in the green band generally lack contrast, but contain information useful in monitoring earth resources. The reproduction is printed at a scale of 1:1,415,000.

Geographic Area

The geographic area serving as a matrix for the study lakes comprises the states of Minnesota, Wisconsin, Michigan, and New York. The area was selected for its abundance of lakes, the availability of pertinent environmental (i.e., ground truth) data and concurrent or near-concurrent LANDSAT-1 MSS frames.

Climate

The climate of the study area is humid continental. Continental polar air masses dominate during the winter, resulting in a mean temperature of less than -10°C for the coldest month. Most of the study lakes are ice-bound for several months, two notable exceptions being the New York Finger Lakes, Seneca and Cayuga, which usually remain open and in full circulation throughout the winter (Berg, 1963). Tropical air masses dominate during the summer and high temperatures prevail. The warmest month has a mean temperature in excess of 18°C. The temperature extremes are less severe in the eastern portion of the study area (New York). Although precipitation is common throughout the year, a summer maximum exists. The mean annual precipitation ranges from a low of approximately 50 centimeters in northwestern Minnesota to a high of about 125 centimeters in north central New York (USGS, 1970).

Detailed descriptions of the climate are found in Trewartha (1968), USDA (1941), Visher (1954), Thornthwaite (1948), and Strahler (1969).

Geology, Soils, and Land Use

The study area extends over three physiographic divisions and includes seven subdivisions (Figure 8). The entire area, excluding a small region in western Wisconsin and southeastern Minnesota (the "Driftless Area"), was exposed to the forces of continental glaciation which were instrumental in the formation of the numerous lake basins.

The bedrock ranges in age from Precambrian to Cretaceous and includes sedimentary, metamorphic, and igneous rocks (Figure 9). Areas underlain with older Precambrian rocks and covered by a thin veil of glacial drift (e.g., northeastern Minnesota) generally have lakes possessing relatively high water quality. The landscape is dominanted by the members of six soil orders (7th Approximation) including Alfisols, Entisols, Histosols, Inceptisols, Mollisols, and Spodosols (Figure 10). Major types of land use are shown in Figure 11. Lakes seriously modified by man are generally found in areas where land use is chiefly agricultural in nature, particularly as cropland.

Lake Selection Criteria and Location

Most of the lakes incorporated into this study were selected from some 220 lakes sampled in 1972 by the U.S. Environmental Protection Agency's (EPA) National Eutrophication Survey (NES). The lakes were selected,

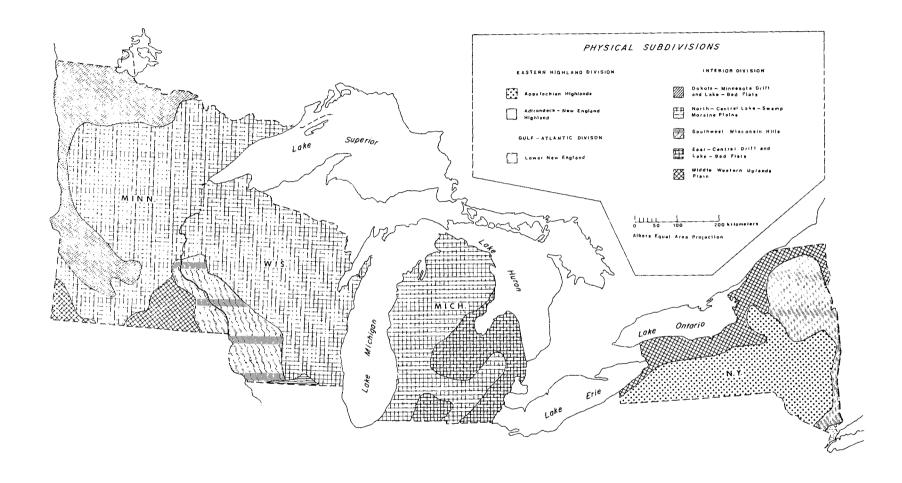


Figure 8. Physical subdivisions. Adapted from U.S. Geological Survey (1970) and Hammond (1964).

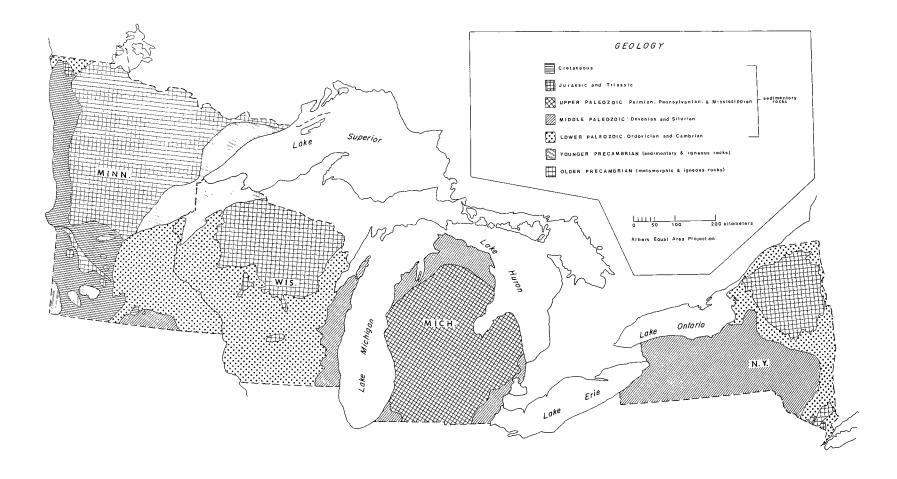


Figure 9. Geology. Adapted from U.S. Geological Survey (1970). For greater detail see U.S. Geological Survey (1965), Geologic Map of North America, 1:5,000,000.

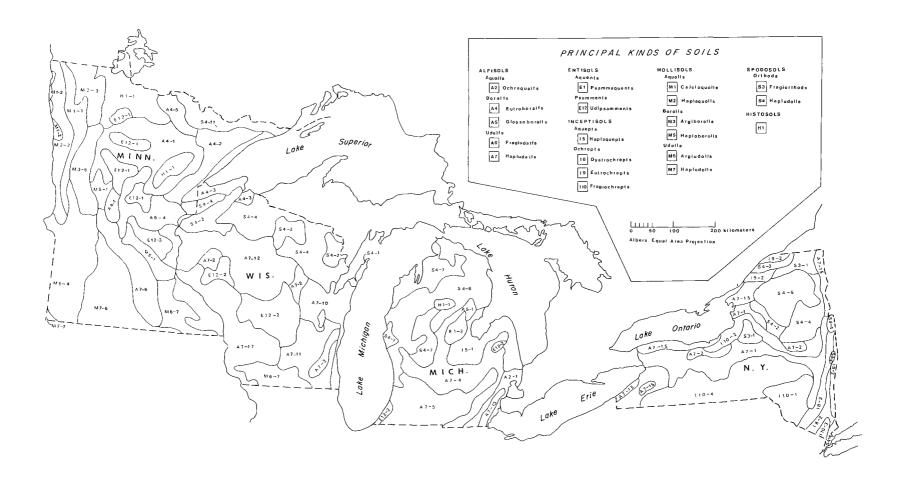


Figure 10. Distribution of principal kinds of soils: Orders, Suborders, and Great Groups. The letter-number symbols in the legend are abbreviated from those on the map. For a complete description, see U.S. Geological Survey (1970). Complete definitions of the soils are found in Soil Classification, A Comprehensive System, 7th Approximation (U.S. Department of Agriculture, 1960) and (USDA, March 1967) Supplement. The map is adapted from U.S. Geological Survey (1970).

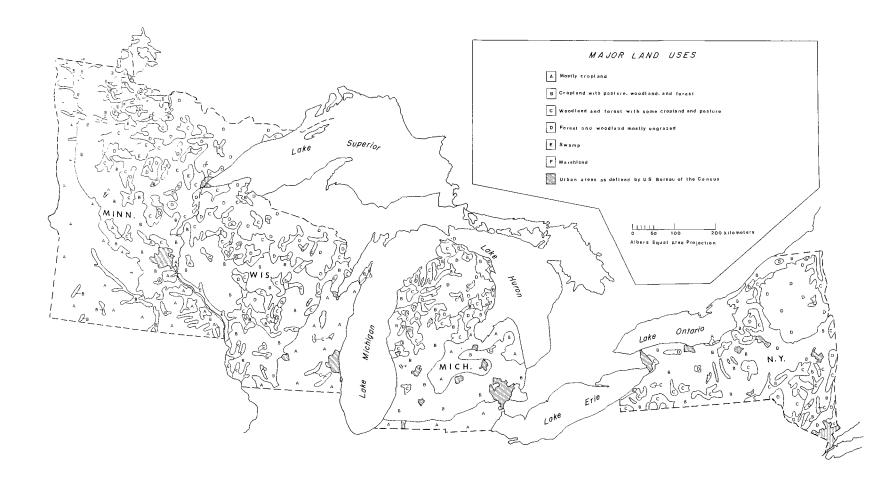


Figure 11. Major land uses. Adapted from U.S. Geological Survey (1970).

for the purposes of this report, to give extensive geographic coverage, trophic indicator values that covered a range representative of the 1972 NES-sampled lakes, and for completeness of sampling records. The study lakes are listed in Table 3. NES-sampled lakes have both a serial number and a STORET (STOrage and RETrieval) number; those with only a serial number are outside the scope of NES. Lake locations are depicted in Figure 12.

GROUND TRUTH COLLECTION

Each NES lake (serial numbers 1-100) was sampled three times (spring, summer, fall) during the 1972 calendar year (Appendix B) by helicopter-borne sampling teams operating from pontoon-equipped Bell UL-1H aircraft. The helicopters were equipped with a submersible pump and appropriate sensors for in situ measurements of conductivity, temperature, optical transmissivity, dissolved oxygen, hydrogen-ion concentrations (pH), and water depth. Additional equipment included an echo sounder, 30 cm Secchi disc, and water sampling equipment.

Lake Site Selection

Lake sampling sites were selected on the basis of lake morphometry, and potential major sources of nutrient input, as well as the on-site judgment of the sampling team's limnologists. The number of sampling sites varied for different lakes, ranging from one to nine (Lake Winnebago).

Lake Sampling Methods

After landing on the lake surface in the general area of a sampling site, the helicopter was taxied to locate the deepest nearby water. There a small reference bouy was deployed to aid the pilot in maintaining his station. Observations were recorded relating to general lake appearance, phytoplankton bloom conditions, aquatic macrophytes, and shoreline developments (e.g., residential units) along with magnetic compass bearings to prominent landmarks. A photograph was taken of the site, including the reference buoy and the prominent landmarks to assure return to the same site on subsequent sampling rounds.

Secchi disc transparency readings were made and water samples were bucket-dipped from the lake surface. The sensor recorders were monitored as the sensor-pump package was slowly lowered through the water column, permitting the limnologists to select depths or levels to be sampled as the package was winched to the surface. After touching bottom, the package was raised to a point approximately 1.2 meters off the bottom. Each sensor's digital output was recorded and the submersible pump activated for the collection of water samples. The package was then raised to the next sampling level and the process was repeated.

^{*} In 1972 the sensor could be deployed to a maximum depth of about 114 meters.

TABLE 3. STUDY LAKES

	<u> </u>	CEOD CE		Lake Coord	linates b
Lake Name	Serial a Number	STORET Number	County	N. Latitude W.	. Longitude
Ploalednole	1	2711	Beltrami	47° 45' 30'' 94	₽° 36' 00''
Blackduck Bemidji	2	27C1	Beltrami	47° 29' 30'' 94	F. 201 0011
Andrusia	3	27C0	Beltrami	47° 26' 30'' 94	l° 381 3011
Wolf	4	27A2	Becker	47° 26' 30'' 94	l° 40' 30''
Cass	5	2715	Cass		F° 281 3011
Leech	6	2746	Cass		l° 13' 00''
Birch	7	2710	Cass	•	l° 31' 30''
Trout	8	2793	Itasca	,	3° 25' 00"
Mashkenode	9	2756	St. Louis		° 36' 00"
Whitewater	10	2749	St. Louis		° 11' 00"
Pelican	11	2765	Crow Wing/		° 50' 00"
			St. Louis	, , , , , , , , , , , , , , , , , , , ,	
Shagawa	12	2780	St. Louis	47°,55' 00' 91	° 53' 00''
Gull	13	2737	Cass		° 211 3011
Rabbit	14	2771	Crow Wing	, -	° 56' 00''
Cranberry	15	2720	Crow Wing	•	° 46' 30''
Darling	16	27B4	Douglas	•	° 23' 00"
Carlos	17	27B9	Douglas	45° 56' 00" 95	° 231 0011
Le Homme Dieu	18	27B5	Douglas	45° 56' 30'' 95	° 21' 30"
Minnewaska	19	2761	Hennepin/ Pope	45° 36' 30'' 95	° 32' 00''
Nest	20	27B3	Kandiyohi	45° 16' 00'' 95	° 561 0011
Green	21	27B2	Kandiyohi	,,	° 52' 00"
Wagonga	22	27B1	Kandiyohi	-	° 561 3011
Clearwater	23	2716	Wright/	-	° 071 0011
			Stearns	,	
Mud (at Maple Lake)	24	2753	Wright	45° 13' 30'' 93	° 59' 00''
Cokato	25	2719	Wright	45° 07' 00" 94	° 091 3011
Buffalo	26	2713	Wright	45° 08' 30'' 93	° 54' 30"
Carrigan	27	2714	Wright	45° 03' 30" 93	° 57' 30''
Silver	28	2782	McLeod	44° 53' 00" 94	° 13' 00"
Minnetonka	29	2760	Hennepin	44° 57' 30'' 93	° 30' 30''
Forest	30	27A9	Washington	45° 17' 30" 92	° 58' 30''
White Bear	31	27B0	Washington	45° 04' 00'' 92	° 58' 30''
St. Croix	32	27A7	Washington	44° 46' 00'' 92	° 49' 00"
Spring	33	27A6	Washington	/	° 52' 30''
Pepin	34	27A4	Goodhue	44° 23' 00" 92	° 02' 00''
Madison	35	2750	Blue Earth		° 49' 00''
Sakatah	36	2777	Le Sueur		° 27' 30"
Bear	37	2706	Freeborn	•	° 30' 00"
Albert Lea	38	2702	Freeborn	, -	° 17' 30''
Yellow	39	5576	Burnett	45° 55' 30'' 92	-
Wapogasset	40	5550	Polk	45° 19' 30'' 92	° 26' 30''

TABLE 3. STUDY LAKES (continued)

	Ci - 1	CT OD FT	·	Lake Co	ordinates b
Lake Name	Serial Number ^a	STORET Number	County	N. Latitude	W. Longitude
Long	41	55 7 3	Price	45° 42' 00''	90° 27' 00''
Elk	42	55 7 5	Price	45° 42' 00"	90° 24′ 30′′
Trout	43	5572	Vilas	46° 04' 00"	89° 40' 00''
Crystal	44	5571	Vilas	46° 00′ 00′′	89° 361 3911
Tainter	45	5546	Dunn	44° 56′ 00′′	91° 53′ 30′′
Shawano	46	5539	Shawano	44° 47' 30''	88° 34' 00''
Poygan	47	5538	Winnebago	44° 06′ 30′′	88° 42' 30''
Butte Des Morts	48	5508	Winnebago	44° 02' 00"	88° 34¹ 00''
Winnebago	49	5554	Winnebago/ Fond Du Lac	44° 12' 00"	88° 27' 30''
Round	50	5566	Waupaca	44° 20' 00''	89° 10' 00''
Green	5 l	5519	Fond Du Lac	43° 51' 30''	88° 57′ 00′′
Swan	52	5545	Columbia	45° 32' 30''	89° 23′ 30′′
Beaver Dam	53	5503	Dodge	43° 27' 30''	88° 50' 30''
Kegonsa	54	5520	Dane	42° 58' 00"	89° 13′ 30′′
Rock	55	5564	Vilas	43° 04' 30''	88° 55′ 00′′
Koshkonong	56	5522	Dane/ Jeffe rs on	42° 50' 00''	89° 01' 30''
Lac La Belle	57	5563	Waukesha	43° 07' 00"	88° 31' 00''
Oconomowoc	58	5532	Waukesha	43° 05' 30''	88° 28′ 30′′
Okauchee	59	5580	Waukesha	43° 06' 30''	88° 28' 30''
Pine	60	5536	Waukesha	43° 07' 00"	88° 23' 30''
Nagawicka	61	5531	Price	44° 04' 00''	88° 24' 30''
Pewaukee	62	5557	Waukesha	43° 05' 00"	88° 16' 00''
Tichigan	63	5559	Racine	42° 46′ 00′′	88° 13' 00''
Browns	64	5560	Racine	42° 41' 00''	88° 14' 30''
Middle	65	5569	Walworth	42° 46' 30''	88° 34' 00''
Delavan	66	5513	Walworth	42° 37' 00''	88° 37' 30''
Como	67	5562	Walworth	42° 37' 00"	88° 27' 30''
Geneva	68	5561	Walworth	42° 36' 00''	88° 26' 00''
Charlevoix	69	2617	Charlevoix	45° 19' 00''	85° 15' 00''
Higgins	70	2695	Roscommon/ Crawford	44° 26' 00''	84° 40' 30''
Houghton	71	2696	Roscommon	44° 24' 30''	84° 47' 30''
Pere Marquette	72	2698	Mason	43° 56′ 30′′	86° 27' 00''
White	73	2688	Muskegon/ Newaygo	43° 22' 30''	86° 25' 30''
Muskegon	74	2659	Newaygo/ Muskegon	43° 14' 00''	86° 20' 00''
Fremont	75	2631	Newaygo	43° 26' 30''	85° 58' 30''
Mona	76	2691	Muskegon	43° 10' 00"	86° 17' 30''
Crystal	77	2694	Montcalm	43° 16' 30''	84° 55' 30''

TABLE 3. STUDY LAKES (continued)

	Serial	STORET		Lake Co	ordinates b
Lake Name	Numbera	Number	County		W. Longitude
Jordan,	78	2640	Ionia/ Barry	42° 45' 30''	85° 09' 00"
Thornapple	79	2683	Barry	42° 37' 00"	85° 21' 30''
Strawberry	80	2699	Livingston	42° 26' 30''	83° 51' 00"
Chemung	81	2618	Livingston	42° 35′ 30′′	83° 51' 30''
Thompson	82	2697	Livingston	42° 37' 30''	83° 55′ 30′′
Ford	83	2629	Washtenaw	42° 12' 30''	83° 33' 30''
Union	84	2685	Branch/ Calhoun	42° 02' 30''	85° 12' 30''
Long	85	2692	Ottawa	41° 55' 30''	84° 20' 00"
Randall	86	2671	Branch	42° 00' 30''	85° 02' 30"
Schroon	87	3624	Warren/ Essex	43° 50' 00''	73° 47' 00"
Black	88	3602	Jefferson/ St. Lawrence	44° 36' 00''	75° 28' 30"
Cassadaga	89	3607	Chautauqua	42° 20' 30''	79° 19' 30"
Chautauqua	90	3610	Chautauqua	42° 06′ 00′′	79° 15' 00"
Conesus	91	3639	Livingston	42° 50' 00"	77° 42' 30"
Canandaigua	92	3604	Ontario	42° 53′ 30′′	77° 15' 30"
Keuka	93	3617	Steuben/ Yates	42° 39' 30''	77° 09' 00"
Seneca	94	3635	Yates/ Senga/ Schuler	42° 56' 30''	76° 52' 00"
Cayuga	95	3608	Cayuga/ Tompkins/ Seneca	42° 58' 00''	76° 44' 30''
Owasco	96	3627	Cayuga	42° 47' 00"	76° 29' 00"
Cross	97	3611	Cayuga	43° 06' 00''	76° 25' 30''
Otter	98	3625	Cayuga	43° 09' 30''	76° 33' 00"
Round	99	3630	Saratoga	42° 55' 00"	73° 45' 00"
Saratoga	100	3633	Saratoga	43° 04' 30''	73° 41' 00"
Winona	101	27Al	Douglas	45° 33' 30''	95° 23' 00"
Trace	102	2792	Todd	45° 50' 30''	94° 451 30"
Calhoun	103	27B6	Hennepin	44° 56′ 00′′	93° 18' 30"
Big Stone	104	2709	Big Stone	45° 18' 00''	94° 27' 00"
Zumbro	105	27 A 5	Olmsted	44° 14' 00"	92° 29' 00"
Oneida	106	3622	Oswego/ Oneida	43° 11' 00''	75° 45' 30"
Canadarago	107	3603	Otsego	42° 50' 00''	75° 00' 00"
Mendota	108		Dane	43° 11' 00''	89° 13' 00"
Monona	109		Dane	43° 08' 30''	89° 16' 00"
Waubesa	110		Dane	43° 01' 30''	89° 29' 30''
Cottonwood	111	27C3	Lyon	44° 36' 00''	95° 40' 00"
Maple	241		Wright	45° 13' 30"	93° 59' 30"

The lakes with the serial numbers 1-31, 33, 35-38, 101-103, 111, and 241 are wholly contained in Minnesota. Lakes 32, 34, and 105, located on the borders of the state, are referred to as "Minnesota" lakes for convenience. Lakes 39-68 and 108-110 are Wisconsin lakes; 69-86 are in Michigan. New York lakes have been assigned the numbers 87-100 and 106-107.

b In the case of seepage lakes, the geographic coordinates represent a point on the lake surface.

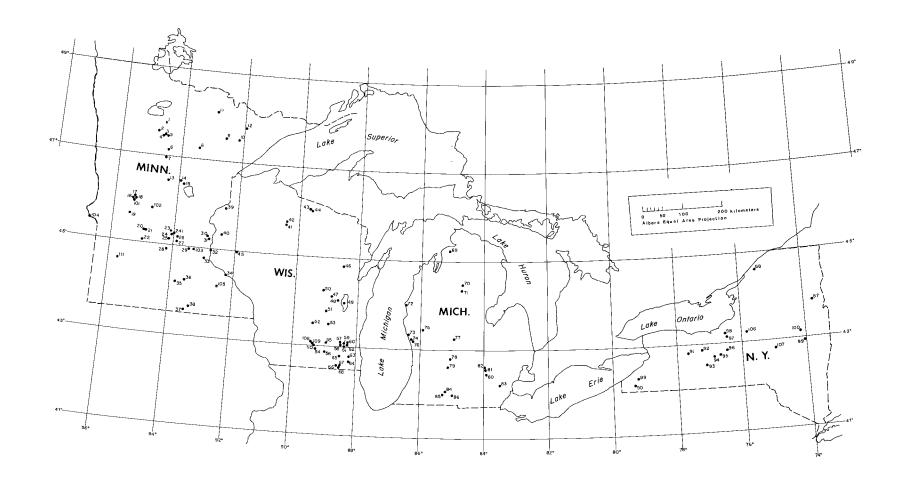


Figure 12. Location of the study lakes. The lakes with serial numbers 1-100 were used in the cluster analyses and principal component ordination analyses.

The procedure was continued until all of the selected levels were sampled.

Water samples were collected from each selected depth for nutrient, alkalinity, pH, conductivity, and dissolved oxygen determinations. The samples collected for alkalinity, nitrate-nitrogen, nitrite-nitrogen, ammonia-nitrogen, and dissolved phosphorus were preserved on-site by the addition of 40 mg/l of mercuric chloride. The samples were filtered through a 0.45 micrometer membrane filter (prerinsed with de-ionized water) and the filtrate was shipped to EPA's National Environmental Research Center (NERC), Las Vegas, Nevada. The samples for total phosphorus determination were preserved with a 40 mg/l mercuric chloride solution, but were not filtered.

Integrated samples for algae enumeration and identification purposes and chlorophyll <u>a</u> determination were collected by raising or lowering the package while continuing to operate the pump. The package movement was timed to provide a water sample representative of the water column from the surface to approximately 4.6 meters, or to a point just above the bottom in water less than 4.6 meters in depth. The algae samples were fixed with Lugol's solution and forwarded to NERC-Las Vegas.

A 18.9-liter water sample, composited from water collected at each sampling depth and every sampling site (\underline{i} . \underline{e} ., station) during the fall sampling period, was airmailed to the Pacific Northwest Environmental Research Laboratory (PNERL), Corvallis, Oregon, for the determination of its productivity potential under a set of standard conditions. The unpreserved sample, unrefrigerated while in transit, was stored in a freezer until the analysis could commence.

Analytical Methods

The water samples for dissolved oxygen, pH, and chlorophyll <u>a</u> determinations were analyzed in a mobile field laboratory at the end of each day of sampling. The dissolved oxygen water samples, fixed and acidified aboard the helicopters, were titrated with phenylarsine oxide in conjunction with a starch indicator. A Beckman Field Laboratory pH meter was used to determine the hydrogen-ion concentration of the water samples. The samples were refrigerated until they were analyzed.

The samples for chlorophyll <u>a</u> determination were refrigerated in the dark and were analyzed using the fluorometric procedure described by Yentch and Menzel (1963). Algal identification and enumeration included total cell count (Sedgewick-Rafter) and a differential count and identification of the five most abundant genera of algae.

Ammonia-nitrogen, nitrate-nitrogen, nitrite-nitrogen, dissolved phosphorus, total phosphorus, and alkalinity were measured at NERC-Las Vegas with a Technicon Autoanalyzer II according to the general methodology described in Working Paper Number 1 (NES, 1974).

The procedures used in the algal assay test, a methodology for the determination of a water sample's productivity potential and limiting nutrients, were those outlined in EPA's National Eutrophication Research Program's publication entitled "Algal Assay Procedure Bottle Test" (U.S. EPA, 1971). The analyses were conducted at PNERL, NERC-Corvallis.

SECTION IV

LAKE CLASSIFICATION

There is far from universal agreement as to what constitutes a lake. Veatch and Humphrys (1966) suggested that to give the word "lake" a precise, limited meaning would probably be an exercise in futility because the word has been in use for a long time and been given a diversity of applications. The word is used as a synonym for pond, reservoir, and sea. It has been applied to bodies of fresh water and saline water; to standing water and widenings in rivers; to bodies of water measuring less than a hectare and to those gauged in hundreds of thousands of hectares; to naturally occurring water bodies and man-made reservoirs; to water-filled or partially filled basins; and to basins void of water. "Lake" is generally more prestigious than other common names (e.g., pond) and is preferred by promoters of water-based tourist and recreational businesses and commercial developers of shoreline property (Veatch and Humphrys, 1966). Nevertheless, numerous attempts have been made to define and delimit the members of lentic series (i.e., lake, pond, marsh, and their intergrades).

Forel defined a lake as a body of standing water occupying a basin and lacking continuity with the sea; he defined a pond as a lake of slight depth (Welch, 1952). Welch (1952) defined a lake as a "...body of standing water completely isolated from the sea and having an area of open, relatively deep water sufficiently large to produce somewhere on its periphery a barren, wave-swept shore." He employed the term "pond" "...for that class of very small, very shallow bodies of standing water in which quiet water and extensive occupancy by higher aquatic plants are common characteristics" and suggested that all larger bodies of standing water be referred to as lakes. Zumberge (1952) defined a lake as an inland basin filled with water. Harding (1942) described lakes as "bodies of water filling depressions in the earth's surface."

LAKES AS NATURAL RESOURCES

The exact number of lakes in the United States is unknown. Welch (1952) estimated that there are at least 40,000 lakes in North America with a combined surface area of no less than 225,000 square miles (583,000 square kilometers). Hasler and Ingersoll (1968) reported a figure of 100,000 lakes in America (\underline{i} . \underline{e} ., United States).

Estimates of lake numbers from different sources or compiled at different times may exhibit wide disparity. The difference in estimates can be related to the lack of agreement as to what constitutes a lake, incompleteness of the inventories, and interpretational differences of maps and aerial photographs (Veatch and Humphrys, 1966). For example, Minnesota, "The Land of 10,000 Lakes," completed an inventory of its surface waters in 1968. The comprehensive final report initially defines a lake as "... an enclosed basin, filled or partially filled with water..." and then extends the term to include "...all natural enclosed depressions, 10 acres

or more in area, which have substantial banks capable of containing water and which are discernable on aerial photographs." Minnesota has, according to the report, 15,291 lake basins of which 3,257 are partly or completely dry (Minnesota Department of Conservation, 1968).

Fresh-water lakes are really insignificant when compared to the earth's total surface as they account for about 0.16 percent of it (Table 4). Nace (1960) estimates that only about 0.009 percent of the earth's total water supply is in the form of fresh-water lakes. In some regions lakes give the impression of dominating the landscape. Yet, in Beltrami County (Minnesota), a place renowned for its abundance of lakes, only about 18 percent of the area is under water (Minnesota Department of Conservation, 1968). Vilas County (Wisconsin), another governmental unit well endowed with lakes, has about 15 percent of its area covered by lakes (Deevey, 1942).

However, the geographic importance of any element of the landscape is not measured merely on the basis of its areal extent. The intrinsic properties of lakes make them a natural resource whose importance is greater than is suggested by area alone. Lakes are used as sources of municipal water, irrigation water, and cooling water for thermal-electric plants. They serve as transportation routes and as focal points for many types of recreational activity. Many lakes, particularly those in a pristine condition, are valued for their aesthetic qualities. They also provide convenient locations for dumping the organic and inorganic wastes of society.

An increasing number of lakes are viewed as merely obstacles in the "way of progress" and are being subjected to drainage or serving as land-fill sites to provide additional farmland or building sites. As the world's human population increases, it is likely that attempts to rid the land-scape of lakes will increase in scope. Although drainage and land-fill schemes threaten some lakes, a problem of much greater magnitude is that of cultural (anthroprogenic) eutrophication.

LAKE SUCCESSION AND EUTROPHICATION

Lake Succession

Lakes, although giving the impression of permanence when measured on the scale of the human life span, are transitory features of the earth's surface. All lakes, regardless of their origin, pass through the process of ecological succession which ultimately results in a terrestrial environment. The ephemeral nature of lakes is a consequence of two fundamental processes, the downcutting of the outlet and, more important, the deposition of allochthonous and autochthonous materials in the basin.

Most lakes commence the successional process as bodies possessing relatively low concentrations of nutrients and, generally, low levels of

TABLE 4. DISTRIBUTION OF THE WORLD'S ESTIMATED WATER SUPPLY^a

Location	Surface A r ea (km² x 10³)	Volume of Water (km³ x 10³)	Percentage of Total Water
or1d	510,228		
and Area	148,924		
urface water on the continents			
Polar icecaps and glaciers	17,871	30,428	2.24
Fresh-water lakes	855	125	0.009
Saline lakes and inland seas	699	104	0.008
Average in stream channels		1	0.0001
lotal surface water	19,425	30,658	2.26
ubsurface water on the continents			
Root zone of the soil	129,499	25	0.0018
Ground water above depth 805m Ground water, depth of 805m to		4,168	0.306
4,024 m		4,168	0.306
Total subsurface water	129,499	8,361	0.61
lorid's oceans	361,303	1,321,314	97.1
otal water on land		39,014	2.87
tmospheric moisture		12	0.001
Total, world supply of water		1,360,340	

^aAdapted from Nace (1960).

productivity.* The importation and deposition of materials ($\underline{e}.\underline{g}$., sediment) from the shoreline and the surrounding watershed gradually decrease the lake depth. The addition of allochthonous materials normally enriches the water and thereby stimulates the production of organic materials. The autochthonous materials increase the sedimentation rate thus accelerating succession. Marked floral and faunal changes occur. Algal blooms become more common along with submergent and eventually emergent aquatic macrophytes. Desirable game fish may be replaced by less desirable species, the so-called "rough fish". A lake will eventually become a marsh or swamp which, in turn, terminates as dry land.

Lindeman (1942) stressed the productivity aspects in relation to lake succession. Figure 13 represents the probable successional productivity relationships for a hypothetical hydrosere developing from a moderately deep lake located in a fertile humid continental region. Productivity is initially low, a consequence of low nutrient levels, but increases rapidly as nutrients become more available. The length of time required for completion of the successional process is a function of several factors including lake basin morphology, climate, and the rate of influx and nutrient value of allochthonous materials. It is readily apparent that allochthonous nutrients can drastically increase lake productivity and thereby shorten the life span of a lake.

The Concept of Eutrophication

The word eutrophication, until recently foreign to the vocabulary of the general public, has appeared in the popular and scientific literature at a rapidly increasing rate over the past decade. The term is often used to denote the process whereby a pristine water body ($\underline{e}.\underline{g}.$, lake) is transformed into one characterized by dense algal scums, obnoxious odors, and thick beds of aquatic macrophytes. However, the word is applied differently, according to the respective interests of its users.

Weber (1907) used the German adjectival form of eutrophication (nährstoff-reichere - eutrophe) to describe the high concentration of elements requisite for initiating the floral sequence in German peat bogs (Hutchinson, 1973). The leaching of nutrients from the developing bog resulted in a condition of "mitterlreiche" (mesotrophe) and eventually "nährstoff-earme" (oligotrophe). Naumann (1919) applied the words oligotrophic (under-fed), mesotrophic, and eutrophic (well-fed) to describe the nutrient levels (calcium, phosphorus, combined nitrogen) of water contained in springs, streams, lakes, and bogs (Hutchinson, 1973). Naumann (1931) defined eutrophication as the increase of nutritive substances, especially phosphorus and nitrogen, in a lake. Hasler (1947) broadly interpreted eutrophication as the "Enrichment of water, be it intentional or unintentional..." Fruh, et al. (1966) defined the word as the "enhancement of nutrients in natural water..." Edmondson (1974) suggested that many limnologists seem to use the term to describe "an increase in the rate of nutrient input..."

^{*}Edmondson (1974) suggested that the idea, that all lakes are born oligotrophic and gradually become eutrophic as they age, is an old misconception.

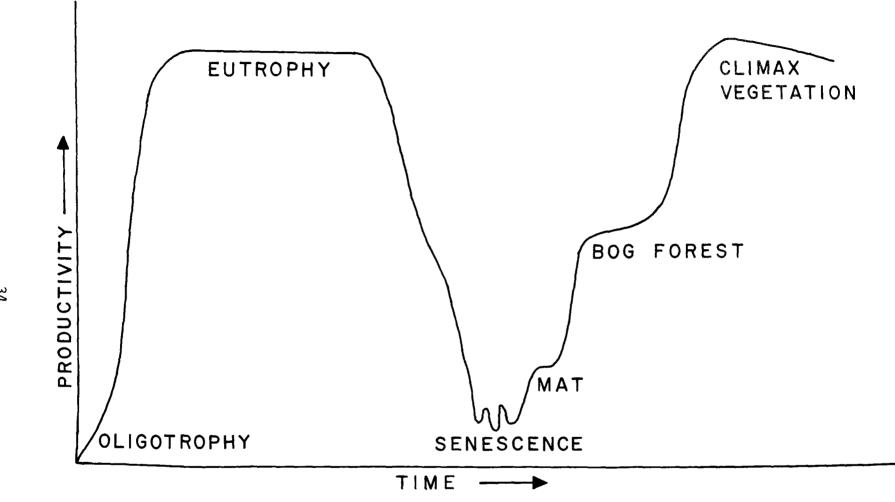


Figure 13. Hypothetical productivity growth-curve of a hydrosere. Adapted from Lindeman (1942).

Hasler and Ingersoll (1968) suggested that eutrophication is the "process of enrichment and aging* undergone by bodies of fresh water". Vollenweider (1968) summarized the eutrophication of waters as meaning "... their enrichment in nutrients and the ensuing progressive deterioration* of their quality, especially lakes, due to the luxuriant growth of plants with its repercussions on the overall metabolism of the waters affected..."

A search of the literature on eutrophication indicates that the meaning of the term, originally limited to the concept of changing nutrient levels, has been gradually expanded to include the consequences of nutrient enrichment⁺.

Eutrophication occurs both naturally and as a result of man's activities (cultural or anthropogenic eutrophication). Many of man's practices relating to the disposition of municipal sewage and industrial wastes and land use impose relatively large nutrient loadings on many lakes and rivers. In many cases, the enrichment results in algal blooms and other symptoms of eutrophication. The consequences of man-induced eutrophication often make the water body less attractive to potential users. More importantly, at least when a long-range viewpoint is adopted, eutrophication accelerates lake succession, thus shortening the time period before a lake loses its identity.

Trophic State and Trophic Indicators

Limnologists and other scientists concerned with lakes have used the term "trophic state" ($\underline{i}.\underline{e}.$, degree of eutrophy) to describe two different lake characteristics, nutrient status and productivity. Thus, trophic state is a hybrid concept as suggested by Margalef (1958). Several different physical, biological, and chemical attributes are required to adequately describe a lake's trophic state, making the concept multidimensional (Brezonik and Shannon, 1971) and precluding its determination through direct measurement. However, it is possible to quantify trophic state through the use of trophic state indicators (indices) in conjunction with appropriate data reduction techniques.

There are numerous indicators of trophic state, each with its merits and shortcomings. Reviews have been written on the subject by Fruh, et al. (1966). Stewart and Rohlich (1967), Vollenweider (1968), and Hooper (1969). A list of some common indicators or indices are found in Table 5. A diversity of opinion exists regarding the number and kinds of indicators which should be considered in the classification of lakes. Use of a

35

^{*} Emphasis added

⁺ The historical aspects and semantical problems associated with the word "eutrophication" and its companion words (oligotrophic, mesotrophic, eutrophic) are found in Weber (1907), Naumann (1919, 1931), Thienemann (1918), Rodhe (1969), Hutchinson (1967, 1973), Beeton and Edmondson (1972), and Edmondson (1974).

Physical	Chemical	Biological
Transparency (d) (Secchi disc reading)	Nutrient concentrations (i) (e.g., at spring maximum)	Algal Bloom frequency (i)
Morphometry (d)	Chlorophyll <u>a</u> (i) Conductivity (i)	Algal species diversity (d) Littoral vegetation (i) Zooplankton (i)
	Dissolved solids (i) Hypolimnetic oxygen deficit (i)	Fish (i) Bottom fauna (i)
	Epilimnetic oxygen supersaturation (i) Sediment type	Bottom fauna diversity (d) Primary production (i)

^aAn (i) after an indicator signifies the value increases with eutrophication; a (d) signifies the value decreases with eutrophication. The biological indicators all have associated qualitative changes (i.e., species changes occur as well as quantitative (biomass) changes as eutrophication proceeds). Adapted from Brezonik (1969).

single indicator has the virtue of simplicity but may produce misleading rankings or groupings because lakes are normally too complex to be adequately gauged on such a simplified basis. On the other hand, the use of a large number of indicators may result in a problem of character redundancy.

MULTIVARIATE CLASSIFICATION OF LAKES*

A multiplicity of classificatory schemes has been devised to group and rank lakes. Examples of some approaches to lake typology are found in: Lueschow, et al. (1970), Rawson (1956, 1960), Margalef (1958), Hansen (1962), Jarnefelt (1958), Larkin and Northcote (1958), Moyle (1945, 1946), Pennak (1958), Round (1958), Whipple (1898, Winner (1972), Zafar (1959), Beeton (1965), Donaldson (1969), and Gerd (1957). Hutchinson (1957, 1967) has reviewed many of the attempts to arrange lakes into orderly systems.

Lacustrine trophic state is a multi-dimensional concept and is, by its very nature, amenable to analysis by multivariate statistical techniques (e.g., cluster analysis, principal component analysis). Multivariate techniques minimize the personal bias often present when data are examined for groups, and rankings are developed. They are of particular value in situations where large numbers of objects or parameters are to be classified.

Numerical taxonomists and quantitative ecologists have been acutely aware of the benefits which can be derived from multivariate techniques and have been very active in promoting their use. Yet, a search of the literature has yielded few publications in which the techniques have been applied to lakes (e.g., Shannon, 1970; Brezonik and Shannon, 1971; Shannon and Brezonik, 1972a, 1972b; Sheldon, 1972). Shannon and Brezonik have devoted their efforts toward the classification and evaluation of 55 lakes in north central Florida. Sheldon reviewed the concept and functions of classification, introduced multivariate techniques of potential value in handling and synthesizing lake information, and applied the techniques to several lake populations.

Lake scientists have been slow to apply multivariate techniques to the problems of lake classification. This is probably because of a lack of familiarity with the techniques, the unavailability of large digital computers and/or the necessary software, and a shortage of comparable data from large numbers of lakes.

The balance of this section is devoted to the application of two multivariate techniques (cluster analysis, principal component analysis) to a

^{*} The term classification is often used in the restricted sense of placing entities into distinct groups, thereby exluding arrangements showing no distinct divisions (e.g., ordination). The term is used here in the broader context suggested by Sneath and Sokal (1973).

group of 100 lakes (Table 3) using selected elements of ground truth collected by NES. The resulting multivariate trophic state index will be used in Section VI to assist in the assessment of LANDSAT-1 MSS as a tool in estimating the trophic status of lakes.

Cluster Analysis

Cluster analysis is a collective term encompassing a broad spectrum of techniques for delineating natural groups ("clusters") of objects or attributes in hyperspace. A multitude of contributions have been published on the subject (e.g., Ward, 1963; Lance and Williams, 1967, 1968; Gower, 1967; Padron, 1969). Three comprehensive publications, written by Sokal and Sneath (1963), Anderberg (1973), and Sneath and Sokal (1973) serve as excellent sources of information. An expose of the various clustering techniques available to researchers is beyond the scope of this investigation, and the reader is referred to the above sources.

Clustering on objects is termed Q-technique as opposed to R-technique which leads to classifications of attributes or characters (Sneath and Sokal, 1973). Williams and Dale (1965) suggested that, when the relationships are represented in hyperspace, the kind of space that is operated on should be called A-space and I-space, not R-space or Q-space. A-space (attribute space) has p dimensions, one for each attribute (character), in which there are n points, each representing an object. I-space (individual space) has n dimensions, one for each object, in which there are p points, each representing an attribute. This study will utilize the Q-technique operating in A-space.

Objects and Attributes

One hundred lakes, sampled by NES in 1972, were selected for analysis. Each lake was assigned a serial number (1-100) which is unique to this report. A careful examination of the physical, chemical, and biological parameters measured by NES resulted in the selection of six indicators for incorporation into both the cluster analysis and principal component analysis (PCA) ordination. A seventh indicator, an abbreviated form of the Pearsall cation ratio inverse was originally included, but was eliminated because it did not appear to contribute significantly to the classification scheme.

The indicators (<u>i.e.</u>, lake attributes) are: conductivity (COND, μ mhos cm⁻¹), chlorophyll <u>a</u> (CHLA, μ g l⁻¹), total phosphorus (TPHOS, mg l⁻¹), total organic nitrogen (TON, mg l⁻¹), algal assay yield (AAY, drywt in mg) and Secchi disc transparency (SECCHI, m). The inverse of Secchi disc transparency (ISEC, m⁻¹) was employed so that all of the indicator values would increase as trophic status increases.

The six indicators were selected because they are quantitative, considered to be important measures of trophic state, and satisfy Hooper's (1969)

^{*} Abbreviated form of cation inverse is: ICAT = sodium / (calcium + magnesium).

criteria for trophic indices. Annual mean values for COND, CHLA, TPHOS, and ISEC were used in the analyses; AAY and TON measurements were limited to the fall overturn sample, precluding the use of an annual mean. The descriptive statistics of the six indicators are found in Table 6. A serious lack of normality in the data necessitated a transformation prior to clustering. Natural logarithms (LN) were found to be adequate for this transformation.

Cluster Method

A complete linkage algorithm (McKeon, 1967) was used to examine the lakes for natural groupings. The method is also known as the furtherest neighbor hierarchical strategy (Lance and Williams, 1967) and the maximum method (Johnson, 1967). The algorithm is characterized as agglomerative, nonoverlapping, and hierarchical, the latter property permitting the output to be modelled in the form of dendrograms. The program was run on an International Business Machines (IBM) Model 370-155E digital computer at Optimum Systems Incorporated (OSI), Bethesda, Maryland.

The LN-transformed trophic indicator data were entered as an N x p matrix where N is the number of observations or objects (<u>i.e.</u>, lakes) and p is the number of dimensions or attributes (<u>i.e.</u>, indicators). The data points in each column (indicator) of the data matrix were standardized by subtracting the column mean from each point and then dividing by the column's standard deviation. This was accomplished using the McKeon program option number three. Standardization was necessary because the data were measured in different units.

Euclidian distance, an extension of the Pythagorean theorem to points in hyperspace, was selected as the similarity coefficient, largely because of its intuitive appeal. The formula for the Euclidian distance, Δ_{jk} , between two objects (e.g., lake "j" and lake "k") is

$$\Delta_{jk} = \begin{bmatrix} p \\ \Sigma \\ j=1 \end{bmatrix} (X_{jj} - X_{jk})^2$$

The distances between all possible (N(N-1)/2) pairs of objects are computed and stored in an N x N symmetrical matrix (S-matrix). The McKeon program uses the squared Euclidian distance, Δ^2 , but the same clusters could be obtained by using Euclidian distance or any monotonic function of that distance.

The clustering procedure carries out successive iterations on the S-matrix which has the maximum squared distance within cluster in the diagonal and the maximum squared distance between clusters in the off-diagonals. Initially the S-matrix is N x N with zeros in the diagonals (Figure 14). At each

TABLE 6. DESCRIPTIVE STATISTICS OF 100 LAKES^a

				`		
Statistic	CHLA	ISEC	COND	TPHOS	TON	AAY
	(µg 1-1)	(m^{-1})	(µmhos cm ⁻¹)	(mg l ⁻¹)	(mg 1 ⁻¹)	(mg dry-wt)
Mean	22.3	0.85	352	0.136	0.80	7.3
Median	11.8	0.54	353	0.048	0.67	2.7
Maximum value	381.2	5.37	808	1.893	3.35	61.3
Minimum value	1.1	0.13	50	0.005	0.08	0.1
Range	380.1	5.24	758	1.888	3.27	61.2
Standard deviation	42.7	0.88	155.9	0.265	0.56	10.6
Skewness	6.4	2.86	0.3	4.264	2.20	2.4

^a The values above represent the statistics for the NES lakes which are incorporated into the cluster and principal component analyses.

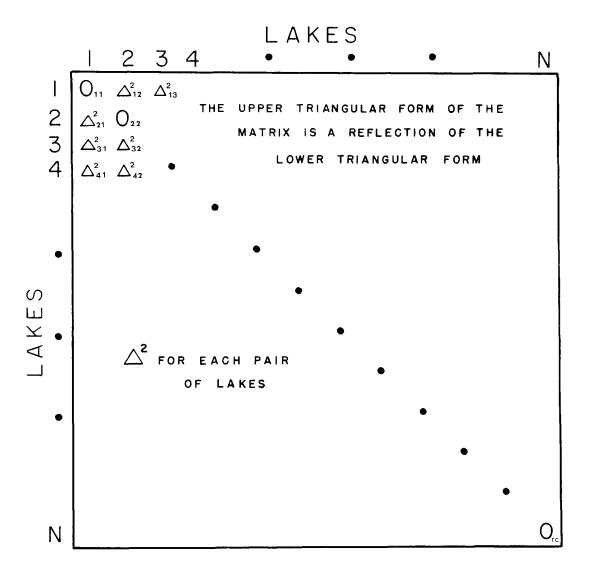


Figure 14. N x N S-matrix. Initially the matrix has only zeros on the diagonal. The off-diagonal elements represent the squared Euclidian distances between each pair of lakes. There are 4,950 distances possible for 100 lakes. Appendix E contains the matrix of Δ^2 used to examine the NES-sampled lakes for clusters.

iteration, those two clusters are combined, which, taken together, form the most compact cluster. The measure of compactness is the maximum distance between any two points $(\underline{i}.\underline{e}., lakes)$ within the cluster. The next pair to be combined are identified by finding the smallest squared distance between points in the off-diagonals.

For example, if N=100, the program will start out with 100 clusters and successively meld the clusters, two per iteration, eventually terminating with one cluster containing 100 objects.

Results and Discussion

The results of the cluster analysis are depicted as a dendrogram (Figure 15). The abscissa is scaled in Euclidian distance with the points of junction between stems implying that the maximum within-cluster distance is the value on the abscissa. Generally, the ordinate of a dendrogram has no special significance. The order of the clusters can be changed by rotating the stems, thereby producing a multitude of apparently different dendrograms. Interpretational problems arise when it is necessary to compare dendrograms developed from different data or algorithms.

Some investigators attempt to "standardize" the ordinate-induced appearance of the dendrogram by rotating the stems to keep the code or serial numbers as ordered as possible, especially if the numbers present linear arrangements of generally established taxonomic groups (Sneath and Sokal, 1973). The author has attempted to order the axis by rotating the stems to reflect the PCA ordination results found in the next section of this chapter. Consequently, the trophic status of the 100 lakes in the dendrogram generally increases along the ordinate in the "downward" direction.

It has become an accepted practice in lake studies to use the terms oligotrophic, mesotrophic, and eutrophic in reference to the trophic status of lakes. The terms, although well established in the literature, are used freely and it is difficult to quantitatively determine what is meant by them (Beeton, 1965). It may be argued that the terms serve to stereotype lakes and unduly restrict, to three categories, what may be members of a trophic continuum. However, this terminology is likely to continue in vogue because, at a very minimum, it gives some indication of trophic state.

The question arises regarding the number of "good" natural clusters which have been depicted by the clustering algorithm. McKeon (1967) asserted that a sudden increase in the maximum within cluster distance suggests that the previous stage may be a good stopping point. The first "sudden" increase occurs between $\Delta 3.70$ and $\Delta 4.35$ indicating that there may be seven relatively coherent clusters (A, B, C, D, E, F, G). There is some difficulty involved in reconciling the seven clusters with the three classic states.

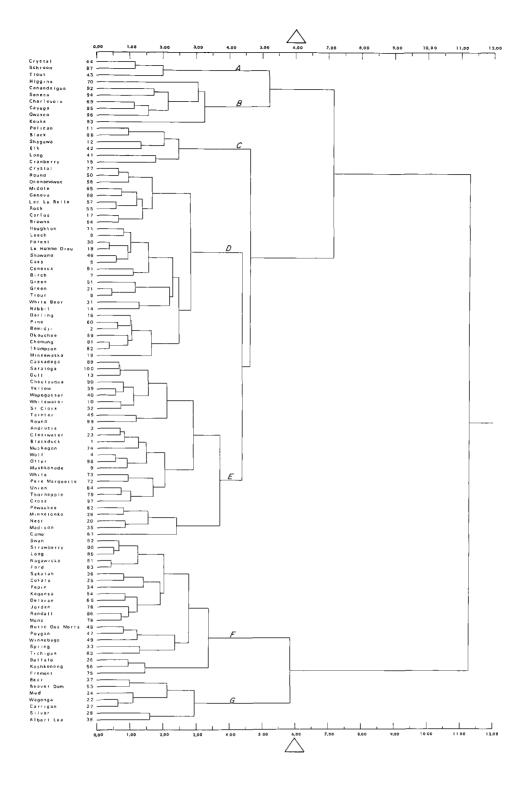


Figure 15. Dendrogram of 100 lakes sampled by the National Eutrophication Survey during 1972. The dendrogram is based on a complete linkage algorithm using generalized Euclidian distance as the measure of similarity.

The NES, cognizant of the advantages and limitations of naming lakes according to a three-class trophic scheme, has applied the trophic names to these lakes using data collected in 1972 and information acquired from various sources, including reports and knowledgeable individuals. Using the NES assessments as a guide, Clusters A and B may be characterized as containing a mixture of oligotrophic and mesotrophic lakes. Cluster C consists of eutrophic lakes; Cluster D is comprised of both mesotrophic and eutrophic lakes. Eutrophic lakes made up Clusters E and F. Cluster G consists of lakes which are very eutrophic (hypereutrophic).

The results of the cluster analysis appear distressing in light of the three-class concept of trophic state. A more careful selection of candidate lakes could have resulted in the "discovery" of three groups matching the classic trophic states. Nevertheless, the clustering approach is of value in showing relationships among lakes. It gives the investigator another way of perceiving his study lakes, and it is hoped will enable him to see more clearly the relationships between large numbers of lakes.

Principal Components Ordination

Hierarchical methods are a rather heavy-handed approach to the problem of reducing the dimensionality of multidimensional systems (Sheldon, 1972). They have the inherent capability to yield some form of clusters regardless of the structure of the data constellation, even if the entities to be analyzed are randomly distributed (Sneath and Sokal, 1973). Another approach that merits consideration is ordination. Ordination is the placement of N entities in A-space varying in dimensionality from 1 to p or N-1, whichever is less. Principal components analysis, one ordination technique, will be used to examine the lakes in A-space for natural clusters and to derive a multivariate trophic state index.

Principal components analysis may be used to reduce the dimensionality of a multivariate system by representing the original attributes as functions of the attributes. The main object is to summarize most of the variance in the system with a lesser number of "artificial" variates (<u>i.e.</u>, principal components).

The computation of principal components can be undertaken using either a covariance matrix (S) or a p x p matrix of Pearson product-moment correlation coefficients (R). Use of the R-matrix is indicated when the variates are measured in different units (e.g., grams and meters). Computation of the R-matrix principal components involves the extraction of its eigenvalues (characteristic or latent roots) and eigenvectors (characteristic or latent vectors). The eigenvalues are a set of r nonzero, positive scalar quantities. The sum of the R-matrix eigenvalues is the matrix trace and is equal to the number of dimensions in the original system (i.e., the number of variates, p). The rank of the matrix is r and is equal to p.

Normalized eigenvectors give the A-space coordinates of an orthogonal set of axes known as the principal axes. The normalized eigenvectors are commonly designated as principal components.

The first principal component of the observations of the p-variates X_1, \ldots, X_p is the linear compound

$$Y_1=a_{11} X_1 + \dots + a_{p1} X_p$$

whose coefficients (a_{i1}) are the elements of the eigenvector associated with the largest eigenvalue of the R-matrix (Morrison, 1967). The variance of the first principal component is associated with the eigenvalue. The jth principal component of the p-variate system is the linear compound

$$Y_j = a_{1j}X_1 + \dots + a_{pj}X_p$$

whose coefficients are the elements of the eigenvector associated with the jth largest eigenvalue extracted from the R-matrix. The jth eigenvalue is a measure of the variance of the jth principal component.

The proportion of the total sample variance in the cloud of dimensionless standard scores attributable to any component is found by dividing its eigenvalue by p. The first principal component has the innate property of explaining the greatest proportion of the sample variance with each successive component explaining progressively smaller amounts of the total sample variance. Frequently, a consequence of the decreasing order of variance, k < r dimensions will adequately summarize the variability of the original variates X_1, \ldots, X_p . The first three components generally account for most of the variation permitting the ordination of the subjects in 1-D, 2-D, and 3-D space. All of the dispersion in the data can be accounted for by using r dimensions, but this negates the analysis objective, the reduction of dimensionality or as Seal (1964) stated the "... parsimonious summarization of a mass of observations."

The principal components of N p-variate observations may be defined geometrically (Morrison, 1967) as "... the new variates specified by the axes of a rigid rotation of the original response coordinate system into an orientation corresponding to the directions of maximum variance in the sample scatter configuration." The normalized eigenvectors give the directions of the new orthogonal axes and the eigenvalues determine the lengths (i.e., variance) of their respective axes. The coordinate system is expressed in standard units (zero mean, unit variances) when the components are extracted from the R-matrix. Figure 16 is a hypothetical bivariate example of the geometric meaning of principal components.

Detailed descriptions of the theoretical and computational aspects of principal components are found in Hotelling (1933a, 1933b, 1936), Anderson (1958), and Morrison (1967).

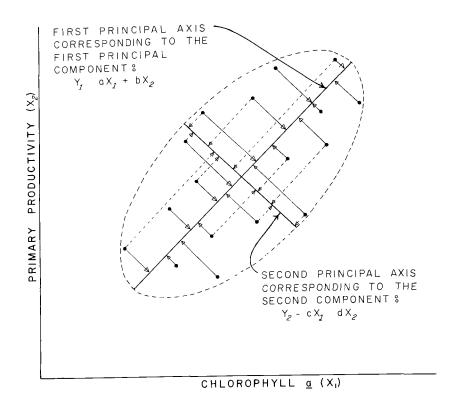


Figure 16. Geometrical interpretation of the principal components for a hypothetical bivariate system. Principal components may be interpreted geometrically as the variates corresponding to the orthogonal principal axes of observation scatter in A-The elements of the first normalized eigenvector space. (i.e., coefficients of the first principal component) define the axis which passes through the direction of maximum variance in the scatter of observations. The associated eigenvalue corresponds to the length of the first principal axis and estimates the dispersion along it. The second principal component corresponds to the second principal axis, the length of which represents the maximum variance in that direction. In our example the first component accounts for most of the dispersion in the data swarm and the original 2-dimensional system could be summarized in one dimension with little loss of information. The new variate value (PC1) for each lake is obtained by evaluating the first component

$$Y_1 = aX_1 + bX_2$$

The PCl for each lake in 1-D A-space is its coordinate on the first component axis and is shown diagrammatically by projecting each observation to the principal axis. (Modified from Brezonik and Shannon, 1971).

Methodology

The principal components analysis was accomplished using the same 100 lakes and LN-transformed trophic state indicator data used in the hierarchical cluster analysis (LNCHLA, LNISEC, LNCOND, LNTPHOS, LNTON, LNAAY). The data matrix was further standardized (zero mean, unit variance) by attributes using the relationship

$$z_{i,j} = (X_{i,j} - \bar{X}_i)/s_i$$

where $z_{i\,j}$ is the standardized values for attribute i of observation (i.e., lake) j; $X_{i\,j}$ is the LN-transformed value of observation j; and X_i and S_i are the mean and standard deviation of attribute j, respectively.

The eigenvectors and eigenvalues were extracted from a p x p correlation matrix (Table 7). All of the computational aspects were executed on a Control Data Corporation digital computer (CDC 3300) at Oregon State University using the Statistical Interactive Programming System (SIPS). A detailed explanation of SIPS, and its operation is found in Guthrie, Avery, and Avery (1973).

TABLE 7. R-MODE CORRELATION MATRIX OF SIX TROPHIC STATE INDICATORS. The coefficients were determined using LN-transformed data for the 100 NES-sampled lakes.

	LNCHLA	LNISEC	LNCOND	LNTPHOS	LNTON	LNAAY
LNCHLA LNISEC LNCOND LNTPHOS LNTON LNAAY	1.000	0.886 1.000	0.397 0.285 1.000	0.801 0.777 0.397 1.000	0.684 0.660 0.378 0.683 1.000	0.686 0.597 0.327 0.810 0.576 1.000

As was asserted earlier, principal components analysis can be used to advantage because often k < 3 dimensions will explain most of the variance in the hyper-dimensional cloud of data points. The resulting ordinations can be expressed as 1-D, 2-D, and 3-D models. The ordinations are usually expressed as a sequential numerical listing (<u>i.e.</u>, 1-D model), a scatter diagram (<u>i.e.</u>, a 2-D model), or as a set of three 2-D scatter diagrams which, when examined carefully, may give some indication of the scatter of observations in an A-space of three dimensions. However, unless the

pattern of diversity is simple, it is rather difficult for most individuals to visualize the pattern in 3-D space using a series of 2-D projections. Fraser and Kovats (1966) and Rohlf (1968) have advocated the use of stereographic projections for ordination in 3-space and have furnished the equations necessary for the development of stereoscopic models (i.e., stereograms). Some examples are found in Schnell (1970), Moss (1967), and Sneath and Sokal (1973).

This investigator has employed the techniques in Rohlf (1968) to construct 3-dimensional ordination models by plotting the lakes in the 3-D space produced by the first three principal components. The models can be examined visually for the presence of clusters. Unlike the clustering approach, no assumptions are made that the lakes must congregate into a series of clusters.

The model, as used here, consists of one member of a stereo pair; the other member is easily produced if the complexity of the data necessitates the advantages inherent in viewing the objects in stereo. The lake coordinates, determined by evaluating the three components for each lake, are standardized to make the scale for the longest axis (X) run from 0.0 to 1.0. The other axes are scaled-down proportionally. The component with the smallest range is assigned to the vertical (Z) axis. The models were plotted on a Calcomp (IBM-1724) 30 inch incremental drum plotter driven by the Oregon State University CDC 3300 computer using subroutines found in GRAFPAC, a plotting routine package developed by Rohlf (1968). The same modelling approach is used in Section VII to depict LANDSAT-1 MSS color ratio relationships.

Results and Discussion

The normalized eigenvectors and eigenvalues are found in Table 8. Although the principal component analysis is of value in reducing the dimensionality of a multivariate system, it is sometimes difficult to interpret the new variates in terms of subject matter identities. Some indication of a principal component's meaning may be ascertained by an examination of the algebraic sign and magnitude of its coefficients.

The coefficients of the first component (Table 8), excluding the coefficient for LNCOND, are nearly equal in magnitude suggesting that it represents a general measure of trophic state, accounting for approximately 68 percent of the variation in the data. Correlations between the new variate and the LN-transformed trophic indicators are found in Table 9.

The first principal component was evaluated for each of the 100 lakes. The resultant values (PCl) are indicative of each lake's respective position on a multivariate trophic scale (Table 10). The procedure followed is essentially that of Brezonik and Shannon (1971), but the

TABLE 8. NORMALIZED EIGENVECTORS AND EIGENVALUESa

Eigenvector Number	LNCHLA	LNISEC	LNCOND	LNTPHOS	LNTON	LNAAY	Eigenvalue	Variance (%)	Cumulative Variance (%)
1	0.457	0.435	0.251	0.458	0.403	0.408	4.081	68.02	68.02
2	-0.112	-0.249	0.952	-0.088	0.010	-0.104	0.810	13.50	81.52
3	-0.222	-0.397	-0.018	0.271	-0.383	0.757	0.477	7.95	89.47
4	-0.346	-0.395	-0.143	-0.040	0.829	0.122	0.387	6.45	96.92
5	-0.436	0.060	-0.006	0.797	-0.056	-0.410	0.152	2.54	98.46
6	-0.647	0.657	-0.099	-0.270	0.008	0.258	0.092 5.999	$\frac{1.54}{100.00}$	100.00

^aThe principal components analysis was performed using an R-matrix of correlation coefficients for six trophic state indicators. The data represent 100 lakes sampled by NES during 1972.

scale was not shifted into the positive domain by correcting each lake's PCl with the PCl obtained from a hypothetical lake. The lake lying at the negative end of the scale, Crystal Lake, is rated as having the lowest trophic status of those studied; in other words, it has relatively high water quality. Trophic state increases in the positive direction on the scale with the lake lying at the positive extreme, Albert Lea Lake, exhibiting the highest trophic state of the 100 lakes studied. Some breaks or gaps are evident on the scale, but only toward the two extremes. A very discernible gap occurs between Beaver Dam Lake (53, position 95) and Mud Lake (24, position 96); the Mud Lake - Albert Lea Lake group might be termed as hypereutrophic.

TABLE 9. PRODUCT-MOMENT CORRELATION COEFFICIENTS OF THE TROPHIC STATE INDICATORS AND THE PRINCIPAL COMPONENTS.

		Principal Component								
	1	2	3	4	5	6				
LNCHLA	0.92	-0.10	-0.15	-0.22	-0.17	-0.20				
LNISEC	0.88	-0.22	-0.27	-0.25	0.02	0.20				
LNCOND	0.51	0.86	-0.01	-0.09	-0.20	0.01				
LNTPHOS	0.92	-0.08	0.19	-0.03	0.31	-0.08				
LNTON	0.82	0.01	-0.26	0.52	-0.02	0.00				
LNAAY	0.83	-0.09	0.52	0.08	-0.16	80.0				

The magnitude of the first component's coordinates suggests that a less elegant approach toward an ordination of the lakes might be undertaken with similar results. The approach, using the same LN-transformed standardized indicator values, involves the summation of a lake's indicator values and then dividing by p, the number of indicators. In other words

$$MCR_{j} = (X_{j1} + ... + X_{jp})/P_{j}$$

where MCR_j is the Mean Composite Rank for the jth lake, X_{jl} is the jth lake's score on the first trophic indicator, X_{jp} is the lake's score on the pth indicator and p is the number of dimensions or indicators. The results of this ranking method are found in Table 10 along with the principal components ordination. The two methods of ordinating the lakes are in close agreement. However, the principal component approach has the advantage of permitting the development of 2-dimensional and 3-dimensional ordinations which explain a very high percentage of the variance.

TABLE 10. PRINCIPAL COMPONENT ORDINATION AND MEAN COMPOSITE RANK ORDINATION OF 100 LAKES

Position	Lake Name	Serial Number	PC1 Value	Lake Name	Serial Number	MCR Value
1	Crystal	44	-5.04	Crystal	44	-2.17
	Schroon	87	-4.59	Schroon	87	-1.99
2 3 4 5 6 7	Higgins	70	-3.92	Higgins	7 0	-1.56
4	Canandai gua	92	-3.63	Canandaigua	92	-1.42
5	Charlevoix	69	-3.60	Charlevoix	69	-1.47
6	Trout	43	-3.24	Trout	43	-1.39
7	Seneca	94	-2.89	Seneca	94	-1.03
8 9	Cayuga	95	-2.74	Cayuga	95	-1.02
9	Crystal	77	-2.52	Owasco	96	-0.98
10	Owas co	96	-2.47	Crystal	77	-0.95
11	Middle	65	-2.29	Middle	65	-0.85
12	Keuka	93	-2.14	Keuka	93	-0.85
13	Round	50	-2.09	Round	50	-0.79
14	Oconomowoc	58	-1.82	Houghton	71	-0.66
15	Geneva	68	-1.71	Pelican	11	-0.65
16	Green	51	-1.67	Oconomowoc	58	-0.64
17	Houghton	71	-1.61	Geneva	68	-0163
18	Carlos	17	-1.55	Green	51	-0.62
19	Lac La Belle	57	-1.43	Long	41	-0.59
20	Leech	6	-1.43	Birch	7	-0.58
21	Conesus	91	-1.41	Leech	6	-0.57
22	White Bear	31	-1.41	Carlos	17	-0.57
23	Birch	7	-1.39	White Bear	31	-0.55
24	Pelican	11	-1.27	Conesus	91	-0.54
25	Forest	30	-1.22	Lac La Belle	57	-0.51
26	Rock	55	-1.21	Forest	30	-0.49

TABLE 10. PRINCIPAL COMPONENT ORDINATION AND MEAN COMPOSITE RANK ORDINATION OF 100 LAKES (continued)

Position	Lake Name	Serial Number	PC1 Value	Lake Name	Serial Number	MCR Value
27	Green	21	-1.10	Cassadaga	89	-0.50
28	Long	41	-1.07	Rock	55	-0.44
29	Browns	64	-1.07	Black	88	-0.42
30	Le Homme Dieu	18	-1.06	Le Homme Dieu	18	-0.41
31	Cassadaga	89	-1.04	Green	21	-0.41
32	Trout	8	-1.01	Shagawa	12	-0.40
33	Shawano	46	-0.94	Shawano	46	-0.40
34	Cass	5	-0.90	Trout	8 5	-0.38
35	Black	88	-0.77	Cass	5	-0.3
37	Darling	16	-0.73	Gull	1 3	-0.3
38	Pine	60	-0.71	Chautauqua	90	-0.3
39	Chautauqua	90	-0.66	Cranberry	15	-0.3
40	Okauchee	59	-0.62	Pine	60	-0.2
41	Shagawa	12	-0.58	Saratoga	100	-0.2
42	Saratoga	100	-0.57	Darling	16	-0.2
43	White	73	-0.47	Whitewater	10	-0.2
44	Rabbit	14	-0.46	Elk	42	-0.2
45	Bemidji	2	-0.44	Okauchee	59	-0.1
46	Cranberry	15	-0.40	Rabbit	14	-0.1
47	Whitewater	10	-0.38	Yellow	39	-0.1
48	Minnewaska	19	-0.32	Bemidji	2	-0.1
49	Andrusia	3	-0.24	St. Croix	32	-0.1
50	Yellow	39	-0.23	White	73	-0.1
51	Pere Marquette	72	-0.21	Wapogasset	40	-0.1
52	St. Croix	32	-0.17	Andrusia	3	-0.1

TABLE 10. PRINCIPAL COMPONENT ORDINATION AND MEAN COMPOSITE RANK ORDINATION OF 100 LAKES (continued)

Position	Lake Name	Serial Number	PC1 Value	Lake Name	Serial Number	MCR Value
53	Wapogasset	40	-0.16	Pere Marquette	72	-0.04
54	E1k ~	42	-0.08	Minnewaska	19	-0.03
55	Chemung	81	-0.06	Blackduck	1	-0.02
56	Blackduck	1	0.01	Chemung	81	0.02
57	Clearwater	23	0.01	Wolf	4	0.02
5 8	Thompson	82	0.03	0tter	98	0.03
59	Wolf	4	0.11	Clearwater	23	0.03
60	0tter	9 8	0.13	Thompson	82	0.08
61	Muskegon	74	0.18	Muskegon	74	0.09
62	Union	84	0.43	Tainter	45	0.10
63	Tainter	45	0.44	Union	84	0.22
64	Thornapple	79	0.58	Mashkenode	9	0.27
65	Pewaukee	62	0.59	Pewaukee	62	0.29
66	Swan	52	0.68	Swan	52	0.30
67	Minnetonka	29	0.73	Minnetonka	29	0.30
6 8	Maskenode	9	0.74	Thornapple	79	0.30
69	Nest	20	0.77	Nest	20	0.32
70	Cross	97	0.86	Round	99	0.37
71	Strawberry	80	0.99	Cross	97	0.41
72	Round	99	1.02	Strawberry	80	0.45
73	Long	85	1.14	Como	67	0.46
74	Como	67	1.15	Butte des Morts	48	0.48
75	Butte des Morts	48	1.27	Long	85	0.50
76	Nagawicka	61	1.27	Madison	35	0.53
77	Ford	83	1.36	Nagawicka	61	0.56
7 8	Madison	3 5	1.36	Sakatah	36	0.57

TABLE 10. PRINCIPAL COMPONENT ORDINATION AND MEAN COMPOSITE RANK ORDINATION OF 100 LAKES (continued)

Position	Lake Name	Serial Number	PC1 Value	Lake Name	Serial Number	MCR Value	
	Sakatah	36	1.38	Jordan	78	0.58	
80	Jordan	78	1.41	Kegonsa	54	0.59	
81	Kegonsa	54	1.48	Ford	83	0.60	
82	Cokato	25	1.61	Poygan	47	0.65	
83	Poygan	47	1.68	Cokato	25	0.71	
84	Randall	86	1.92	Randall	86	0.80	
85	Delavan	6 6	2.03	Delavan	66	0.83	
86	Pepin	34	2.10	Pepin	34	0.8	
87	Mona	76	2.17	Mona	76	0.8	
88	Buffalo	26	2.31	Winnebago	49	0.9	
89	Spring	3 3	2.33	Buffalo	26	0.9	
90	Winnebago	49	2.36	Spring	33	0.9	
91	Koshkonong	56	2.45	Koshkonong	56	1.0	
92	Fremont	7 5	3.06	Bear	37	1.2	
93	Tichigan	63	3.11	Fremont	75	1.2	
94	Bear	37	3.15	Tichigan	63	1.2	
95	Beaver Dam	53	3.29	Beaver Dam	53	1.2	
96	Mud (at Maple Lake)	24	4.32	Mud (at Maple Lake)	24	1.7	
97	Wagonga	2 2	4.40	Carrigan	27	1.7	
98	Carrigan	27	4.40	Wagonga	22	1.7	
99	Silver	28	4.79	Silver	28	1.8	
100	Albert Lea	3 8	5.90	Albert Lea	3 8	2.3	

The second component (Table 8) explains about 14 percent of the variation in the data. The LNCOND coordinate of the component is very large suggesting that the second variate is largely a measure of conductivity. The second component has a good correlation with LNCOND (Table 9).

The third component (Table 8) accounts for approximately 8 percent of the variance. LNAAY is the trophic indicator which shows the strongest correlation with the third component (Table 9), but is not readily interpretable.

Approximately 89 percent of the total sample variance can be attributed to the first three components. Figure 17 depicts the 100 lakes ordinated in 3-D space defined by the first three components. Some small clusters are apparent, but they are not well defined. The long axis is the first principal component axis (I). The axis labelled II is the second component and the vertical axis (III) is the third component.

The failure to discern well defined clusters may be partially a consequence of the trophic state of the lakes incorporated into this analysis; the NES lake population is heavily weighted toward lakes having water quality problems.

Summary

One hundred lakes were subjected to two complementary multivariate analyses, a complete linkage hierarchical cluster analysis and ordination using the technique of principal components. Well-defined clusters or natural groupings were not found through either approach. This may be a consequence, at least partially, of the "kinds" of lakes incorporated into the analyses.

The first principal component was evaluated for each lake and the resulting value (PC1), its coordinate on the axis, used as a multivariate index of the lake's trophic state. The PC1's are purported to represent an assessment of lacustrine trophic state and will be used in Section VII to evaluate LANDSAT-1 MSS color - lake relationships.

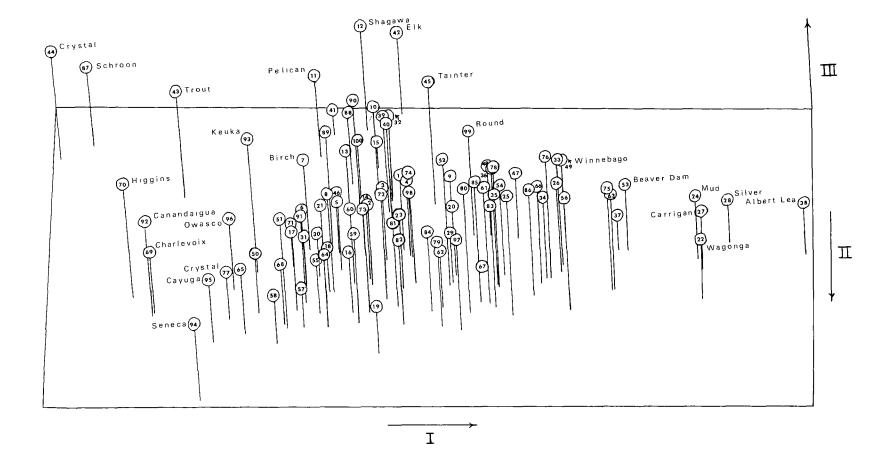


Figure 17. The three-dimensional principal component ordination of 100 lakes sampled by the National Eutrophication Survey during 1972.

SECTION V

LANDSAT-1 DATA EXTRACTION TECHNIQUES AND PRODUCTS

LANDSAT-1 MSS data are available from EROS in the form of photographic products and computer-compatible digital magnetic tapes (CCT's). The data forms permit investigators two general approaches to the problem of data extraction and utilization, the photographic approach and the CCT approach. Each has its particular advantages and limitations.

MSS DATA EXTRACTION APPROACHES

Photographic Approach

The photographic products available from EROS include black and white (b&w) negative and positive transparencies, and prints. False color prints and transparencies are available for a very limited number of scenes. All are either third or fourth generation photographic products. The photographs may be examined visually, as was done in Section III, for differences in gray tone, texture, shape, size, and pattern. Techniques common to the interpretation of aerial photographs may be employed to extract information pertinent to many different fields of science.

Quantification of the information contained in the undodged photographic products may be achieved through microdensitometry and photographic techniques including false color enhancement and density slicing. Manual and automatic microdensitometry can be used to digitize the information contained on the photographic positive or negative transparencies. This is easily accomplished with a microdensitometer by directing a light beam of known intensity through a small segment (e.g., lake image or portion of a lake image) of the transparency and measuring any changes in intensity on a numerical scale as percent transmission or as optical density. The quantitative data may then be used to examine correlations between MSS bands and lake indicators relating to trophic state.

Automatic scanning systems permit density slicing, the separation of the different densities on a transparency and their coding for later reproduction as b&w and color-enhanced products or symbolized listings. Reliance upon sophisticated instrumentation for the determination of areas of equal density (<u>i.e.</u>, equidensities) can be avoided by using various photographic enhancement techniques. Nielsen (1972) summarizes a simple process reported by Ranz and Schneider (1970) which utilizes Agfacontour film for the production of equidensities.

The photographic approach is attractive because it can be accomplished with relatively simple equipment (unless a fully automated scanner is used) and is inexpensive. The four transparencies required to give all band (green, red, IR1, IR2) coverage of a LANDSAT-1 MSS scene cost only ten percent of the listed (November 1975) EROS price for a comparable set of CCT's (\$20.00/\$200.00). Many investigators, lacking the necessary computer and software for processing the CCT's, are able to explore possible applications of LANDSAT-1 data in their areas of specialization using the photographic approach.

However, the approach has several limitations which are particularly serious in water resources studies and which merit mention. The transparencies have a relatively small density range when compared to the sensitivity range of the MSS; this results in a scale compression when the MSS data are transformed into a film image on an electron beam recorder (EBR). The range of energy returns from water bodies is small and located at the lower end of the MSS intensity scale. Compression of the overall scale increases the difficulty of discriminating differences in water quality.

As mentioned previously, the photographic materials are third and fourth generation products (the first generation is the film image produced by the EBR), and the errors common to photographic processing are compounded. Chemical adjacency effects and the nonlinearity of the density-log exposure (D-log E) curve increase the magnitude of the problem. An additional element of uncertainty is introduced by the microdensitometer.

This investigator is not trying to assert that the photographic approach is totally lacking in merit, but rather that its limitations seriously limit the investigator attempting a quantitative estimation of lake parameters relating to trophic indicators and trophic state.

CCT Approach

The use of computer compatible tapes to study LANDSAT-1 MSS sensed phenomena is not only more expensive, but it is also more restrictive because there are relatively few research centers with the requisite computer software and output devices to use the digital data to full advantage. However, these limitations are overshadowed by the fact that the tapes contain, in digital form, the actual data point values recorded by the MSS. Investigators can avoid the numerous uncertainties introduced when the original MSS data are coded by an electron beam recorder (EBR) into photographic forms and then re-quantified through microdensitometry.

This investigation was initiated using the photographic approach. A manually operated microdensitometer was used to measure the optical density (OD) of lake images. Differences in OD were detected, but

several difficulties were encountered ($\underline{e}.\underline{g}.$, variation in the quality of the transparencies, locating the lakes on the green band transparencies), and the approach was abandoned in favor of the CCT approach.

The CCT approach permits the rapid determination of picture element (pixel) counts, descriptive statistics ($\underline{e}.\underline{g}.$, means, standard deviations, and histograms), density slicing, and affords the opportunity to enhance optional photographic products through both linear and non-linear contrast stretching.

The utilization of CCT's is not without its problems, most of which are related to the quality of the information contained on the tapes. Defects commonly contained in the MSS data recorded on the tapes include missing lines and random bit-dropout for major portions of lines. The defective tapes can be repaired using existing software, but at additional cost both in time and money. Another problem is the receipt of CCT's not meeting the specification of the purchase order (e.g., receipt of 9-track instead of 7-track tapes; 556 bpi instead of 800 bpi tapes). While this is a minor problem, it does cost the investigator valuable time.

CCT DATA EXTRACTION TECHNIQUES

The LANDSAT-1 MSS CCT's used in this investigation were processed at the Image Processing Laboratory (IPL), a support facility of the Jet Propulsion Laboratory (JPL), California Institute of Technology. In this section, the author will briefly discuss the image processing system and, using one lake as an example, outline the data extraction techniques employed.

Image Processing System

The IPL system consists of an IBM 360/44 computer with five tape drives, four disc drives, a quick-look Polaroid pictorial output device, and a core-refreshed interactive display (Blackwell and Boland, 1974). A video film converter (VFC) provides offline hardcopy pictorial input and output capabilities. This device has a precision cathode ray tube (CRT), and 70-mm and 35-mm cameras. In the pictorial output mode, the VFC reads a digital magnetic tape, containing a digital image, and displays that image on the CRT, exposing the film which is then developed and printed, producing a hardcopy output of the digital image. In the pictorial input mode, the VFC functions as a flying spot scanner producing a digital output picture on magnetic tape.

The IPL IBM 360/44 operates under the control of a special software system, VICAR (Video Information Communication and Retrieval). Presently, a highly stylized Operating System (OS) is operational which permits foreground-background, roll-in and roll-out capabilities. VICAR is designed to allow very flexible manipulation of digital pictures consisting of rectangular arrays of optical measurements. The system

contains a library of more than two hundred operationally executable image-processing programs. Each program operates on an input digital picture stored on magnetic tape or disc. Processing line-by-line, it generates an output picture on tape or disc, preserving the input data. Additional information regarding the system and existing programs is found in Frieden (1971), Anon (1973), and Blackwell and Billingsley (1973).

Data Extraction Technique

LANDSAT-1 MSS Frame 1017-16093 and one of its lakes, Lake Koshkonong (56), will be used to illustrate the methodology used to extract the digital information contained in a set of CCT's.

The extraction process commences with a change in the format of the Goddard Space Flight Center (GSFC) CCT's and an expansion to 8-bit mode giving a total of 256 digital number (DN) levels (0 to 255) of optical intensity. The system is capable of handling the data contained on two CCT's at a time, resulting in an initial output consisting of one half of an LANDSAT-1 frame. An example of the left half of Frame 1017-16903 is shown in Figure 18. The image has been reconstructed using the IR2 DN values and a fiducial system has been applied to the edges.

The section of Frame 1017-16093 containing Lake Koshkonong and a portion of the surrounding terrain is extracted from the tapes in each of the four MSS bands by supplying the computer with the appropriate coordinates. Figure 19 shows the extracted section for Band 7 (IR2). The histogram below the picture represented the full range of DN values present within the scene on a scale of 0 (black) to 255 (white). The prominent DN values, centered at approximately DN 128 and spreading symmetrically, are related to the land features within the section. The small cluster of DN values at the lower end of the DN scale is associated with water features including Lake Koshkonong and the Rock River.

In this study, the land DN values are of little interest and must be eliminated, leaving just the water body values. Previous testing has verified that the IR2 band is a good indicator of the areal extent of surface water. As was noted in Figure 19, IR2 water-related intensity values fall within the lower end of the DN scale and are essentially isolated from the land IR2 DN values. This characteristic permits the development of a binary mask which is used to eliminate the land image.

The mask is created by setting all intensity values at and below a specific numeric value equal to a value of one and setting all of the remaining DN values equal to zero. Each spatially equivalent Lake Koshkonong pixel within each band (green, red, IR1, and IR2) is multiplied by the IR2 binary mask. The net effect is to "zero out"



Figure 18. Left half of MSS Frame 1017-16093 reproduced using IR2 DN values. A fiducial system has been imposed along the edge of the image to aid in the determination of feature locations on the basis of line and picture element counts. Lake Koshkonong is the large dark object in the upper center of the photograph.

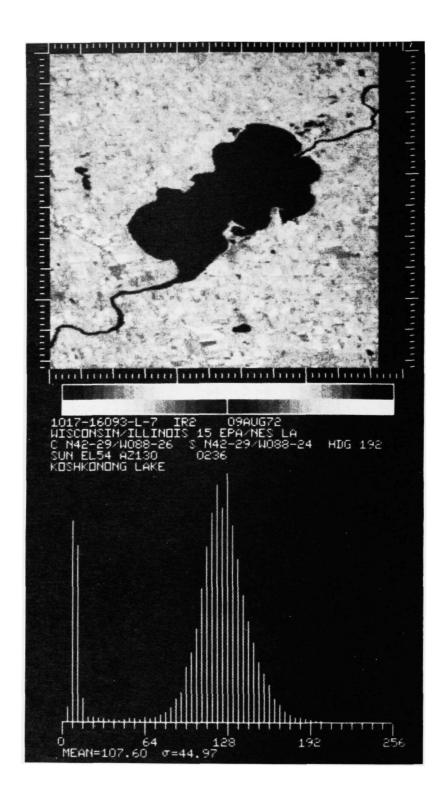


Figure 19. An extracted section of LANDSAT-1 MSS Frame 1017-16093. Lake Koshkonong, the Rock River, several small lakes and land features are evident. A histogram of the section, seen below the image, displays the range of DN values contained within the section. Water DN values cluster toward the lower end of the scale.

the unwanted background, leaving just the water features. Figures 20 and 21 were created by multiplication with a binary mask produced by setting all IR2 DN values of 28 or lower to a value of one. Images constructed from the IR1 and IR2 would be similar, showing only variations in the spectral signature for the water, and therefore in their pixel DN histograms.

A final cleanup is done by upgrading the binary mask prior to multiplying all of the bands. This is done by eliminating all of the smaller water bodies, streams, and swamp features which may be present. After the final cleanup and examination of a test multiplication, the mask is used on all of the bands for Lake Koshkonong. The pictorial expression of the final cleanup for the four spectral bands is depicted in Figure 22.

The concatenation technique is a very convenient method for summarizing the areal aspects of data extracted from the CCT's. Unlike line-printer copy, areal coverage afforded for several different lakes can be depicted in one simple photograph ($\underline{e}.\underline{g}.$, Figure 23). Differences among the lakes in Figure 23 are not apparent because the range of IRs DN values is very small, and no effort has been made to enhance the images.

The VICAR photographic products displayed up to this point serve mainly to aid the investigator in the extraction of digital data from the CCT's. Typical numeric output from the system includes pixel counts, DN means and standard deviations for each of the four MSS bands, and histograms of the DN distributions. Pertinent data extracted from the example, Lake Koshkonong, are listed in Table 11.

TABLE 11. DESCRIPTIVE STATISTICS OF LAKE KOSHKONONG MSS DATA EXTRACTED FROM FRAME 1017-16093 CCT'S

		LANDSAT-1	MSS BANDS	
	Green	Red	IR1	IR2
DN Mean DN Standard Deviation	46.85 1.814	31.15 2.446	27.95 2.933	10.08 2.890
Pixel Count	9,247	9,247	9,247	9,247

The DN values are used in determining correlations with ground ($\underline{i.e.}$, water) truth, developing regression models for selected lake trophic indicators and trophic state, and for image enhancement.

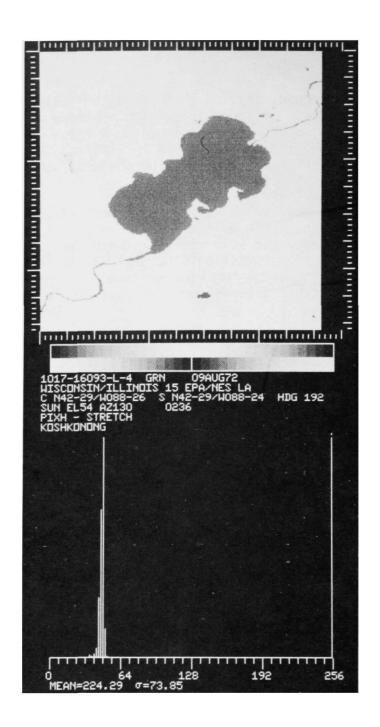


Figure 20. First-stage MSS Band 4 (GRN) cleanup picture of Lake Koshkonong. This picture was created by multiplying the Band Four scene equivalent of Figure 19 by the binary mask. All pixels corresponding spatially to IR2 pixels with DN values greater than 28 have been multiplied by zero, and thereby removed from the scene. The Rock River and miscellaneous water bodies still have to be eliminated.



Figure 21. First-stage MSS Band 5 (RED) cleanup picture of Lake Koshkonong. This picture was created by multiplying the Band Five scene equivalent of Figure 19 by the binary mask. All pixels corresponding spatially to IR2 pixels with DN values greater than 28 have been multiplied by zero, and thereby removed from the scene.

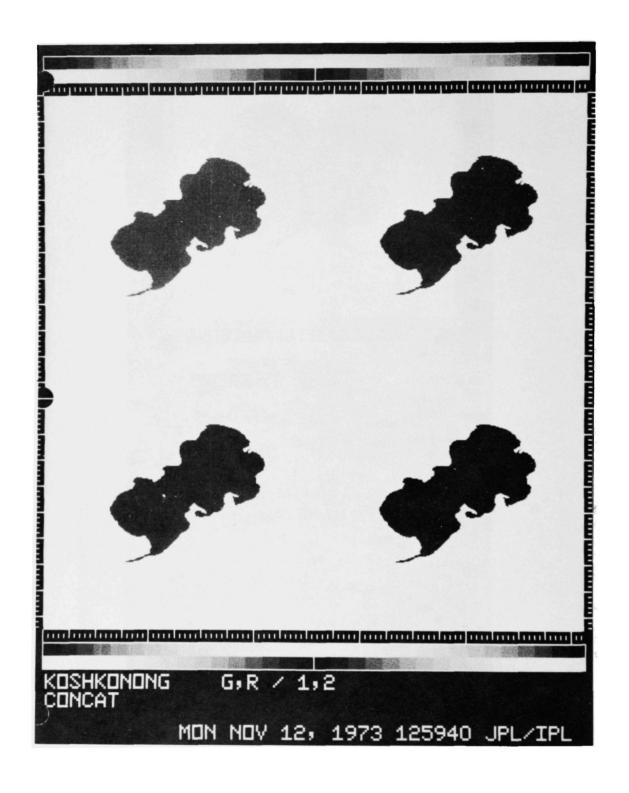


Figure 22. Four band (GRN, RED, IR1, IR2) concatenation of Lake Koshkonong after final cleanup. All of the unwanted land and water body pixels have been eliminated.

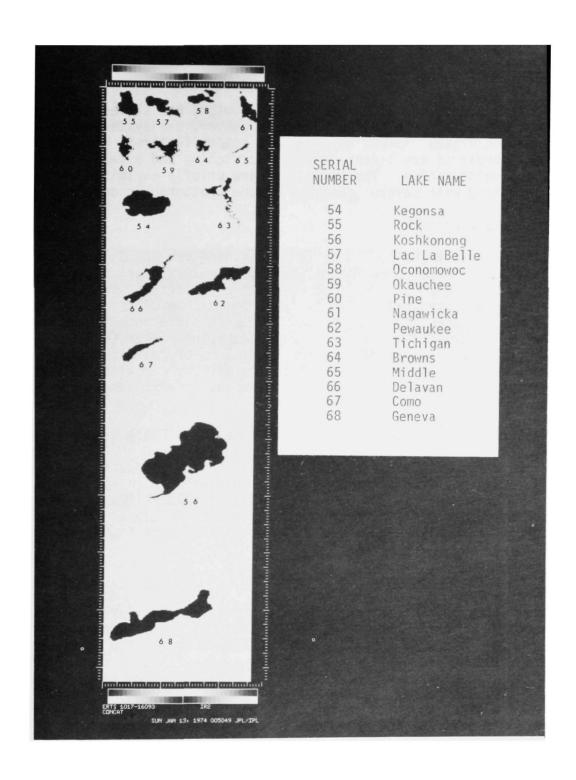


Figure 23. IR2 concatenation of 15 lakes extracted from LANDSAT-1 MSS Frame 1017-16093. The lake images are all reproduced at the same scale. However, they have not been skewed to correct the geometric distortion induced by the earth's rotation.

DIGITAL IMAGE ENHANCEMENT TECHNIQUES

Up to this point, the VICAR photographic output has served as an aid in the extraction of lake MSS DN values. However, the system can also enhance the digital images to bring out latent features. Two methods commonly employed are linear contrast stretching and a technique which utilizes color ratios. The techniques are briefly explained in this section along with several examples of the photographic output.

Color Ratio Technique

The color ratio technique consists of dividing the MSS DN values of one LANDSAT-1 band by another LANDSAT-1 band, pixel by pixel (i.e., data point by data point). Water colors which are difficult to discriminate generally have spectral reflectivity curves with similar but not identical slopes (Blackwell and Boland, 1974). The difference in the curve slopes will form the basis of the discrimination rather than absolute reflectivities. Application of the digital color ratio technique between selected bands will normalize the data by removing the common brightness components and will tend to emphasize differences due to slope.

The digital image of Lake Koshkonong (Frame 1017-16093) was enhanced using the ratio technique and subsequently reproduced in the form of a concatentation (Figure 24). Compare the enhanced images with Figure 22. It is readily apparent that considerable differences in lake color exist, particularly in the GRNRED, GRNIR1, and REDIR1 images. These ratios appear to merit further consideration. Additional information concerning ratio techniques and their applications is found in Billingsley and Goetz (1973).

Linear Contrast Stretching Technique

Another technique for detecting MSS color differences involves the enhancement of digital contrast of selected MSS bands through a "stretching" process. As is evident in Figure 18-23, the images of Lake Koshkonong are of very low contrast and essentially featureless. This is a consequence of the restricted DN value-range present for the lake in all MSS bands. An expansion of the lake's DN ranges to fill the entire black to white range (0 to 255) by linear expansion will enhance the contrast and bring out latent features. Stretching in the digital domain has the advantage that it does not suffer from the toe and shoulder saturations encountered with photographic stretching (Billingsley and Goetz, 1973).

The contrast stretch was performed on Lake Koshkonong data extracted from two LANDSAT-1 MSS frames (1017-16093, 9 August 1972; 1036-16152, 28 August 1972). The results are presented as Figures 25 and 26. The very strong banding effect is an artifact created by an inherent defect

in the MSS system. A comparison of the lake images suggests that the MSS is capable of monitoring spatial-temporal changes in lakes. A scarcity of ground truth precludes a full interpretation of the physical significance of the patterns. This is one area in need of additional investigation.

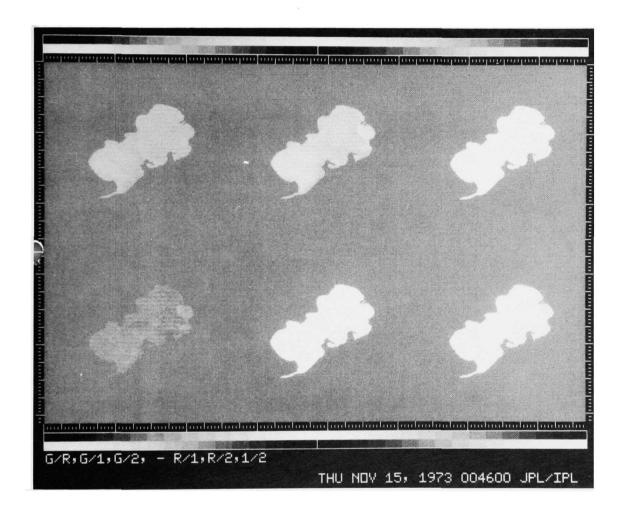


Figure 24. Lake Koshkonong image enhancement using six LANDSAT-1 MSS ratios. The ratios are, scanning from the top row left, GRNRED, GRNIR1, GRNIR2, REDIR1, REDIR2, IR1IR2. Differences in lake color are particularly evident among the GRNRED, GRNIR1, and REDIR1 ratios. The MSS data were extracted from Frames 1017-16093 (9 August 1972). Compare with Figure 22.

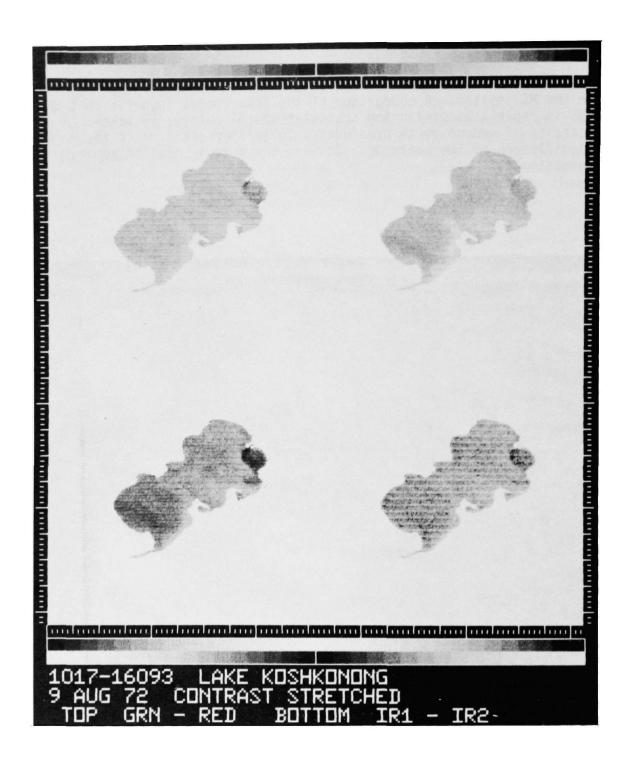


Figure 25. Contrast stretched images of Lake Koshkonong. Frame 1017-16093 recorded by the LANDSAT-1 MSS on 9 August 1972. Upper row, left to right: GRN, RED; lower row, left to right: IR1, IR2. The banding or striping is an artifact.

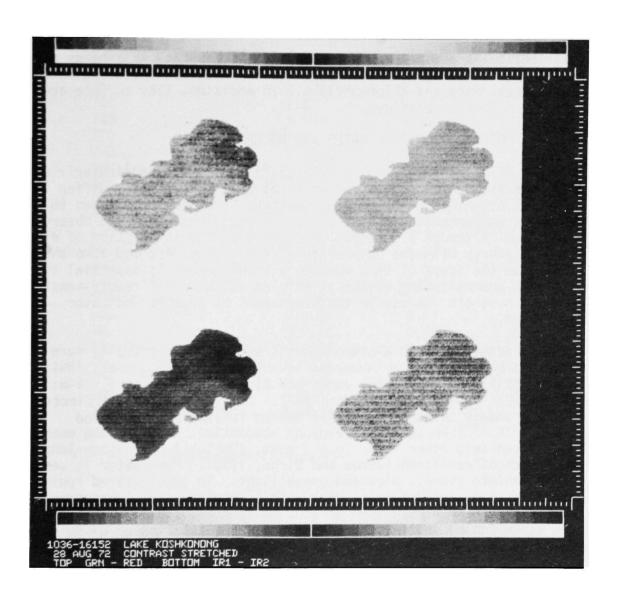


Figure 26. Contrast stretched images of Lake Koshkonong. Frame 1036-16152 recorded by the LANDSAT-1 MSS on 28 August 1972. Upper row, left to right: GRN, RED; lower row, left to right: IR1, IR2. Compare with Figure 25.

SECTION VI

LANDSAT-1 MSS-TROPHIC INDICATOR RELATIONSHIPS

This section is devoted to the evaluation of MSS data as a means of estimating the magnitude of trophic state indicators including Secchi disc transparency and chlorophyll \underline{a} . In addition, lake surface area estimation is also examined.

OPTICAL PROPERTIES OF PURE WATER AND NATURAL WATERS

It is readily apparent, even to the casual observer, particularly if he or she is looking downward from an aircraft, that lakes differ in color and brightness. Many investigations have been undertaken to develop a comprehension of the processes which result in the observed phenomena. Although a detailed discussion of the interaction of electromagnetic energy with the components of the hydrosphere and atmosphere is outside the scope of this report, a brief survey is essential to gain some understanding of the principles which permit remote sensing and yet constrain its use in the assessment of trophic indicator magnitudes.

The interaction between electromagnetic energy and chemically pure water has been studied by numerous investigators (e.g., Ewan, 1894; Sawyer, 1931; Collins, 1925; James and Birge, 1938; Hulburt, 1945; Raman, 1922; Dawson and Hulburt, 1937). The transmission of electromagnetic energy through a material medium is always accompanied by the loss of some radiant energy by absorption. Some of the energy is transformed into other forms (e.g., heat, chemical) or to some longer wavelength of radiation (James and Birge, 1938). Pure water is very transparent to violet, blue and green light. In the infrared region, the extinction coefficient is high with a complementary low degree of transmission (Table 12). The absorption spectral characteristics of pure water can be modified greatly through the addition of dissolved and particulate materials.

The absorption spectra of natural waters ($\underline{e}.\underline{g}$., lake and ocean) have been studied in detail by Jerlov (1968), Duntley (1963), Atkins and Poole (1952). Birge and Juday (1929, 1930, 1931, 1932), and Juday and Birge (1933), to mention a few. Hutchinson (1957) has summarized the more important attempts to elucidate the interactions of light with natural waters, particularly in regards to lakes.

The attenuation of electromagnetic radiation in lake waters is a consequence of the relatively unselective effect of suspended particulate materials and the highly selective effect of dissolved coloring matter,

TABLE 12. OPTICAL PROPERTIES OF PURE WATER (ROOM TEMPERATURE)^a

Wavelength (nanometers)	Extinction Coefficient	Percentile Absorption	Refractive Index		
820 (infrared)	2.42	91.1			
800	2.24	89.4			
780	2.31	90.1			
760	2.45	91.4	1.329		
740	2.16	88.5			
720	1.04	64.5			
700	0.598	45.0			
680 (red)	0.455	36.6			
660	0.370	31.0	1.331		
640	0.310	26.6			
620 (orange)	0.273	23.5			
600	0.210	19.0			
580 (yellow)	0.078	7.0	1.333		
560	0.040	3.9			
540	0.030	3.0			
520 (green)	0.016	1.6			
500	0.0075	0.77			
480	0.0050	0.52	1.338		
460 (blue)	0.0054	0.52			
440	0.0078	0.70			
420	0.0088	0.92	_		
400 (violet)	0.0134	1.63	1.343		
380 (ultraviolet)	0.0255	2.10			

^aAdapted from Hutchinson (1957).

usually of organic origin, on the electromagnetic spectrum. The dissolved matter absorbs strongly in the violet and blue wavelengths, moderately in the middle wavelengths (e.g., green), and much less strongly at longer wavelengths (Hutchinson, 1957). When the dissolved materials are present in small quantities, the water will be most transmissive in the green wavelengths. Lake waters with large amounts of dissolved substances will be more transmissive in the orange and red wavelengths than in the shorter wavelengths. However, the transmission of the red and orange light is still greater in pure water than in water containing particulate and/or dissolved materials. As water transparency diminishes, the detectable electromagnetic energy will be of progressively longer wavelength, at increasingly shallower depths (Hutchinson, 1957).

Scherz, et al. (1969) have investigated the total reflectance (surface reflectance plus volume reflectance) curves of pure water and natural waters under laboratory conditions using a spectrophotometer. The resulting curve for distilled water is shown in Figure 27. They reported that the addition of dissolved oxygen, nitrogen gases, and salts (e.g., NaCl, Na $_2$ SO $_4$, Na $_3$ PO $_4\cdot$ H $_2$ O) had no apparent effect on the reflection curve. However, water from lakes in the Madison (Wisconsin) area had reflectance curves that both differ from the distilled water curve and from each other. Scherz, et al. suggest that the differences can be attributed to the presence of different algal organisms. Filtration of the lake waters produced similar reflectance curves, though different from that of pure water (Figure 28).

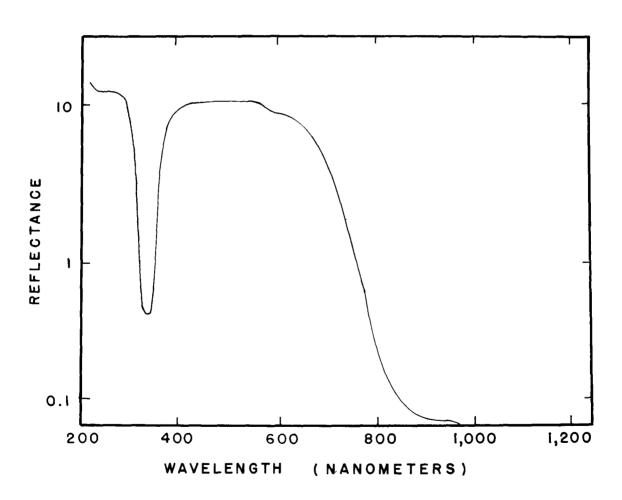
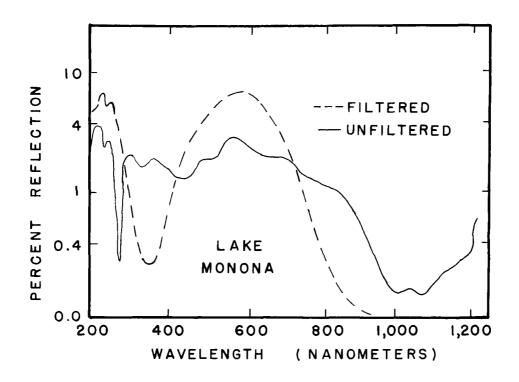


Figure 27. Reflectance curve for distilled water. Adapted from Scherz, et al. (1969).



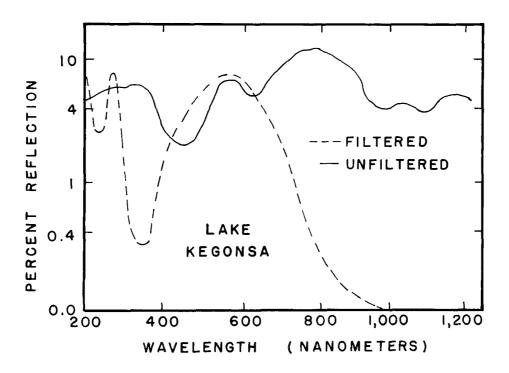


Figure 28. Reflection characteristics of filtered and unfiltered water samples from two Wisconsin lakes in the area of Madison. Adapted from Scherz, et al. (1969).

The color of a lake is the color of the electromagnetic energy backscattered from the lake body to the sensor. Lake color ranges from the blue of pure water through greenish blue, bluish green, pure green, yellowish green, greenish yellow, yellow brown, and clear brown (Hutchinson, 1957). It is a common practice to record lake color on an empirical scale such as the so-called Forel-Ule color scale, originally devised by Forel (1889) and subsequently modified and extended by Ule (1892). Lake color need not be, and is usually not the same as, the color of the lake water*.

Lakes which are blue in color lack appreciable quantities of humic materials and colored materials in suspension (e.g., phytoplankton). The bluer the lake color, the smaller the amount for free-floating organisms contained in the water (Ruttner, 1963). Water with high plankton content possess a characteristic yellow-green to yellow color. The characteristic color may not be apparent due to masking by other materials (e.g., suspended sediments). Ruttner (1963) suggested that

A lake with very transparent and dark blue, blue-green, or green water is always oligotrophic. On the other hand, eutrophic lakes always have a relatively low transparency and are yellow-green to yellow brown in color; but the determination of these optical properties alone will not establish the productivity type, for the turbidity can be of inorganic origin, and the color can come from humic substances.

Seston color, attributable to the reflection spectra of suspenoids of microscopic or submicroscopic size, is often observed in highly productive lakes. Lakes containing large quantities of suspended inorganic matter (e.g., silt) may acquire a characteristic seston color, but in most cases the color is related to large concentrations of phytoplanktonic organisms (Hutchinson, 1957).

Peripheral Effects

The character of the electromagnetic energy impinging on the remote sensor, the LANDSAT-1 MSS in this case, has been shaped through interaction with numerous environmental phenomena.

The earth's atmosphere has a pronounced effect on the solar spectrum. The spectral distribution of the sun's radiation at the outer edge of the atmosphere and the normal energy distribution at the earth's surface

^{*} Welch (1952) defines water color as "...those hues which are inherent within the water itself, resulting from colloidal substances or substances in solution" (i.e., true color). The platinum-cobalt scale (Hazen, 1892) has found favor in the United States for the determination of water color.

are illustrated in Figure 29. Atmospheric conditions ($\underline{e}.\underline{g}$., degree of cloudiness; presence of fog, smoke, and dust; amount of water vapor) affect the degree of insolation attenuation. Weather conditions strongly affect the distribution of energy between sunlight and skylight (Piech and Walker, 1971), contributing a degree of uncertainty in water quality assessment through remotely sensed color measurements. Hulstrom (1973) has pointed out the adverse impact that cloud bright spots can have on remote sensing techniques which utilize reflected energy.

The degree of scattering and absorption imposed on the return signal from water bodies is related to the atmospheric transmittance and can result in changes in lake color when sensed at aircraft high flight and satellite altitudes. The attenuated return signal is also contaminated by electromagnetic radiation from the air column (path radiance). Rogers and Peacock (1973) have reported that solar and atmospheric parameters have a serious adverse impact on the radiometric fidelity of LANDSAT-1 data. Path radiance was found to account for 50 percent or more of the signal received by the MSS when viewing water and some land masses.

The magnitude of the adverse atmospheric effects can be reduced, though not completely eliminated, by using imagery or digital data collected on clear, cloudless days. This is the approach used in this investigation.

The LANDSAT-1 spacecraft passes over the same point on the earth at essentially the same local time every 18 days. However, even though the time of passover will remain essentially the same throughout the year, solar elevation angle changes (Figure 30) cause variations in the lighting conditions under which the MSS data are obtained. are due primarily to the north or south seasonal motion of the sun (NASA, 1972). Changes in solar elevation angle produce changes in the average scene irradiance as seen by the sensor from space. The change in irradiance is influenced both by the change in the intrinsic reflectance of the ground scene and by the change in atmospheric backscatter (path radiance). The actual effect of changing solar elevation angle on a given scene is very dependent on the scene itself (NASA, 1972). For example, the intrinsic reflectance of sand is significantly more sensitive to changing solar elevation angle than are most types of vegetation (NASA, 1972). The effects of changing solar elevation angle are of particular importance when comparing scenes taken under significantly different angles. The use of color ratios in lieu of raw data values may be of value in reducing the magnitude of the solar angle induced effects by normalizing the brightness components. This is the approach used in this investigation.

A portion of the radiation impinging on the lake surface will be reflected. The percentage of surface-reflected energy is a strong function of the angle of incidence (Figure 31). Surface roughness is

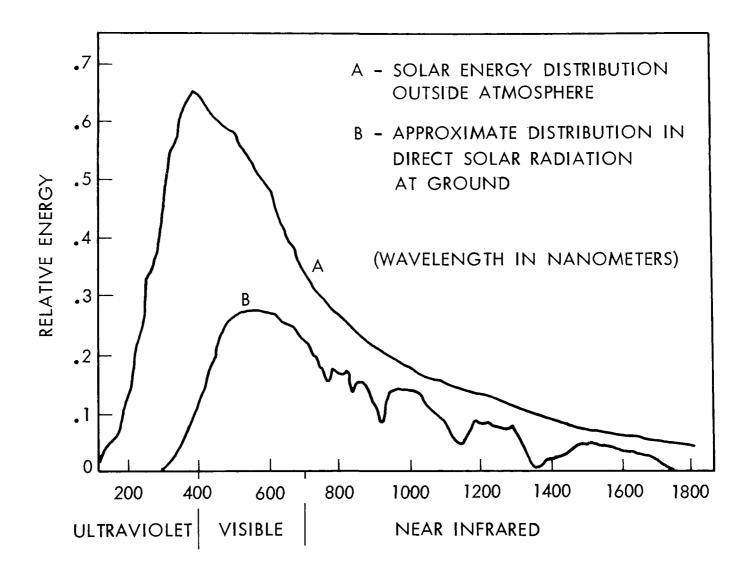


Figure 29. Spectral distribution of solar energy. Adapted from Hutchinson (1957).

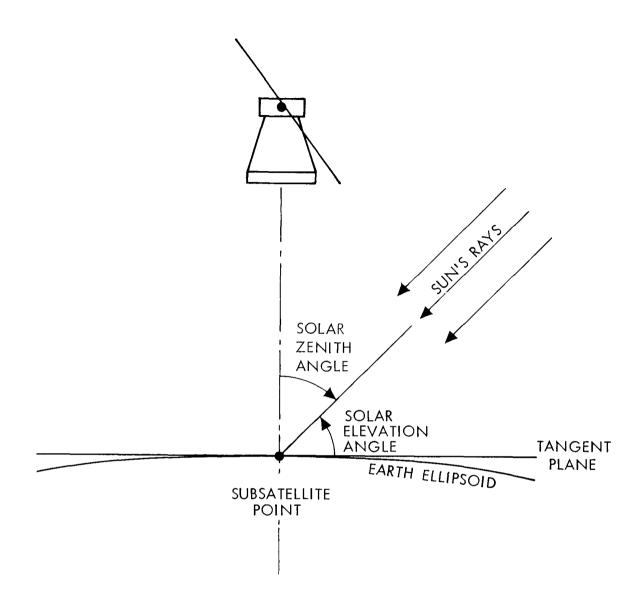


Figure 30. Solar zenith and solar elevation relationship. Source NASA (1972).

known to have an effect on the percentages of light reflected and refracted at the interface (Jerlov, 1968). However, the effect of surface is negligible in estimating total radiation entering a water body when the solar elevation angle is greater than 15 degrees (Hutchinson, 1957).

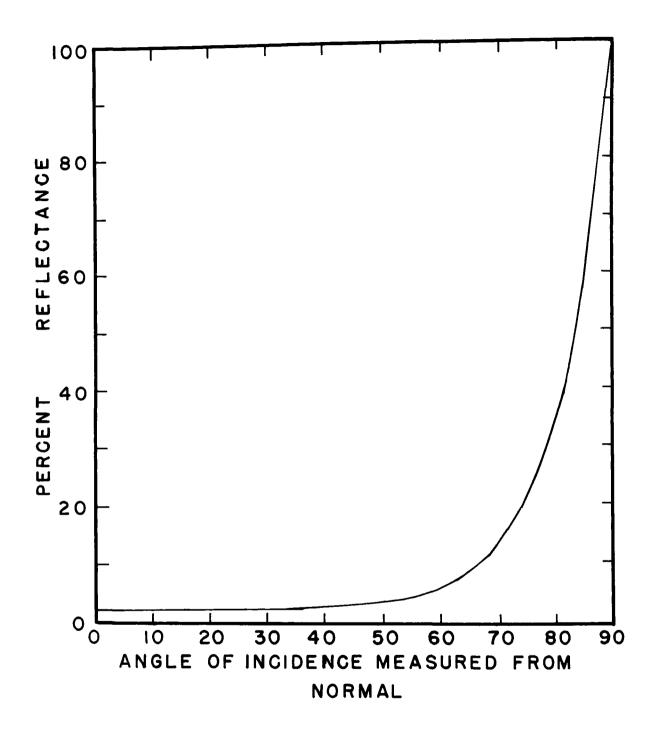


Figure 31. Percentage reflectance of the air-water interface as a function of the angle of incidence measured from normal direction. Values are for unpolarized light only. Source, Piech and Walker (1971).

The light reflected from the interface is composed of diffuse light from the sky (skylight) and specularly reflected sunlight. Specular reflection areas contained in a scene are of little value in most water studies, the possible exception being the determination of surface roughness. The specularly reflected radiation exceeds, by several orders of magnitude, the reflected energy emanating from beneath the water surface (Curran, 1972). Surface reflected skylight, containing no water quality color information, can compose from 10 percent of the return signal on a clear day to 50 percent on a cloudy day (Piech and Walker, 1971). The surface reflected skylight not only increases the apparent reflectance from the water body (volume reflectance), but also affects the shape of the reflectance curve.

An electromagnetic wave impinging on the surface of a lake decomposes into two waves, one of which is refracted, proceeding into the aquatic medium and a second wave which is reflected back to the atmosphere (Jerlov, 1968). The wave entering the water is refracted as it passes through the air-water interface according to Snell's Law which may be expressed as:

$n = \sin i/\sin r$

where (i) is the angle of incidence, (r) is the angle of refraction, and (n) is the refractive index, which for water is approximately 1.33 (see Table 12).

Most of the electromagnetic energy entering a lake is attenuated through the process of absorption. Although only a small percentage (less than 3 percent; Davis, 1941) of the incident energy is backscattered from the lake water volume, this light (volume reflectance) is the focus of interest in remote sensing of water quality investigations. Its spectral characteristics have been shaped by the materials found in the lake waters (dissolved and suspended materials, plankton, aquatic macrophytes, and air bubbles).

The lake bottom characteristics (color and composition) will also affect the intensity and/or the spectrum of the volume reflectance in settings where water transparency permits the reflection of a significant amount of radiation from the bottom materials. In studies involving the estimation of water depth or the mapping of bottom features, it is essential that the lake bottom be "seen" by the sensor. Bottom effects are capitalized upon and put to a beneficial use.

However, in this investigation, bottom effects are considered to be an undesirable peripheral effect. A sensor with the capabilities of the LANDSAT-1 MSS is not able to "see" much deeper into a lake than Secchi disc depth. The Secchi disc transparency of the selected NES lakes is, in most cases, relatively small when compared to the mean depth of each lake The assumption is made, as a first approximation, that bottom

effect is relatively insignificant when considering each of the selected lakes as an entity.

It is evident that many factors influence the intensity and spectral characteristics of the electromagnetic radiation which is collected by the sensor. A peripheral effect, desirable in one study, may have a deleterious effect in another study. Absolute quantification of remotely sensed phenomena requires that all of the effects be accounted for in the return signal. Although the approach used here to reduce the magnitude of the undesirable peripheral effects might be criticized as simplistic or naive, it does serve as a starting point in the investigation of lake color-trophic indicator relationships using satellite-borne sensors. Although the results may be of a semi-quantitative nature, general trends in the data may be of value in lake classification studies.

RELEVANT REMOTE SENSING LITERATURE

A wealth of literature exists relating to the theoretical, applications, and instrumentation aspects of remotely sensed water quality. The advantages and limitations of remotely assessing water quality have been discussed by many investigators (Robinove, 1965; Hom, 1968; Kolipinski and Higer, 1968; Clarke, 1969; Fortunatov, 1957; Kiefer and Scherz, 1970, 1971; Conrod and Rottweiler, 1971; Gramms and Boyle, 1971; Scherz, 1971; Clapp, 1972; Wezernak and Polcyn, 1972; Colwell, 1973).

Wezernak and Polcyn (1972) examine the question of making eutrophication assessments from the standpoint of current remote sensing technology. They suggest, that of some 16 factors which often serve as measures of eutrophication (Table 13), several can be remotely sensed using operational and near-operational systems. The parameters include chlorophyll, colored water masses, suspended solids, transparency, aquatic macrophytes, and algal blooms. In addition, remote sensing technology can also provide an economic method of obtaining morphometric and land use information (e.g., shoreline development, lake surface area, and cultural impact) which has a direct bearing on the trophic state of a water body.

Most of the water-oriented investigations have focused on the oceanic environment and point source pollution of fresh waters using aerial photography (black and white, color, black and white infrared, color infrared, multispectral). Investigations utilizing airborne multispectral scanners and lasers are becoming increasingly common. Many aspects of water quality have been examined using remote sensors mounted on non-satellite platforms; pertinent aspects are discussed below.

Remotely determined estimates of chlorophyll levels in natural waters (in situ) have been made by several investigators (Clarke, et al., 1969,

TABLE 13. INDICES COMMONLY USED TO ASSESS EUTROPHICATION^a

Standing crop of algae and aquatic plantsb Amount of suspended solidsb Volume of algae Chlorophyll levelsb Number of algal bloomsb Transparencyb Plant regression^b Photosynthesis Primary production Aquatic plant nutrient content Hypolimnetic oxygen concentrations Sediment composition Dissolved solids Conductivity Nutrient concentrations Cation ratio (Na + K) / (Mg + Ca)

1970; Mueller, 1972; Curran, 1972; White, 1969; Atwell and Thomann, 1972; Arvensen, et al., 1971; Bressette and Lear, 1973). Curran (1972) reported a strong correlation between wavelength-dependent albedo ratios, made from measurements collected by high-flight aircraft, and phytoplankton chlorophyll concentrations, from satellite altitudes, to an uncertainty of 0.1 mg/m³. Blackwell and Billingsley (1973) have utilized multispectral photography in conjunction with digital computer enhancement techniques to detect algae. Crew (1973) has mapped and identified an algal species in Clear Lake (California) employing an airborne multispectral scanner.

Aerial photography, utilizing color and color-infrared films, is a relatively simple technique that has demonstrated utility in mapping aquatic macrophytes (Kolipinski and Higer, 1968; Kiefer and Scherz, 1971) and shallow water benthos (Kelly and Conrod, 1969). Photographs are used routinely to map wetlands (Anderson and Wobber, 1973). It is an accepted practice to use aerial photographs in the delineation and enumeration of lakes (Minnesota Department of Conservation, 1968).

Remote sensors are employed to estimate water turbidity (Crew, 1973; Schmer, et al., 1972, Williams and Samol, 1968). Some investigators (Brown, et al., 1972; Specht, et al., 1973) have used remote sensors to

a Adapted from Wezernak and Polcyn (1972).
Index can be remotely sensed using operational or near-operational sensors.

estimate water depth and bottom topography. Dybdahl (1973) has demonstrated an airborne remote sensing technique for the determination of dissolved oxygen levels in fresh water.

Relevant LANDSAT-1 Investigations

Prior to the insertion of LANDSAT-1 into its near-polar orbit, investigators interested in assessing and monitoring the earth's natural resources from satellite altitudes were restricted to using poorly suited satellite-borne sensors. The spacecraft were largely equipped with sensors designed for studies oriented toward the atmosphere or, in some cases, the ocean.

The length of the list of NASA-designated LANDSAT-1 principal investigators -- some 300 are found on it (Data Users Handbook, Appendix M, February, 1972) -- suggests that there is a great interest in assessing the advantages and limitations of remotely sensing the earth's resources from satellite altitudes. The major focus, as evidenced by project titles, is on the terrestrial environment; less than 10 percent of the investigations relate to water quality and the majority of these concentrate on the oceanic environment and the Laurentian Great Lakes. Some of the water-related investigations bear mentioning.

Wezernak and Polcyn (1972) have detected a municipal-industrial waste disposal in the New York Bight. Lind and Henson (1973) and Lind (1973) have discovered and documented a pollution plume emanating from a mill located on the shore of Lake Champlain. It is apparent from a literature review that the detection of large turbidity plumes and turbidity related patterns is easily accomplished using the LANDSAT-1 multispectral scanner-generated imagery (e.g., Watanabe, 1973; Klemas, 1973; Carlson, 1973; Wright, Sharma, and Burbank, 1973; Pluhowski, 1973; Coker, Higer, and Goodwin, 1973; Kritikos, Yorinks, and Smith, 1973).

Enhanced and density-contoured imagery appears to permit water depth estimation to a depth of at least five meters in the clear waters around the Bahama Islands (Ross, 1973). Polcyn and Lyzenga (1973), using digital processing techniques on an LANDSAT-1 MSS frame taken over the Bahama Islands, have mapped shallow water features and calculated water depths to five meters. The waters in the area are known for their clarity and are conducive to remote sensor mapping activities.

Hidalgo, et al. (1973) have identified large mats of duckweeds (Lemnaceae) on Lake Pontchartrain and surrounding bayous and swamps in southeastern Louisiana. Seasonal changes have been detected. Strong (1973) has noted algal blooms in Utah Lake (Utah) and in Lake Erie.

Barr (1973) has mapped a total of 2,272 water bodies in Saline County (Kansas) where a topographic map (1955) indicates 1,056. A preliminary comparison of imagery and maps indicates that bodies larger than four

hectares (10 acres) are consistently detectable. Most water bodies between about two to four hectares are usually detectable; water areas less than two hectares are occasionally resolved. Erb (1973), using nine-inch-square transparencies, has determined that ponds as small as one hectare are detectable within forested areas. The initial findings of Chase, Reed, and Smith (1973) indicate that water bodies of about 0.5 hectares are detectable under fair conditions (haze and 70 percent cloud cover); distortion of lake size, shape, and orientation is minimal. The benefits of using LANDSAT-1 imagery to enumerate lakes have been demonstrated by Reeves (1973) and Work, et al. (1973).

Yarger, et al. (1973), using electronically sliced imagery, have found a good correlation between suspended load (predominantly composed of inorganic materials) and film densities of two federal reservoirs in Kansas. Bowker, et al. (1973) reported that there appears to be a positive correlation between particulate count and chlorophyll level in Lower Chesapeake Bay. A rough correlation exists between suspended sediments and MSS imagery, but no correlation is apparent for the chlorophyll bearing portion of the load. Szekielda and Curran (1972) indicate that a correlation exists between chlorophyll and LANDSAT-1 MSS imagery (green band) in the general area of St. John's River estuary in Florida.

Rogers and Smith (1973), reporting on their investigation of six lakes in Michigan, suggested that deep water and shallow water can be separated by a trained photo-interpreter using reflectance printout gray-scales or a cathode tube monitor. Lakes were best discriminated in band seven (IR2) due to the strong contrast between land and water (Rogers and Smith, 1973). Classifying lake eutrophication on the basis of algal scum or macrophytes in shallow water appears to be a "straight-forward" matter with LANDSAT-1 MSS data. Estimations of water depth may be possible in some lake areas where there are extensive shallows and the water is clear and unencumbered with vegetation (early spring).

TROPHIC INDICATOR ESTIMATION

Although the LANDSAT-1 provides 18-day cyclic coverage, a point stressed in many of the reports and articles written on the spacecraft, obtaining good coverage in the study area was (and still is) a major problem. This is a problem shared with many other investigators. On numerous dates of coverage, cloud cover was excessive (greater than 10 percent) and on several occasions, when the weather conditions were conducive to monitoring the lakes, one or more of the MSS bands were either missing or rated as poor. The formation of ice cover on the study lakes, lasting for several months, further reduced the opportunity to obtain repetitive coverage.

A search of the LANDSAT-1 MSS imagery and CCT's for the study area (Minnesota, Wisconsin, Michigan, New York) for the period from August, 1972 through July. 1973, resulted in the selection of the frames found in Table 14. The lakes which were examined in this investigation are listed in Table 15. Several additional frames were not included because they contain less than three lakes sampled under the National Eutrophication Survey Program. Frames from the 1973 calendar year were not selected if LANDSAT-1 MSS coverage was not available for the 1972 sampling year.

TABLE 14. LANDSAT-1 MSS FRAMES

Frame Number	Date	Area	Number of Lakes
1017-16091 1017-16093	9 August 1972 9 August 1972	Eastern Wisconsin Southeastern Wisconsin	5 ^b 15 ^b
1036-16152	28 August 1972	South central Wisconsin	6
1323-16094 1323 - 16100	11 June 1973 11 June 1973	Eastern Wisconsin Southeastern Wisconsin	4 ^b 23 ^b
1359-16091 1359-16094	17 July 1973 17 July 1973	Eastern Wisconsin Southeastern Wisconsin	4 ^b 18 ^b
1022-16373	14 August 1972	Central Minnesota	12
1075-16321	6 October 1972	Central Jinnesota	15
1077-16431	8 October 1972	West central Minnesota	10
1309-16325	28 May 1973	Central Minnesota	13
1345-16322	3 July 1973	East central Minnesota	14
1346-16381	4 July 1973	Central Minnesota	8
1027-15233	19 August 1972	Northwestern New York	7
1080-15180	11 Qctober 1972	Northwestern New York	5

^aLakes extracted from frames recorded on the same flightline and data bare pooled to increase sample size. Some of the lakes appear in both frames; $\underline{e} \cdot \underline{g}$, Lake Winnebago is

often split between two frames.

TABLE 15. DATES OF LANDSAT-1 COVERAGE

					LAN	DSAT	-1 C	over	a ge	Data			
Lake Name and Serial Number					1972				1973				
		9 Aug	14 Aug	19 Aug	28 Aug	6 Oct	8 Oct	11 Oct	28 May	11 June	3 July	4 July	17 July
Shawano Butte des Morts Poygan Winnebago Green Beaver Dam Kegonsa Rock Koshkonong Lac la Belle Oconomowoc Okauchee Pine Nagawicka Pewaukee Tichigan Browns Middle Delavan Como Geneva Mendotaa Mononaa Waubesa	46 47 48 49 51 53 54 55 56 57 58 60 61 62 63 64 65 66 67 68 109 110	X			X X X X					X			X
Darling Carlos Le Homme Dieu Minnewaska Nest Green Wagonga Clearwater Maple Cokato Buffalo Carrigan	16 17 18 19 20 21 22 23 24 25 26 27		X X X X X X X X X			X X X X	X X X X X X		X X X X		X X X X	X X X X	

TABLE 15. DATES OF LANDSAT-1 COVERAGE (continued)

					LAN	DSAT	-1 C	over	age	Data			
I I Nama and			1972									73	
Lake Name and Serial Number		9 Aug	14 Aug	19 Aug	28 Aug	6 Oct	8 Oct	11 Oct	28 May	11 June	3 July	4 July	17 July
Silver Minnetonka Forest White Bear St. Croix Spring Pepin Madison Sakatah Winona Trace Calhoun Big Stone Zumbro Cottonwood	28 29 30 31 32 33 34 35 36 101 102 103 104 105 111		X			X X X X X X X	X X X		X X X X X X		-X X X X X X	X	
Conesus Canandaigua Keuka Seneca Cayuga Owasco Cross Oneida Canadarago	91 92 93 94 95 96 97 106 107			X X X X X X				X X X X					

^aThis lake fell outside the scope of the National Eutrophication Survey Program, but was included here because it is a well-known lake on which considerable eutrophication research has been conducted.

Every effort was made to get MSS coverage which was concurrent with the collection of the ground truth by the helicopter-borne field teams. This goal was achieved in the case of only one frame (1080-151800). Unfortunately the number of NES sampled lakes contained in the frame is too small to incorporate into a regression model. The dates on which ground truth was collected from the study lakes are found in Appendix B.

Ideally, the estimation of the magnitude of trophic state indicators should be done using concurrent data to derive the maximum benefit. However, in this investigation it was necessary to use what may be called "near concurrent" ground truth which was collected several days before or after satellite overflight. Nevertheless, models developed from such a temporal arrangement are of some value in illustrating general relationships existing between the MSS data and ground truth.

Estimations of the magnitude of two trophic state indicators (chlorophyll a and Secchi disc transparency), using LANDSAT-1 MSS data and NES collected ground truth, are demonstrated in the remainder of this section using two of the frames in Table 14. The frames, 1017-16091 and 1017-16093, are treated as one frame to increase the lake sample size. The frames are in juxtaposition on the same flightline, were recorded on the same day, and prior to Goddard Space Flight Center Processing, were elements in a continuous strip. The frames were selected on the basis of temporal proximity to NES ground truth dates, the quality of the MSS data (good MSS band ratings, little cloud cover and haze), and the presence of a relatively large number of NES lakes (N=20). An examination of Table 15 indicates that coverage is available for the same 20 lakes on two other occasions.

MSS frames from 12 different dates and three states (Minnesota, Wisconsin, and New York) are examined in this report. The fragmentary LANDSAT-1 coverage, very evident in Table 15, makes it difficult to give a coherent demonstration of the MSS's capabilities and limitations. In an attempt to reduce the magnitude of the problem, the author has taken the liberty of focusing on the Wisconsin frames and relegating the other frames to Appendix D. The appendix is divided into a series of subappendices (one for each LANDSAT-1 date) which contain descriptive statistics of the MSS data, LANDSAT-1 MSS estimates of lake area, area ratios, lake concatenations, three-dimensional color ratio models, and regression models.

Data reduction was accomplished on the Oregon State University CDC 3300 computer using the Statistical Interactive Programming System (SIPS). The regression models were developed using the backward selection procedure (Guthrie, et al., 1973). The backward method was selected largely on the basis of its intuitive appeal.

LANDSAT-1 Lake Area Estimation

A straightforward method of estimating the area of an extracted lake involves a summation of the pixel counts in one band (e.g., IR2) and subsequent multiplication by a conversion factor of $0.\overline{48}$ (1 pixel = 0.48 ha = 1.18 ac) to get the area in hectares. The conversion factor used here was obtained from R. J. Blackwell (personal communication. 1973). A comparison of lake area estimations from other sources with LANDSAT-1-derived area values acts as a check to verify that the pixels and their respective DN's are those of the water body under scrutiny. A topographic area/LANDSAT-1 area ratio greater than one indicates that the extracted image is smaller than the area covered by the MSS lake image. A ratio less than one suggests that the extracted image includes wet lands and/or land features. Underestimation of lake size is preferable to overestimation (inclusion of wetland and/or land) in this study. The surface areas of the 20 lakes extracted from Frames 1017-16091 and 1017-16093 are generally within 10% of values derived from U.S.G.S. topographic sheets and publications of the Wisconsin Department of Natural Resources (see Table 16).

Discrepancies between LANDSAT-1 and topographic sheet-derived area estimates may be a consequence of: changes in the lake area since the topographic sheet was constructed; inaccurate delineation of the shoreline on aerial photographs or during the preparation of the sheet; inclusion of wetlands or exclusion of portions of the lake during the preparation of the IR2 binary mask; or failure to use a correct conversion factor.

The estimated lake areas using LANDSAT-1 MSS pixel counts are in good agreement for most of the lakes in Table 16. The very large error for Middle Lake is due to the contiguous nature of the Lauderdale Lakes. The computer extraction process resulted in a sample taken from the area mapped as Middle Lake. Some of the lakes, particularly those which occupy shallow basins, are known to fluctuate greatly in surface area and topographic sheets do not account for the variation.

Adding the 20 lake areas derived from the topographic sources and then comparing the resultant value with the composite LANDSAT-1 MSS lake area value, excluding Middle Lake, results in a ratio of 1.016:1.000. A visual examination of the area ratios for the other frames (see the subappendices of Appendix D) indicates that the MSS can be used to give good estimates of lake surface area when a DN value of 28 is used as the "cutoff" point in extracting the lakes from their terrestrial matrix. The lake area estimation capabilities of the MSS are of value, not only in the study of lakes with established areas, but also in geographic regions for which there is no accurate topographic or aerial photographic coverage.

The photographic products (concatenations), fabricated by the VICAR system, are of immense value in extracting the lake "images" stored on

TABLE 16. AREAL ASPECTS OF 20 NES-SAMPLED LAKES EXTRACTED FROM LANDSAT-1 MSS FRAMES 1017-16091 and 1017-16093.

	Serial	Pixel	LANDSAT-1 Lake	Map Lake	Map Area:
Lake Name	Number	Count	Area (ha)	Area (ha)	LANDSAT-1 Area Ratio
Poygan	47	9,177	4,382.5	4,448.5	1.015
Butte des Morts	48	7,395	3,531.5	3,584.4	1.015
Winnebago	49	114,186	54,529.1	55,730.4	1.022
Green	51	6,613	3,158.0	2,972.9	0.942
Beaver Dam	53	5,162	2,465.1	2,671.0	1.084
Kegonsa	54	2,675	1,277.4	1,099.2	0.861
Rock	55	1,009	481.8	554.8	1.152
Koshkonong	56	9,247	4,415.9	4,241.3	0.961
Lac la Belle	57	944	450.8	452.1	1.003
Oconomowoc	58	652	311.4	317.7	1.015
Okauchee	59	871	415.9	450.8	1.085
Pine	60	56 8	271.3	284.5	1.049
Nagawicka	61	751	358.6	415.2	1.155
Pewaukee	62	1,996	953.2	1,008.9	1.058
Tichigan	63	689	329.0	449.8	1.367
Browns	64	309	147.6	160.3	1.086_
Middle	65	117	55.9	104.8	1.876 ^a
Delavan	66	1,541	735.9	717.9	0.976
Como	67	703	335.7	383.0	1.151
Geneva	6 8	4,543	2,169.5	2,129.5	0.982

^aMiddle Lake is contiguous with Mill Lake and Green Lake; the lakes are commonly referred to as the Lauderdale Lakes. The extraction process resulted in a sample of the area mapped as Middle Lake. The Green Lake of the Lauderdale Lakes is not to be confused with Green Lake (51).

the CCT's. They permit the investigator to examine the extracted lake for geometric fidelity, truncation of the water body, and for the inclusion of other water bodies. The photographic products are superior to output in the form of line printer copy in studies relating to the areal aspects of water bodies.

Secchi Disc Transparency Estimation

Although it is beyond the capabilities of the MSS to directly measure chemical indicators, its areal and spectral resolution permit the detection of phenomena related to eutrophication (such as Secchi disc transparency, chlorophyll a) together with some degree of quantification.

An R-mode Pearson product-moment correlation analysis was made using the MSS data and ground truth collected from the 20 NES lakes in Frames 1017-16091 and 1017-16093. The correlations, based on data means and transformed means, are found in Table 17.

TABLE 17. CORRELATIONS BETWEEN GROUND TRUTH AND LANDSAT-1 MSS DATA (COLORS AND COLOR RATIOS) FOR 20 LAKES IN FRAMES 1017-16091 AND 16093.

	PC1	CHLA	LNCHLA	SECCHI	LNSECCHI
GRN	0.518	0.812	0.718	-0.623	-0.662
RED IR1	0.722 0.807	0.888 0.899	0.860 0.886	-0.788 -0.741	-0.857 -0.866
IR2	0.589	0.680	0.696	-0.492	-0.642
GRNRED	-0.823	-0.821	-0.886	0.865	0.919
GRNIR1 GRNIR2	-0.806 -0.470	-0.777 -0.442	-0.838 -0.521	0.685 0.357	0.803
REDIR1	-0.544	-0.442 -0.476	-0.521	0.357	0.476 0.430
REDIR2	-0.026	0.028	-0.017	-0.156	-0.042
IR1IR2	0.516	0.522	0.474	-0.527	-0.507

Several multiple regression models were developed to predict Secchi disc transparency using MSS colors and color ratios as the independent variables. The use of color ratios as independent variables has appeal because the use of ratios tends to normalize the data by removing the brightness components. The best model, as measured by the magnitude of its coefficient of multiple determination (R^2) and standard error of estimate, for estimating Secchi disc transparency is:

LNSECCHI = 0.784 + 2.638 GRNIR1 - 3.731 REDIR1 - 0.754 IR1IR2

The model explains approximately 87 percent of the variance about the mean (Table 18). The observed and predicted Secchi disc transparency values for the 20 lakes are given in Table 19. Although the number of observations is limited (N = 20) and the ground truth is sparse, it is apparent that the LANDSAT-1 MSS can be used to estimate Secchi disc transparency in freshwater lakes.

The most glaring disparity occurs with Middle Lake. Several factors may individually or collectively account for the large residual, including: bottom effects, presence of extensive beds of aquatic macrophytes, the overlap of lake pixels onto land, or some still unsuspected factor. Middle Lake has good water clarity, is relatively shallow, and does have a problem with submerged aquatic macrophytes.

An effort was made to estimate the Secchi disc transparency of 11 Minnesota lakes found in Frame 1022-16373. The regression model, found in subappendix D5, must be viewed with caution because the ground truth was collected approximately two and one-half weeks after the date of LANDSAT-1 coverage. Lakes are dynamic and significant changes may have occurred during the intervening period.

Chlorophyll <u>a</u> Estimation

Bressette and Lear (1973), using an infrared photographic technique, have detected algal blooms (primarily Anacystis) in the "salt wedge" area of the Potomac River near Maryland Point. The inherent characteristics of the spectral reflectance curve for chlorophyll-bearing plants (Figure 32) were used to advantage. The reflectance of the chlorophyll-bearing plants varies greatly as illustrated by the curve with an abrupt increase at about 700 nanometers. Although the water tends to attenuate the infrared energy in a relatively short distance, the magnitude of the plant reflectance in the near-infrared allows the detection of chlorophyll-bearing plants on or near the water surface. Bressett and Lear (1973) proposed that "it is also probable that the magnitude of the reflected solar energy in the NIR will also depend upon the concentration of phytoplankton in the water..." and demonstrated their infrared technique for the mapping of chlorophyll a concentrations.

An examination of the correlations between the MSS data (colors and color ratios) and the chlorophyll \underline{a} data from the 20 NES-sampled lakes (Table 17) suggests that it may be possible to estimate mean chlorophyll \underline{a}^* levels using the MSS data.

A multiple regression analysis yielded the model:

^{*} Mean value for each lake as determined from ground truth acquired on a specific date.

TABLE 18. ANALYSIS OF VARIANCE TABLE OF A REGRESSION MODEL FOR THE PREDICTION OF SECCHI DISC TRANSPARENCY

		Ana 1	ysis of Varian	ce
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected)	19	16.340	0.860	
Regression Residual	3 16	14.152 2.188	4.717 0.137	34.431

^aThe model was developed using MSS data from Frames 1017-16091 and 1017-16093.

TABLE 19. SECCHI DISC TRANSPARENCY RESIDUALSa

Lake Name	Serial Number	SECCHI (m)	SECCHI (m)	SECCHI-SECCHI
Poygan Butte des Morts Winnebago Green Beaver Dam Kegonsa Rock Koshkonong Lac la Belle Oconomowoc Okauchee Pine Nagawicka Pewaukee Tichigan Browns	47 48 49 51 53 54 55 56 57 58 59 60 61 62 63 64	0.46 0.52 0.71 5.69 0.38 0.99 2.39 0.32 1.91 3.51 1.83 3.05 0.91 1.82 0.57 2.13	0.55 0.48 0.51 4.87 0.58 0.55 2.68 0.35 1.42 3.27 0.64 4.85 1.03 1.18 0.70	-0.09 0.04 0.20 0.82 -0.20 0.44 -0.29 -0.03 0.49 0.24 1.19 -1.80 -0.12 0.64 -0.13 0.26
Middle Delavan Como Geneva	65 66 67 68	5.18 0.58 0.41 3.37	2.57 1.07 0.55 4.53	2.61 -0.49 -0.14 -1.16

^aThe model was developed using MSS data from Frames 1017-16091 and 1017-16093.

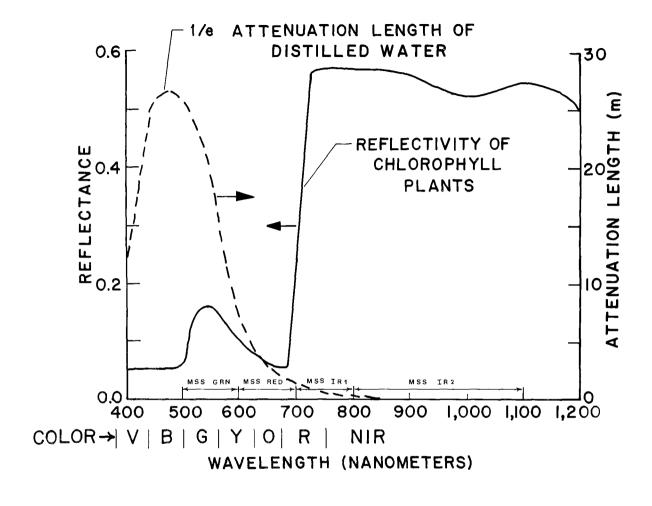


Figure 32. Comparison of the reflectance of chlorophyll-containing plants with the attenuation length of sunlight in distilled water. From Bressette and Lear (1973). The attenuation curve is based on Spiess (1970) and the plant reflectivity curve on Katzoff (1962).

The model explains about 83 percent of the variance about the mean (Table 20). The observed and predicted chlorophyll a values, along with their residuals, are found in Table 21. Although the model is purported to estimate chlorophyll a, caution must be exercised in assuming that the model is applicable to other lakes or even to the same 20 lakes on a different date. The spectral and spatial resolution of the scanner is low and many factors influence the signal returned to it.

In this case a strong inverse correlation exists between the trophic indicators LNSECCHI and LNCHLA (-0.012) and some percentage of the return signal detected by the multispectral scanner is undoubtly due to the presence of chlorophyll-bearing plants. However, the impact of different types and concentrations of inorganic suspenoids on the chlorophyll \underline{a} are not known at this time. The estimates of chlorophyll \underline{a} derived from the regression model are more properly treated as index numbers than as absolute values.

TABLE 20. ANALYSIS OF VARIANCE TABLE OF A REGRESSION MODEL FOR THE PREDICTION OF CHLOROPHYLL \underline{A} LEVELS^a

Same		Anal	ysis of Variand	ce
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected)	19	23.998	1.263	
Regression Residual	2 17	19.876 4.123	9.938 0.243	40.897

^aThe model was developed using MSS data from Frames 1017-16091 and 1017-16093.

TABLE 21. CHLOROPHYLL A RESIDUALSa

Lake Name	Serial	CHLA	CHLA	CHLA-CĤLA
	Number	(µg/l)	(µg/1)	(μg/1)
Poygan Butte des Morts Winnebago Green Beaver Dam Kegonsa Rock Koshkonong Lac la Belle Oconomowoc Okauchee Pine Nagawicka Pewaukee Tichigan Browns Middle Delavan Como Geneva	47 48 49 51 53 54 55 56 57 58 59 61 62 63 64 65 66 67 68	29.7 26.5 27.2 0.8 14.1 26.9 4.8 23.0 4.9 1.5 4.1 3.8 13.5 6.9 20.5 5.1 4.1 30.3 29.1 2.1	17.0 29.9 33.7 2.4 26.0 24.4 3.7 41.3 3.5 2.2 3.9 2.1 9.0 8.9 19.0 5.5 5.5 16.9 14.1 2.2	12.7 - 3.4 - 6.5 - 1.6 -11.9 2.5 1.1 -18.3 1.4 - 0.7 0.2 1.7 4.5 - 2.0 1.5 - 0.4 - 1.4 13.4 15.0 - 0.1

^aThe model was developed using MSS data from Frames 1017-16091 and 1017-16093.

SECTION VII

LAKE CLASSIFICATION USING LANDSAT-1 MSS DATA

General relationships between MSS data and the trophic state of NES-sampled lakes, as defined by lake position on the first principal component axis (PCl value), are examined in this section using regression analysis, three-dimensional color ratio models, and color-enhanced photographic products generated through automatic classificatory techniques.

LANDSAT-1 MSS data recorded on 12 different dates (Table 14) were examined in this investigation. Although the temporal coverage of the NES-sampled lakes (Table 15) is fragmentary, a relatively coherent time series exists for 20 lakes in eastern-southeastern Wisconsin. This section will focus on the MSS frames obtained from the Wisconsin area on three occasions (9 August 1972, 11 June 1973, and 17 July 1973). Reference will be made to the other MSS coverage dates and frames which have been largely relegated to Appendix D.

TROPHIC STATE INDEX PREDICTION USING ERTS-1 MSS DATA

As was discussed in Section IV, trophic state is a multi-dimensional concept and can not be adequately assessed by measuring any single indicator. With this in mind, 100 NES-sampled lakes were subjected to the multivariate technique of principal component analysis using LN transformed measurements of six trophic state indicators (LNISEC, LNCHLA, LNTPHOS, LNCOND, LNAAY, LNTON). The position of each lake on the first principal component axis, the PCl value, is purported to be a trophic state index. The larger the PCl value, the closer the water body is to the eutrophic end of the scale and, conversely, the smaller the PCl value, the closer the lake is to the oligotrophic end of the scale.

In Section VI the utility of using the LANDSAT-1 MSS data for the prediction of Secchi disc transparency and chlorophyll <u>a</u> levels was examined. While the estimation of specific trophic indicators is of value, the question arises, "Can the position of a lake on the first principal component axis be predicted using MSS data?"

Investigations relating to lake appearance as related to trophic status (Section VI) support the premise that the multitude of interactions occuring within a lake give the lake volume reflectance an intensity and spectral curve which is indicative of its trophic state. While it can be argued that the MSS lacks the spectral resolution to detect some of the variables incorporated into the trophic state index (such as

conductivity and total phosphorus), the elimination of the variables would make the index less stable and therefore more susceptible to a large deviation from normal for a given indicator.

PC1-MSS Regression Analyses

The Wisconsin MSS frames are treated in chronological order starting with those collected on 9 August 1972. Regression models are developed for the prediction of the trophic state index (PC1) values for 20 NES-sampled lakes for each sampling date and then for the same lakes on the basis of mean MSS values for the three dates of LANDSAT-1 coverage.

The product-moment correlation coefficients between the PC1 values for the 20 Wisconsin lakes and the MSS data (colors and color ratios) extracted from MSS frames recorded on the three MSS sampling dates are found in Table 22. The correlations of 9 August 1972 and 17 July 1973 are of similar magnitudes.

TABLE 22. CORRELATIONS BETWEEN LANDSAT-1 MSS DATA (COLORS AND COLOR RATIOS) COLLECTED ON THREE DATES AND THE TROPHIC STATUS OF 20 WISCONSIN LAKES

MCC Colour	Date	of LANDSAT-1 Fly	over
MSS Colors and Ratios	9 August 1972	11 June 1973	17 July 1973
GRN	0.518	0.151	0.479
RED IR1	0.722 0.807	0.533 0.512	0.721 0.836
IR2 GRNRED	0.589 -0.823	0.174 -0.712	0.628 -0.749
GRNIR1	-0.806	-0.540	-0.820
GRNIR2 REDIR1	-0.470 -0.544	-0.091 0.084	-0.485 -0.422
REDIR2 IR1IR2	-0.026 0.516	0.298 0.445	0.109 0.479

Numerous regression models were developed during the investigation; only the "best" models are presented in this report. Criteria used in the selection of the "best" models included the magnitude of the coefficient of multiple determination (R^2) and the standard error of estimate. All regression coefficients were required to be significant at the 0.05 level.

The best regression model for the prediction of the trophic state index (PC1) values of the 20 Wisconsin lakes for 9 August 1972 is:

$$\widehat{PC1} = 7.682 - 6.074 \text{ GRNIR1} + 1.155 \text{ GRNIR2}$$

The model explains about 81 percent of the variance about the mean and has a standard error (s.e.) of estimate of 0.840 (Table 23).

TABLE 23. ANALYSIS OF VARIANCE TABLE OF A REGRESSION MODEL FOR THE PREDICTION OF THE TROPHIC STATUS OF 20 WISCONSIN LAKES FOUND IN LANDSAT-1 MSS FRAMES 1017-16091 AND 1017-16093 (9 AUGUST 1972)

	Alla I	ysis of Variand	ce
df	Sum of Squares	Mean Square	Calculated F
19	62.555 50.572	3.292 25.286	35.867
17	11.983	0.705	33.337
	19 2	19 62.555 2 50.572	19 62.555 3.292 2 50.572 25.286

When considering the R^2 value of the above model it must be kept in mind that the PCl was developed using mean values of the ground truth measurements taken on three occasions during the 1972 open water season. The MSS data were collected within a few seconds on 9 August 1972.

An examination of the residuals (PCl-PCl) in Table 24 reveals relatively large absolute values for Middle, Tichigan, Pine, Beaver Dam, and Butte des Morts. Middle Lake and Butte des Morts are predicted to be in worse condition (closer to the eutrophic end of the scale) than their PCl values indicate. The other three lakes are estimated to be in better condition (closer to the oligotrophic end of the scale) than their PCl values suggest. The model produced poor results when it was used to predict the trophic state index values of lakes in other MSS frames.

A regression model was developed for the same 20 Wisconsin lakes using MSS data collected by the LANDSAT-1 on 11 June 1973. The model:

$$\widehat{PC1}$$
 = 42.761 - 18.423 GRNRED - 18.948 REDIR1 + 3.057 GRNIR2

explains about 70 percent of the variation about the mean and has a

TABLE 24. TROPHIC STATE INDEX (PC1) RESIDUALS OF 20 WISCONSIN LAKES FOUND IN LANDSAT-1 MSS Frames 1017-16091 AND 1017-16093 (9 AUGUST 1972)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Poygan	47	1.68	1.41	0.27
Butte des Morts	48	1.27	2.39	-1.12
Winnebago	49	2.36	2.70	-0.34
Green	51	-1.67	-1.53	-0.14
Beaver Dam	53	3.29	2.14	1.15
Kegonsa	54	1.48	2.13	-0.65
Rock	55	-1.21	-0.85	-0.36
Koshkonong	56	2.45	2.87	-0.42
Lac la Belle	57	-1.43	-0.94	-0.49
Oconomowoc	58	-1.82	-1.82	0.00
Okauchee	59	-0.62	-0.89	0.27
Pine	60	-0.71	-1.88	1.17
Nagawicka	61	1.27	0.58	0.69
Pewaukee	62	0.59	0.45	0.14
Tichigan	63	3.11	1.51	1.60
Browns	64	-1.07	-0.43	-0.64
Middle	65	-2.29	-0.56	-1.73
Delavan	66	2.03	1.46	0.57
Como	67	1.15	1.18	-0.03
Geneva	68	-1.71	-1.78	0.06

standard error of estimate of 1.087 (Table 25). The residuals are are displayed in Table 26. The model has less practical value for the prediction of trophic state than the PC1 model for 9 August 1972.

The MSS data collected on 17 July 1973 were also used to develop a regression model for the prediction of the PCl values for the same lakes with the results:

This model explains about 81% of the variance about the mean and has a standard error of estimate of 0.892 (Table 27). The residuals are displayed in Table 28.

Each date of LANDSAT-1 coverage has its unique model for the prediction of the trophic state of the 20 lakes.

TABLE 25. ANALYSIS OF VARIANCE TABLE OF A REGRESSION MODEL FOR THE PREDICTION OF THE TROPHIC STATUS OF 20 WISCONSIN LAKES FOUND IN LANDSAT-1 MSS Frames 1323-16194 AND 1323-16100 (11 June 1973)

		Anal	ysis of Varian	ce
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected) Regression Residual	19 3 16	62.555 43.649 18.906	3.292 14.550 1.182	12.313

 $R^2 = 0.6978 \times 100 = 69.78\%$ s.e. of estimate = 1.087

TABLE 26. TROPHIC STATE INDEX (PC1) RESIDUALS OF 20 WISCONSIN LAKES FOUND IN LANDSAT-1 MSS Frames 1323-16194 AND 1323-16100 (11 June 1973)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Poygan Butte des Morts	47 48	1.68 1.27	1.19 1.52	0.49 -0.25
Winnebago	49	2.36	1.30	1.06
Green	51	-1.67	-0.45	-1.22
Beaver Dam	53	3.29	3.29	0.00
Kegonsa Rock	54 55	1.47 -1.21	0.05 -0.63	1.42 -0.58
Koshkonong	56	2.45	3.64	-1.19
Lac la Belle	57	-1.43	-0.11	-1.32
Oconomowoc	58	-1.82	-0.66	-1.16
Okauchee	59	-0.62	-0.36	-0.98
Pine	60	-0.71	-2.16	1.45
Nagawicka Pewaukee	61 62	1.27	1.10	0.17
Tichigan	62 63	0.59 3.11	0.55 1.36	0.04 1.75
Browns	64	-1.07	-1.30	0.23
Middle	65	-2.29	-1.22	-1.07
Delavan	66	2.03	0.71	1.32
Como	67	1.15	1.29	-0.14
Geneva	68	-1.71	-1.70	-0.01

TABLE 27. ANALYSIS OF VARIANCE TABLE OF A REGRESSION MODEL FOR THE PREDICTION OF THE TROPHIC STATUS OF 20 WISCONSIN LAKES FOUND IN LANDSAT-1 MSS Frames 1359-16091 AND 1359-16094 (17 July 1973)

		Ana 1	ysis of Varian	ce
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected) Regression Residual	19 4 15	62.555 50.631 11.925	3.292 12.658 0.795	15.922

 $R^2 = 0.8094 \times 100 = 80.94\%$ s.e. of estimate = 0.892

TABLE 28. TROPHIC STATE INDEX (PC1) RESIDUALS OF 20 WISCONSIN LAKES FOUND IN LANDSAT-1 MSS FRAMES 1359-16091 AND 1359-16094 (17 July 1973)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Poygan Butte des Morts Winnebago Green Beaver Dam Kegonsa Rock Koshkonong Lac la Belle Oconomowoc Okauchee Pine		1.68 1.27 2.36 -1.67 3.29 1.48 -1.21 2.45 -1.43 -1.82 -0.62 -0.71	3.06 1.76 1.73 -1.84 2.15 0.63 -1.20 3.17 -1.48 -1.15 -0.21 -1.59	-1.38 -0.49 0.63 0.17 1.14 0.85 -0.01 -0.72 0.05 -0.67 -0.41 0.88
Nagawicka Pewaukee Tichigan Browns Middle Delavan Como Geneva	61 62 63 64 65 66 67 68	1.27 0.59 3.11 -1.07 -2.29 2.03 1.15 -1.71	0.80 0.29 2.83 -0.49 -0.52 0.92 0.70 -1.41	0.47 0.30 0.28 -0.58 -1.77 1.11 0.45 -0.30

Although the lake color ratios vary from frame to frame (date to date), it is not unreasonable to expect that over a period of time a lake would present an average color or appearance, which would be more representative of the water body's position on a trophic scale. With this in mind, a new regression model was developed using mean color ratios derived from the three dates of LANDSAT-1 coverage. For example, a lake's mean GRNRED color ratio was determined by establishing its GRNRED ratio for each of the three LANDSAT-1 dates, summing these ratios and dividing by the number of LANDSAT-1 dates. Stated more simply,

$$XGRNRED = (GRNRED_1 + GRNRED_2 + GRNRED_3)/3$$

where XGRNRED is the mean color ratio for a lake, GRNRED, is the ratio determined for the first LANDSAT-1 date, GRNRED₂ is the ratio for the second date of LANDSAT-1 coverage, and GRNRED₃ is the ratio for the third date of coverage. The coverage dates are 9 August 1972, 11 June 1973, and 17 July 1973.

The model which best predicts the PC1 values for the 20 lakes is:

$$\widehat{PC1}$$
 = 4.127 - 6.623 XGRNRED - 3.511 XREDIR2 + 8.040 XIR1IR2

It explains about 80 percent of the variation about the mean and has a standard error of estimate of 0.887 (Table 29). The residuals are displayed in Table 30. Relatively large residuals (absolute values) exist for Middle, Pine, and Butte des Morts. The elimination of the 11 June 1973 data and use of average ratios developed from the two remaining dates (9 August 1972 and 17 July 1973) would result in a better model.

Regression models were also developed for NES-sampled lakes in Minnesota and New York where LANDSAT-1 MSS coverage was available. The best model, as measured by the criteria stated previously, for each date of LANDSAT-1 MSS coverage is displayed in Table 31 along with the models for the Wisconsin lakes.

Although a model is included for all of the LANDSAT-1 MSS coverage dates, except for the two dates with very small sample sizes, some of the models are clearly inadequate. For example, the models with an R^2 less than about 0.80 (80 percent) do not have much predictive value. This effectively eliminates a model for the Wisconsin lakes (11 June 1973) and several models for the Minnesota lakes (6 October 1972, 28 May 1973, 3 July 1973). Another model, 19 August 1972 (New York) is of dubious value because the number of observations is small (N = 7), and there are only four degrees of freedom associated with the residuals.

TABLE 29. ANALYSIS OF VARIANCE TABLE OF A REGRESSION MODEL FOR THE PREDICTION OF THE TROPHIC STATUS OF 20 WISCONSIN LAKES USING MEAN MSS COLOR RATIOS FROM THREE DATES (9 AUGUST 1972, 11 JUNE 1973, 17 JULY 1973)

		Anal	ysis of Variand	ce
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected) Regression Residual	19 3 16	62.555 50.003 12.529	3.292 16.676 0.783	22.575

 $R^2 = 0.7997 \times 100 = 79.97\%$ s.e. of estimate = 0.887

TABLE 30. TROPHIC STATE INDEX (PC1) RESIDUALS OF 20 WISCONSIN LAKES FROM A REGRESSION MODEL INCORPORATING MEAN MSS COLOR RATIOS FROM THREE DATES (9 AUGUST 1972, 11 JUNE 1973, 17 JULY 1973)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Poygan	47	1.68	1.66	0.02
Butte des Morts	48	1.27	2.45	-1.18
Winnebago	49	2.36	1.77	0.59
Green	51	-1.67	-1.61	-0.06
Beaver Dam	53	3.29	3.05	0.24
Kegonsa	54	1.48	1.33	0.15
Rock	55	-1.21	-0.93	-0.28
Koshkonong	56	2.45	3.32	-0.87
Lac la Belle	57	-1.43	-1.05	-0.38
Oconomowoc	58	-1.82	-1.23	-0.59
Okauchee	59	-0.62	-0.47	-0.15
Pine	60	-0.71	-1.99	1.28
Nagawicka	61	1.27	0.42	0.85
Pewaukee	62	0.59	0.29	0.30
Tichigan	63	3.11	1.48	1.63
Browns	64	-1.09	-0.69	-0.40
Middle	65	-2.29	-0.36	-1.93
Delavan	66	2.03	1.45	0.58
Como	67	1.15	0.98	0.17
Geneva	68	-1.71	-1.74	0.03

TABLE 31. REGRESSION MODELS DEVELOPED FOR THE ESTIMATION OF TROPHIC STATE USING LANDSAT-1 MSS DATA^a

Date, Frame(s) and Area	··· Number of Lakes	Regression Model	$R^2 \times 100$	Standard Error of Estimate	Appendix
9 August 1972 1017-16091 1017-16093 Wisconsin	20	PC1 = 7.682 - 6.074 GRNIR1 + 1.155 GRNIR2	80.84%	0.840	Dl
11 June 1973 1323-16194 1323-16100 Wisconsin	20	PC1 = 42.761 - 18.423 GRNRED - 18.948 REDIR + 3.057 GRNIR1	1 69.78%	1.087	D3
17 July 1973 1359-16091 1359-16094 Wisconsin	20	PC1 = 140.430 - 9.375 GRNRED - 98.913 REDIR + 45.672 REDIR2 - 57.330 IR1IR2	1 80.94%	0.892	D4
1017-16091 1017-16093 1323-16194 1323-16100 1359-16091 1359-16094	20	PC1 = 4.127 - 6.623 XGRNRED - 3.511 XREDIR2 + 8.040 XIR1IR2	79.97%	0.887	
14 August 1972 1022-16373 Minnesota	11	PC1 = 13.150 - 10.626 GRNIR1 + 2.327 GRNIR2	96.06%	0.456	D5

TABLE 31. REGRESSION MODELS FOR THE ESTIMATION OF TROPHIC STATE USING LANDSAT-1 MSS DATA (continued)

Date, Frame(s) and Area	Number of Lakes	Regression Model	$R^2 \times 100$	Standard Error of Estimate	Appendix
6 October 1972 1075-16321 Minnesota	12	PC1 = 11.533 - 7.132 REDIR1	43.91%	1.540	D6
8 October 1972 1077-16431 Minnesota	7	PC1 = 35.509 - 18.548 GRNRED	95.12%	0.247	D7
28 May 1973 1309-16325 Minnesota	11	PC1 = -16.537 + 9.844 IR1IR2	49.33%	1.525	D8
3 July 1973 1345-16322 Minnesota	12	PC1 = 10.544 - 7.240 REDIR1	70.09%	1.117	D9
4 July 1973 1346-16381 Minnesota	7	PC1 = 11.715 - 8.277 REDIR1	92.34%	0.669	D10
19 August 1972 1027-15233 New York	7	PC1 = -4.891 - 8.805 GRNIR1 + 19.301 REDIR1	82.82%	0.740	Dll

^aRegression models were not constructed for Frames 1036-16152 (28 August 1972, Wisconsin) and 1080-15180 (11 October 1972, New York) due to the relatively small number of observations.

An examination of the remaining models indicates that they all differ from one another. Attempts to predict the PCl values for a particular LANDSAT-1 coverage date, using a model from another date, produced statistically insignificant results.

Although their regression coefficients are different, some models have the same variables in common. For example, the 9 August 1972 (Wisconsin) model and the 14 August 1972 (Minnesota) model incorporate the variables GRNIR1 and GRNIR2. Both models have an R² exceeding 0.80 and are of value in predicting the PC1 values of water bodies contained in their respective frames.

The models for 3 July 1973 (Minnesota) and 4 July 1973 (Minnesota) contain a single independent variable, IRl. Yet, the first model has an R^2 of about 70 percent and the latter model an R^2 of about 92 percent. Some of the lakes are common to both models. An attempt to use the 4 July 1973 model to predict the PCl values of the NES lakes in the 3 July 1973 frame drew statistically insignificant results.

The degree of success in the prediction of lake trophic state, as defined by a lake's position on the first principal component axis, varies considerably from date to date. Several factors could account for the variability.

Lakes are, by their very nature, dynamic and can change significantly in appearance over a matter of days or weeks. Algal blooms, the growth of aquatic macrophytes, the influx of silt carried by rainswollen streams, and, in the case of shallow lakes with sufficient fetch, sediments churned up by wind-induced turbulence can produce changes in the volume reflectance detectable by both human observers and other sensors such as the MSS. Super-imposed on the variations associated with lake dynamics are variations related to atmospheric conditions and solar angle.

The impact of antecedent precipitation on lake volume reflectance can not be ascertained with any degree of certainty in this study. The relatively poor regression model for the 3 July 1973 (Minnesota) may be a consequence of the heavy rains on 2 July 1973, but this is largely conjecture.

THREE-DIMENSIONAL MSS COLOR RATIO MODELS

In the preceding section, several regression models were developed to predict the trophic status of selected lakes using MSS ratios. The assumptions were made that the PCl values adequately represent the position of the lakes on a trophic scale and that lake phenomena that correlate with the index are detectable using the MSS.

A less sophisticated but practical approach to evaluating relationships between MSS data and trophic state involves the visual examination of MSS data patterns in light of a general knowledge of the lakes as well as their trophic state index values (PC1). Although this could be done through the use of data matrices, a graphic approach is favored because it is very conducive to pattern detection and interpretation. An examination of the various MSS ratios incorporated into the regression models in Table 31 indicates that the MSS ratios GRNIR1, GRNRED, and REDIR1 might be used to advantage.

The three-dimensional models in this section were produced using the same program and equipment as in the PCA ordination model found in Section IV. The numerals inside the "ball" are the lake's serial number and those near the lake's name represent its PCl value. Lakes with a serial number greater than 100 fell outside the scope of the PCA ordination and therefore lack a PCl value. Although a MSS color ratio model was developed for each date of LANDSAT-1 coverage, the Wisconsin lakes will serve as a focal point. The other models are found in Appendix D.

The color ratio model for 9 August 1972 (Wisconsin: 1017-16091, 1017-16093) is found in Figure 33. The model can be examined using both a general knowledge acquired about the lakes and their PC1 values as guides. There is a very definite trend for the color ratios to increase as one moves from lakes considered to be located near the eutrophic end of the scale (e.g., Beaver Dam) toward those situated more closely to the oligotrophic end (e.g., Green, 51).

It is unrealistic to expect complete agreement between the position of the lakes in the color ratio model and their respective PCl values. In addition to the problems created by the dynamic nature of the lakes, some additional uncertainty is generated by the sampling methods. The lake MSS data for the three-dimension model were acquired by sensing the lake body, at least to Secchi depth (or to the bottom if the Secchi depth is greater than the water depth), on a pixel-by-pixel basis. The PCl values were derived from ground truth collected at selected points (stations) ranging in number from one $(\underline{e},\underline{g}, Middle Lake)$ to nine (Lake Winnebago). As will be seen in the next section, the number of sampling sites and their location on a lake can have a significant effect on the lake's trophic index value. In addition, the sensor data represent lake phenomena at a single point in time; the PCl values were derived using annual mean values.

Assuming that the PC1 value of Middle Lake is representative of its trophic state, it is "out of position" relative to the other lakes in the 9 August 1972 model. The lake's color ratio coordinates are indicative of a lake situated more closely to the eutrophic end of the trophic scale. Several factors may be responsible for this apparent misclassification.

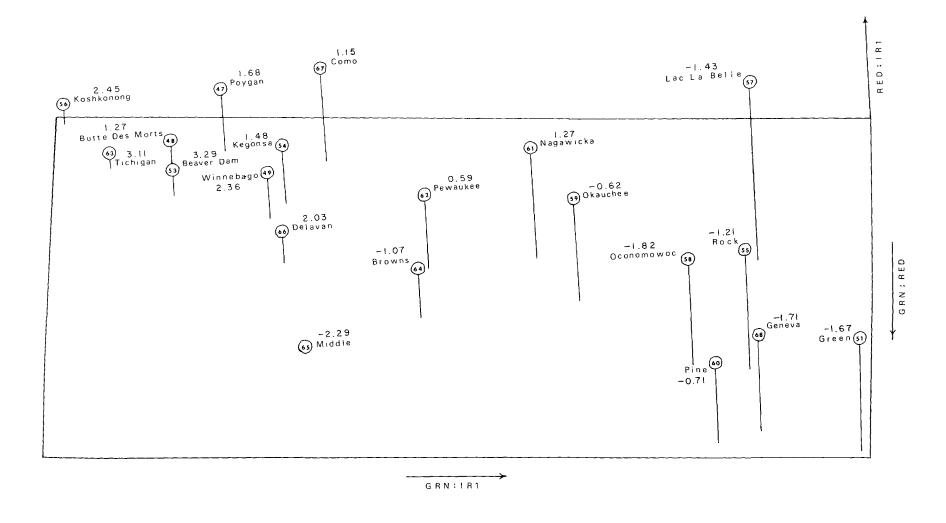


Figure 33. Three-dimensional color ratio model for 9 August 1972. The 20 Wisconsin lakes were extracted from LANDSAT-1 MSS Frames 1017-16093 and 1017-16091. The frames are in juxtaposition on the same flight line.

As discussed previously, the trophic scale does not <u>directly</u> incorporate the extent of aquatic macrophytes and algal organisms in the lakes, nor does it include a direct measure of lake morphometry. The sensor may very well be "seeing" large masses of plants and/or the lake bottom. Middle Lake is known to have weed problems and it has extensive shallows. The incorporation of some direct measure of aquatic weeds into the trophic state index would shift Middle Lake toward the eutrophic end of the scale and bring the lake index value in closer agreement with the lake's coordinates in the color ratio model.

The 11 June 1973 model of the same 20 lakes is shown in Figure 34 along with three other lakes (Mendota, Monona, and Waubesa). Many of the lakes have shifted their position significantly (e.g., Winnebago, Kegonsa, Geneva, Rock, and Oconomowoc). The color ratio-trophic state relationships so evident in the three-dimensional model of 9 August 1972 are not as obvious in 11 June 1973. Efforts to develop a regression model, using the PCl values as the dependent variable in the preceding section, yielded statistically insignificant results.

The Wisconsin lakes are incorporated into a three-dimensional color ratio model using MSS data from 17 July 1973 (Figure 35). Although not identical in all respects, the model bears a marked resemblence to the 9 August 1972 model. The positional change of Lake Poygan may be due in part to the large portion of cloud coverage (approximately 50 percent).

The model in Figure 36 represents the <u>mean</u> color ratio relationships among the 20 Wisconsin lakes using the MSS data for three dates (9 August 1972, 11 June 1973, 17 July 1973). The mean ratios were determined in the previous section. The model may be thought of as a representation of the general appearance of the lakes. A more extended time series is desirable, but cloud cover and poor quality MSS bands have made this impossible despite the 18-day repetitive coverage cycle.

A three-dimensional color ratio model was constructed for each of the remaining dates of LANDSAT-1 MSS coverage (Table 15). The models are found in Appendix D. It will be noted in some of the models of Minnesota lakes (14 August 1972, 6 October 1972, 8 October 1972) that certain lakes (Wagonga, Silver) are isolated from the other lakes. These lakes have IR1 DN values which exceed their respective RED DN values. The lakes are at the extreme end of the trophic scale and are sometimes referred to as being hypereutrophic.

An examination of both the three-dimensional color ratio models and their associated regression models suggests that the utility of the MSS for the estimation of trophic state is dependent to a substantial degree upon the time of year. The Wisconsin and Minnesota frames recorded relatively early during the open water season (28 May 1973,

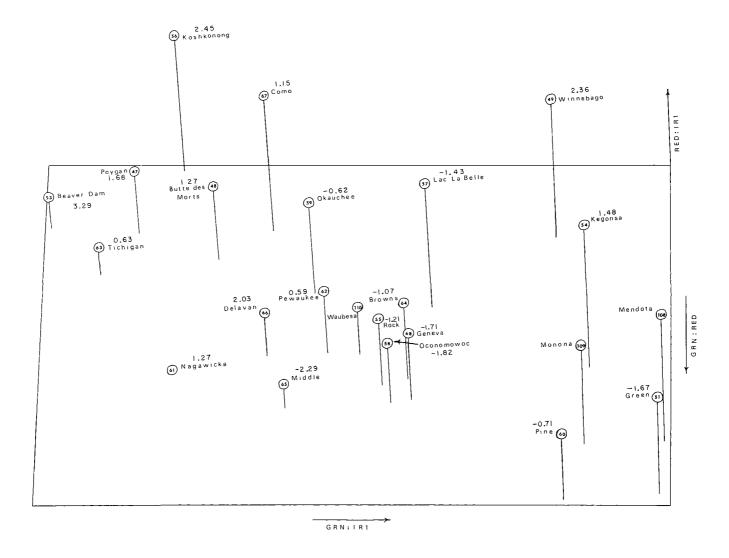


Figure 34. Three-dimensional color ratio model for 11 June 1973. The 23 Wisconsin lakes were extracted from LANDSAT-1 MSS Frame 1323-16100. Three of the lakes (Mendota, Monona, and Waubesa) fall outside the scope of the investigation, but are included because they are well-known by lake scientists.

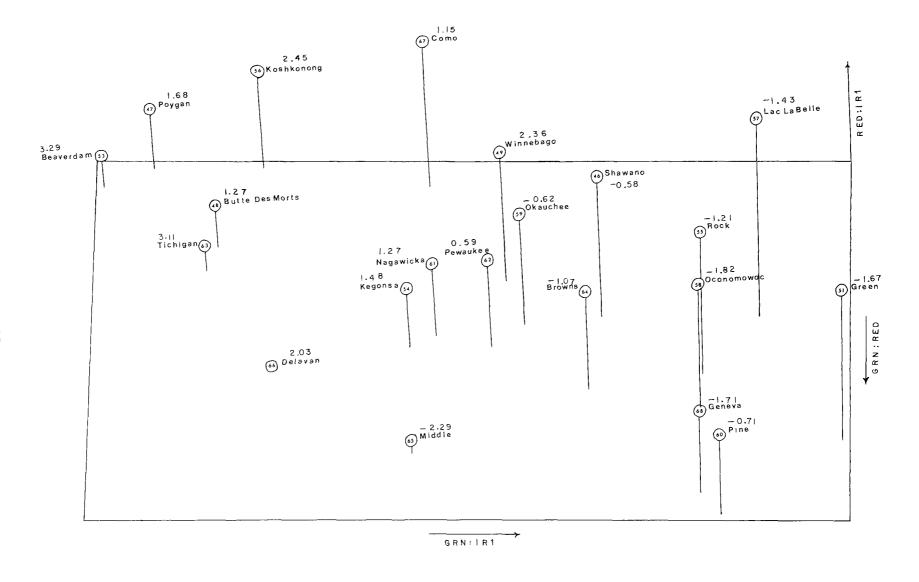


Figure 35. Three-dimensional color ratio model for 17 July 1973. The 20 Wisconsin lakes were extracted from LANDSAT-1 MSS Frames 1359-16091 and 1359-16094.

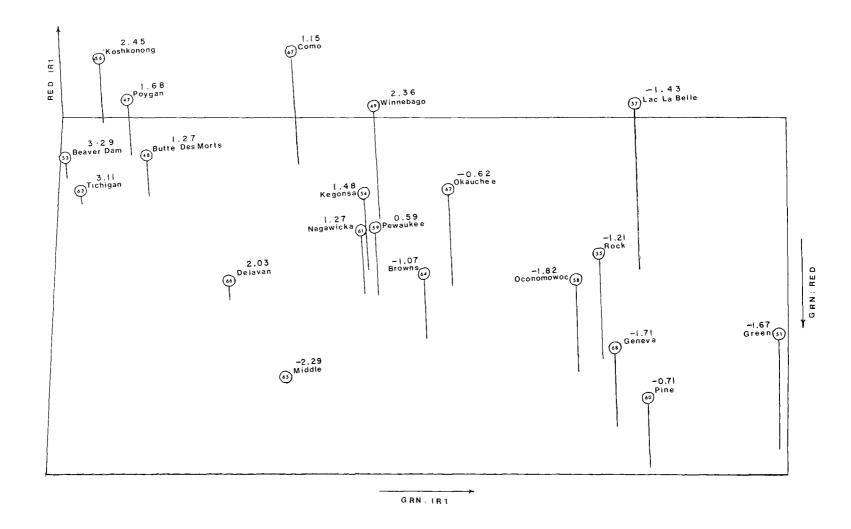


Figure 36. Three-dimensional color ratio model for three dates of LANDSAT-1 MSS coverage (9 August 1972, 11 June 1973, 17 July 1973). The model was developed using mean color ratios derived from MSS data collected on the three dates.

11 June 1973) have spectral curves which correlate poorly with the lake PCl values. The correlations are much stronger in the case of MSS frames recorded later in the season (9 August 1972, 14 August 1972, 17 July 1973, 8 October 1972) when the contrast between lakes at different points on the trophic scale tend to be at a maximum.

LAKE CLASSIFICATION USING MSS DATA IN CONJUNCTION WITH AN AUTOMATIC DATA PROCESSING TECHNIQUE

Up to this point the lake MSS data have been examined using regression techniques and three-dimensional color ratio models. The investigations were undertaken using mean color values and mean color ratios for each LANDSAT-1 date. The lakes were treated as entities without regard to differences which might be present within them. Automatic data processing techniques are well-suited, not only for classifying lakes, but also for classifying different types of water within individual lakes (Boland, 1975; Boland and Blackwell, 1975).

It is becoming increasingly common to use automatic data processing (ADP) techniques in remote sensing studies ($\underline{e}.\underline{g}.$, Hoffer, \underline{et} $\underline{al}.$, 1972). ADP techniques merit consideration because they permit the reduction of large masses of data in realistic time periods and add objectivity to the classificatory process.

With the advantages of ADP in mind, an effort was undertaken by Blackwell (1974, personal communication) to apply the techniques to the 20 lakes found in MSS Frames 1017-16091 and 1017-16093 (9 August 1972). The equipment and software at the JPL/IPL were used to process the MSS data reported here and produce hard copy in the form of black and white photographs and color-enhanced prints. The methodology employed is briefly described below.

Utilizing a LARS-developed (Laboratory for Applications of Remote Sensing, Purdue University) spectral pattern-recognition-algorithm, the IPL IBM 360/44 was trained using the GRN, RED, and IR1 MSS data in conjunction with the lake PCl values. Preliminary processing indicated that the IR2 band data would be of little value in distinguishing one lake from another or one area of a lake from another area of the same water body. The IR2 data were not included, thereby reducing the amount of CPU time required for classification.

The number of spectral classes was set by establishing one class for each different PCl value among the 20 Wisconsin lakes. This resulted in the formation of 19 different classes (Table 32). Butte des Morts and Nagawicka have the same PCl value and were assigned to the same class. The computer was statistically trained to recognize each lake as belonging to a particular class. For example, the computer was trained to perceive Beaver Dam Lake as belonging to Class 1, Tichigan as Class 2, ..., Middle Lake as Class 19. Each pixel in the 20 lakes

was then classified by the computer into one of the 19 classes. The results of the classification procedure are found in Table 33.

TABLE 32. LAKE TROPHIC STATE INDEX CLASS ASSIGNMENTS FOR THE ADP TECHNIQUE

Serial		Computer Trained
Number	PC1 Value	to Recognize as Class:
53	3.29	1
		2 3 4 5 6 7
		3
		4
		5
		6
54		
48	1.27	8
,61	1.27	8
67	1.15	9
62	0.59	10
59	-0.62	11
60	-0.71	12
64	-1.07	13
55	-1.21	14
57	-1.43	15
51	-1.67	16
6 8	-1.71	17
58	-1.82	18
65	-2.29	19
	53 63 56 49 66 47 54 48 61 67 62 59 60 64 55 57 51 68 58	Number Value 53 3.29 63 3.11 56 2.45 49 2.36 66 2.03 47 1.68 54 1.48 48 1.27 61 1.27 67 1.15 62 0.59 59 -0.62 60 -0.71 64 -1.07 55 -1.21 57 -1.43 51 -1.67 68 -1.71 58 -1.82

All of the pixels in a homogeneous lake would be classified as falling into the class for which the lake served as a training area. It is very unlikely to find a lake that has the same trophic characteristics throughout its areal extent. Some indication of the heterogeneous nature of the 20 Wisconsin lakes may be obtained by examining Table 33. Beaver Dam Lake, for example, has 69.4 percent of its pixels classified as belonging to Class 1, 10 percent to Class 2, ..., and 1.3 percent to Class 7. Lake Kegonsa exhibits the least heterogeneity with 87.4 percent of its pixels falling in Class 7. The percentages expressed here should be treated as approximations because the "sixth line" banding affects the results of any such classification scheme. If the classificatory results had indicated homogeneous conditions in each lake,

TABLE 33. ADP RESULTS FOR 9 AUGUST 1972 USING A 19 CLASS CLASSIFICATION^a

Lake Name	Serial Number	PC1 Value	Trained as Class:		Six Major Classes Found in the Lake (Percentage)					
Beaver Dam	53	3.29	1	1	10	2	19	4	7	
Tichigan	63	3.11	2	(69.4) 2	(13.0) 5	(9.8)	(3.2)	(2.5) 8	(1.3) 7	
Koshkonong	56	2.45	3	(41.6) 7	(17.0) 17	(16.3) 16	(8.5) 12	(8.5) 2	(3.9)	
Winnebago	49	2.36	4	(44.5) 4	(12.6) 10	(6.0) 5	(5.1) 2	(4.8) 7	(4.7) 1	
Delavan	66	2.03	5	(18.0) 5 (66.0)	(16.3) 3 (8.0)	(13.8) 8 (6.1)	(9.8) 7 (4.2)	(9.5) 1 (4.0)	(9.1) 2 (3.5)	
Poygan	47	1.68	6	(00.0) 7 (24.0)	(8.0) 6 (18.3)	(0.1) 9 (13.4)	8 (10.1)	(4.0) 5 (8.0)	(3.5) 4 (6.7)	
Kegonsa	54	1.48	7	(24.0) 7 (87.4)	(18.3) 9 (7.4)	(13.4) 6 (3.0)	(10.1)	2 (0.1)	(0.7)	
Butte des Morts	48	1.27	8	(29.3)	(7.4) 8 (23.3)	5 (18.4)	(7.8)	3 (7.0)	(5.8)	
Nagawicka	61	1.27	8	15 (41.3)	10 (16.5)	5 (9.3)	(8.3)	17 (6.0)	(5.0)	
Como	67	1.15	9	7 (39.1)	(31.2)	7.5)	(5.0)	(3.4)	(3.4)	
Pewaukee	62	0.59	10	10 (35.0)	14 (14.9)	(13.0)	11 (8.9)	13 (5.2)	19 (5.2)	
Okauchee	59	-0.62	11	(32.7)	16 (19.5)	14 (13.0)	10 (11.8)	(6.6)	12 (5.8)	
Pine	60	-0.71	12	12 (35.9)	16 (30.9)	11 (4.6)	17 (4.1)	19 (4.1)	13 (3.7)	

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TABLE 33. ADP RESULTS FOR 9 AUGUST 1972 USING A 19 CLASS CLASSIFICATION^a (continued)

Lake Name	Serial Number	PC1 Value	Trained as Class:		Six Major	ix Major Classes Found in the Lake (Percentage)			
Browns	64	-1.07	13	11 (22.0)	13 (17.1)	19 (15.5)	12 (10.0)	16 (6.5)	1 (6.1)
Rock	55	-1.21	14	16 (31.1)	12 (15.6)	14 (12.7)	11 (12.5)	15 (9.9)	17 (4.6)
Lac la Belle	57	-1.43	15	15	` 10 <i>`</i>	14	7	` 5 <i>`</i>	`11
Green	51	-1.67	16	(43.0) 16	(11.9) 12	(11.8) 14	(5.3) 17	(4.9) 11	(4.8)
Geneva	6 8	-1.61	17	(45.0) 17	(27.8) 16	(7.7) 12	(5.7) 14	(5.2) 18	(1.9) 10
Oconomowoc	58	-1.82	18	(38.0) 16	(18.3) 12	(15.6) 14	(12.7) 17	(5.4) 15	(2.3) 11
Middle	65	-2.29	19	(23.6) 12 (22.2)	(19.2) 19 (15.4)	(12.4) 13 (12.8)	(9.4) 1 (11.1)	(8.7) 11 (10.2)	(7.9) 16 (10.2)

^aThe six trophic classes listed for each lake were assigned most of the pixels representing the lake. The percentage of pixels assigned to each class is given in parentheses.

the analysis could stop at this point. However, this is not the case, and the question arises: "What trophic-related patterns exist in each lake?" This necessitates the development of some sort of imagery.

Images of the machine-classified lakes can be produced in the form of line printer copy using different symbols to represent the various trophic classes and also as photographic prints and transparencies. Output in the form of photographs was selected because they are compact, easily handled, have much greater resolution than line printer copy of equal size, and are readily interpretable, particularly when in color.

The ADP-classified lakes (9 August 1972) are displayed in Figure 37 using 19 gray-levels, one for each class. Class 1 is located toward the eutrophic end of the trophic scale (black) and Class 19 (white) is toward the oligotrophic end. It would be incorrect to call a Class 19 pixel or lake oligotrophic because none of the lakes examined are considered to possess the necessary attributes. The pronounced linear features are artifacts introduced by a defect in the MSS and are generally referred to as "sixth line" banding. It is important to overlook their presence when studying the patterns present in the lake images.

Figure 38 is a color-enhanced version of the 19-class classification of the 20 lakes (9 August 1972). Black has been assigned to represent Class 1, and each of the remaining 18 classes has been assigned its unique color. The colors were produced by using different ratios of the three primary colors: blue, green, and red. Detailed information regarding the principles involved is found in the work by Committee on Colorimetry (1966).

Differences among and within the lakes are readily apparent. Some of the lakes (Kegonsa and Beaver Dam) present a relatively homogeneous appearance. Others (Winnebago and Poygan) exhibit a diversity of trophic classes. Some of the lakes have features which bear mentioning.

The appendix-like structure which appears attached to the northeast quadrant of Delavan Lake is the entry point of Jackson Creek, the major stream feeding the lake. Its waters, known to be nutrient-rich through contributions from sewage treatment plants and agricultural drainage, have been placed in Class 1.

In this study, Lake Tichigan has been defined to include the lake proper and what is commonly referred to as the "widening" in the Fox River. The lake proper has been assigned to Class 5 and the "widening" to several classes including 1, 2, and 4. Ground truth measurements indicate that the "widening" has a lower Secchi disc transparency and a substantially high chlorophyll \underline{a} level.

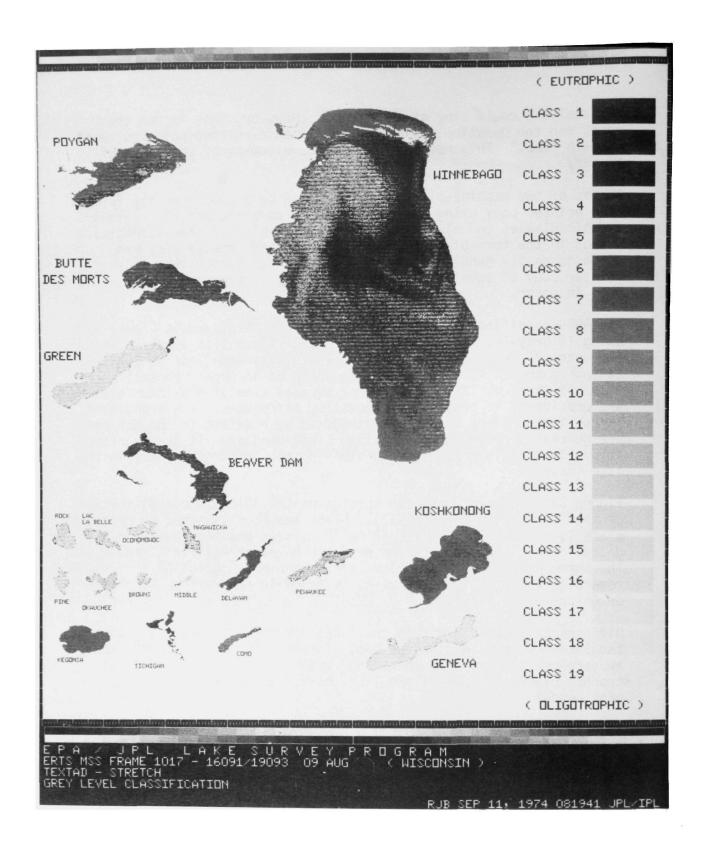


Figure 37. ADP-classified lakes (9 August 1972), using 19 gray-levels, one for each class.

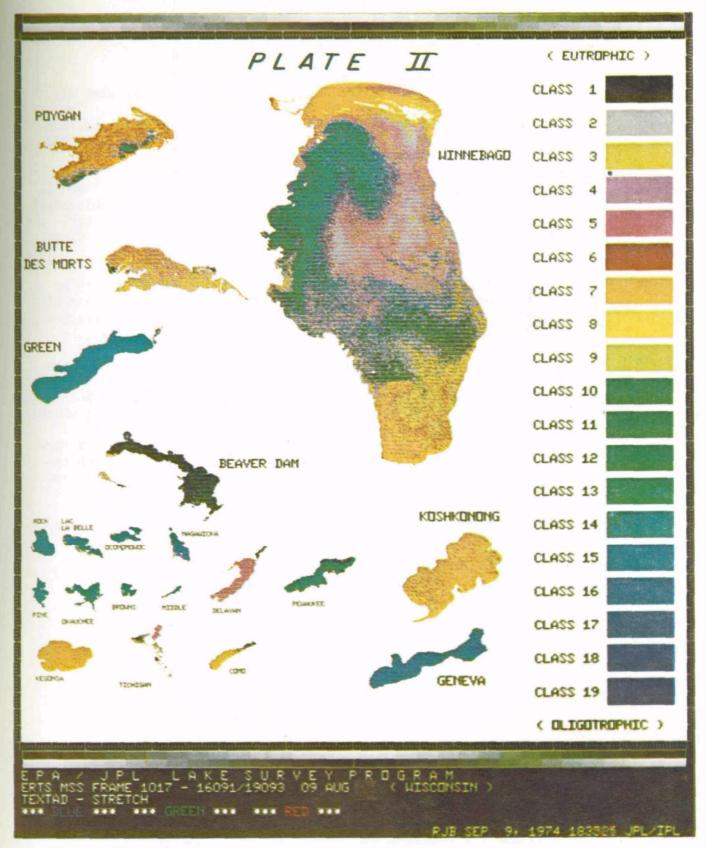


Figure 38. A color-enhanced version of the 19-class classification of the 20 lakes (9 August 1972).

The Class I water found along the northern shore of Lake Pewaukee may be related to the presence of algae and rooted emergent plants. The helicopter-borne survey teams reported algal scum covering the surface of the northern portion of the lake on 21 June 1972 and 19 August 1972. Heavy growths of emergents covered the lake shallows.

The appendix-like portion of Green Lake located at its northeast end is the area into which Silver Creek flows. The area receives a substantial nutrient load from a sewage treatment plant and the surrounding agricultural lands. Its pixels have been classified as belonging to Class 1 and Class 2.

White areas within the lake images are indicative of either clouds or land-related phenomena. The white area in the northeastern portion of Lake Winnebago represents cloud cover. The north-south linear feature located in the eastern end of Lake Butte des Morts is a causeway.

Complete accord does not exist between the trophic index values of the 20 lakes and the results of the ADP technique. The disparity is very evident in the cases of lakes Nagawicka, Koshkonong, and Oconomowoc where few, if any, pixels were found that fell into the class for which the lake served as a training area. Middle Lake contains pixels classified as belonging to Class 19, but they constitute only 15.4 percent of the total. This is not surprising because there is an indication in the three-dimensional color ratio model and the PCl regression model for 9 August 1972 that a disparity exists between some of the lake PCl values and their MSS data. The use of a smaller number of classes may very well yield more consistent results. This is an area in need of additional study.

The color-enhanced imagery, produced through an ADP technique, should prove to be of value, not only in comparing lakes with each other, but also for supplying information which can be used in the selection of future lake sampling sites. Further refinement should make the imagery a valued tool in lake survey and monitoring activities.

SECTION VIII

GENERAL SUMMARY

This research has focused on relationships between Earth Resources Technology Satellite-One (LANDSAT-1) multispectral scanner (MSS) data and the trophic status of selected lakes in Minnesota, Wisconsin, Michigan, and New York sampled by the U.S. Environmental Protection Agency's National Eutrophication Survey. Analyses were directed toward lake classification on the basis of ground truth, and the prediction of lacustrine trophic state indicator magnitudes and trophic state using MSS data.

Initially, 100 NES-sampled lakes were analyzed to ascertain their trophic status. Trophic indicators selected as parameters in the analyses included: chlorophyll <u>a</u>, conductivity, total phosphorus, total organic nitrogen, the inverse of Secchi disc transparency, and the yield of a standard algal assay procedure. Natural logarithm transformations were made on the data to produce a more-nearly normal distribution.

A complete linkage algorithm (McKeon, 1967) was used in conjunction with squared-Euclidian distance to examine the trophic status of the lake population for the presence of natural clusters or groups. The results are displayed in the form of a dendrogram (Figure 15).

The lake trophic indicator data were also subjected to a principal components analysis to reduce the dimensionality of the data from six-dimensional hyperspace to space of three or fewer dimensions. The eigenvectors and their associated eigenvalues were extracted from a p x p Pearson product-moment correlation matrix. The first principal component (normalized eigenvector) accounts for approximately 68 percent of the variation in the data. The second and third components represent about 14 percent and 8 percent of the variation, respectively. The results of the principal components analysis were used to ordinate the lakes in one-, two-, and three-dimensional space. The three-dimensional ordination is displayed as a "ball and wire" model (Figure 17).

A multivariate trophic state index was developed by evaluating the first principal component for each of the 100 NES-sampled lakes. The resultant values (PCl) are indicative of each lake's respective position on a multivariate trophic scale (the first principal axis). The larger the PCl values, the closer the lake lies toward the eutrophic end of the scale. The coefficients of the first component are nearly equal in magnitude, suggesting that the first principal component represents a general measure of trophic state.

LANDSAT-1 MSS data, collected on 12 different dates from Minnesota, Wisconsin, and New York, were extracted from computer-compatible magnetic digital tapes (CCT's) using VICAR, a sophisticated software system at the Image Processing Laboratory (IPL), a support facility of the Jet Propulsion Laboratory (JPL). Each lake image was extracted from its terrain matrix through the use of a binary mask technique which employs a digital number (DN) level of 28 (8-bits of precision; 256 DN levels) as the water-land cutoff point. Descriptive statistics were computed for each lake including total number of pixels, mean DN values, standard deviations, and histograms. This was accomplished for each of the four MSS bands (GRN, RED, IR1, and IR2). A photographic concatenation was produced of the lakes extracted from each frame.

Regression models were developed to predict the magnitude of two trophic state indicators (Secchi disc transparency and chlorophyll a) using MSS data from two dates, 9 August 1972 (Wisconsin) and 14 August 1972 (Minnesota). A regression model was developed for each date of LANDSAT-1 MSS coverage using the multivariate trophic state index (PC1) as the dependent variable and the MSS color ratios as independent variables. Most of the modelling effort was directed toward NES-sampled lakes in eastern-southeastern Wisconsin. The Wisconsin area was selected because good LANDSAT-1 MSS coverage was available for a group of 20 lakes on three different dates.

A more flexible approach toward the study of PCl-MSS relationships was undertaken using three-dimensional MSS color ratio models. The MSS ratios GRNIR1, GRNRED, and REDIR1 were used to develop the three-dimensional "ball and wire" models. A model was constructed for each date of MSS coverage. In addition, a model was created for the Wisconsin lakes using mean color ratio values for the three sampling dates (9 August 1972, 11 June 1973, and 17 July 1973; Figure 36).

Automatic data processing (ADP) techniques were used in conjunction with the PCl values for 20 Wisconsin lakes and MSS data 9 August 1972) to classify the lakes. A computer was programmed to recognize 19 trophic classes using the MSS color information contained in the 20 lakes. The classification was accomplished on a pixel-by-pixel basis using the MSS GRN, RED, and IRl data. Output is in the form of statistical data and photographic products including 19-step gray scale prints (Figure 37) and 19-class color-enhanced photographs (Figure 38).

LAKE CLASSIFICATION USING GROUND TRUTH

The examination and classification of large numbers of lakes within realistic periods of time necessitates the use of automatic data processing techniques which incorporate classificatory methods, such as cluster analysis and principal components ordination.

The complete linkage algorithm used in this research did not produce three well-isolated clusters (groups) that can be readily associated with the traditional trophic classes of lakes - oligotrophic, mesotrophic, and eutrophic. This apparent failure is due in part to the lakes used in the study. Although the 100 lakes were selected to cover the range of lakes sampled during 1972 by the National Eutrophication Survey, the NES-sampled lake population is heavily weighted toward lakes with relatively poor water quality. The three-dimensional principal component ordination does not contain large well-defined clusters. The ordination results support the findings of the cluster analysis.

It is likely that there are no sharp discontinuities which clearly separate the members of a large population of lakes into the three commonly-referred-to trophic classes. Lakes of such a population may be characterized as constituting a hyper-dimensional cloud possessing a low degree of organization.

Cluster analysis techniques are a "heavy handed" approach to the lake classification problem because they will lead to clusters even if the data are random. The principal component analysis ordination does not presume the existence of clusters. The two methods are complementary and should be used in conjunction with one another.

The concept of a multivariate trophic state index, as defined by the position of a lake on the first principal component axis, merits further consideration. However, it must be kept in mind that a less sophisticated method, the mean composite rank (MCR) index, yielded similar results as measured by lake rank. The MCR system has the advantages of conceptual simplicity and ease of computation.

MSS Estimation of Lake Area and Selected Trophic State Indicators

The LANDSAT-1 MSS is an effective tool for the determination of the number and the areal extent of lakes. The use of a DN level of 28 (8-bits of precision) as the water-land cutoff point for the generation of the binary mask in conjunction with a pixel conversion factor of 0.48 (1 pixel = 0.48 hectares) gives lake area estimates generally within 10 percent of values derived from topographic sheets.

While the use of near-concurrent ground truth precludes more precise estimates, it has been demonstrated that good predictions of Secchi disc transparency can be achieved through the incorporation of MSS color ratios into regression models.

A measure of the chlorophyll \underline{a} level can be obtained by using MSS color ratios as independent variables in regression models. However, caution

must be used in the interpretation of the chlorophyll model predictions. The predicted values should be treated as a crude index rather than accurate estimations of chlorophyll <u>a</u>.

Models for the prediction of Secchi disc transparency and chlorophyll \underline{a} are unique to the date of LANDSAT-1 MSS coverage. The models do not give good predictions when used with MSS data collected on different dates. Ground truth must be collected concurrently or near-concurrently with MSS coverage, and then the appropriate models must be constructed.

Although the need for ground truth places a restriction on the use of MSS data for the prediction of trophic state indicators, it still has utility in regions where lake concentrations result in the inclusion of hundreds and even thousands of lakes within a single MSS frame. Under such circumstances the collection of ground truth from a small number of "bench mark" lakes for the development of regression models would pay handsome dividends.

MSS Prediction of Lacustrine Trophic State

The MSS data can be used to give fair to very good estimates of lacustrine trophic state as defined by lake position on the first principal component axis. The regression models, developed using MSS color ratios as independent variables, are unique to the date of LANDSAT-1 coverage. Predictions made employing a specific model in conjunction with MSS data from other dates were statistically insignificant. Models developed from MSS data collected early in the open-water season are inadequate; better models were constructed using MSS data collected later in the season when the contrasts between lakes at different points on the trophic scale tend to be maximized.

Extraction Techniques and Products

While it is possible to extract MSS data related to lake trophic state and trophic indicators from EROS-supplied imagery, efforts to use this imagery are seriously impeded because the photographic products lack the requisite radiometric fidelity, a consequence of the scale compression induced by condensing the MSS intensity resolution from 127 levels (7-bit precision) to 16 gray levels. Data extracted from computer-compatible tapes (CCT's) must be used if the maximum benefits are to be derived from the LANDSAT-1 MSS. This is particularly important in water quality-related studies because the full range of water quality differences is contained in a relatively small number of DN levels. The computer-compatible tape approach to the problem of MSS data extraction has the added advantage of eliminating the errors introduced by differences in photographic products and the microdensitometer. CCT data extraction and processing techniques, which produce both MSS data

statistics and photographic products, greatly increase the utility of the multispectral scanner.

Photographic products permit the rapid visual assessment of lake coverage by providing greater spatial resolution and a fraction of the bulk characteristic of line printer copy. It has been demonstrated that automatic digital processing techniques can produce trophic classifications which, when displayed as photographic imagery, can be incorporated into studies of lake water quality, water circulation patterns, and supply information for the selection of lake water sampling sites. The advantages of using CCT-produced photographs are particularly evident when the products are in the form of color-enhanced prints and transparencies.

LANDSAT-1 Coverage and Quality

Although LANDSAT-1 gives 18-day repetitive coverage, good frames were available for only a few days in the study area encompassing Minnesota, Wisconsin, Michigan, and New York. On many occasions, excessive cloud cover (greater than 10 percent) was present or one or more of the MSS bands was rated as poor or missing. Good coverage was virtually non-existent for NES-sampled lakes in Michigan during 1972.

While it is recognized that the number of days with excessive cloud cover is a function of a region's weather and climate, and therefore its geographic location, - some regions (southwestern U.S.) have viewing conditions which are consistently better than other regions (northeastern U.S.) - it is apparent that good LANDSAT-1 MSS coverage is available on a very erratic basis, making systematic time-series studies difficult if not impossible in the study area and, indeed, for much of the eastern United States.

Information relating to water quality is found in each of the four MSS bands (GRN, RED, IR1, and IR2). However, the DN levels sensed for water bodies are few in number and are located at the lower end of the intensity scale. Surface water resource investigations would derive substantial benefits if the instrument gain were to be increased on the MSS. It is possible to switch to high gain in the GRN and RED bands.

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SECTION X

LIST OF ACRONYMS AND SYMBOLS

AAY: algal assay yield ESB: Eutrophication Survey Branch

ADP: automatic data processing GRN: Green (MSS Band 4)

AIP: automatic image processing GRNIR1: ratio of green to infrared-

one

A-space: attribute space GRNIR2: ratio of green to infrared-

black and white two

b&w:

CRT:

CCT:

cm:

EPA:

cathode ray tube

centimeter

computer-compatible tape

bit: binary digit GRNRED: ratio of green to red

bpi: bits per inch GRAFPAC: standard graphic output

subroutines

GSFC: Goddard Space Flight Center

ha: hectare

CDC: Control Data Corporation hz: hertz

CHLA: chlorophyll <u>a</u>

IBM: International Business Machines

COND: conductivity

IFOV: instantaneous field of view

°C: degrees Celsius IPL: Image Processing Laboratory (Jet Propulsion Laboratory)

DN: digital number IR1: infrared-one

DCS: data collection system IR2: infrared-two

EBR: electron beam recorder IR1IR2: ratio of infrared-one to infrared-two

Environmental Protection

Agency (United States) ISEC: inverse of Secchi disc transparency

EROS: Earth Resources Observation Systems I-space: individual space

ERTS-1: Earth Resources Tech- JPL: Jet Propulsion Laboratory

nology Satellite Number
One km: kilometer

l: liter

NIR: near-infrared LANDSAT-1: Land Satellite One (i.e., ERTS-1) nanometers nm: natural logarithm LN: OD: optical density natural log-transformed LNAAY: operating system 0S: algal assay yield OSI: Optimum Systems Incorporated natural log-transformed LNCHLA: chlorophyll a Oregon State University OSU: natural log-transformed LNCOND: PCA: principal components analysis conductivity principal component trophic PC1: natural log-transformed LNISEC: state index inverse of Secchi disc transparency pixel: picture element natural log-transformed LNSECCHI: Secchi disc transparency PMT: photomultiplier tube natural log-transformed PNERL: Pacific Northwest Environ-LNTON: total organic nitrogen mental Research Laboratory natural log-trans-LNTPHOS: RBV: return beam vidicon formed total phosphorus RED: red (MSS Band 5) m: meter R-space: row space (i.e., attribute space) MCR: mean composite rank REDIR1: ratio of red to infrareduq: microgram REDIR2: usec: microsecond ratio of red to infraredtwo mg: milligram SECCHI: Secchi disc transparency MSS: multispectral scanner SIPS: Statistical Interactive N: number of observations Programming System NASA: National Aeronautics and S-matrix: similarity matrix Space Administration STORET: Storage and Retrieval NERC: National Environmental number

TPHOS:

TON: total organic nitrogen

total phosphorus

Recearch Center

Survey

National Eutrophication

NES:

USGS: United States Geological

Survey

VFC: video film converter

VICAR: Video Communication and

Retrieval

XGRNIR1: mean of green to infrared-

one ratios

XGRNIR2: mean of green to infrared-

two ratios

XGRNRED: mean of green to red

ratios

XIR1IR2: mean of infrared-one to

infrared-two ratios

XREDIR1: mean of red to infrared-

one ratios

XREDIR2: mean of red to infrared-

two ratios

 Δ : Euclidian distance

 Δ^2 : squared Euclidian distance

predicted value

SECTION XI

APPENDICES

- A. Trophic Indicator Data for 100 NES-sampled Lakes
- B. Sampling Dates for 100 NES-sampled Lakes (1972)
- C. Morphometry and Hydrology of Study Lakes
- D. LANDSAT-1 MSS Models, Concatenations, Areal Relationships, and Descriptive Statistics
- E. N x N Squared Euclidian Distance Matrix
- F. Listing of the McKeon Cluster Analysis Program

APPENDIX A

TROPHIC INDICATOR DATA FOR 100 NES-SAMPLED LAKES

Blackduck Bemidji Andrusia Wolf	1 2 3 4 5	1.72 2.15 1.37 1.19	0.58 0.47	244	0.051	0 00		
Bemidji Andrusia	2 3 4	2.15 1.37	0.47			0.80	14.6	2.2
Andrusia	3 4	1.37		315	0.049	0.69	9.5	1.3
	4		0.73	276	0.035	0.58	13.0	1.8
		+ + + /	0.84	384	0.068	0.48	17.2	1.6
Cass		1.88	0.53	272	0.027	0.53	9.8	0.8
Leech	6	2.17	0.46	262	0.020	0.53	6.2	0.5
Birch	7	2.44	0.41	205	0.024	0.42	7.1	1.4
Trout	8	2.81	0.36	325	0.045	0.43	7.0	1.6
Mashkenode	9	1.05	0.95	301	0.100	0.56	25.3	2.6
Whitewater	10	1.71	0.59	139	0.066	0.67	9.8	2.9
Pelican	11	1.71	0.59	88	0.033	0.39	11.4	1.3
Shagawa	12	1.77	0.57	71	0.084	0.53	11.3	4.5
Gull	13	2.32	0.43	204	0.031	0.51	12.5	2.4
Rabbit	14	2.71	0.37	276	0.036	1.25	6.7	2.0
Cranberry	15	1.18	0.85	107	0.038	0.78	30.2	0.2
Darling	16	2.56	0.39	391	0.019	0.80	11.8	0.8
Carlos	17	2.74	0.37	353	0.014	0.56	4.6	0.9
Le Homme Dieu	18	2.31	0.43	315	0.022	0.67	12.4	0.2
Minnewa s ka	19	1.71	0.59	638	0.035	0.90	7.6	0.4
Ne s t	20	1.36	0.74	353	0.050	1.03	21.4	3.8
Green	21	2.79	0.36	353	0.051	0.46	4.9	1.3
Wagonga	22	0.29	3.41	808	0.940	1.54	94.5	13.9
Clearwater	23	1.57	0.64	362	0.033	0.77	12.7	2.4
Mud (at Maple Lake	24 e)	0.35	2.88	530	1.893	1.31	132.3	8.5
Cokato	25	1.34	0.54	540	0.208	1.39	10.7	29.0
Buffalo	26	1.27	0.79	597	0.224	1.65	38.1	16.2
Carrigan	27	0.28	3.58	595	1.164	1.81	84.3	13.2
Silver	28	0.25	3.94	470	0.540	3.35	126.1	25.9
Minnetonka	29	1.38	0.73	361	0.070	1.45	16.6	1.2
Forest	30	2.16	0.46	273	0.024	0.61	10.5	0.2
White Bear	31	3.45	0.29	253	0.019	1.32	5.2	0.3
St. Croix	32	1.11	0.90	159	0.054	0.57	10.2	3.4
Spring	33	0.47	2.15	450	0.237	0.64	21.8	34.5
Pepin	34	0.96	1.05	417	0.187	2.13	14.9	14.0
Madison	35	0.86	1.16	305	0.064	1.24	30.4	3.8
Sakatah	36	1.89	0.53	389	0.324	1.21	10.8	14.8
Bear	37	0.28	3.58	431	0.191	1.57	61.2	5.5
Aibert Lea	38	0.19	5.37	650	1.002	2.50	381.2	61.3
Yellow	39	1.49	0.67	174	0.071	0.43	13.7	3.3

APPENDIX A (continued)
TROPHIC INDICATOR DATA FOR 100 NES-SAMPLED LAKES

Long		Serial umber	SECCHI	ISEC	COND	TPHOS	TON	CHLA	AAY
Long	Wapoga ss et	40	1.80	0.56	198	0.053	0.45	16.6	5 . 5
Elk 42 0.93 1.07 66 0.140 0.83 7.1 2. Trout 43 4.12 0.24 96 0.042 0.24 2.7 0. Crystal 44 8.03 0.13 50 0.007 0.15 1.5 0. Tainter 45 1.39 0.72 173 0.115 0.50 13.7 16. Shawano 46 2.00 0.50 220 0.021 0.66 11.9 0. Poygan 47 0.48 2.07 306 0.077 1.09 19.4 8. Butte des 48 0.58 1.73 289 0.063 0.70 25.4 6. Morts Winnebago 49 0.55 1.82 316 0.156 1.02 48.4 13. Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.49 43.9 19. Comonomowa 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.59 5.8 0. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.		41		1.13	72	0.046			0.2
Trout 43 4.12 0.24 96 0.042 0.24 2.7 0. Crystal 44 8.03 0.13 50 0.007 0.15 1.5 0. Tainter 45 1.39 0.72 173 0.115 0.50 13.7 16. Shawano 46 2.00 0.50 220 0.021 0.66 11.9 0. Poygan 47 0.48 2.07 306 0.077 1.09 19.4 8. Butte des 48 0.58 1.73 289 0.063 0.70 25.4 6. Morts Winnebago 49 0.55 1.82 316 0.156 1.02 48.4 13. Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Conomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Fere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.		42	0.93	1.07	66	0.140			2.8
Crystal 44 8.03 0.13 50 0.007 0.15 1.5 0. Tainter 45 1.39 0.72 173 0.115 0.50 13.7 16. Shawano 46 2.00 0.50 220 0.021 0.66 11.9 0. Poygan 47 0.48 2.07 306 0.077 1.09 19.4 8. Butte des 48 0.58 1.73 289 0.063 0.70 25.4 6. Morts Winnebago 49 0.55 1.82 316 0.156 1.02 48.4 13. Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Charquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.	Trout	43	4.12	0.24	96	0.042	0.24		0.7
Tainter 45	Crystal	44	8.03	0.13	50	0.007	0.15		0.2
Shawano 46 2.00 0.50 220 0.021 0.66 11.9 0. Poygan 47 0.48 2.07 306 0.077 1.09 19.4 8. Butte des 48 0.58 1.73 289 0.063 0.70 25.4 6. Morts Winnebago 49 0.55 1.82 316 0.156 1.02 48.4 13. Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Swan 52 1.91 0.53 378 0.158 0.13 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32		45	1.39	0.72	173	0.115	0.50		16.8
Poygan 47 0.48 2.07 306 0.077 1.09 19.4 8. Butte des 48 0.58 1.73 289 0.063 0.70 25.4 6. Morts Winnebago 49 0.55 1.82 316 0.156 1.02 48.4 13. Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17 Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12 Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8 Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Bock 55 2.32	Shawano	46	2.00	0.50	220	0.021	0.66		0.7
Butte des Morts Winnebago 49	Poygan	47	0.48	2.07	306	0.077	1.09		8.9
Morts Winnebago 49 0.55 1.82 316 0.156 1.02 48.4 13. Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.33 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle 0.00 0.04		48	0.58	1.73	289	0.063	0.70		6.7
Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.	Morts								
Round 50 3.40 0.29 323 0.018 0.60 3.5 0. Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49	Winnebago	49	0.55	1.82	316	0.156	1.02	48.4	13.4
Green 51 5.78 0.17 386 0.043 0.43 4.8 1. Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Gomo 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.	Round	50	3 . 40	0.29	323	0.018	0.60		0.2
Swan 52 1.91 0.53 378 0.158 0.71 8.2 17. Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle 0 0.49 434 0.013 0.57 7.9 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 <t< td=""><td>Green</td><td>51</td><td>5.78</td><td>0.17</td><td>386</td><td>0.043</td><td>0.43</td><td></td><td>1.0</td></t<>	Green	51	5.78	0.17	386	0.043	0.43		1.0
Beaver Dam 53 0.43 2.34 422 0.388 0.31 69.5 12. Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle 0 0.49 434 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435	Swan	52	1.91	0.53	378	0.158	0.71		17.2
Kegonsa 54 1.10 0.91 403 0.140 0.73 30.9 8. Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58	Beaver Dam	53	0.43	2.34	422	0.388	0.31		12.7
Rock 55 2.32 0.43 378 0.019 0.63 8.1 0. Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle 0.000 0.49 434 0.013 0.57 7.9 0. Ocanomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. 15. Tichigan 63 0.58 1.71	Kegon s a	54	1.10	0.91	403	0.140	0.73		8.0
Koshkonong 56 1.58 0.63 580 0.333 1.29 36.1 29. Lac La 57 2.04 0.49 434 0.013 0.57 7.9 0. Belle 0.00 0.49 434 0.015 0.93 3.1 0. Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399	Rock	55	2.32	0.43	378	0.019	0.63	8.1	0.3
Lac La Belle 57 2.04 0.49 434 0.013 0.57 7.9 0.0 Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0.0 Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52<	Koshkonong	56	1.58	0.63	580	0.333	1.29		29.0
Belle Oconomowoc 58 3.34 0.30 437 0.015 0.93 3.1 0.0 Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 <td></td> <td>57</td> <td>2.04</td> <td>0.49</td> <td>434</td> <td>0.013</td> <td>0.57</td> <td></td> <td>0.2</td>		57	2.04	0.49	434	0.013	0.57		0.2
Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pawaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. O. 79 45.0 0.012 0.39 4.7 0. O. 70 0.042 0.042 0.042 0.042 0.042 0.042	Belle								
Okauchee 59 2.49 0.40 446 0.016 0.70 8.4 3. Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31				0.30	437	0.015	0.93	3.1	0.2
Pine 60 1.84 0.54 308 0.026 0.67 7.5 1. Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27				0.40	446	0.016	0.70	8.4	3.5
Nagawicka 61 1.30 0.77 503 0.135 0.77 12.0 21. Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Houghton 71 2.01 0.50				0.54	308	0.026	0.67	7. 5	1.4
Pewaukee 62 1.72 0.58 435 0.036 1.63 15.5 2. Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Pere 72 1.31 0.77 <	_				503	0.135	0.77	12.0	21.8
Tichigan 63 0.58 1.71 599 0.479 0.97 44.7 26. Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				0.58	435	0.036	1.63		2.1
Browns 64 2.78 0.36 435 0.021 0.68 6.4 0. Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.	_				599	0.479	0.97		26.0
Middle 65 3.59 0.28 399 0.012 0.39 4.7 0. Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1				0.36	435	0.021	0.68	6.4	0.8
Delavan 66 1.26 0.79 451 0.144 1.02 43.9 19. Como 67 0.52 1.94 390 0.064 1.05 36.4 0. Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.428 0.79 27.3 31. <tbod< td=""><td></td><td></td><td></td><td>0.28</td><td>399</td><td>0.012</td><td>0.39</td><td>4.7</td><td>0.2</td></tbod<>				0.28	399	0.012	0.39	4.7	0.2
Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				0.79	451	0.144	1.02		19.9
Geneva 68 3.22 0.31 386 0.015 0.59 5.8 0. Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				1.94	390	0.064	1.05	36.4	0.3
Charlevoix 69 3.78 0.27 289 0.007 0.19 3.0 0. Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				0.31	386	0.015	0.59		0.3
Higgins 70 6.21 0.16 231 0.040 0.13 1.1 0. Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.					289	0.007	0.19		0.1
Houghton 71 2.01 0.50 236 0.015 0.52 9.2 0. Pere 72 1.31 0.77 438 0.035 0.29 11.8 5. Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				0.16	2 31	0.040	0.13		0.1
Pere Marquette 72 1.31 0.77 438 0.035 0.29 11.8 5. White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				0.50	236	0.015	0.52		0.2
Marquette White 73 2.09 0.48 442 0.031 0.42 9.2 4. Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.		72	1.31	0.77	438	0.035	0.29		5.5
Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.									
Muskegon 74 1.61 0.52 347 0.081 0.61 9.5 7. Fremont 75 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.			2.09	0.48	442	0.031	0.42	9.2	4.5
Mona 76 1.48 0.68 486 0.482 3.35 28.5 44. Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.			1.61	0.52	347	0.081	0.61		7.3
Mona 76 1.23 0.82 446 0.428 0.79 27.3 31.				0.68	486				44.0
Cmratal 77			1.23	0.82	446				31.6
0.00/ 0.00/ 0.9 ()	Crystal	77	3.4 0	0.29	327	0.009	0.62		0.1
Jordan 78 1.84 0.54 416 0.187 0.84 20 5 22			1.84	0.54	416				22.2
Thornson 70 1 45 0 (0 55)	Thornapple	79	1.45	0.69					4.5

APPENDIX A (continued)
TROPHIC INDICATOR DATA FOR 100 NES-SAMPLED LAKES.

Lake Name	Serial Number	SECCHI	ISEC	COND	TPHOS	TON	CHLA	AAY
Ctuo b o	9.0	1.07	0 51	405	0.160	0 7.5	11 2	14 0
Strawberry		1.97	0.51	405	0.168	0.75	11.2	16.9
Chemung	81	2.43	0.41	402	0.037	0.83	13.5	2.7
Thompson	82	2.34	0.43	490	0.040	0.83	12.0	2.9
Ford	83	1.11	0.90	539	0.111	0.81	14.7	14.6
Union	84	1.13	0.88	510	0.055	0.51	15.7	2.7
Long	85	1.93	0.52	452	0.197	1.00	10.1	17.4
Randall	86	1.08	0.92	518	0.203	0.78	27.2	18.8
Schroon	87	3.73	0.27	51	0.005	0.16	2.1	0.1
Black	88	1.86	0.54	116	0.036	0.67	13.1	1.3
Ca ss adaga	89	2.57	0.39	204	0.029	0.36	9.7	4.4
Chautauqua	90	2.00	0.50	152	0.036	0.41	13.3	5.4
Conesus	91	3.19	0.31	341	0.022	0.36	9.9	0.9
Canandaigu	a 92	4.33	0.23	318	0.014	0.08	4.3	0.1
Keuka	93	3.57	0.28	246	0.010	0.18	5. 9	6.0
Seneca	94	4.14	0.24	778	0.012	0.11	6.1	0.1
Cayuga	95	2.80	0.36	442	0.015	0.23	3.0	0.1
Owa sc o	96	2.71	0.37	280	0.010	0.19	8.5	0.2
Cross	97	1.36	0.74	641	0.127	0.50	19.5	3.2
Otter	98	1.14	0.88	283	0.078	0.63	13.3	1.1
Round	99	1.17	0.86	262	0.073	0.58	28.3	18.4
Saratoga	100	2.52	0.40	202	0.073	0.51	11.8	7.5
Daratoga	100	2.52	0.40	441	0.020	0.51	11.0	1.5

Indicator acronyms: SECCHI = Secchi disc transparency (m)^a

ISEC = inverse of Secchi disc transparency (m¹)^a

COND = conductivity (micromhos cm⁻¹)^a

TPHOS = total phosphorus (mg 1⁻¹)^a

TON = total organic nitrogen (mg 1⁻¹)^b

CHLA = chlorophyll a (µg 1⁻¹)^a

AAY = algal assay control yield (mg dry wt)^b

Lakes 1-38 are located in Minnesota; 39-68 are in Wisconsin; 69-86 are found in Michigan; 87-100 are in New York. The serial numbers are unique to this report.

^aMean values based on three sampling periods.

^bValues based on composite fall sample.

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APPENDIX B

SAMPLING DATES FOR 100 NES-SAMPLED LAKES (1972)

			77.37.31.22.1104.2	7/1123 701/ 10	O NES-SAMELLO	LAKES (13	,,,,,		
Lake Name	Serial Number	l s t Sample	2nd Sample	3rd Sample	Lake Name	Serial Number	lst Sample	2nd Sample	3rd Sample
Blackduck	1	07/12	09/08	10/21	Cokato	25	06/30	08/29	10/26
Bemidji	2	07/11	09/08	10/21	Buffalo	26	06/30	08/2 9	10/26
Andrusia	3	07/11	09/08	10/21	Carrigan	27	06/30	08/29	10/26
Wolf	4	07/11	09/08	10/21	Silver	28	07/03	08/29	10/26
Cass	5	07/11	09/07	10/21	Minnetonk	a 29	06/ 2 9	09/05	10/29
Leech	6	07/11	09/08	10/21	${ t Forest}$	30	06/ 2 9	08/27	11/05
Birch	7	07/12	09/03	10/24	White Bea	r 31	06/29	08/27	11/05
Trout	8	07/11	09/08	10/22	St. Croix	32	06/28	08/26	11/04
Mashkenode	e 9	07/10	09/09	10/19	${ t Spring}$	3 3	06/28	08/26	11/04
Whitewater	10	07/06	09/02	10/25	Pepin	34	06/28	09/03	11/04
Pelican	11	07/10	09/07	10/22	Madison	35	07/01	08/30	10/29
Shagawa	12	07/08	09/07	10/22	Sakatah	36	07/01	08/30	10/29
Gull	13	07/02	09/05	10/24	Bear	37	07/01	08/30	10/29
Rabbit	14	07/02	09/04	10/24	Albert Lea	a 38	07/01	08/30	10/29
Cranberry	15	07/02	09/04	10/24	Yellow	39	06/26	08/27	11/03
Darling	16	07/06	09/01	10/25	Wapoga ss	et 40	06/26	08/26	11/03
Carlos	17	07/10	09/02	10/28	Long	41	06/25	08/25	11/04
Le Homme	18	07/06	09/02	10/28	Elk	42	06/25	08/25	11/04
Dieu		•			Trout	43	06/25	08/23	11/04
Minnewa s ka	a 19	07/06	09/01	10/25	Crystal	44	06/25	08/23	11/04
Nest	20	07/02	08/31	10/25	Tainter	45	06/26	08/26	11/03
Green	21	07/02	08/31	10/25	Shawano	46	06/22	08/24	11/08
Wagonga	22	07/02	08/31	10/25	Poygan	47	06/22	08/21	11/08
Clearwater		07/03	08/29	10/27	Butte	48	06/22	08/20	11/09
Mud (at Maple)	24	06/30	08/29	10/26	de s Mort	s			•

APPENDIX B (continued)

SAMPLING DATES FOR 100 NES-SAMPLED LAKES (1972)

Lake Name	Serial Number	l s t Sample	2nd Sample	3rd Sample	Lake Name I	Serial Number	l s t Sample	2nd Sample	3rd Sample
Winnebago	49	06/24	08/20	11/09	Fremont	75	06/13	09/15	11/13
Round	50	06/23	08/22	11/08	Mona	76	06/13	09/19	11/14
Green	51	06/22	08/21	11/08	Crystal	77	06/15	09/17	11/14
Swan	52	06/22	08/20	11/10	Jordan	78	06/15	09/18	11/15
Beaver Da	m 53	06/20	08/21	11/09	Thornapple	79	06/13	09/18	11/14
Kegonsa	54	06/22	08/20	11/10	Strawberry		06/17	09/19	11/13
Rock	55	06/23	08/20	11/10	Chemung	81	06/16	09/19	11/15
Koshkonon	g 56	06/22	08/17	11/10	Thompson	82	06/16	09/19	11/15
Lac La Be	Île 57	06/23	08/19	11/09	Ford	83	06/16	09/19	11/13
Oconomow	oc 58	06/21	08/19	11/11	Union	84	06/14	09/16	11/12
Okauchee	59	06/21	08/19	11/10	Long	85	06/13	09/17	11/12
Pine	60	06/21	08/19	11/09	Randall	86	06/14	09/16	11/12
Nagawicka	61	06/21	08/19	11/10	$\operatorname{Schroon}$	87	06/01	07/25	10/10
Pewaukee	62	06/21	08/19	11/10	Black	88	05/20	07/25	10/10
Tichigan	63	06/21	08/17	11/10	Ca ss adaga	89	05/26	07/27	10/13
Brown s	64	06/21	08/16	11/10	Chatauqua	90	05/26	07/27	10/12
Middle	65	06/22	08/19	11/10	Conesus	91	05/27	07/27	10/13
Delavan	66	06/23	08/17	11/10	Canandaigu	ıa 92	05/27	07/21	10/14
Como	67	06/21	08/16	11/10	Keuka	93	05/27	07/21	10/14
Geneva	68	06/21	08/16	11/10	Seneca	94	05/16	07/23	10/14
Charlevois	× 69	06/16	09/14	11/12	Cayuga	95	05/16	07/23	10/13
Higgin s	70	06/15	09/16	11/12	Owasco	96	05/28	07/24	10/12
Houghton	71	06/15	09/20	11/14	Cross	97	05/28	07/24	10/13
Pere	72	06/17	09/18	11/13	Otter	98	05/17	07/24	10/13
Marquette	9				Round	99	05/28	07/25	10/10
White	73	06/13	09/18	11/14	Saratoga	100	05/15	07/25	10/11
Muskegon	74	06/13	09/19	11/14	_				, –

APPENDIX C

MORPHOMETRY AND HYDROLOGY OF STUDY LAKES^a

				THE HIDROLOGI	OI STODI EARL	.5	
Lake Name	Serial Number	Area (ha)	Mean Depth (m)	Maximum Depth (m)	Volume (m ³) x 10 ⁶	Shore Line (km)	Retention Time ^b
Blackduck	01	1,110	4.6	8 . 5	50.733	16.0	4.3 y
Bemidji	02	2,598	9.6	23.2	253.407	23.8	268 d
Andrusia	03	614	7.9	18.3	48.426	14.7	47 d
Wolf	04	425	8.5	17.7	36 . 299	12.1	37 d
Cass	05	6,312	7.6	36.6	480.934	63.1	313 d
Leech	06	45,326	4.7	45.7	214.132		5.2 y
Birch	07	519	3.1	13.7	15.826	22.7	,
Trout	08	765	15.2	41.2	116.564	21.7	17.4 y
Ma sh kenode	09	41	2.1	4.3	0.872	3.06	9 á
Whitewater	10	490	6.1	22.3	29.701	21.1	
Pelican	11	4,429	3 . 7	11.6	162.005	56.1	5.0 y
Shagawa	12	955	5 . 7	14.7	54.436	29.0	0.9 ý
Gull	13	3,812	9.1	26.2	348.508	64.2	2.9 y
Rabbit	14	340	3.7	12.8	43.520	9.81	,
Cranberry	15	8. 1		10.4	0.275		
Darling	16	386	6.2	18.9	23.888	10.8	
Carlos	17	1,020	13.1	49.7	133.660	19.2	3.7 y
Le Homme Die	eu 18	706	6.4	25.9	45.175	15.3	7.9 y
Minnewaska	19	2,877	6.0	9.8	171.893	29.6	12.7 y
Nest	20	382	4.6	12.2	17.485		190 á
Green	21	2,187	6.4	33.5	140.032	19.8	3.7 y
Wagonga	22	654	1.2	4.6	7.978	20.9	1.3 y
Clearwater	23	1,288	5.2	22.9	66.724	27.9	1.4 y
Mud (at Maple Lake)	24	•		= .			- - ,

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APPENDIX C (continued)

			ואושויוטוויואטויו	AND RIDKULU	GY OF STUDY LAKES	<u> </u>	
Lake Name	Serial Number	Area (ha)	Mean Depth (m)	Maximum Depth (m)	Volume (m ³) x 10 ⁶	Shore Line (km)	Retention Time
Cokato	25	220	7.6	15.2	16.775	7.15	413 d
Buffalo	26	611	4.2	9.1	27.007	9.25	1.4 y
Carrigan	27	66	0.9	2.4	0.594		
Silver	28	170	1.2	2.1	2.040	6.87	3.5 y
Minnetonka	29	5,855	4.3	27.8	401.727	175.0	15 y
Forest	30	893	3.4	11.3	30.204	23.1	6.5 y
White Bear	31	1,077	6.9	24.4	74 . 152	21.6	
St. Croix	32	3,322	8.7	23.8	291.619		23 d
Spring	33	2 , 392		3 . 1		33.8	
Pepin	34	10,118	5.1	17.1	514 . 979		9 d
Madison	35	541	4.0	18.0	17.847	15.8	3.3 y
Sakatah	36	497	2.1	3. 7	7.607		44 d
Bear	37	556		1.1			
Albert Lea	38	985	1.1	1.8	10.591	36.0	73 d
Yellow	39	926	5.8	9.8	53 . 330	11.3	
Wapoga ss et	40	480	5.2	9.8	25.248		194 d
Long	41	169	3.4	16.5	5.632		15 d
Elk	42	36	1.8	6.4	0.691		2 d
Trout	43	1,544	11.7	35.1	180.276	30.6	
Crystal	44	36	9.8	21.0	3.552	2.25	C
Tainter	45	709	4.0	11.3	27.806		45 d
Shawano	46	2,491	3.2	10.7	80.231	26.6	1.5 y
Poygan	47	4,449	2.1	3 . 4	94.305		13 d
Butte des Mo	rts 48	3 , 584	1.8	2.7	65 . 550		6 d
Winnebago	49	55 , 730	4.0	6.4	2,208.184	116.9	210 d
Round	50	5.7	5.7	17.1	0.321		
Green	51	2,972	31.7	71.9	939.021	34.1	20.7 y

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APPENDIX C (continued)

			7.07.11.1107.12.11(1	THE HIDROLOGI	OI STODI EARL	<u> </u>	
Lake Name	Serial Number	Area (ha)	Mean Depth (m)	Maximum Depth (m)	Volume (m³) x 106	Shore Line (km)	Retention Time
Swan	52	164	9.8	25.0	15.908		179 d
Beaver Dam	53	2,671	1.4	3.4	37.840	63.7	155 ′ d
Kegon s a	54	1,099	5.2	8.8	58.234	15.4	139 d
Rock	55	555	4.9	17.1	26.325	14.2	3.6 y
Koshkonong	56	4,241	1.5	2.1	68 . 829	48.9	24 d
Lac la Belle	57	452	4.7	14.0	21.080	14.0	8 m
Oconomowoc	58	318	6.3	18.9	20.043	11.3	
Okauchee	59	451	9.5	28.7	40.320	24.1	10 m
Pine	60	285	11.8	25.9	33.448	11.8	
Nagawicka	61	415	10.1	27.4	41.147	13.8	1.5 y
Pewaukee	62	1,009	3.1	13.7	45.698	22.1	4.2 y
Tichigan	63	450	1.8	19.2	8.096	20.0	19 d
Browns	64	160	2.4	13.4	3.867	8.04	
Middle	65	72	4.6	13.7	3 . 293	8.53	
Delavan	66	718	7.6	17.1	54.810	28.5	2.8 y
Como	67	383	1.2	2.7	4.795	13.5	1.6 y
Geneva	68	2,130	18.6	41.2	395.928	32.5	29.9 y
Charlevoix	69	6 , 985	16.8	37.2	1,170.944	54.1	3.2 y
Higgins	70	3,885	14.9	41.2	580.230		15.6 y
Houghton	71	8,112	2.3	6.4	187.901	49.6	1.3 y
Pere Marquette	e 72	224		11.6			-
White	73	1,040	6.7	21.3	71.468	20.8	56 d
Mu s kegon	74	1,680	7.0	21.0	120.295	18.8	23 d
Fremont	75	320	10.1	26.8	32 .1 57	8,66	1.9 y
Mona	76	281	4.0	12.8	11.487	18.6	76 d
Crystal	77	293		21.3			

APPENDIX C (continued)

Lake Name	Serial Numbe:		Mean Depth (m)	Maximun Depth (m)		Shore Line (km)	Retenti Time	
Jordan	78	174	7.3	17.7	12.995	7.19	304	
Thornapple	79	166	4.3	9.5	7.063		11	d
Strawberry	80	104	6.7	15.2	7,006	6.34	13.2	d
Chemung	81	126	8.5	21.3	10.821	7.93	4.2	У
Thompson	82	106	2.7	15.8	2.909	7.35	152	d
Ford	83	425	4.4	11.9	18.521		15.2	d
Union	84	213	0.9	4.3	1.943	23.2	2	d
Long	85	85	5.2	12.5	4.425		31	d
Randall	86	208	5.5	14.9	11.263	5. 89	41	d
Schroon	87	1,671	14.3	46.3	239.315	39.9	153	d
Black	88	3,380	2.7	5.2	92.718	92.7	0.1	У
Ca ss adaga	89	85	3 . l	8.8	2.603	8.21	4	m
Chautauqua	90	5,720	6.7	23.5	392.266	68.3	1. 4	У
Conesus	91	1,347	11.5	18.0	154.760	29.7	2.3	У
Canandaigua	92	4,300	39.0	83.5	1,677.377	57 . 8	15	y
Keuka	93	4,740	22.4	56 . 7	1,063.356	94.0	7.8	У
Seneca	94	17, 252	88.4	188.4	15, 249. 165	121.3	33.1	У
Cayuga	95	17,198	52.4	132.6	9,375.141	136.5	10.9	У
Owasco	96	2,746	29.3	54.0	802.997	39.8		
Cross	97	881	5.5	16.8	49.339	20.0	7	d
Otter	98	114				5 . 86		
Round	99	127				4.35		
Saratoga	100	1,632	7.9	29.3	129.308	37.1	150	ત
Winona Trace	101 102	73	1.2	2.4	0.876	2.74	1.3	У
Calhoun	103	170	8.2	25.0	13.940			

APPENDIX C (continued)

Lake Name	Serial Number	Area (ha)	Mean Depth (m)	Maximum Depth (m)	Volume (m ³) x 106	Shore Line (km)	Retention Time	
Big Stone	104	5, 103	3.4	4.9	17.35	96.4	1.6	у у
Zumbro	105	345						•
Oneida	106	20,721		16.7				
Canadarago	107							
Mendota	108	3,983						
Monona	109	1,350						
Waube s a	110	855						
Cottonwood	111	150	1.6	2.4	0.240	5.63	347	d
Maple	241	240	5.8	23.2	13.920			_

^a This table has been compiled from information contained in the files of the Eutrophication Survey Branch, Pacific Northwest Environmental Research Laboratory (NERC-Corvallis).

b y = year, m = month, d = day

Seepage lake.

APPENDIX D

LANDSAT-1 MSS MODELS, CONCATENATIONS, AREAL RELATIONSHIPS AND DESCRIPTIVE STATISTICS

This appendix contains information relevant to each LANDSAT-1 MSS Frame examined during the investigation. It is divided into a series of subappendices, one for each frame or pair of frames. Frames in juxtaposition on the same flightline are treated as one. Each subappendix is in turn divided into five sections:

Section D_.1. Regression Models and Correlation Coefficients

Section D_.2. Three-dimensional Color Ratio Model

Section D .3. Concatenation of Extracted Lakes

Section D .4. MSS-Lake Surface Area Relationships

Section D .5. Lake MSS Descriptive Statistics

APPENDIX D1. 9 August 1972 (1017-16091, 1017-16093)

Section D1.1. Regression Models and Correlation Coefficients

The regression models for the prediction of Secchi disc transparency and chlorophyll \underline{a} are in Section VI along with the coefficients of correlation between the MSS data (colors and color ratios), the trophic indicators and the multivariate trophic state index. The model for the prediction of trophic state is in Section VII.

Section D1.2. Three-dimensional Color Ratio Model

The color ratio model is in Section VII (Figure 33).

Section D1.3. Concatenation of Extracted Lakes

The concatenation of lakes extracted from Frame 1017-16093 is in Section V; the Frame 1017-16091 concatenation is in this appendix (Figure D1-1).

Section D1.4. MSS-Lake Surface Area Relationships

The estimates of lake surface area using MSS data are in Section VI (Table 16).

Section D1.5. Lake MSS Descriptive Statistics

The MSS statistics for Frame 1017-16093 are in Table D1-1 and those for Frame 1017-16091 are in Table D1-2.

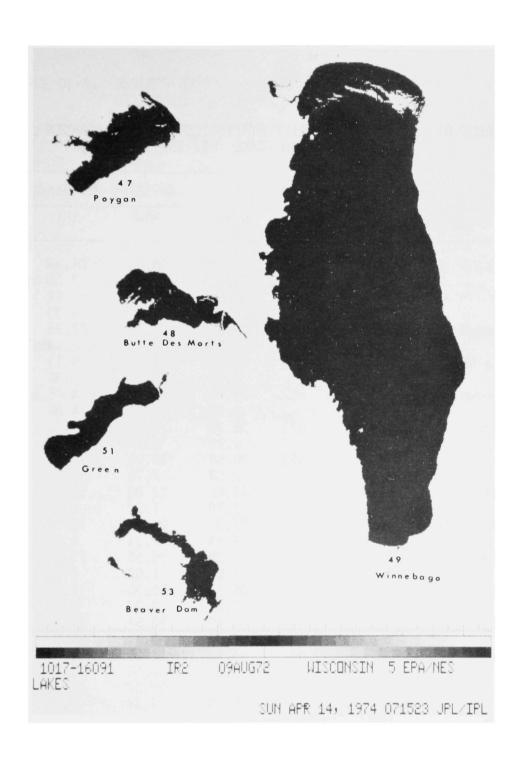


Figure D1-1. IR2 concatenation of five Wisconsin lakes extracted from Frame 1017-16091 (9 August 1972). The images have not been skewed to correct for geometric distortions. Cloud cover is evident over the northern (upper) end of Lake Winnebago.

TABLE D1-1. MSS DESCRIPTIVE STATISTICS FOR 15 WISCONSIN LAKES EXTRACTED FROM FRAME 1017-16093 (9 AUGUST 1972)

	Serial	Pixe1		LANDSAT-1	MSS Bands	
Lake Name	Number	Count	Green	Red	IR1	IR2
Kegonsa	54	2,675	50.18 ^a 1.63 ^b	30.08 1.50	24.38 3.30	8.34 5.24
Rock	55	1,009	38.86 3.27	19.39 3.07	13.62 3.38	5.10 3.74
Koshkonong	56	9,247	46.85 1.81	31.15 2.45	27.95 2.93	10.08
Lac La Belle	57	944	43.30 4.81	2.45 24.27 4.07	15.11 3.35	5.69 3.73
Oconomowoc	58	652	39.87	19.99 4.27	14.46 4.48	6.35
0kauchee	59	871	4.90 36.78	19.70	14.35	4.72
Pine	60	568	1.73 36.54	2.17 16.99	4.27 13.04	4.68 5.66
Nagawicka	61	751	2.89 42.46	2.70 23.85	3.95 17.06	4.58 6.12
Pewaukee	62	1,996	2.78 37.35	1.83 20.75	3.71 16.19	3.94 6.36
Tichigan	63	689	2.54 40.78	2.34 25.56	4.44 23.21	4.01 10.47
Browns	64	309	3.06 36.23	1.67 19.06	4.28 15.78	5.26 7.17
Middle	65	117	2.59 36.49	2.87 18.54	3.99 17.38	4.63 9.35
Delavan	66	1,541	2.77 45.42	3.27 25.39	6.53 22.07	6.91 8.35
Como	67	703	2.62 47.86	1.66 30.27	3.00 22.51	3.98 8.62
Geneva	68	4,543	5.20 39.42 2.12	4.24 18.53 2.16	3.25 13.71 2.81	4.39 5.69 3.25

^aMean DN value for the lake. ^bStandard deviation for the lake pixels.

TABLE D1-2. MSS DESCRIPTIVE STATISTICS FOR 5 WISCONSIN LAKES EXTRACTED FROM FRAME 1017-16091 (9 AUGUST 1972)

Lala Nasa	Serial	Pixel	LAi	LANDSAT-1 MSS Bands		
Lake Name	Number	Count	Green	Red	IR1	IR2
Poygan	47	9,177	46.05 ^a 4.82 ^b	29.50 5.07	23.62 5.25	9.55 5.24
Butte des Morts	48	7,395	42.99 2.55	26.74 1.83	23.08 2.78	8.25 3.59
Winnebago	49	114,186	42.38 3.22	24.95 2.67	20.86 5.50	6.65 3.92
Green	51	6,613	36.90 2.00	17.03	12.12 3.21	4.59 3.18
Beaver Dam	53	5,162	37.57 2.09	22.76	20.12	7.48 4.57

^aMean DN value for the lake. ^bStandard deviation of the lake DN values.

APPENDIX D2. 28 August 1972 (1036-16152)

Section D2.1. Regression Models and Correlation Coefficients

No models were developed because the sample size is insufficient; only three NES-sampled lakes were extracted from the frame. The three lakes (Rock, Kegonsa, and Koshkonong) have higher mean DN levels than on 9 August 1972, but have maintained their relative positions.

Section D2.2. Three-dimensional Color Ratio Model

No model was constructed.

Section D2.3. Concatenation of Extracted Lake

The concatenation of extracted lakes is displayed as Figure D2-1.

Section D2.4. MSS-Lake Surface Area Relationships

The estimates of lake surface using the MSS pixel counts and a conversion factor of 0.48 (1 pixel = 0.48 hectares) are in Table D2-1.

Section D2.5. Lake MSS Descriptive Statistics

The MSS statistics are in Table D2-2.

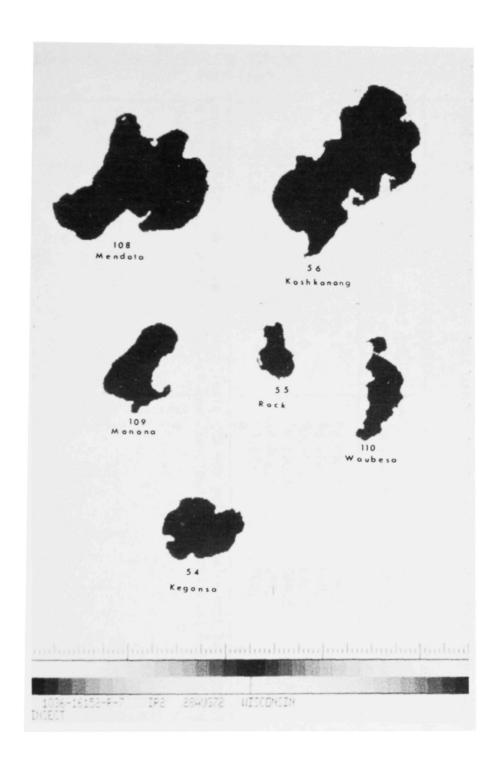


Figure D2-1. IR2 concatenation of six Wisconsin lakes extracted from Frame 1036-16152 (28 August 1972).

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TABLE D2-1. AREAL ASPECTS OF 6 WISCONSIN LAKES EXTRACTED FROM FRAME 1036-16152 (28 AUGUST 1972)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT-1 Area Ratio
Kegonsa	54	2,805	1,340.8ª	1,099.2	0.820
Rock	55	1,039	496.6a	554.8	1.117
Koshkonong	56	9,364	4,476.0 ^a	4,241.5	0.948
Mendota	108	8,460	4,043.9	3,937.7	0.974
Monona	109	2,729	1,304.5	1,349.7	1.035
Waubesa	110	1,938	926.4	855.1	0.923

^aThe estimated areas of these lakes using the MSS pixel counts from Frame 1017-16093 are, respectively: 1,277.4 hectares, 481.8 hectares, and 4,415.9 hectares.

TABLE D2-2. MSS DESCRIPTIVE STATISTICS FOR 6 WISCONSIN LAKES EXTRACTED FROM FRAME 1036-16152 (28 AUGUST 1972)

Lake Name	Serial	Serial Pixel		LANDSAT-1 MSS Bands		
	Number	Count	Green	Red	IR1	IR2
Kegonsa	54	2,805	46.97 ^a 2.01 ^b	26.62 1.40	17.88 2.64	6.57 3.41
Rock	55	1,039	42.90 2.38	22.93 1.74	15.22 3.92	6.78 4.49
Koshkonong	56	9,364	43.47 2.72	27.82 1.64	22.23 2.55	8.19 3.15
Mendota	108	8,460	40.07 2.01	21.71	13.88 2.97	5.24 3.31
Monona	109	2,729	39.24 2.84	21.84 2.17	14.29 3.38	6.05 3.70
Waubesa	110	1,938	46.78 4.01	26.50 2.07	20.28 3.08	7.92 4.03

^aMean DN value for the lake. ^bStandard deviation of the lake DN values.

APPENDIX D3. 11 June 1973 (1323-16100, 1323-16094)

Section D3.1. Regression Models and Correlation Coefficients

The regression model for the prediction of trophic state is found in Section VII; it is of little practical value.

Section 3.2. Three-dimensional Color Ratio Model

The color ratio model is in Section VII (Figure 34).

Section 3.3. Concatenations of Extracted Lakes

The 23 lakes extracted from the frames are displayed in the form of two concatenations, Figures D3-1 and D3-2. The fragmented appearance of Lake Geneva is a result of cloud cover. Lake Winnebago is partially truncated, a consequence of separating the continuous MSS strip into discrete frames. Cloud cover is responsible for the mottled appearance of Lake Poygan. Middle Lake has not been excised from the Lauderdale Lakes as was the case for 9 August 1972.

<u>Section D3.4.</u> MSS-Lake Surface Area Relationships

The estimates of lake surface area using the MSS pixel count are found in Table D3-1. Area estimates have not been determined for truncated water bodies or those partially covered by clouds.

<u>Section D3.5.</u> Lake MSS Descriptive Statistics

The MSS statistics are in Table D3-2.

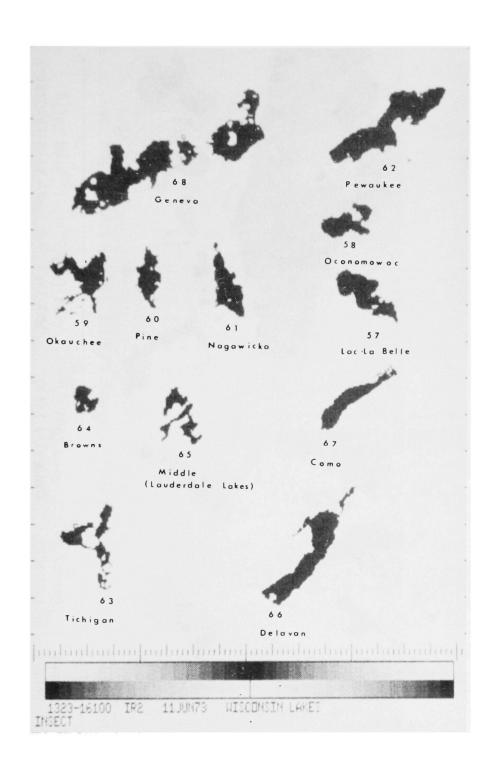


Figure D3-1. IR2 concatenation of 12 Wisconsin lakes extracted from Frame 1323-16100 (11 June 1973). The 11 other lakes extracted from the frame are in Figure D3-2.

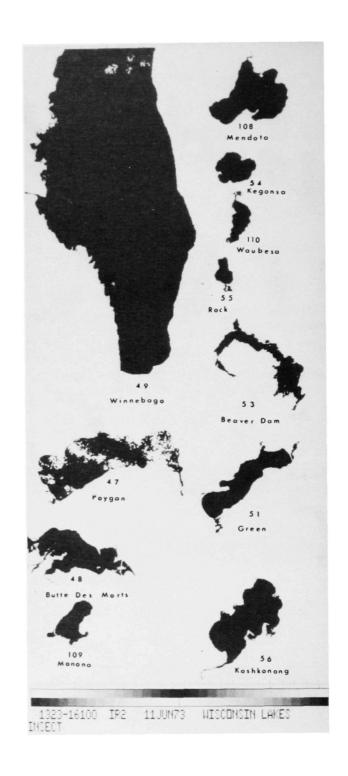


Figure D3-2. IR2 concatenation of 11 Wisconsin lakes extracted from Frame 1323-16100 (11 June 1973). The other 12 lakes extracted from the frame are in Figure D3-1.

TABLE D3-1. AREAL ASPECTS OF 23 WISCONSIN LAKES EXTRACTED FROM FRAMES 1323-16094 and 1323-16100 (11 JUNE 1973)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT- Area Ratio
Poygan	47	11,829	5,648.9	4,448.5	a
Butte Des Morts	48	8,053	3,845.3	3,584.4	0.932
Winnebago	49	98,821	47,206.8	55,730.4	1.181 ^b
Green	51	6,742	3,220.7	2,972.9	0.923
Beaver Dam	53	5,485	2,618.8	2,671.0	1.010
Kegonsa	54	2,706	1,292.7	1,099.2	0.850
Rock	55	1,127	538.4	554.8	1.031
Koshkonong	56	9,516	4 , 545.8	4,241.3	0.933
Lac La Belle	57	939	448.6	452.1	1.008
Oconomowoc	58	627	299.5	317.7	1.061
Okauchee	59	928	443.3	450.8	1.017
Pine	60	550	262.7	284.5	1,083
Nagawicka	61	7 75	370.2	415.2	1.122
Pewaukee	62	1,982	945.8	1,008.9	1.066
Tichigan	63	7 07	337.7	449.8	1.332
Browns	64	304	145.2	160.3	1.104
Middle	65	563	268.9	337.6	1.254 ^C
Delavan	66	1,517	724.7	717.9	0.991
Como	67	740	353.5	383.0	1.084 _d
Geneva	68	3,555	1,698.2	2,129.5	^a
Mendota	108	8,488	4,054.7	3,937.7	0.971
Monona	109	2,791	1,333.3	1,349.7	1.012
Waubesa	110	1,882	889.0	855.1	0.951

aThe extracted image includes Lake Winneconne and substantial cloud cover.

bThe northern end of the lake is outside the sensor field of view.

CThe Lauderdale lakes complex was extracted and treated as a single lake.

dThe presence of cloud cover has resulted in the low LANDSAT-1 area estimate.

TABLE D3-2. MSS DESCRIPTIVE STATISTICS FOR 23 WISCONSIN LAKES EXTRACTED FROM FRAME 1323-16100 (11 JUNE 1973)

Laka Nama	Serial	Pixel	LA	NDSAT-1	MSS Bands	
Lake Name	Number	Count	Green	Red	IRI	IR2
Poygan	47	11,829	50.53	33.74	25.52	13.95
D 11 - 1- 14 - 1	40	0.053	4.97	5.24	5.89	5.69
Butte des Morts	48	8,053	47.28 2.83	30.78 2.73	22.83 4.06	11.47 4.14
Winnebago	49	98,821	49.43	32.87	20.14	8.80
williebago	72	50,021	2.98	3.07	2.65	2.80
Green	51	6,742	43.53	23.59	16.93	7.75
		-	2.59	2.67	3.67	3.75
Beaver Dam	53	5,485	51.55	34.55	27.40	13.25
1/	 α	2 706	1.99	2.57	3.34	3.75
Kegonsa	54	2,706	49.01 2.48	29.20 2.03	19.67 3.50	9.18 3.49
Rock	55	1,127	50.02	29.41	22.14	11.66
NOCK	33	1,127	3.07	2.21	3.35	3.73
Koshkonong	57	9,516	51.94	36.81	25.61	11.26
J		•	2.40	3.31	2.97	3.43
Lac La Belle	57	939	52.02	32.55	22.49	11.37
•	50		4.28	4.34	3.49	3.92
Oconomowoc	58	627	46.24	26.80	20.38	10.65
Okauchee	59	928	3.68 49.49	3.15	3.72	4.09
okauchee	39	920	2.49	31.32 2.28	22.68 4.13	11.75 4.69
Pine	60	550	51.83	27.97	21.03	10.99
		333	2.45	2.20	3.47	4.20
Nagawicka	61	77 5	46.71	27.70	23.09	11.77
			2.65	2.18	5.17	4.74
Pewaukee	62	1,982	53.19	32.02	24.20	12.08
Tichican	63	707	5.65	3.70	4.24	4.15
Tichigan	63	707	48.19	31.03	24.85	13.54
Browns	64	304	2.82 50.40	2.37 29.75	5.11 22.03	5.04 12.11
2. 00	0,	304	2.49	2.37	3.84	4.31
Middle	65	563	48.94	28.25	22.74	13.05
			3.04	2,46	5.31	5.22
Delavan	66	1,517	51.76	31.16	24.30	12.29
^			3.05	2.72	5.01	4.10
Como	67	740	60.33	40.42	28.28	14.07
Geneva	68	2 555	5.56	5.37	4.02	4.22
deneva	00	3,555	54.15 5.71	31.44	23.63	13.26
Mendota	108	8,488	51.01	4.87 28.74	5.23 19.80	4.90 8.59
	.50	0,100	2.58	2.36	3.19	3.16
Monona	109	2,791	49.27	27.68	19.81	9.36
		-	3.08	2.39	4.39	3.90
Waubesa	110	1,882	47.56	27.53	21.31	10.38
			2 .7 6	2.16	6.56	5.28

APPENDIX D4. 17 July 1973 (1359-16091, 1359-16094)

<u>Section D4.1.</u> Regression Models and Correlation Coefficients

The regression model for the prediction of the multivariate trophic state index is in Section VII.

Section D4.2. Three-dimensional Color Ratio Model

The MSS color ratio model is in Section VII (Figure 35). It is very similar in appearance to the model constructed from 9 August 1972 data.

Section D4.3. Concatenations of Extracted Lakes

Eighteen of the 21 lakes extracted from the frames are found in Figures D4-1 and D4-2. Lake Winnebago is common to both frames. Cloud interference is noted over some of the lakes.

Section D4.4. MSS-Lake Surface Area Relationships

The estimates of lake surface area using the MSS pixel counts are found in Table D4-1.

<u>Section D4.5.</u> Lake MSS Descriptive Statistics

The MSS statistics for Frame 1359-16091 are in Table D4-2 and those for Frame 1359-16094 are in Table D4-3.

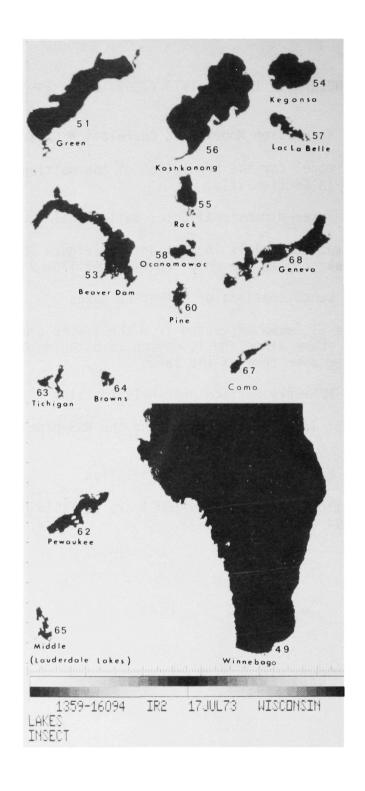


Figure D4-1. IR2 concatentation of 15 Wisconsin lakes extracted from Frame 1359-16094 (17 July 1973).

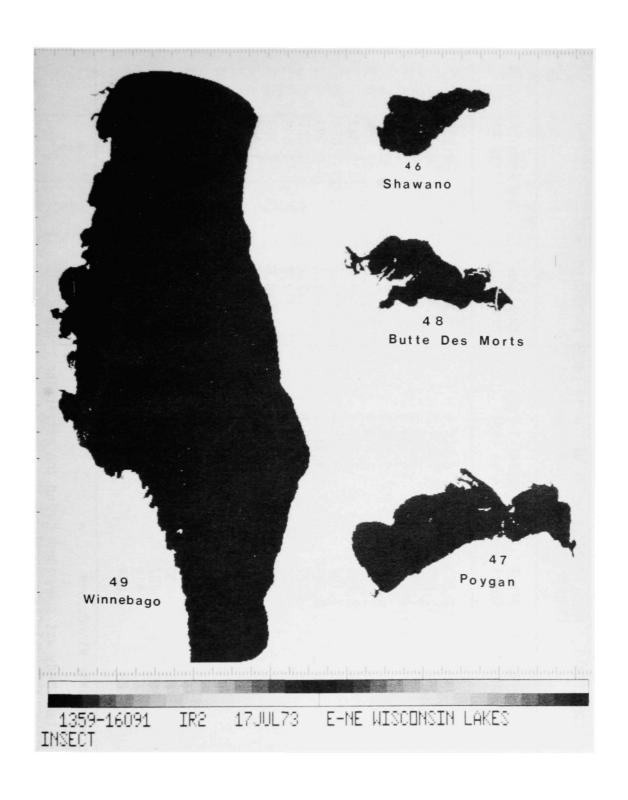


Figure D4-2. IR2 concatenation of 4 Wisconsin lakes extracted from Frame 1359-16091 (17 July 1973).

TABLE D4-1. AREAL ASPECTS OF 21 WISCONSIN LAKES EXTRACTED FROM FRAMES 1359-16091 and 1359-16094 (17 JULY 1973)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT- Area Ratio
Shawano	46	5,263	2,514.1	2,491.3	0.991
Poygan	47	15,836	7,564.9	4,448.5	a
Butte des Morts	48	7,600	3,630.5	3,584.4	0.987
Winnebago	49	112,887	53,926.1	55,730.4	1.034
Green	51	6,594	3,150.0	2,972.9	0.944
Beaver Dam	53	5,057	2,415.7	2,671.0	1.106
Kegonsa	54	2,716	1,297.4	1,099.2	0.847
Rock	55	1,102	526.4	554.8	1.054
Koshkonong	56	9,029	4,313.2	4,241.3	0.983
Lac La Belle	57	927	442.8	452.1	1.021
Oconomowoc	58	613	292.8	317.7	1.085
Okauchee	59	791	377.9	450.8	1.193
Pine	60	563	269.0	284.5	1.058
Nagawicka	61	505	241.2	415.2	b
Pewaukee	62	1,851	884.2	1,008.9	1.141 ^b
Tichigan	63	561	268.0	449.8	1.141c
•					1.050
Browns	64 65	317	151.4	160.3	1.059
Middle	65 66	630	301.0	337.6	1.122 ^d
Delavan	66 67	1,487	710.3	717.9	1.011
Como	67	615	293.8	383.0	1.304 ^b
Geneva	68	3,684	1,759.9	2,129.5	1.210 ^b

apixel count includes Lake Winneconne. bCloud interference.

CA portion of the lake body was truncated during the extraction process. dIncludes the entire Lauderdale lake complex.

TABLE D4-2. MSS DESCRIPTIVE STATISTICS FOR 4 WISCONSIN LAKES EXTRACTED FROM FRAME 1359-16901 (17 JULY 1973)

Lake Name	Serial	Pixel	LA			
	Number Count		Green	Red	IR1	IR2
Poygan	47	15,836	56.74 2.96	39.27 3.45	32.09 4.37	16.74 3.32
Butte des Morts	48	7,600	53.31	34.49	28.99	13.44
Winnebago	49	112 , 887 ^a	3.04 51.41 3.29	3.45 32.40 3.31	4.51 23.94 3.62	3.67 10.74 3.35
Shawano	46	5,263	46.38 2.69	28.38 2.89	20.61 3.57	10.16 3.54

aSouthern end of Lake Winnebago is outside the sensor field of view.

TABLE D4-3. MSS DESCRIPTIVE STATISTICS FOR 17 WISCONSIN LAKES EXTRACTED FROM FRAME 1359-16094 (17 JULY 1973)

Laka Nama	Serial	Pixel	LA	NDSAT-1	MSS Bands	Bands	
Lake Name	Number	Count	Green	Red	IR1	IR2	
Green	51	6,594	52.65	29.40	21.00	10.69	
Beaver Dam	53	5,057	2.27 56.88	2.10 38.74	3.37 33.17	3.35 14.70	
Kegonsa	54	2,716	2.40 60.79	2.72 36.33	3.80 20.71	3.40 13.97	
Rock	55	1,102	2.59 51.85	2.25 30.38	4.06 21.99	3.83 11.42	
Koshkonong	56	9,029	3.04 54.72	3.13 37.93	4.44 29.03	4.37 12.26	
Lac La Belle	57	927	2.79 56.55	3.52 34.60	3.89 23.29	3.21 12.00	
Oconomowoc	58	613	5.43 49.58	5.24 28.35	4.48 21.04	4.64	
0kauchee	59	791	3.45 50.77	3.31	3.86 23.42	4.17	
Pine	60	563	3.57 53.20	3.46 28.25	5.13 22.35	5.27 12.95	
Nagawicka	61	505	4.07 51.92	3.37 31.30	4.87 25.04	5.51 13.91	
Pewaukee	62		6.11 52.27	5.26	5.73	5.46	
		1,851	3.75	31.26	24.50 5.26	13.04	
Tichigan	63	561	52.04 4.75	33.00	28.48 5.43	15.30 5.08	
Browns	64	317	53.91 2.12	31.25 2.28	24.09 3.39	13.07 3.72	
Middle	65	630	46.91 2.95	25.95 2.71	22.87 5.07	10.73 6.94	
Delavan	66	1,487	57.85 3.49	33.98 2.87	30.45 4.78	14.74 4.03	
Como	67	615	59.61 4.50	40.60 4.35	28.89 4.43	15.20 4.35	
Geneva	68	3,684	52.22 4.11	28.12 3.68	22.14 4.57	12.67 4.71	

APPENDIX D5. 14 August 1972 (1022-16373)

Section D5.1. Regression Models, and Correlation Coefficients (Table D5-1)

Twelve Minnesota lakes were extracted from the frame; Maple Lake (241) was not included in the final regression model efforts.

 Darling (16)
 Clearwater (23)

 Le Homme Dieu (18)
 Maple (241)

 Minnewaska (19)
 Cokato (25)

 Nest (20)
 Buffalo (26)

 Green (21)
 Silver (28)

 Wagonga (22)
 Minnetonka (29)

TABLE D5-1. CORRELATIONS BETWEEN GROUND TRUTH AND MSS DATA (COLORS AND COLOR RATIOS) FOR 11 MINNESOTA LAKES IN FRAME 1022-16373 (14 AUGUST 1972).

	PC1	CHLA	LNCHLA	SECCHI	LNSECCHI
GRN RED IR1 IR2 GRNRED GRNIR1 GRNIR2 REDIR1 REDIR2 IR1IR2	0.422	0.487	0.461	-0.749	-0.734
	0.547	0.613	0.610	-0.766	-0.801
	0.890	0.763	0.620	-0.791	-0.920
	0.764	0.758	0.698	-0.626	-0.801
	-0.585	-0.646	-0.725	0.415	0.492
	-0.920	-0.704	-0.539	0.557	0.728
	-0.644	-0.602	-0.558	0.268	0.475
	-0.940	-0.670	-0.454	0.562	0.728
	-0.636	-0.568	-0.495	0.220	0.439
	0.536	0.195	-0.052	-0.597	-0.518

The best regression model for the prediction of trophic state is

It explains about 96 percent of the variation about the mean (Table D5-2) The observed and predicted PCl values are in Table D5-3.

TABLE D5-2. ANALYSIS OF VARIANCE TABLE OF PC1 REGRESSION MODEL FOR 11 MINNESOTA LAKES IN FRAME 1022-16373 (14 AUGUST 1972).

		Analy	sis of Variance	2
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected)	10	42,423	4.242	
Regression Residual	2 8	40.750 1.673	20.375 0.209	97.488

 $R^2 = 0.9606 \times 100 = 96.06\%$ s.e. of estimate = 0.456

TABLE D5-3. PC1 RESIDUALS OF 11 MINNESOTA LAKES IN FRAME 1022-16373 (14 AUGUST 1972).

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Darling	16	-0.73	-0.34	-0.39
Le Homme Dieu	18	-1.06	-0.84	-0.22
Minnewaska	19	-0.32	-0.68	0.36
Nest	20	0.77	1.04	-0.27
Green	21	-1.10	-1.00	-0.10
Wagonga	22	4.40	4.65	-0.25
Clearwater	23	0.01	0.08	-0.07
Cokato	25	1.61	1.05	0.56
Buffalo	26	2.31	2.92	-0.61
Silver	28	4.79	4.23	0.46
Minnetonka	29	0.73	0.29	0.44

The best model for the prediction of Secchi disc transparency is:

LNSECCHI = -4.105 - 154.13 GRNIR1 + 76.641 GRNIR2 + 265.290 REDIR1 - 130.200 REDIR2

It explains about 87 percent of the variation about the mean (Table D5-4). The observed and predicted Secchi disc transparency values are in Table D5-5. Caution is advised in using this model because a relatively large number of variables are incorporated into it.

TABLE D5-4. ANALYSIS OF VARIANCE TABLE OF THE SECCHI DISC TRANSPARENCY REGRESSION MODEL FOR 11 MINNESOTA LAKES IN FRAME 1022-16373 (14 AUGUST 1972).

	Analysis of Variance						
Source	df	Sum of Squares	Mean Square	Calculated F			
Total (corrected)	10	9.529	0.953				
Regression Residual	4 6	8.324 1.205	2.081 0.201	10.353			

 $R^2 = 0.8735 \times 100 = 87.35\%$ s. e. of estimate - 0.448

TABLE D5-5. SECCHI DISC TRANSPARENCY RESIDUALS OF 11 MINNESOTA LAKES IN FRAME 1022-16373 (14 AUGUST 1972).

Lake Name	Serial Number	SE CC HI	SECCHI	SECCHI-SECCHI
Darling Le Homme Dieu Minnewaska Nest Green Wagonga Clearwater Cokato Buffalo Silver Minnetonka	16	2.79	1.87	0.92
	18	1.73	2.45	-0.72
	19	1.55	1.73	-0.18
	20	0.97	0.97	0.00
	21	2.29	2.68	-0.39
	22	0.23	0.16	0.07
	23	1.80	1.25	0.55
	25	2.74	2.82	-0.08
	26	1.98	1.44	0.54
	28	0.15	0.31	-0.16
	29	1.47	1.60	-0.13

Efforts to construct a regression model for the prediction of chlorophyll \underline{a} drew negative results.

Section D5.2. Three-dimensional Color Ratio Model

The color ratio model is displayed in Figure D5-1. Wagonga Lake and Silver Lake are isolated from the other lakes because their IRl values exceed their RED DN values. The two lakes are often referred to as being hypereutrophic.

Section D5.3. Concatenation of Extracted Lakes

The Frame 1022-16373 concatenation is in Figure D5-2. Portions of Lake Minnetonka and Lake Le Homme Dieu were outside the sensor field of view, resulting in the linear shore line effects. Minnetonka is a complex lake consisting of 15 large bays.

Section D5.4. MSS-Lake Surface Area Relationships

The areal aspects of Frame 1022-16373 are in Table D5-6.

Section D5.5. Lake MSS Descriptive Statistics

The MSS statistics for Frame 1022-16373 are in Table D5-7.

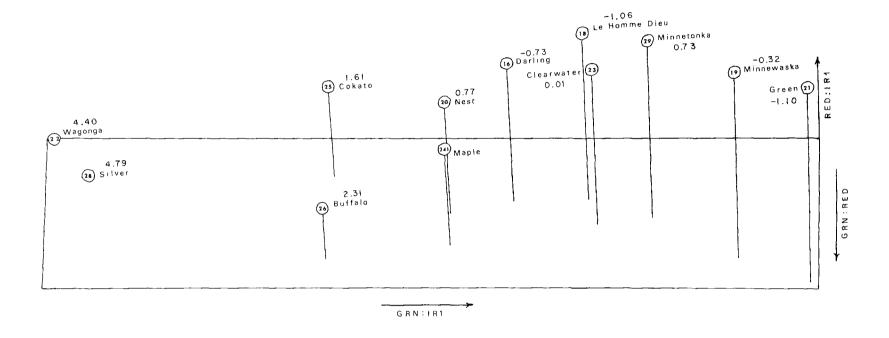


Figure D5-1. Three-dimensional MSS color ratio model of 12 Minnesota lakes extracted from Frame 1022-16373 (14 August 1972).

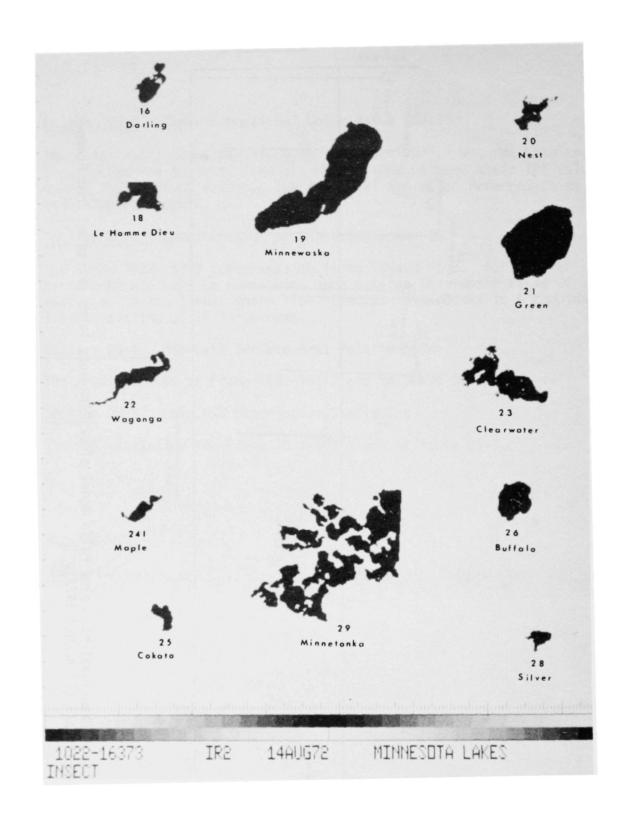


Figure D5-2. IR2 concatenation of 12 Minnesota lakes extracted from Frame 1022-16373 (14 August 1972).

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TABLE D5-6. AREAL ASPECTS OF 12 MINNESOTA LAKES EXTRACTED FROM FRAME 1022-16373 (14 AUGUST 1972).

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT-1 Area Ratio
Darling	16	824	393.5	386.1	0.981
Le Homme Dieu	18	1,127	538.2	765.7	a
Minnewaska	19	6,996	3,340.9	3,144.5	0.941
Nest	20	778	376.3	382.4	1.016
Green	21	4,846	2,314.2	2,355.8	1.018
Wagonga	22	1,339	639.4	725.2	1.134
Clearwater	23	2,561	1,223.0	1.287.8	1.053
Maple	241	518	247.4	287.3	1.161
Cokato	25	470	224.5	220.2	0.981
Buffalo	26	1,334	637.1	611.1	0.959
Silver	28	367	175.3	170.8	0.974
Minnetonka	29	9,787	4,673.7	5,855.6	a

 $^{^{\}it a}$ A portion of the lake was outside the sensor field of view.

TABLE D5-7. MSS DESCRIPTIVE STATISTICS FOR 12 MINNESOTA LAKES EXTRACTED FROM FRAME 1022-16373 (14 AUGUST 1972).

Lake Name	Serial Number	Pîxel Count	LA Green	NDSAT-1 J Red	MSS Bands IR1	IR2
Darling	16	825	49.30 ^a 4.00 ^b	29.37 4.27	23.89 5.28	13.59 5.57
Le Homme Dieu	18	1,163	51.76	30.90	24.02	13.51
Minnewaska	19	6.996	3.01 50.56	3.33 28.74	4.45 21.66	5.03 10.72
Nest	20	788	2.65 46.81	2.11 27.60	3.32 23.54	3.97 12.08
Green	21	4,846	2.67 46.25	1.98 25.78	4.62 19.12	5.48 9.31
Wagonga	22	1,339	2.06 55.77	1.59 34.92	2.74 36.92	3.34 17.18
Clearwater	23	2.561	3.48 47.64	2.96 27.82	3.33 22.00	3.90 11.15
Maple	241	5.8	2.47 44.22	2.09 25.38	4.56 22.23	5.14 12.43
Cokato	25	470	2.16 41.37	1.80 25.19	4.81 22.37	5.26 12.74
Buffalo	26	1,334	2.87 46.68	1.80 26.49	4.19 25.36	5.39 11.64
Silver	28	376	2.28 55.75	1.46 33.86	4.37 35.89	3.88 17.10
Minnetonka	29	9.787	2.46 53.81 5.30	2.30 31.60	2.72 24.11	4.10 11.53
			5.30	4.31	4.87	4.85

Mean DN value for the lake. Standard deviation of the lake DN values.

APPENDIX D6. 6 OCTOBER 1973 (1075-16321)

Section D6.1. Regression Models, and Correlation Coefficients (Table D6-1)

Sixteen Minnesota lakes were extracted from the frame. Lakes Sakatah, Calhoun, Zumbro, and Maple were not used in the construction of the regression model.

Clearwater (23	Minnetonka (29)	Madison (35)
Maple (241)	Forest (30)	Sakatah (36)
Cokato (25)	White Bear (31)	Calhoun (103)
Buffalo (26)	St. Croix (32)	Zumbro (105)
Carrigan (27)	Spring (33)	•
Silver (28)	Pepin (34)	

Table D6-1. CORRELATIONS BETWEEN GROUND TRUTH AND MSS DATA (COLOR RATIOS) FOR 12 MINNESOTA LAKES IN FRAME 1075-16321 (6 OCTOBER 1972).

	PC1	CHLA	LNCHLA	SECCHI	LNSECCHI
GRNRED	-0.375	0.067	-0.197	0.582	0.517
GRNIR1	-0.793	-0.391	-0.494	0.706	0.827
GRNIR2	-0.620	-0.425	-0.305	0.424	0.545
REDIR1	-0.663	-0.471	-0.425	0.425	0.606
REDIR2	-0.393	-0.410	-0.173	0.105	0.250
IR11R2	0.220	-0.146	0.205	-0.349	-0.353

The best model for the prediction of trophic state is:

$$\widehat{PC1} = 11.553 - 7.132 \text{ REDIR } 1$$

This model explains about 44 percent of the variation about the mean (Table D6-2). It is of little practical value. The observed and predicted PCl values are in Table D6-3.

TABLE D6-2. ANALYSIS OF VARIANCE TABLE FOR THE PC1 REGRESSION MODEL FOR 12 MINNESOTA LAKES EXTRACTED FROM FRAME 1075-16321 (6 OCTOBER 1972).

	Analysis of Variance						
Source	df	Sum of Squares	Mean Square	Calculated F			
Total (Corrected)	11	42.274	3.843				
Regression Residual	1 10	18.561 23.713	18.561 23.713	7.827			

 $R^2 = 0.4391 \times 100 = 43.91\%$ s. e. of estimate = 1.540

TABLE D6-3. PC1 RESIDUALS OF 12 MINNESOTA LAKES EXTRACTED FROM FRAME 1075-16321 (6 OCTOBER 1972).

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Clearwater Cokato Buffalo Carrigan Silver Minnetonka Forest White Bear St. Croix Spring Pepin Madison	23 25 26 27 28 29 30 31 32 33 34 35	0.01 1.61 2.31 4.40 4.79 0.73 -1.22 -1.41 -0.17 2.33 2.10 1.36	0.95 0.84 0.14 3.11 4.81 1.06 0.45 1.31 1.40 1.22 0.87 0.67	-0.94 0.77 2.17 1.29 -0.02 -0.33 -1.67 -2.72 -1.57 1.10 1.23 0.69

Section D6.2. Three-dimensional Color Ratio Model

The color ratio model is displayed in Figure D6-1.

Section D6.3. Concatenation of Extracted Lakes

The 15 lakes are displayed in two concatenations, Figure D6-2 and Figure D6-3. A portion of Lake Pepin is outside the sensor field of

view, accounting for the linear shoreline. The lake images are in scale and this results in the very small image of Lake Zumbro. Lake St. Croix was truncated during processing.

Section D6.4. MSS-Lake Surface Area Relationships

The areal aspects of the lakes extracted from Frame 1075-16321 are in Table D6-4.

Section D6.5. Lake MSS Descriptive Statistics

The MSS statistics are in Table D6-5.



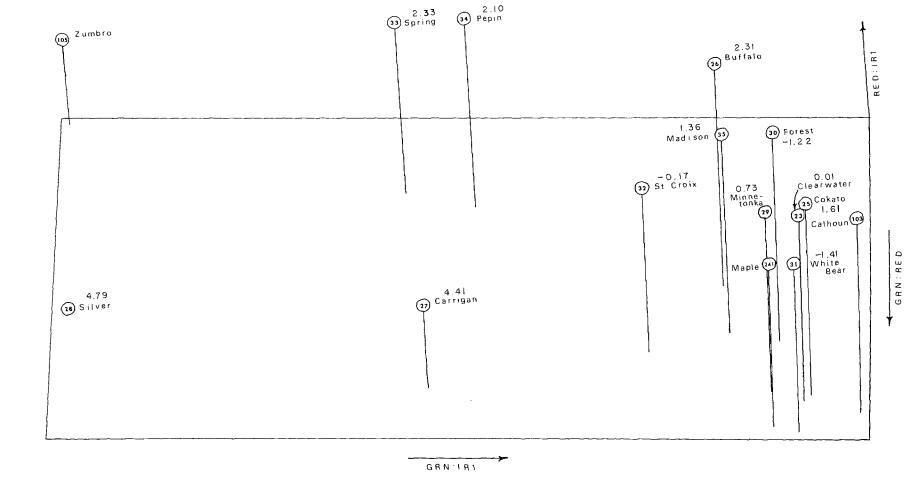


Figure D6-1. Three-dimensional MSS color ratio model of 15 Minnesota lakes extracted from Frame 1075-16321 (6 October 1972).

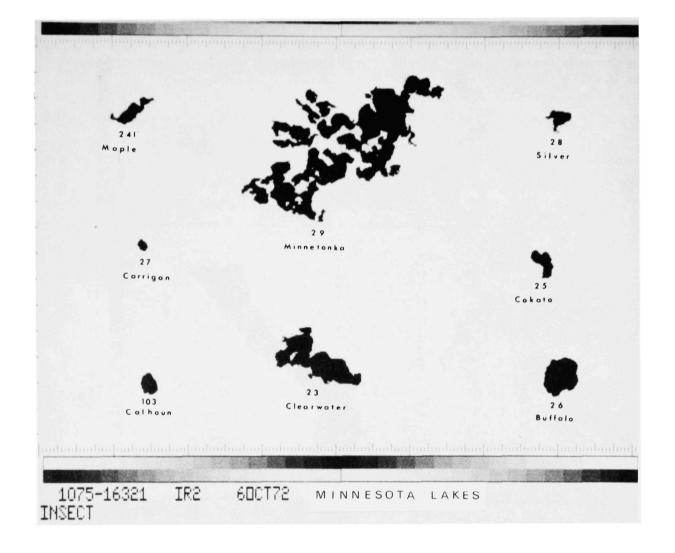


Figure D6-2. IR2 concatenation of 8 Minnesota lakes extracted from Frame 1075-16321 (6 October 1972). Figure D6-3 contains 8 additional lakes extracted from the same frame.

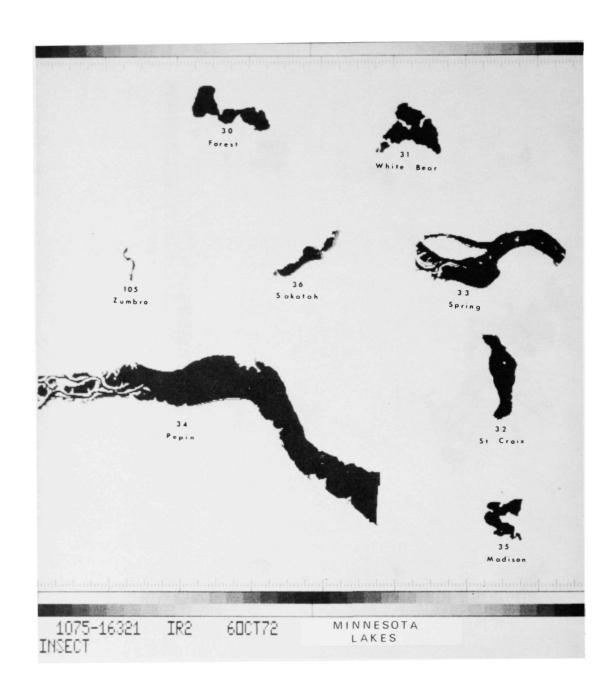


Figure D6-3. IR2 concatenation of 8 Minnesota lakes extracted from Frame 1075-16321 (6 October 1972).

[.]aThe entire image was not extracted from the CCT's.

bA portion of the lake was outside the sensor field of view.

CThe disparity may be related to the long sinuous shape of the water body.

TABLE D6-5. MSS DESCRIPTIVE STATISTICS FOR 15 MINNESOTA LAKES EXTRACTED FROM FRAME 1075-16321 (6 OCTOBER 1972)

	Serial	Pixel	LAI	LANDSAT-1 MSS Bands			
Lake Name	Number	Count	Green	Red	IRI	IR2	
Clearwater	23	2,797	33.13 ^a 2.42 ^b	17.03 2.93	11.46 5.70	5.14	
Maple	241	561	32.95 2.42	16.49 2.81	11.59 6.11	5.97	
Cokato	25	481	31.53 2.90	16.31 2.72	10.86 5.66	5.16	
Buffalo	26	1,350	35.22 2.16	20.43 1.95	12.77 4.25	4.46	
Carrigan	27	125	32.12 2.34	16.71 2.75	14.12 6.40	7.11	
Silver	28	386	41.15 1.61	23.20 1.64	24.56 2.95	8.83	
Minnetonka	29	12,131	35.90 2.49	18.61 2.54	12.65 5.23	5.09	
Forest	30	1,945	34.35 2.09	18.76 2.39	12.05 4.84	4.99	
White Bear	31	2,233	33.36 2.98	16.63 3.60	11.57 6.25	5.20	
St. Croix	32	2,202	31.19 2.64	16.84 3.46	11.83 4.98	5.17	
Spring	33	5,338	34.64 2.28	22.52 2.47	15.55 4.76	6.60	
Pepin	34	16,910	33.72 2.09	21.56	14.39 4.40	5.88	
Madison	35	1,224	35.37 2.23	19.50 2.35	12.78 5.24	5.67	
Zumbro	105	129	38.29 5.44	27.39 2.83	23.05 5.20	14.17	
Calhoun	103	363	33.79 2.18	17.15 3.12	11.32 5.28	4.93	

^aMean DN value for the lake bStandard deviation of the lake DN values.

APPENDIX D7. 8 October 1972 (1077-16431)

Section D7.1. Regression Models, and Correlation Coefficients (Table D7-1)

Ten lakes were extracted from the frame; Lake Winona, Trace Lake, and Big Stone Lake were not used to develop the regression model.

Darling (16) Minnewaska (19) Winona (101)
Carlos (17) Nest (20) Trace (102)
Le Homme Dieu (18) Green (21) Big Stone (104)
Wagonga (22)

TABLE D7-1. CORRELATIONS BETWEEN GROUND TRUTH AND MSS DATA (COLOR RATIOS) FOR 7 MINNESOTA LAKES EXTRACTED FROM FRAME 1077-16431 (8 OCTOBER 1972)

	PC1	CHLA	LNCHLA	SECCHI	LNSECCHI
GRNRED	-0.975	-0.936	-0.945	0.876	0.935
GRNIR1	-0.941	-0.962	-0.968	0.738	0.858
GRNIR2	-0.770	-0.786	-0.918	0.474	0.579
REDIR1	-0.918	-0.963	-0.953	0.679	0.826
REDIR2	-0.675	-0.716	-0.864	0.370	0.473
IR11R2	0.453	0.466	0.168	-0.581	-0.660

The best model for the prediction of trophic state is:

This model explains about 95 percent of the variation about the mean (Table D7-2). The observed and predicted PC1 values are in Table D7-3

TABLE D7-2. ANALYSIS OF VARIANCE TABLE OF THE PC1 REGRESSION FOR 7 MINNESOTA LAKES EXTRACTED FROM FRAME 1077-16431 (8 OCTOBER 1972)

6		Ana1	ysis of Varianc	e
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected)	6	25.269	4.212	
Regression Residual	1 5	24.035 1,233	24.035 0.247	97.433

 $R^2 = 0.9512 \times 100 = 95.12\%$ s.e. of estimate = 0.49/

TABLE D7-3. PC1 RESIDUALS OF 7 MINNESOTA LAKES EXTRACTED FROM FRAME 1077-16431 (8 OCTOBER 1972)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Darling Carlos Le Homme Dieu Minnewaska Nest Green Wagonga	16 17 18 19 20 21 22	-0.73 -1.55 -1.06 -0.32 0.77 -1.10 4.40	-0.92 -1.18 -0.68 -0.06 1.09 -1.90 4.07	0.19 -0.37 -0.38 -0.26 -0.32 0.80 0.33

Section D7.2. Three-dimensional Color Ratio Model

The MSS color ratio model is displayed in Figure D7-1. The PCl values are in very good agreement with the model.

Section D7.3. Concatenation of Extracted Lakes

The 10 lakes are shown in Figure D7-2.

Section D7.4. MSS-Lake Surface Area Relationships

The areal aspects of the lakes extracted from Frame 1077-16431 are in Table D7-4.

<u>Section D7.5.</u> Lake MSS Descriptive Statistics The MSS statistics are presented in Table D7-5.

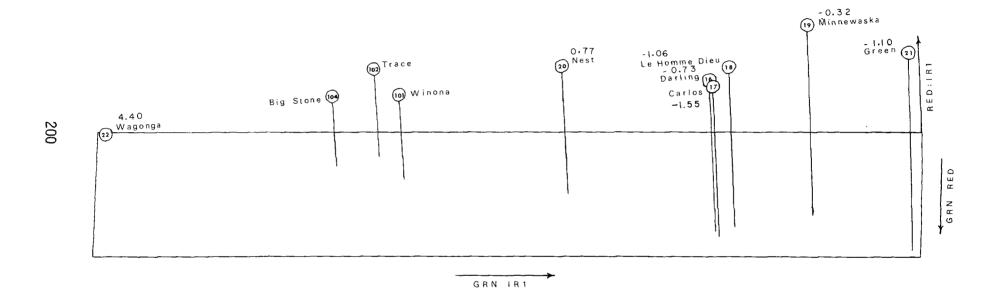


Figure D7-1. Three-dimensional MSS color ratio model of 10 Minnesota lakes extracted from Frame 1077-16431 (8 October 1972).

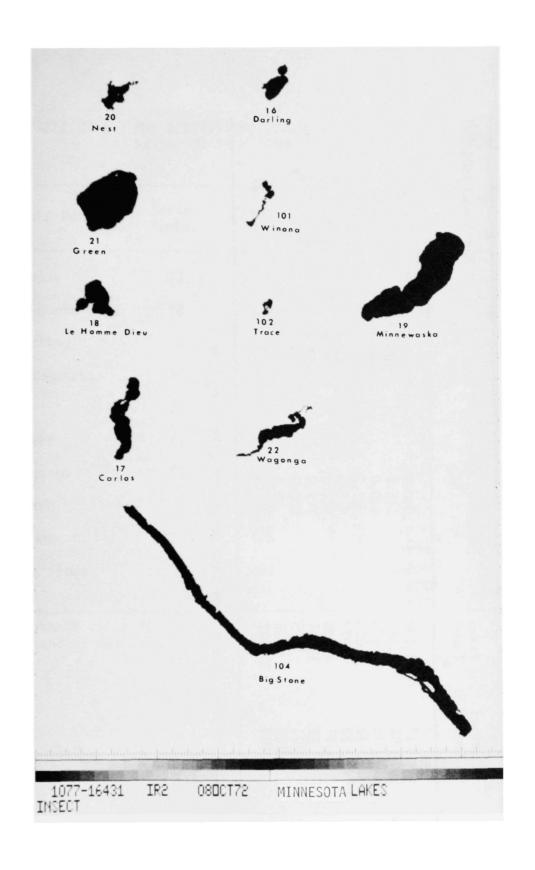


Figure D7-2. IR2 concatenation of 10 Minnesota lakes extracted from Frame 1077-16431 (8 October 1972).

TABLE D7-4. AREAL ASPECTS OF 10 MINNESOTA LAKES EXTRACTED FROM FRAME 1077-16431 (8 OCTOBER 1972)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT-1 Area Ratio
Carlos	17	2,200	1,050.9	1,019.8	0.970
Le Homme Dieu	18	1,561	745.7	705.8	0.947
Darling	16	923	440.9	386.1	0.876
Minnewaska	19	7,028	3,357.3	2,877.4	0.857
Nest	20	872	416.6	382.4	0.918
Green	21	4,986	2,381.8	2,187.8	0.919
Wagonga	22	1,501	717.0	654.4	0.913
Winona	101	425	203.0	73.3	a
Trace	102	102	89.8		
Big Stone	104	10,407	4,971.4	5,103.3	1.027

 $^{^{\}mathrm{a}}$ The LANDSAT-1 image includes pixels from Lake Agnes and Lake Henry.

TABLE D7-5. MSS DESCRIPTIVE STATISTICS FOR 10 MINNESOTA LAKES EXTRACTED FROM FRAME 1077-16431 (8 OCTOBER 1972)

Lake Name	Serial	Pixel	LAI	NDSAT-1 M	ISS Bands	
Lake Name	Number	Count	Green Red		IR1	IR2
Carlos	17	2,200	33.19 ^a 2.86 ^b	17.25 3.36	10.58 4.56	4.74
Le Homme Dieu	18	1,561	33.27	17.54	10.48	4.50
Darling	16	923	2.56 31.72 1.91	2.95 16.61 2.76	4.16 10.14 4.29	4.64
Minnewaska	19	7,028	37.48 1.68	20.11	11.14 3.05	4.173 3.46
Nest	20	872	31.94 1.95	17.73 2.26	11.53 4.87	5.79
Green	21	4 , 986	33.69 2.27	17.16 2.12	9.35 2.81	3.87 3.20
Wagonga	22	1,501	40.97 2.47	24.96 2.11	24.91 3.20	9.28 4.96
Trace	102	188	36.20 4.62	21.38	15.68 7.02	9.49 8.05
Winona	101	425	35.02 2.40	19.92	14.76 6.02	7.57 6.91
Big Stone	104	10,407	38.76 1.93	22.56 3.05	17.58 3.78	6.11 4.50

^aMean DN value for the lake. ^bStandard deviation of the lake DN values.

APPENDIX D8. 28 MAY 1973 (1309-16325)

Section D8.1. Regression Models, and Correlation Coefficients (Table D8-1)

Thirteen Minnesota lakes were extracted from the frame. Lakes Calhoun and Maple were not used in the development of the regression model.

Clearwater (23)	Carrigan (27)	Spring (33)
Maple (24)	Silver (28)	Madison (35)
Cokato (25)	Forest (30)	Sakatah (36)
Buffalo (26)	White Bear (31)	Calhoun (103)
• •	St. Croix (32)	

TABLE D8-1. CORRELATIONS BETWEEN MSS DATA (COLORS AND COLOR RATIOS) AND PC1 VALUES FOR 11 MINNESOTA LAKES EXTRACTED FROM FRAME 1309-16325 (28 MAY 1973)

	PC1
GRN RED IR1 IR2 GRNRED GRNIR1 GRNIR2 REDIR1	-0.068 -0.040 -0.014 -0.259 0.061 0.017 0.316 -0.036
REDIR2 IR11R2	0.434 0.702

The best model for the prediction of trophic state is:

$$\widehat{PC1} = -16.537 + 9.844 IR1IR2$$

This model explains about 49 percent of the variation about the mean (Table D8-2) and is not adequate. The observed and predicted PC1 values are in Table D8-3.

TABLE D8-2. ANALYSIS OF VARIANCE TABLE OF THE PC1 REGRESSION MODEL FOR 11 MINNESOTA LAKES EXTRACTED FROM FRAME 1309-16325 (28 MAY 1973)

Source		Ana 1	ysis of Varianc	e
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected)	10	41.326	4.133	
Regression]	20.385	20.385	8.761
Residua1	9	20.941	2.327	

 $R^{-} = 0.4933 \times 100 = 49.33\%$ s.e. of estimate = 1.525

TABLE D8-3. PC1 RESIDUALS OF 11 MINNESOTA LAKE EXTRACTED FROM FRAME 1309-16325 (28 MAY 1973)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Clearwater Cokato Buffalo Carrigan Silver Forest White Bear St. Croix Spring Madison Sakatah	23 25 26 27 28 30 31 32 33 35 36	0.01 1.61 2.31 4.40 4.78 -1.22 -1.41 -0.17 2.33 1.36 1.38	2.88 2.07 2.29 1.78 3.89 -0.19 -0.04 -0.82 1.65 1.51 0.38	-2.87 -0.46 0.02 2.62 0.89 -1.03 -1.34 0.65 0.68 -0.15

Section D8.2. Three-dimensional Color Ratio Model

The MSS color ratio model is displayed in Figure D8-1. There appears to be little agreement between lake position in the model and trophic state as defined by the PC1 value.

Section D8.3. Concatenation of Extracted Lakes

The concatenation of 13 lakes is displayed as Figure D8-2. Sakatah Lake includes both Upper Sakatah Lake and Lower Sakatah Lake.

Section D8.4. MSS-Lake Surface Area Relationships The areal aspects of the lakes are in Table D8-5. Section D8.5. Lake MSS Descriptive Statistics The MSS statistics are in Table D8-4.

TABLE D8-4. DESCRIPTIVE STATISTICS FOR 13 MINNESOTA LAKES EXTRACTED FROM FRAME 1309-16325 (28 MAY 1973)

l al Mana	Serial	Pixel	LAI	NDSAT-1 M	ISS Bands	
Lake Name	Number	Count	Green	Red	IR1	IR2
Clearwater	23	2,689	45.89 ^a	26.74	19.09	9.68
Maple	24	584	3.24 ^b 49.09	2.94 28.11	3.92 21.15	4.18
Cokato	25	442	3.04 44.73	2.48 26.60	4.40 20.32	4.91 10.75
Buffalo	26	1,327	2.47 51.01	2.08 31.60 2.17	3.51 22.04	4.05 11.52
Carrigan	27	401	2.06 48.12 2.37	28.29 2.12	2.82 20.86 3.49	3.24 11.21 4.26
Silver	28	368	51.79 1.71	31.92 1.58	28.36 3.04	13.67 3.80
Forest	30	1,871	52.71 6.32	33.06 2.59	26.18 3.04	15.76 3.31
White Bear	31	2,093	53.58 2.31	32.92 2.80	26.85 3.47	16.02
St. Croix	32	2,133	53.50 2.11	37.24 2.62	30.31 2.76	18.98 2.77
Spring	33	4,856	61.44 2.89	47.49 3.61	37.79 2.91	20.46
Madison	35	1,177	50.78 2.10	31.15 2.19	22.67	12.36 3.89
Sakatah	36	977	53.09 2.16	35.79 2.98	27.31 3.27	15.90 3.78
Calhoun	103	339	51.72 1.95	30.17 2.21	23.93 2.89	13.81

^aMean DN value for the lake. bStandard deviation of the lake DN values.

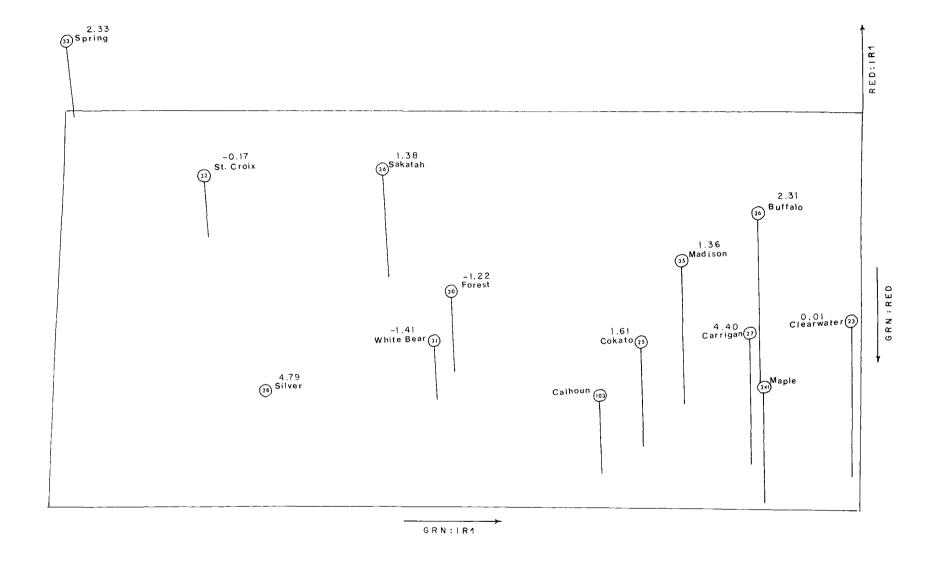


Figure D8-1. Three-dimensional MSS color ratio model of 13 Minnesota lakes extracted from Frame 1309-16325 (28 May 1973).

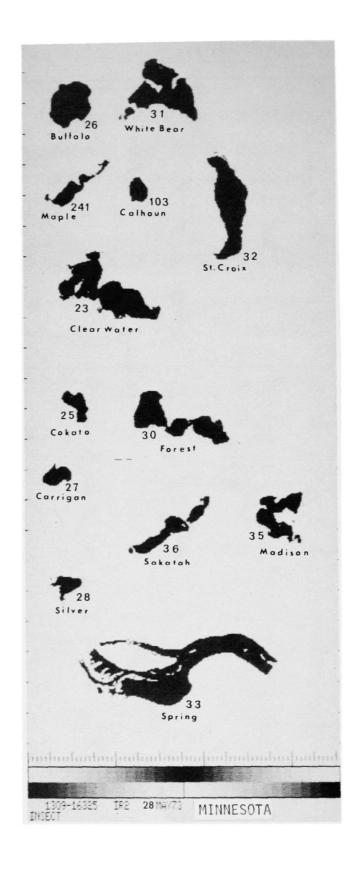


Figure D8-2. IR2 concatenation of 13 Minnesota lakes extracted from Frame 1309-16325 (28 May 1973).

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TABLE D8-5. AREAL ASPECTS OF 13 MINNESOTA LAKES EXTRACTED FROM FRAME 1309-16325 (28 MAY 1973)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT-1 Area Ratio
Clearwater	23	2,689	1,284.5	1,287.8	1.003
Maple	241	584	279.0	287.3	1.030
Cokato	25	442	211.1	220.2	1.043
Buffalo	26	1,327	633.0	611.1	0.965 _a
Carrigan	27	401	191.6	65.0	a
Silver	28	368	175.8	170.8	0.972
Forest	30	1,871	893.8	892.8	0.999
White Bear	31	2,093	999.8	1,076.5	1.077 _b
St. Croix	32	2,133	1,018.9	3,322.2	D
Spring	3 3	4,856	2,319.7	2,391.8	1.031
Madison	35	1,177	562.3	541.1	0.962
Sakatah	36	977	466.7	497.0	1.065
Calhoun	103	339	161.9	169.6	1.048

aA portion of the lake was outside the sensor field of view. The entire lake image was not extracted from the CCT's.

APPENDIX D9. 3 July 1973 (1345-16322)

Section D9.1. Regression Models, and Correlation Coefficients (Table D9-1)

Fourteen Minnesota lakes were extracted from the frame. Lakes Calhoun and Maple were not used in developing the regression model.

Clearwater (23)	Silver (28)	St. Croix (32)
Maple (241)	Minnetonka (29)	Spring (33)
Cokato (25)	Forest (30)	Madison (35)
Buffalo (26)	White Bear (31)	Sakatah (36)
Carrigan (27)		Calhoun (103)

TABLE D9-1. CORRELATIONS BETWEEN MSS DATA (COLOR RATIOS)
AND PC1 VALUES FOR 12 MINNESOTA LAKES EXTRACTED
FROM FRAME 1345-16322 (3 JULY 1973)

	PC1
GRNRED	0.239
GRNIR1	-0.788
GRNIR2	-0.641
REDIR1	-0.837
REDIR2	-0.642
IR1IR2	0.172

The best model for the prediction of trophic state is:

This model explains about 70 percent of the variation about the mean (Table D9-2), but is of little practical value. The observed and predicted PC1 values are in Table D9-3.

TABLE D9-2. ANALYSIS OF VARIANCE TABLE OF THE PC1 REGRESSION MODEL FOR 12 MINNESOTA LAKES EXTRACTED FROM FRAME 1345-16322 (3 JULY 1973)

Source		Anal	ysis of Varianc	е
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected) Regression Residual	11 1 10	41.744 29.260 12.484	3.795 29.260 1.248	23.438

 $R^2 = 0.7009 \times 100 = 70.09\%$ s.e. of estimate = 1.117

TABLE D9-3. PC1 RESIDUALS OF 12 MINNESOTA LAKES EXTRACTED FROM FRAME 1345-16322 (3 JULY 1973)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Clearwater Cokato Buffalo Carrigan Silver Minnetonka Forest White Bear St. Croix Spring Madison Sakatah	23 25 26 27 28 29 30 31 32 33 35 36	0.01 1.61 2.31 4.40 4.79 0.73 -1.22 -1.40 -0.17 2.33 1.36 1.38	-0.08 0.33 3.05 3.13 4.90 -0.31 -0.54 0.75 0.76 1.25 0.98 1.92	0.09 1.28 -0.74 1.27 -0.11 1.04 -0.68 -2.15 -0.93 1.08 0.38 -0.54

Section D9.2. Three-dimensional Color Ratio Model

The MSS color ratio model is displayed in Figure D9-1. Silver Lake's IR1 DN level exceeds its RED DN level; this isolates it from the other lakes.

Section D9.3. Concatenation of Extracted Lakes

The concatenation of the 14 lakes is in Figure D9-2.

Section D9.4. MSS-Lake Surface Area Relationships The areal aspects of the 14 lakes are in Table D9-5. Section D9.5. Lake MSS Descriptive Statistics The MSS statistics are in Table D9-4.

TABLE D9-4. MSS DESCRIPTIVE STATISTICS FOR 14 MINNESOTA LAKES EXTRACTED FROM FRAME 1345-16322 (3 JULY 1973)

	Serial	Pixel	LAI	NDSAT-1 M	ISS Bands	
Lake Name	Number	Count	Green	Red	IR1	IR2
Clearwater	23	2,485	47.29 ^a 3.25 ^b	26.59 2.49	18.11	7.21
Maple	241	505	43.43 2.49	2.49 24.15 2.21	9.85 16.94 7.55	5.19 7.86 5.43
Cokato	25	437	41.50 2.45	22.54	15.98 3.67	6.88 4.42
Buffalo	26	1,285	47.77 2.01	26.01 1.63	25.12 4.68	9.04 3.72
Carrigan	27	106	47.41 2.04	25.16 1.37	24.56 4.44	13.35
Silver	28	346	50.44 1.68	27.61 1.25	35.42 3.30	13.43
Minnetonka	29	11,239	47.05 3.79	25.44 3.26	16.96 9.07	6.89 4.66
Forest	30	1,818	42.24 2.27	24.61 2.24	16.07 3.99	7.82 4.22
White Bear	31	2,094	40.94 3.05	22.78 3.27	16.84 8.33	7.94 4.41
St. Croix	32	2,145	38.78 2.26	22.50 2.77	16.66 7.24	6.59 4.26
Spring	33	4,945	43.93 2.51	28.36 2.27	22.09 1.68	8.03 4.55
Madison	35	1,151	46.84 2.23	27.10 1.70	20.51 8.51	7.79 4.63
Sakatah	36	986	44.46 2.25	26.43 1.87	22.18 4.13	9.22 4.40
Calhoun	103	342	50.45 2.22	24.91 2.57	15.65 3.75	6.29 4.13

^aMean DN value for the lake.

Standard deviation of the lake DN values.

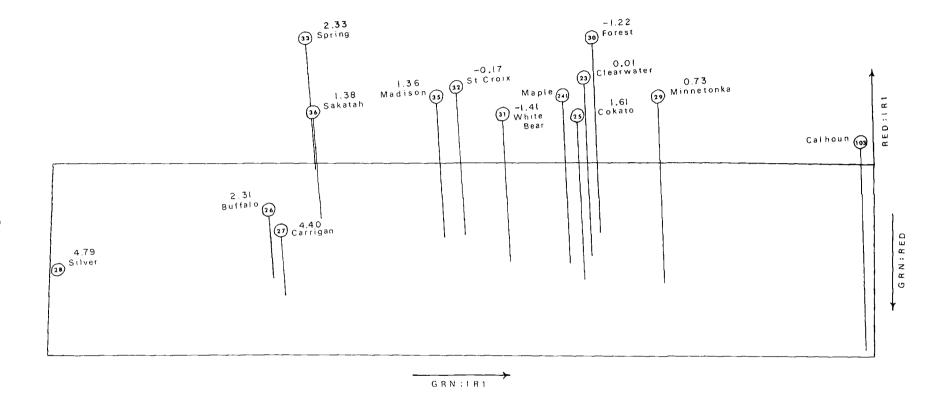


Figure D9-1. Three-dimensional MSS color ratio model of 14 Minnesota lakes extracted from Frame 1345-16322 (3 July 1973).

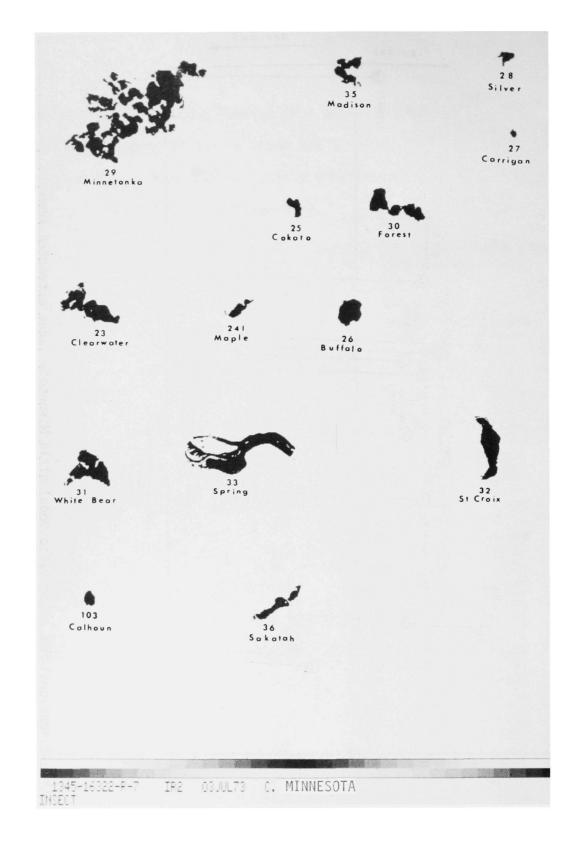


Figure D9-2. IR2 concatenation of 14 Minnesota lakes extracted from Frame 1345-16322 (3 July 1973).

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TABLE D9-5. AREAL ASPECTS OF 14 MINNESOTA LAKES EXTRACTED FROM FRAME 1345-16322 (3 JULY 1973)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT-1 Area Ratio
Clearwater	23	2,485	1,187.1	1,287.8	1.085
Maple	241	505	241.2	287.3	1.191
Cokato	25	437	208.8	220.2	1.055
Buffalo	26	1,285	613.8	611.1	0.996
Carrigan	27	106	50.6	65.6	1.296
Silver	28	346	165.3	170.8	1.033
Minnetonka	29	11,239	5,368.9	5,855.6	1.091
Forest	30	1,818	868.5	892.8	1.028
White Bear	31	2,094	1,000.3	1,076.5	1.076 _a
St. Croix	32	2,145	1,024.7	3,322.2	a
Spring	33	4,945	2,362.2	2,391.8	1,013
Madison	35	1,151	549.8	541.1	0.984
Sakatah	36	986	471.0	497.0	1.055
Calhoun	103	342	163.4	169.6	1.038

^aThe entire lake image was not extracted from the CCT's.

APPENDIX D10. 4 July 1973 (1346-16381)

Section D10.1. Regression Models, and Correlation Coefficients (Table D10-1)

Eight Minnesota lakes were extracted from the frame; Cottonwood Lake was not used in developing the regression model.

Nest (20)	Buffalo (26)
Green (21)	Carrigan (27)
Wagonga (22)	Silver (28)
Cokato (25)	Cottonwood (111)

TABLE D10-1. CORRELATIONS BETWEEN MSS DATA (COLORS AND COLOR RATIOS) AND PC1 VALUES FOR 7 MINNESOTA LAKES EXTRACTED FROM FRAME 1346-16381 (4 JULY 1973)

	PC1
GRN	0.874
RED	0.829
IR]	0.903
IR2	0.829
GRNRED	-0.595
GRNIR1	-0.956
GRNIR2	-0.800
REDIR1	-0.961
REDIR2	-0.839
IR1IR2	0.573

The best model for the prediction of lake trophic state is:

$$\widehat{PC1} = 11.715 - 8.277 \text{ REDIR1}$$

This model accounts for about 92 percent of the variation about the mean (Table D10-2). The observed and predicted PC1 values are in Table D10-3.

TABLE D10-2. ANALYSIS OF VARIANCE TABLE OF THE PC1 REGRESSION MODEL FOR 7 MINNESOTA LAKES EXTRACTED FROM FRAME 1346-16381 (4 JULY 1973)

Course		Anal	ysis of Variand	e
Source	df	Sum of Squares	Mean Square	Calculated F
Total (corrected) Regression	6	29.233 26.994	4.872 26.994	60.255
Residual	5	2.238	0.448	00.255

 $R^2 = 0.9234 \times 100 = 92.34\%$ s.e. of estimate = 0.669

TABLE D10-3. PC1 RESIDUALS OF 7 MINNESOTA LAKES EXTRACTED FROM FRAME 1346-16381 (4 JULY 1973)

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Nest	20	0.77	0.33	0.44
Green	21	-1.10	-0.34	-0.76
Wagonga	22	4.40	4.04	0.36
Cokato	25	1.61	0.86	0.75
Buffalo	26	2.31	3.07	-0.76
Carrigan	27	4.40	4.71	-0.31
Silver	28	4.79	4.49	0.30

Section D10.2. Three-dimensional Color Ratio Model

The MSS color ratio model is displayed in Figure D10-1. Lakes Wagonga, Carrigan, and Silver have IR1 values which exceed their RED DN values.

Section 10.3. Concatentation of Extracted Lakes

The concatenation of eight lakes is in Figure D10-2.

Section 10.4. MSS-Lake Surface Area Relationships

The areal aspects of the eight lakes are in Table D10-4.

Section D10.5. Lake MSS Descriptive Statistics

The MSS statistics are in Table D10-5.

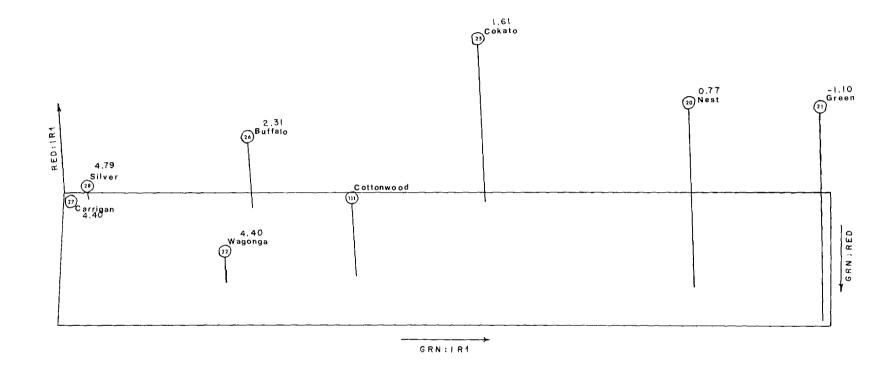


Figure D10-1. Three-dimensional MSS color ratio model of 8 Minnesota lakes extracted from Frame 1346-16381 (4 July 1973).

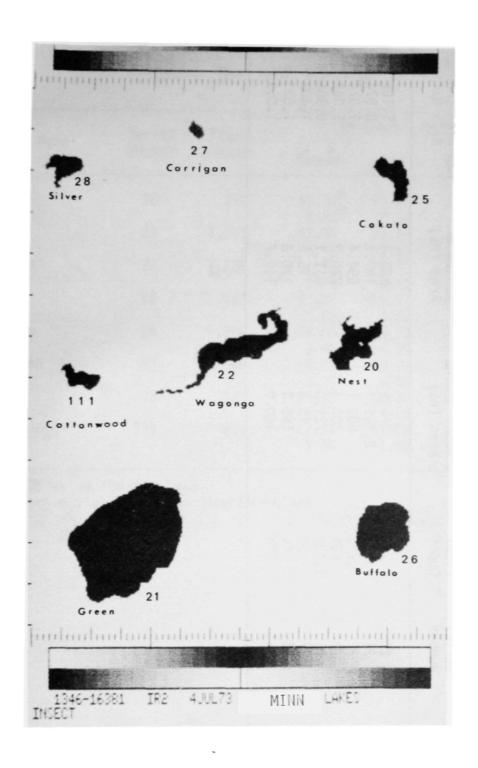


Figure D10-2. IR2 concatenation of 8 Minnesota lakes extracted from Frame 1346-16381 (4 July 1973).

TABLE D10-4. AREAL ASPECTS OF 8 MINNESOTA LAKES EXTRACTED FROM FRAME 1346-16381 (4 JULY 1973)

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area:LANDSAT-1 Area Ratio
Nest	20	724	345.9	382.4	1.106
Green	21	4,701	2,245.7	2,187.8	0.974
Wagonga	22	1,275	609.1	654.4	1.074
Cokato	25	434	207.3	220.2	1.062
Buffalo	26	1,300	721.0	611.1	0.984
Carrigan	27	98	46.8	75.6	1.402
Silver	28	346	165.3	170.8	1.033
Cottonwood	111	293	140.0	149.7	1.069

TABLE D10-5. MSS DESCRIPTIVE STATISTICS FOR 8 MINNESOTA LAKES EXTRACTED FROM FRAME 1346-16381 (4 JULY 1973)

Laka Name	Serial	Pixel	LAI	NDSAT-1 M	ISS Bands	
Lake Name	Number	Count	Green	Red	IR1	IR2
Nest	20	724	45.37 ^a 2.86 ^b	27.24 2.38	19.79 3.61	10.34 4.12
Green	21	4,701	47.34 3.48	27.54 2.93	18.91 2.71	10.06
Wagonga	22	1,275	58.42 2.79	35.47 3.09	38.25 3.04	15.45 3.39
Cokato	25	434	52.32 3.83	35.20 4.22	26.85 3.72	16.04 4.02
Buffalo	26	1,300	59.55 3.90	39.73 4.23	38.07 4.13	18.97 3.52
Carrigan	27	98	59.77 3.37	39.97 3.42	47.26 3.73	24.08 3.28
Silver	28	346	60.43 3.67	40.78 4.02	46.73 3.33	22.61 3.39
Cottonwood	111	293	52.35 1.46	32.04 1.38	30.10 3.50	12.13

^aMean DN value for the lake. ^bStandard deviation of the lake DN values.

APPENDIX D11. 19 August 1972 (1027-15233)

Section Dll.1. Regression Models, and Correlation Coefficients (Table Dll-1)

Seven New York lakes were extracted from the frame; all were incorporated into the regression model.

Conesus (91) Cayuga (95)
Canandaigua (92) Owasco (96)
Keuka (93) Cross (97)
Seneca (94)

TABLE D11-1. CORRELATIONS BETWEEN GROUND TRUTH AND MSS DATA (COLORS AND COLOR RATIOS) FOR 7 NEW YORK LAKES EXTRACTED FROM FRAME 1027-15233 (19 AUGUST 1972).

	PC1	CHLA	LNCHLA	SECCHI	LNSECCHI
GRN RED IR1 IR2 GRNRED GRNIR1 GRNIR2 REDIR1 REDIR2 IR1IR2	0.245	0.601	0.463	-0.792	-0.804
	0.772	0.833	0.664	-0.507	-0.572
	0.752	0.632	0.550	0.063	-0.013
	0.890	0.599	0.510	0.116	0.023
	-0.906	-0.717	-0.580	0.072	0.158
	-0.596	-0.331	-0.307	-0.419	-0.356
	-0.740	-0.337	-0.284	-0.389	-0.315
	-0.286	-0.032	-0.084	-0.621	-0.583
	-0.645	-0.207	-0.186	-0.490	-0.423
	-0.860	-0.349	-0.268	-0.239	-0.152

The best model for the prediction of the lake trophic state index is:

$$\widehat{PC1} = -4.981 - 8.805 \text{ GRNIR} + 19.301 \text{ REDIR}$$

This model explains about 83 percent of the variation about the mean (Table D11-2). The observed and predicted PCl values are in Table D11-3.

TABLE D11-2. ANALYSIS OF VARIANCE TABLE OF THE PC1 REGRESSION MODEL FOR 7 NEW YORK LAKES EXTRACTED FROM FRAME 1027-15233 (19 AUGUST 1972).

Source	Analysis of Variance						
	df	Sum of Squares	Mean Square	Calculated F			
Total (corrected) Regression Residual	6 2 4	12.741 10.552 2.189	2.124 5.276 0.547	9.645			

 $R^2 = 0.8282 \times 100 = 82.82\%$ s.e. of estimate = 0.740

TABLE D11-3. PC1 RESIDUALS OF 7 NEW YORK LAKES EXTRACTED FROM FRAME 1027-15233 (19 AUGUST 1972).

Lake Name	Serial Number	PC1	PC1	PC1-PC1
Conesus	91	-1.41	-1.82	0.41
Canandaigua	92	-3.63	-2.67	-0.96
Keuka	93	-2.14	-2.82	0.68
Seneca	94	-2.89	-2.58	-0.31
Cayuga	95	-2.74	-3.28	0.52
Owasco	96	-2.47	-1.98	-0.49
Cross	97	0.86	0.73	0.13

<u>Section D11.2</u>. Three-dimensional Color Ratio Model

The MSS color ratio is displayed in Figure D11-1. Lake Canandaiqua appears to be misplaced if its PC1 value is an accurate assessment of its trophic state.

Section D11.3. Concatenation of Extracted Lakes

The concatenation of seven lakes is found in Figure D11-2.

Section D11.4. MSS-Lake Surface Area Relationships

The areal aspects of the seven lakes are in Table Dll-4.

Section D11.5. Lake MSS Descriptive Statistics

The MSS statistics are in Table D11-5.

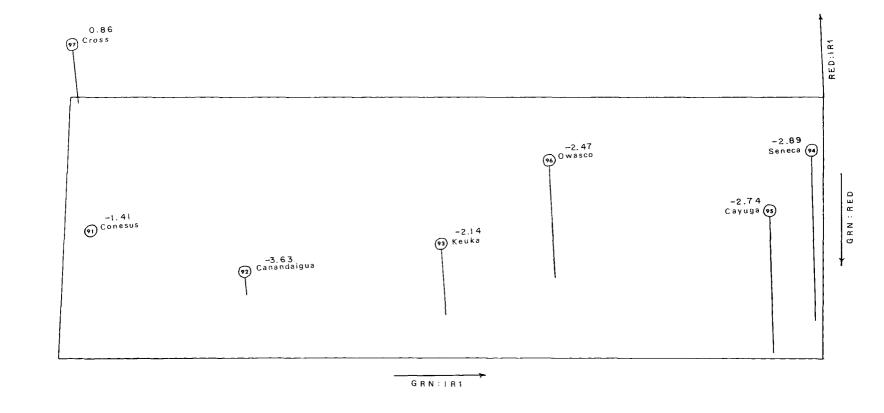


Figure D11-1. Three-dimensional MSS color ratio model of 7 New York lakes extracted from Frame 1027-15233 (19 August 1972).

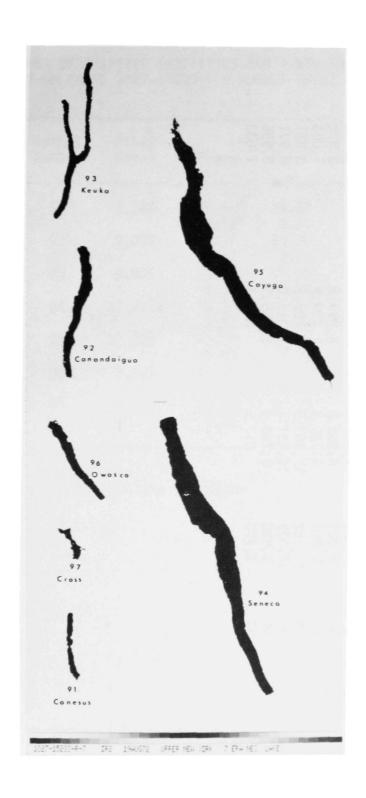


Figure D11-2. IR2 concatenation of 7 New York lakes extracted from Frame 1027-15233 (19 August 1972).

TABLE D11-4. AREAL ASPECTS OF 7 NEW YORK LAKES EXTRACTED FROM FRAME 1027-15233 (19 AUGUST 1972).

Lake Name	Serial Number	Pixel Count	LANDSAT-1 Lake Area (ha)	Map Lake Area (ha)	Map Area: LANDSAT-1 Area Ratio
Conesus	91	2,764	1,319.9	1,347.3	1.021
Canandaigua	92	9,009	4,302.2	4,219.8	0.998
Keuka	93	9.896	4,725.8	4,739.9	1.003
Seneca	94	37,782	17,583.9	17,252.5	0.981
Cayuga	95	37,339	17,831.1	17,319.9	0.971
Owas co	96	5,835	2,786.5	2,745.5	0.985
Cross	97	1,712	817.6	844.4	1.033

TABLE D11-5. MSS DESCRIPTIVE STATISTICS FOR 7 NEW YORK LAKES EXTRACTED FROM FRAME 1027-15233 (19 AUGUST 1972).

Lake Name	Serial Pixel LANDSAT-1 MSS Bands					
	Number	Count	Gree n	Red	IRI	IR2
Conesus	91	2,764	37.38 ^a 2.12 ^b	19.67 2.21	16.47 3.49	7.83 4.14
Canandaigua	92	9,009	40.17 3.14	20.20 2.68	16.32 2.04	6.05 3.83
Keuka	93	9,896	38.49 2.32	19.09 2.19	14.23 3.37	5.99 4.09
Seneca	94	37,782	42.53 2.68	21.02	13.49 3.61	5.04 3.45
Cayuga	95	37 ,339	41.11 1.92	19.86 3.01	13.25 3.41	5.11 3.42
0wasco	96	5,835	40.79 4.00	20.78 4.05	14.38 3.72	5.94 3.81
Cross	97	1,712	43.25 3.62	25.34 3.16	19.26 4.10	9.11 4.68

^aMean DN value for the lake. ^bStandard deviation of the lake DN values

APPENDIX D12. 11 October 1972 (1080-15180)

Section D12.1. Regression Models and Correlation Coefficients

Five lakes were extracted from the frame. No regression models were constructed due to the small number of observations. Correlation coefficients between ground truth and MSS data were not determined for the same reason.

Section D12.2. Three-dimensional Color Ratio Model

The MSS color ratio model is displayed in Figure D12-1. The large shift in position of Lake Cayuga (95) - compare with Figure 58 - may be a consequence of the thin cloud deck over it.

Section D12.3. Concatenation of Extracted Lakes

The extracted lakes are in Figure D12-2. Lakes Cross and Cayuga are only partially in the sensor field of view; this accounts for the linear "shore lines".

Section D12.4. MSS-Lake Surface Area Relationships

The areal aspects of the lakes are in Table D12-1.

Section D12.5. Lake MSS Descriptive Statistics

The MSS statistics are in Table D12-2.

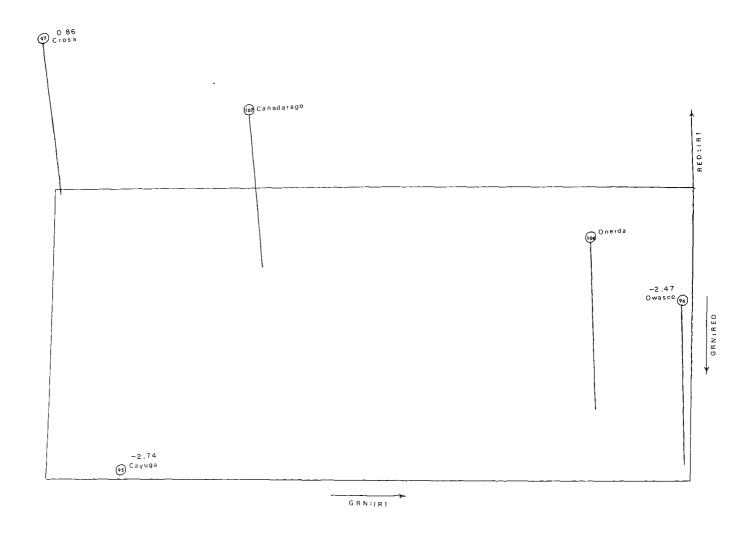


Figure D12-1. Three-dimensional MSS color ratio model of five New York lakes extracted from Frame 1080-15180 (11 October 1972).

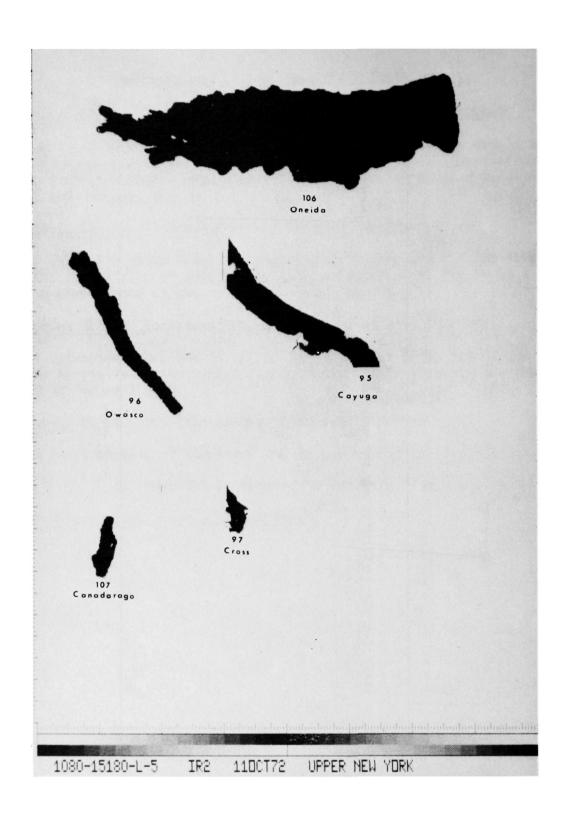


Figure D12-2. IR2 concatenation of five New York lakes extracted from Frame 1080-15180 (11 October 1972).

TABLE D12-1. AREAL ASPECTS OF 5 NEW YORK LAKES EXTRACTED FROM FRAME 1080-15180 (11 OCTOBER 1972).

Lake Name	Serial	Pixel	LANDSAT-1	Map Lake	Map Area: LANDSAT-1
	Number	Count	Lake Area (ha)	Area (ha)	Area Ratio
Cayuga Owasco Cross Oneida Canadarago	95 96 97 106 107	8,799 6,018 1,072 44,934 1,644	4,206.0 2,876.6 512.4 21,478.5 785.8	17,319.9 2,745.5 844.4 20,720.6	a 0.955 a 0.963

^aOnly a fraction of the lake surface is in the sensor field of view.

TABLE D12-2. MSS DESCRIPTIVE STATISTICS FOR 5 NEW YORK LAKES EXTRACTED FROM FRAME 1080-15180 (11 OCTOBER 1972).

Lake Name	Serial Number	Pixel Count	LAN Green	IDSAT-1 M	ISS Bands IRI	IR2
Cayuga	95	8,799	36.31ª 2.72 ^b	18.18 2.89	12.49 4.88	6.23 5.63
Owasco	96	6,018	38.66 2.94	19.46 3.63	11.40 3.75	4.53 4.00
Cross	97	1,072	38.68 1.28	22.63 3.01	13.58 3.87	4.93 4.68
Oneida	106	44,934	34.89 2.11	18.07 2.15	10.53 2.77	4.17 2.93
Canadarago	107	1,664	35.53 2.18	19.89 2.62	11.75 4.20	4.63

^aMean DN value for the lake. ^bStandard deviation of the lake DN values.

APPENDIX E

N x N SQUARED EUCLIDIAN DISTANCE MATRIX

The dendrogram of 100 NES-sampled lakes (Figure 15) was created using the output of the McKeon hierarchical cluster analysis program. The clustering procedure was carried out using the matrix in this appendix. Only the lower triangular form of the matrix is reproduced here.

MCKEON CLUSTER ANALYSIS VERSION I.1 CONTROL INPUT: 100 :(3X,6F10.5) FIRST ROW OF DATA FOR VERIFICATION-2.678F 00 -5.413E-01 -2.976E 00 -2.206E-01 7.655E-01 SQUARED DISTANCES BETWEEN POINTS BEFORE CLUSTERING .8. 10 11 12 13 14 15 0 .633 3 .511 .728 1.052 •505 1.490 1.511 3.307 2.961 .571 •542 1.191 2.536 1.271 1.730 .395 .695 2.258 1.551 .679 1.658 n .760 2.244 1.756 .951 1.244 .962 1.564 2.666 1.439 .431 3.280 5.833 5.290 4.401 3.515 2.568 10 1.319 2.450 2.050 2.589 3.605 3.528 2.155 6.044 4.698 5.546 1.847 4.580 5.190 4.318 4.884 7.145 7.828 6.684 6.858 7.412 8.634 5,540 8.561 7.854 1,642 1.421 1.131 .896 2.736 1.774 1.617 1.314 3.177 1.278 2.697 •566 4.672 5.238 2.396 5.425 2.571 6.758 1-646 1.209 3.070 2.707 5.927 3.232 7.943 8.772 2.622 4.553 6.822 5.087 3.375 8.718 5.156 2.370 8.601 1.741 6.605 9.630 6.036 4.071 5.346 2.03? 1.002 1.968 5.008 5.363 8.134 12.168 5.214 3.294 1.361 8.189 17 3.929 1.900 2.991 1.409 •696 1.552 7.975 5.845 12.181 2.790 2.568 11.240 2.501 1.469 2.072 .851 .952 2.373 2.379 5.216 5,128 2.526 11.120 3.021 5.661 2.385 4.818 4.325 3.705 3.191 3.481 6.090 8.991 2.907 20 .936 1-477 1.840 3-097 5.192 5.376 4.397 1.444 4.005 9.164 9.789 3.156 7.214 2.998 5.512 1.033 3.402 1.436 4.293 7.498 9.894 .204 2.281 22.133 25.375 23.284 19.575 29.635 35.780 36.401 31.353 14.676 28.494 39.817 36.582 30.258 29.357 .489 23 .657 1.350 1.129 2.342 2.727 2.011 3.337 7.454 9-325 1.713 1.802 7.334 22.071 25.930 23.830 19.299 30.077 36.507 31.833 26.961 36.974 6.173 5.819 6.436 7.887 7.886 10.346 12.829 12.407 8.642 6.556 9.523 19.213 17.974 16.559 9.711 6.218 19.590 26 8.049 7.981 11.475 14.650 4.604 9.423 11.985 10.320 7.092 15.137 8.627 14.305 25.121 29.424 31.508 14.417 18.172 26.603 28.481 21.351 23.003 35,476 39,725 37.647 33.579 29.636 28 23.864 26.324 23.642 40.050 40.641 35.882 32.866 30.494 29.962 2.532 3.000 1.530 2.119 3.684 5.317 10.684 7.009 .691 4.457 30 2.564 1.555 2.020 3.166 .630 1.885 2.275 5.310 5.688 9.832 2.323 3.261 4.990 2.394 10.609 6.205 9.321 12.213 4.862 8.987 4.547 3.223 5.379 3.440 4.110 1.609 31 8.133 1.360 3.829 1.578 2.689 11.355 18.630 14,228 8.760 10.724 8.534 6.602 12.953 16.994 15.817 13.246 4.447 16.682 12.429 18,229 11.679 10.899 11.043 13.889 14.202 5.839 18.537 6.965 15.510 7.815 5.909 7.541 7.722 34 8.050 5.554 2.281 4.371 3.025 2.886 5.592 8.361 1.738 5.215 10.509 10.454 5.548 4.890 5.083 15.716 6.512 12.798 8.679 7.167 7.782 36 4.586 6.034 11.067 10.305 6.644 15.121 12.203 5.311 15.560 7.558 16.692 17.877 23.367 18.586 12.202 10.813 37 38.964 47.677 55.855 55.514 51.164 27.557 43.687 55.890 50.561 46.610 46.502 43.655 3.748 2.074 2.811 1.818 2.241 2.732 4.827 2.183 1.016 1.313 1.078 4.710 39 1.373 2.334 1.211 3.857 2.025 2.491 12.584 1.853 1.208 3.100 3.631 1.169 2.111 10.062 8.767 9.644 8.384 8.271 8.426 11.652 5.286 4.148 5.601 8.733 10.557 3.121 10.007 11.161 9.036 3.002 4.073 7.980 10.196 7.268 9.988 8.649 8.696 6.141 6.323 11.275 13.706 18.326 8.577 22.704 7.279 11.877 8.212 4.519 8.003 5.147 8.843 12.322 10.826 22.066 15.198 29.181 26.758 27.907 31.161 22.466 18.838 16.490 20.440 21.185 27.697 27,000 3.246 5.223 4.854 1.726 4.825 6.309 8.351 2.756 45 2.714 4.360 .340 7.917 3.986 2.796 .798 7.966 1.149 1.078 .938 2.255 .692 -972 2.012 2.280 3.551 6.517 2.191 10.875 10.778 10.326 6.572 12.328 6.701 4.095 11.622 4.370 4.492 8.248 9.885 8.777 8.212 8.045 1.242 5.216 9.341 5.337 2.837 2.169 5.815 9.592 8.041 7.748 48 3.220 11.356 15.559 9.497 7.102 5.545 14.697 13.484 3.082 9.105 15,342 13,567 10.444 12.016 6.350 7.932 9.643 7.835 1.290 3.058 11.291 14.419 5.125 6.285 3.503 5.557 4.043 11.675 1.344 3.065 3.122 9.885 7.664 10.679 5.998 3.099 5.836 7.215 4,345 15.287 3.972 3.857 5.566 7.443 6.252 3.659 4.703 11.341 9.857 4.686 4.197 3.211 3.118 52 22.882 18.115 20.228 6.717 15.684 24.023 21.256 12.904 10.344 17.644 18.125 17.746 3.487 9.451 8.760 6.617 .947 6.121 4.377 6.202 12.033 7.119 10.479 3.046

55	3.091	1.405	2.293	3.842	.893	.643	2.250	1.818	6.095	5.932	8.278	12.722	2.932	2.795	8.224
			10.169	8.836	13.723	17.709	16.927	12.687	6.167	12.659	22.389	19.388	12.575	10.932	19.969
56	8.208	9.624		5.336	1.915	1.403	3.691	3.316	7.954	8.560	10.384	16.150	4.813	4.859	9.717
57	5.089	2.986	3.651					4.780	13.281	10.666	14.168	18.984	7.580	4.006	14.787
58	7.649	4.562	7.192	10.031	4.522	2.853	5.616						2.657	2.081	12.070
59	2.756	1.568	2.264	4.167	1.984	2.399	2.850	1.816	5.676	5.911	10.057	12.864		1.330	7.120
60	1.100	.378	•666	2.029	.345	.654	1.145	1.022	3.665	2.817	5.803	8.364	1.204		
δĪ	4.125	4.405	4.494	4.097	6.933	9.477	8.761	5.804	3.227	7.031	14.515	13.370	6.545	6.019	15.821
62	2.252	2.495	3.207	4.523	4.140	5.514	6.898	5.491	4.467	6.372	12.752	13.851	5.087	1.978	9.640
			12.389	9.802	17.274	22.154	21.519	17.452	6.481	15.922	25.254	22.465	16.825	17.103	21.589
63	11.530	13.762			1.368	1.134	2.385	1.271	6.495	6.092	9.695	13.297	2.979	1.910	10.997
64	3.111	1.170	2.587	4.385					11.803	10.096	10.935	17.014	5.620	6.344	13.624
65	7.676	4.485	6.079	8.156	3.188	1.845	3.448	3.062		10.070			8.491	8.831	14.029
66	5.095	6.972	6.282	5,260	9.647	13.461	12.542	9.894	3.101	8.981	16.387	14.746			
67	6.039	7.416	5.608	4.759	7.555	10.051	12.318	11.640	4.030	10.327	14.479	17.172	10.054	10.522	6.979
68	4.870	2.448	4.027	6.109	1.850	.961	2.5°	2.128	9.011	7.532	9.627	14.506	3.946	3.404	10.909
69	15.745	11.669	12.830	15.059	8.457	5.997	7.412	8.502	20.389	16.450	13.643	21.929	11.344	14.926	18.792
70	21.170	16.064	19.025	20.417	14.144	11.215	11.141	11.073	26.140	19.146	17.160	22.834	15.942	19.369	27.082
			2.697	4.181	1.051	.633	1.787	3.045	6.854	5.025	4.980	9.862	2.713	4.515	5.065
71	3.713	2.687					3.914	2.639	3.082	6.323	9.098	11.846	3.425	7.283	12.529
_ 72	4.033	3,334	2.202	2.104	3.078	4.668									
73	2.656	1.495	1.666	2.415	1.813	2.772	2.442	.983	3.692	5.173	8.792	11.266	2.171	3.778	12.024
74	1.381	1.159	1.586	1.809	2.547	4.038	3.216	1.637	2.214	2.962	7.884	8.000	2.103	2.637	10.401
75	12.380	14.671	15.909	15.185	20.061	24.045	23.653	19.561	11.817	16.540	28.537	23.338	18.612	13.367	24.353
76	7.037	8.526	8.319	6.432	11.917	15.846	14.254	10.698	4.155	9.801	17.975	14.936	10.460	11.029	17.671
		5.796	7.785	10.787	4.478	2.368	4.672	5.134	14.864	10.796	11.808	17.767	7.338	5.963	13.835
77	8.931				7.571	10.541	9.217	6.353	3.062	6.512	13.793	11.820	6.219	6.155	14.376
78	_ 3.841	4.706	5.095	4.381	2 455			3.401	2.401	6.681	12.569	14.172	4.337	4.121	12.266
79	2.562	2.126	2.165	2.403	3.455	5.312	5.827								
80	4.035	3.785	4.792	4.443	6.602	8.855	8.046	4.691	3.828	6.847	14.380	13.141	6.048	5.188	16.232
81	_1.107_	.650	1.439	2.450	1.712	2.847	3.147	1.758	3.096	4.220	8.962	10.576	2.015	1.409	9.074
82	1.813	.985	1.978	2.943	2.300	3.430	4.021	2.013	3.546	5.478	10.925	12.654	2.987	1.860	11.052
83	3.869	4.269	4.031	3.607	6.549	9.200	8.947	6.079	2.644	7.375	14.721	14.181	6.611	6.119	14.756
84	2.520	2.177	1.508	1.196	2.781	4.709	5.110	3.156	1.389	6.052	10.592	12.813	3.889	5.411	10.384
			5.346	5.178	7.290	9.488	8.789	5.608	4.391	6.557	14.663	12.679	6.623	4.645	15.953
85	4.043	4.103					12 020						8.650	9.150	15.617
86	5.388	6.541	6.000	4.615	9.258	12.849	12.029	8.761	2.756	9.006	16.645	15.145			
87	25.252	23.701	23.250	26.207	18.687	15.566	13.874	20.152	32.518	19.321	11.366	17.378	18.195	25.397	20.835
88	1.983	3.329	2.604	3,515	2.608	3.352	2.150	4.561	4.871	.642	•929	1.850	1.400	4.061	2.161
89	2.441	2.220	1.939	2.815	1.677	2.368	.631	1.301	4.583	2.209	3.152	4.934	•489	4.189	8.028
90	2.103	3.063	2.039	2.583	2.495	3.710	1.501	2.985	3.787	1.071	1.688	2.481	•645	4.903	5.631
91	3.453	1.759	2.430	3.486	1.068	1.184	1.194	.698	5.789	5.406	6.696	10.732	1.743	4.241	9.569
92	20.187	15.770	16.489	17.186	12.349	10.675	10.606	10.767	22.346	20.451	16.548	24.834	14.391	21.830	24.288
					5.710	5.460				8.825	7.960	11.902	4.671	10.224	16.852
93	9.146	7.447	7.158	8.843			3.325	4.187	12.075						
94	19.975	14.725	16.114	16.875	12.376	11.162	12.874	10.636	21.252	24.083	23.336	32.578	16.040	20.739	27.895
95	12.260	8.077	9.468	10.978	6.069	4.296	6.208	5.562	15.361	14.256	14.044	21.369	9.533	11.626	18.028
96	9.001	4 703													
97		0.102	6.417	7.569	3.928	3.243	3.470	4.432	11.254	10.109	7.877	14.630	5.424	10.853	11.799
98	4.214	6.702 3.641		7.569 2.515	5.226	7.711				8.410	14.340	15.686	6.192		11.799
	4.214	3.641	6.417 3.651	2.515	5.226	7.711	7.971	4.558	2.066	8.410	14.340	15.686	6.192	10.853 7.415	13.748
	.810	3.641 1.123	6.417 3.651 .595	2.515 .326	5.226 1.442	7.711 2.927	7.971 3.192	4.558 2.696	2.066 .815	8.410 2.354	14.340 5.631	15.686 7.093	6.192 2.193	10.853 7.415 3.555	13.748
99	.810 2.549	3.641 1.123 4.488	6.417 3.651 .595 2.806	2.515 .326 2.228	5.226 1.442 5.441	7.711 2.927 8.461	7.971 3.192 6.535	4.558 2.696 6.057	2.066 .815 1.355	8.410 2.354 3.925	14.340 5.631 7.944	15.686 7.093 7.238	6.192 2.193 3.694	10.853 7.415 3.555 6.873	13.748 4.819 8.848
	.810	3.641 1.123	6.417 3.651 .595	2.515 .326	5.226 1.442	7.711 2.927	7.971 3.192	4.558 2.696	2.066 .815	8.410 2.354	14.340 5.631	15.686 7.093	6.192 2.193	10.853 7.415 3.555	13.748
99	.810 2.549 1.541	3.641 1.123 4.488 1.785	6.417 3.651 .595 2.806 1.575	2.515 .326 2.228 2.666	5.226 1.442 5.441 1.869	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100	.810 2.549 1.541	3.641 1.123 4.488	6.417 3.651 .595 2.806	2.515 .326 2.228	5.226 1.442 5.441	7.711 2.927 8.461	7.971 3.192 6.535	4.558 2.696 6.057	2.066 .815 1.355	8.410 2.354 3.925	14.340 5.631 7.944	15.686 7.093 7.238	6.192 2.193 3.694	10.853 7.415 3.555 6.873	13.748 4.819 8.848
99 100	.810 2.549	3.641 1.123 4.488 1.785	6.417 3.651 .595 2.806 1.575	2.515 .326 2.228 2.666	5.226 1.442 5.441 1.869	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100	.810 2.549 1.541 16 0	3.641 1.123 4.488 1.785	6.417 3.651 .595 2.806 1.575	2.515 .326 2.228 2.666	5.226 1.442 5.441 1.869	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100 16 17	.810 2.549 1.541 16 0 1.386	3.641 1.123 4.488 1.785	6.417 3.651 .595 2.806 1.575	2.515 .326 2.228 2.666	5.226 1.442 5.441 1.869	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100 16 17 18	.810 2.549 1.541 16 0 1.386 .702	3.641 1.123 4.488 1.785 17	6.417 3.651 .595 2.806 1.575	2.515 .326 2.228 2.666	5.226 1.442 5.441 1.869	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100 16 17 - 18 19	.810 2.549 1.541 16 0 1.386 .702 1.685	3.641 1.123 4.488 1.785 17 0 1.996 3.091	6.417 3.651 .595 2.806 1.575 18	2.515 .326 2.228 2.666 19	5.226 1.442 5.441 1.869	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223	2.515 .326 2.228 2.666 19	5.226 1.442 5.441 1.869 20	7.711 2.927 8.461 2.922	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226	6.417 3.651 2.895 1.575 18 0 2.458 4.223 2.785	2.515 .326 2.228 2.666 19	5.226 1.442 5.441 1.869 20	7.711 2.927 8.461 2.922 21	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21	.810 2.549 1.541 16 0 1.386 .702 1.685 2.765 2.348 29.282	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824	2.515 .326 2.228 2.666 19	5.226 1.442 5.441 1.869 20 0 5.268 15.775	7.711 2.927 8.461 2.922 21	7.971 3.192 6.535 1.319 22	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349	5.226 1.442 5.441 1.869 20	7.711 2.927 8.461 2.922 21	7.971 3.192 6.535 1.319	4.558 2.696 6.057 1.696	2.066 .815 1.355 3.829	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349	5.226 1.442 5.441 1.869 20 0 5.268 15.775 .709	7.711 2.927 8.461 2.922 21	7.971 3.192 6.535 1.319 22	4.558 2.696 6.057 1.696 23	2.066 .815 1.355 3.829 24	8.410 2.354 3.925 2.031	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21 22 23 24	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116 30.948	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444	6.417 3.651 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.234 32.318	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824	5.226 1.442 5.441 1.869 20 0 5.268 15.775 .709 16.918	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366	7.971 3.192 6.535 1.319 22	4.558 2.696 6.057 1.696 23	2.066 .815 1.355 3.829 24	8.410 2.354 3.925 2.031 25	14.340 5.631 7.944 4.282	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21 22 23 24 25	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116 30.948 9.144	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244 42.318 12.858	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385	5.226 1.442 5.441 1.869 20 0 5.268 15.775 .709 16.918 4.123	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082	4.558 2.696 6.057 1.696 23	2.066 .815 1.355 3.829 24	8.410 2.354 3.925 2.031 25	14.340 5.631 7.944 4.282 26	15.686 7.093 7.238 5.334	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21 22 23 24 25 26	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116 30.948 9.144 10.573	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 32.318 12.858 13.277	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031	5.226 1.442 5.441 1.869 20 5.268 15.775 .709 16.918 4.123 3.065	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 3.36674 13.054	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076	4.558 2.696 6.057 1.696 23	2.066 .815 1.355 3.829 24	8.410 2.354 3.925 2.031 25	14.340 5.631 7.944 4.282 26	15.686 7.093 7.238 5.334 27	6.192 2.193 3.694 .471	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
16 17 18 19 20 21 22 23 24 25 26 27	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116 30.948 9.144 10.573 29.668	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.624 2.244 32.318 12.858 13.273 13.841	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031 25.792	5.226 1.442 5.441 1.869 20 5.268 15.775 7.09 16.918 4.123 3.065 15.598	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529	2.066 .815 1.355 3.829 24 0 16.184 8.540 .808	8.410 2.354 3.925 2.031 25	14.340 5.631 7.944 4.282 26	15.686 7.093 7.238 5.334 27	6.192 2.193 3.694 .471 28	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100 16 17 18 20 21 22 23 24 25 26 27 28	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 29.282 1.116 30.948 9.144 10.573 29.668 32.638	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631 42.921	6.417 3.655 2.806 1.575 18 0 2.458 4.223 2.785 31.624 2.244 32.318 12.858 13.277 31.841 35.564	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031 15.792 30.272	5.226 1.442 5.441 1.869 20 5.268 15.775 .709 16.918 4.123 3.065 15.598 17.285	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649 38.617	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401 2.722	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529 24.329	2.066 .815 1.355 3.829 24	8.410 2.354 3.925 2.031 25 2.530 14.044 16.850	14.340 5.631 7.944 4.282 26	15.686 7.093 7.238 5.334 27	6.192 2.193 3.694 .471 28	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100 16 17 18 19 20 21 22 23 24 25 26 27 28	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 20.348 21.116 30.948 9.144 10.573 29.668 32.638 2.876	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631 42.921 6.504	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244 32.318 12.858 13.877 31.841 35.564 3.783	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031 25.792	5.226 1.442 5.441 1.869 20 5.268 15.775 7.09 16.918 4.123 3.065 15.598	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529	2.066 .815 1.355 3.829 24 0 16.184 8.540 .808	8.410 2.354 3.925 2.031 25	14.340 5.631 7.944 4.282 26	15.686 7.093 7.238 5.334 27	6.192 2.193 3.694 .471 28	10.853 7.415 3.555 6.873 2.889	13.748 4.819 8.848 8.039
99 100 16 17 18 20 21 22 23 24 25 26 27 28	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 20.348 21.116 30.948 9.144 10.573 29.668 32.638 2.876	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631 42.921 6.504	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244 32.318 12.858 13.877 31.841 35.564 3.783	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 27.824 8.385 11.031 25.792 30.272 2.964	5.226 1.442 5.441 1.869 20 5.268 15.775 .709 16.918 4.123 3.065 15.598 17.285 .799	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649 38.617 5.661	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401 2.722 16.358	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529 24.329 1.519	2.066 .815 1.355 3.829 24 0 16.184 8.540 .808 3.634 17.338	8.410 2.354 3.925 2.031 25 2.530 14.044 16.850 4.767	14.340 5.631 7.944 4.282 26 7.539 8.475 3.797	15.686 7.033 7.238 5.334 27	6.192 2.193 3.694 .471 28	10.853 7.415 3.555 6.873 2.889 29	13.748 4.819 8.848 8.039
99 100 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 29.282 1.116 30.948 9.144 10.573 29.668 32.638 2.8768	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 36.305 2.739 40.444 12.010 16.371 38.631 42.921 6.500	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 3.785 31.824 2.244 32.318 12.858 13.277 31.841 35.564 3.783 .136	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031 25.792 30.272 2.964 3.078	5.226 1.442 5.441 1.869 20 5.268 15.775 7.09 16.918 4.123 3.065 15.598 17.285 4.849	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649 38.617 5.661	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401 2.722 16.358 33.256	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529 24.329 1.519 2.623	2.066 .815 1.355 3.829 24 0 16.184 8.508 3.634 17.338 33.356	8.410 2.354 3.925 2.031 25 25 2.530 14.044 16.850 4.767 13.830	14.340 5.631 7.944 4.282 26 26 7.539 8.475 3.797 14.362	15.686 7.033 7.238 5.334 27 0 1.750 15.779 32.988	6.192 2.193 3.694 .471 28	10.853 7.415 3.555 6.873 2.889 29	13.748 4.819 8.848 8.039 30
99 100 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 2.9.282 1.116 30.948 9.144 10.573 29.668 32.638 2.876 1.238 2.363 2.3	3.641 1.123 4.488 1.785 17 0.1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631 42.921 6.504 2.506	6.417 3.655 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244 32.318 12.858 13.277 31.841 35.564 3.783 2.387	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031 25.792 30.272 2.964 4.408	5.226 1.442 5.441 1.869 20 5.268 15.775 .709 16.918 4.123 3.065 15.559 17.285 .799 4.849 7.046	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649 38.617 5.661 2.615	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401 2.722 16.358 33.256 40.173	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529 24.329 1.519 2.623 4.718	2.066 .815 1.355 3.829 24 24 0 16.184 8.540 .808 3.634 17.338 33.356 41.193	8.410 2.354 3.925 2.031 25 2.530 14.044 16.850 4.767 13.830	14.340 5.631 7.944 4.282 26 26 7.539 8.475 3.797 14.362 16.095	15.686 7.033 7.238 5.334 27 27 0 1.750 15.779 32.988 39.186	0.192 2.193 3.694 .471 28 17.597 37.041 41.382	10.853 7.415 3.555 6.873 2.889 29	13.748 4.819 8.848 8.039 30
99 100 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 20.282 1.116 30.948 9.144 10.573 29.668 32.638 2.876 1.238 2.876 1.238	3.641 1.123 4.488 1.785 17 0 1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631 42.921 6.504 2.009 2.508 6.084	6.417 3.651 .595 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244 32.318 12.858 13.277 31.841 35.564 3.783 1.365 2.387 5.415	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 27.824 8.385 11.031 25.792 30.272 2.964 3.078 4.408 8.483	5.226 1.442 5.441 1.869 20 5.268 15.775 709 16.918 4.123 3.065 15.598 17.285 17.285 4.849 7.046 3.466	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649 38.617 5.661 2.615 4.234 4.669	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401 2.722 16.358 33.256 40.173 25.427	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529 24.329 1.519 2.623 4.718 2.807	2.066 .815 1.355 3.829 24 24 0 16.184 8.540 .808 3.634 17.338 33.356 41.193 24.626	8.410 2.354 3.925 2.031 25 25 2.530 14.044 16.850 4.767 13.830 13.446 9.588	14.340 5.631 7.944 4.282 26 26 7.539 8.475 3.797 14.362 16.095 9.196	15.686 7.033 7.238 5.334 27 27 0 1.750 15.779 32.988 39.186 39.196	0 17.597 37.041 41.382 26.759	10.853 7.415 3.555 6.873 2.889 29 29 0 4.350 5.323 4.764	13.748 4.819 8.848 8.039 30
99 100 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31	.810 2.549 1.541 16 0 1.386 .702 1.685 2.764 2.348 2.9.282 1.116 30.948 9.144 10.573 29.668 32.638 2.876 1.238 2.363 2.3	3.641 1.123 4.488 1.785 17 0.1.996 3.091 6.084 1.226 38.305 2.739 40.444 12.010 16.371 38.631 42.921 6.504 2.506	6.417 3.655 2.806 1.575 18 0 2.458 4.223 2.785 31.824 2.244 32.318 12.858 13.277 31.841 35.564 3.783 2.387	2.515 .326 2.228 2.666 19 0 4.032 3.320 24.940 2.349 27.824 8.385 11.031 25.792 30.272 2.964 4.408	5.226 1.442 5.441 1.869 20 5.268 15.775 .709 16.918 4.123 3.065 15.559 17.285 .799 4.849 7.046	7.711 2.927 8.461 2.922 21 0 32.522 2.518 33.366 8.674 13.054 32.649 38.617 5.661 2.615	7.971 3.192 6.535 1.319 22 21.452 1.193 14.082 8.076 .401 2.722 16.358 33.256 40.173	4.558 2.696 6.057 1.696 23 0 23.002 5.507 6.291 21.529 24.329 1.519 2.623 4.718	2.066 .815 1.355 3.829 24 24 0 16.184 8.540 .808 3.634 17.338 33.356 41.193	8.410 2.354 3.925 2.031 25 2.530 14.044 16.850 4.767 13.830	14.340 5.631 7.944 4.282 26 26 7.539 8.475 3.797 14.362 16.095	15.686 7.033 7.238 5.334 27 27 0 1.750 15.779 32.988 39.186	0.192 2.193 3.694 .471 28 17.597 37.041 41.382	10.853 7.415 3.555 6.873 2.889 29	13.748 4.819 8.848 8.039 30

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89 6.944 2.369 13.382 13.560 8.232 9.125 22.414 51.563 1.455 .965 11.307 9.457 5.931 19.049 3.060
90 8-307 1.169 11.966 12.395 6.688 8.920 19.424 46.586 .617 .414 8.813 6.179 7.185 20.795 1.697 91 4.913 5.604 16.959 15.733 9.748 11.241 24.533 55.718 4.228 3.584 13.975 15.715 7.603 20.492 7.734
91 4.913 5.604 16.959 15.733 9.748 11.241 24.533 55.718 4.228 3.584 13.975 15.715 7.603 20.492 7.734 92 19.048 20.313 39.529 43.608 32.738 34.168 53.071 95.868 17.421 17.793 26.440 32.571 9.135 14.094 24.553
93 12-131 8.627 22.468 24-958 17-977 18.375 36.182 70.726 7.114 6.067 20.045 19.069 5.123 15.496 9.608

94 95 96 97 98	18.327 8.876 9.327 12.600 6.445	23.317 13.957 9.681 7.112 1.663 2.881	36.262 29.600 25.929 4.800 7.130 3.708	38.993 28.817 27.420 6.380 6.436	29.926 21.671 17.382 4.533 2.512	31.409 23.151 22.132 4.445 5.315	47.456 38.724 34.248 9.968 10.249	86.224 79.232 71.468 28.890 34.777	20.271 12.906 8.173 5.709 1.602	19.725 13.360 8.136 5.109 2.065	33.117 18.703 15.184 20.738 8.046	40.186 25.412 20.454 17.991 7.756	17.246 9.132 6.067 23.535 14.122	27.003 18.388 15.095 45.307 31.646	27.387 19.305 13.962 6.328 3.440
100	6.350	2.247	11.328	5.584 10.148	5.933	4.646 6.865	19.068	26.418 45.652	2.332 1.626	.735	15,239 12,161	9.746 9.490	19.533 8.612	40.142 23.685	1.371 2.477
46	46 _	47	. 48	49	50_	51	52	53	54	55	56	57	58	59	60
47	8.340	0													
48	_6.328	.636	Ģ												
49 50	11.732	1.354	1.492	22 726											
51	3.260 4.874	17.764 18.119	15.776 15.509	23.736 21.795	0 2.477	n									
52	7.022	5.549	5.258	6.937	11.331	6.979	0	_							
53	18.827	4.002	4.932	1.222	31.879	29.286	10.900	0							
_ 54 55	.7.161 1.307	. 2.409 11.297	1.621 9.357	1.688_		12.180	2.758	4.014	0						
56	14.861	6.371	6.941	15.554 4.108	1.251 23.377	3.129 17.392	8.095 4.335	22.268 4.370	9.070 2.448	0 16.316	0				
. 57	2.451	13.403	11.213	18.242	1.579	4.602	11.108	25.144	11.460	344		0			
58	4.945	18.203	17.228	24.706	•759	3.902	12.208	32.128	16.419	1.865	22.905	2.015	0		
59 60	2.678 .780	8.857 6.915	7.495 5.584	12.566 10.847	4.254	3.484	4.479	19.206	6.572	1.976	11.326	3.171	4.327	0	0
61	8.579	3.658	3.675	4.517	2.844 14.248	3,606 10,167	4.297 .758	17.367 7.381	1.510	1.005 9.351	12.200 2.642	2.199 12.000	3.759 14.485	1.059 5.092	<u>0</u>
62	4.021	5.001	5.314	7.275	8.147	8.642	4.876	11.151	4.176	4.149	6.581	5.785	6.965	2.816	2.864
63	18.990	4.845	5.535	2.261	29.922	25,106	7.685	1.183	3.040	21.031	2.268	24.010	30.035	16.644	16.116
64 65	2.083 4.057	11.146 19.708	9.619 16.642	15.450 25.252	1.567 .765	2.016 2.442	5.987 12.794	22.110 33.810	8.470 16.002	.502 1.452	14.135 24.886	1.287 1.277	1.729 1.968	.815 4.219	.846 3.652
66	10.342	3.481	3.248	1.796	19.861	15.513	3.865	3.396	.721	12.600	.979	15.515	20.178	8.412	8.754
67	7.620	4.551	4.099	5.601	14.921	18.445	12.170	7.515	5.523	8.496	11.757	8.897	15.132	11.071	7.955
68	2.337	15.202	13.028	20.209	•472	2.162	9.696	27.842	12.300	.391	19.677	•673	1.037	2.407	1.870
69 70	9 <u>.</u> 482 16.208	31.201 39.026	26 <u>.464</u> 34.361	38.312_ 46.149	<u>4.130</u> . 8.338	7.291 8.124	23.210 23.999	_49 <u>•280</u> 57•190	27 <u>.3</u> 69 33.074	6.721 13.535	44.807	5.711 13.916	7.092 12.555	11.976 18.460	10.084 15.612
71	.886	12.731	10.089	17.216	1.937	5.180	11.245	25.023	11.426	.988	21.164	1.220	3.804	4.431	1.992
72	4.923	7.118	4.545	9.348	9.014	_ 6.629	4.267	15.175	4.372	5.117	11.011	6.216	11.129	3.213_	3.152
73	3.221	7.942	5.886	10.717	5.597	3.353	3.022	16.894	4.723	2.856	10.046	4.194	6.846	.937	1.420
74 _75.	3.662 20.394	5.110 8.829	4.066	7.004 6.928	7.628	4.738 24.585	.627 8.108	11.952 6.200	2.487 7.016	4,609 _22,684	6.044 2.090	6.951 27.014	8.851 27.729	2.293 16.963	1.850 17.460
76	13.462	4.952	4.900	3.039	22.301	16.208	2.872	4.000	1.499	15.697	1.009	19.211	23.243	11.217	10.917
77	4.725	21.257	19.169	28.367	•417	4.311	15.314	37.432	19.576	2.212	28.701	2.004	.879	5.701	4.475
78_ 79	_ 8 • 679	4.732	4.371	4.083	15.634	10.402	1.071	6.717	1.133	10.406	1.399	13.633 5.675	16.327 8.777	2.002	6.508
80	4.755 8.256	4.393 5.845	3.555 5.568	6.067 6.489	8.805 12.665	6.932 7.735	2.506 .379	9.876 9.580	1.973 2.175	4.256 8.612	5.174 2.743	11.459	13.005	4.683	2.565 5.245
81	2.153	6.455	5.307	8.560	5.339	3.983	2.907	13.762	3.572	2.236	7.225	3.927	5.615	.843	1.089
82	3.089	6.681	5.732	8.917	5.631	4.052	2.738	13.733	3.641	2,473	6.799	4.035	5.515	.813	1.432
83 84	8.081 4.251	2.811 4.104	2.818 2.649	3.623 5.744	14.080 8.719	10.834 7.431	1.469 3.347	6.215 9.707	1.045 1.923	8.667 4.057	2.578 6.896	10.952 5.146	14.094 9.594	4.899 2.967	5.195 2.535
85	8.630	5.460	5.830	6.276	13.235	8.762	.443	9.112	2.552	9.363	2.489	12.505	13.221	5.422	5.646
86	10.749	3.346	3.129	2.274	18.879	14.262	2.609	3.709	•553	12.197	1.179	14.937	19.380	8.226	8.280
87	17.744	43.073	37.650	_51.355_	16.102	20.755	36.393	66.370	42.649	20.834 5.619	16.508	7.831	22.492	6.796	3.383
88 89	1.636 2.166	8.747 10.110	6.799 7.234	11.454 12.844	7.516 5.953	8.636 3.932	8.118 4.909	18.906 20.830	8.468 7.203	4.225	14.486	6.202	8.994	3.145	2.119
90	2.467	8.238	5.624	10.317	8.630	7.000	5.384	17.935	6.453	6.119	13.890	8.508	12.098	5.066	3.119
91	1.883	13.060	9.853	16.221	2.619	1.694	7.026	23.772	8.712	1.317	16.151	2.164	4.652	2.066	1.677
92	14.475	36.313	29.800	41.529	9.884	9.585	25.507 11.169	52.378 34.487	29.334 15.616	11.842 7.672	43.075 24.959	11.036 8.935	14.742 11.745	16.620 5.937	14.937 6.337
9 <u>3</u>	15.092	19.773 34.044	15.432 28.382	24.013 38.708	8.057 9.402	5.317 8.861	23.899	47.377	26.153	9.760	37.092	8.224	11.878	13.569	14.082
95	7.842	24.549	20.837	30.973	2.705	4.915	17.029	39.778	20.730	4.184	31.667	3.317	4.660	8.458	7.013
96	4.818	20.744	15.930	25,219	4.337	5.512	15.620	34.717	16.743	3.979	28.614	3.651	7.778	7.215	5.715
97	7.173	5.650	4.230	5.874	11.632	8.360	3.119 3.830	8.453 10.246	1.578 2.734	6.489 3.297	4.647 8.871	7.971 4.773	12.400 8.391	5.019 4.213	4.951 1.660
98 99	2.029 5.944	3.725 2.810	2.493 1.416	5.777 2.652	6.792 15.297	7.184 12.041	3.082	6.944	1.193	9.465	5.209	12,168	17,420	6.103	5.290
100	2.098	7.894	5.737	10.220	6.834	4.606	3.559	17.513	5.400	4.337	11.113	6.592	9.044	2.165	1.786
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                                    4.602
                                                                            8.742
                                                                                      4.089
                                                                                                         11.643
                                                                                                                   18.285
                                                                                                                              5.369
      37.928
                                                                                                                                                 16.434
 92
               10.210
                         31.148
                                   22.093
                                             27.214
                                                       19.295
                                                                 19.745
                                                                           29.575
                                                                                     18.981
                                                                                               30.566
                                                                                                         34.076
                                                                                                                   13.088
                                                                                                                             19.322
                                                                                                                                       12.194
     21.137
                9.272
9.578
                         15.071
28.078
                                   10.812
17.321
                                             13.015
                                                       8.472
16.312
                                                                 9.161
15.766
                                                                                     9.946
15.346
                                                                                               15.152
27.256
                                                                                                         18.526
                                                                                                                             9.053
23.563
                                                                                                                                                 4.775
93
                                                                           14.759
25.143
                                                                                                                                       2.446
 94
                                             23.686
                                                                                                                                                 13.052
95
      28.789
                2.764
                         22.354
                                                                 10.632
                                                                                     11.123
                                                                                                         24.505
                                                                                                                   16.043
                                                                                                                                        9.071
                                                                                                                              8.69
                                   11.361
                                             2.082
                                                                  9.569
2.540
                                                                                      9.234
                                                                                               19.253
3.208
                                                                                                         21.293
1.945
                                                                                                                                        4.865
7.072
96
     25,246
                4.781
                         19.153
                                                        8.849
                                                                            7.497
                                                                                                                   12.020
                                                                                                                                                   7.332
                                                                                                                             10.975
       3.638
               15.319
                                                        3.087
                                    1.022
                                                                            1.512
                                                                                                                                                  8.127
98
       6.859
                9.616
                          4.692
                                    2.519
                                              4.519
                                                        2.315
                                                                  2.743
                                                                                                                                                  3.465
                                                                                      1.561
                                                                                                4.804
               19.162
       3.252
                          2.075
                                    3.297
                                              3.438
                                                        3.948
                                                                  4.564
                                                                            2.468
                                                                                      3.022
                                                                                                3.915
                                                                                                          2.372
                                                                                                                   35.313
                                                                                                                              5.713
                                                                                                                                        4-426
                                                                                                                                                  3.198
```

100	9.206	9.234	4.985	3.896	4.775	1.946	2.751	5.563	4.020	5.411	7.617	21.199	2.760	•452	.800
91	91 0	92	93	94	95	96	97	98	99	100					
92	8.031	0													
93	3.366	7.562	0												
94	7.520	2.979	10.480												
95	4.125	3.572	7.774	3.017	n										
96	2.174		3.864		2.370	0									
97		21.791	13.081	16.975	14.000	12.595	0								
98	4.064	18.793	10.709	18.192	10 973	0 620	2.965	0							
99 .	7.840	27.277	11.360	26.876	20.796	14.749	3.891	_3,217	0						
100	2.445	46.529	3.997	17.701	11.621	7.204	6.119	3.395	2.968						

APPENDIX F

LISTING OF THE MCKEON CLUSTER ANALYSIS PROGRAM

```
00001
     PROGRAM MCKEON
                                                                         00002
   THIS PROGRAM OBTAINED FROM NATIONAL INSTITUTES OF HEALTH
                                                                         00003
C
     COMPUTER CENTER IN BETHESDA, MARYLAND. MODIFIED TO RUN
                                                                         00004
C
     UNDER 053, AND CERTAIN CONVENIENCE CHANGES MADE
                                                                         00005
С
     JUNE 1974 BY K. BYRAM, US ENVIRONMENTAL PROTECTION AGENCY
                                                                         00006
C
                                                                         00007
C
                                                                         80000
                                 VERSION I
     MCKEON CLUSTER ANALYSIS
     DIMENSION B(150, 150), LV(150, 150),
                                                                         00009
                                                                         00010
     1 KV(150), KC(150), C(150), FMT(180)
                                                                         00011
     2 ,R(150),H(150),IOUT(150)
     INTEGER C.FMT. HARDWARE
                                                                         00012
                                                                         00013
     REAL1 B
     EQUIVALENCE (B,LV), (R,C), (H,KV), (FMT, IOUT)
                                                                         00014
                                                                         00015
  PROGRAM READS UNIT 60
                                                                         00016
         WRITE UNIT 61
                                                                         00017
С
                                                                         00018
     DO 1 LUN=1,63
                                                                         00019
      IF (.NOT. HARDWARE (LUN)) GO TO 3
                                                                         00020
    1 CONTINUE
                                                                         00021
     STOP 1
                                                                         00022
    3 CALL EQUIP(LUN. SHFILE )
                                                                         00023
00024
                     INPUT FROM USER
                                                                         00025
00026
C....SPECIFICATIONS INPUT
                                                                         00027
    2 READ(60,2020)N,KOP,NV,KRIT1,KRIT2,MMCOL,MATOP
                                                                         00028
     IF(EOF(60))GO TO 216
                                                                         00029
 2020 FORMAT (1014)
                                                                         00030
     IF (N.LE.O) STOP
                                                                         00031
     NNCOL=20*MMCOL
                                                                         00032
     READ(60,1199) (FMT(II), II=1, NNCOL)
                                                                         00033
 1199 FORMAT (20A4)
                                                                         00034
     WRITE(61,1198)N,KOP,NV,KRIT1,KRIT2,MMCOL,MATOP
                                                                         00035
     MATOP=1+MATOP
                                                                         00036
 1198 FORMAT( 1MCKEON CLUSTER ANALYSIS VERSION I.1 /
                                                                         00037
        OCONTROL INPUT: ,1014)
                                                                         00038
     WRITE(61,1197)(FMT(II),II=1,NNCOL)
                                                                         00039
 1197 FORMAT (14X, 1H:, 20A4)
                                                                         00040
     WRITE(61,1196)
                                                                         00041
 1196 FORMAT ( OF IRST ROW OF DATA FOR VERIFICATION- )
                                                                         00042
     NM1=N-1
                                                                         00043
     FN=N
                                                                         00044
     GO TO (5,18,7,7),KOP
                                                                         00045
С
                                                                         00046
C....KOP=1
             INPUT DATA AS CORRELATION MATRIX IN UPPER
                                                                         00047
C....
             TRIANGULAR FORM, MINUS DIAGONALS
                                                                         00048
С
                                                                         00049
   5 DO 6 I=1,NM1
                                                                         00050
     B(I,I)=1.
                                                                         00051
     IP1=I+1
                                                                         00052
     READ(60,FMT) (B(I,J),J=IP1,N)
                                                                         00053
     IF (I.EQ.1) WRITE (61,1195) (B(I,J),J=IP1,N)
                                                                         00054
 1195 FORMAT (10E12.3)
                                                                         00055
   6 CONTINUE
                                                                         00056
                                     240
```

```
B(N,N) = 1.
                                                                                     00057
       IF (NV.NE.1) GO TO 25
                                                                                     00058
С
                                                                                     00059
Ċ
   REFLECTION IF REQUESTED
                                                                                     00060
                                                                                     00061
       WRITE(61,802)
                                                                                     00062
  802 FORMAT(1H ,19HVARIABLES REFLECTED//)
                                                                                     00063
       DO 804 I=1.N
                                                                                     00064
       DO 804 J=I+N
                                                                                     00065
  804 B(J,I) = B(I,J)
                                                                                     00066
       WRITE(LUN) ((B(I,J),J=1,N),I=1,N)
                                                                                     00067
       REWIND 2
                                                                                     00068
       DO 856 J=1.N
                                                                                     00069
       B(J_{*}J) = 0.
                                                                                     00070
       KC(J)=1
                                                                                     00071
       BM=0.
                                                                                     00072
       DO 854 I=1.N
                                                                                     00073
       TEMP=ABS (B(I,J))
                                                                                     00074
       IF (TEMP.LE.BM) GO TO 854
                                                                                     00075
       BM=TEMP
                                                                                     00076
       H(J) = B(I,J)
                                                                                     00077
       IM=I
                                                                                     00078
  854 B(I,J)=0.
                                                                                     00079
  856 B(IM,J)=H(J)
                                                                                     00080
       DO 810 I=1,N
                                                                                    00081
       R(I)=0.
                                                                                    00082
       DO 810 J=1+N
                                                                                     00083
  810 R(I) = R(I) + B(I,J)
                                                                                     00084
       ITR=0
                                                                                    00085
  811 RM=FN
                                                                                    00086
       DO 816 I=1.N
                                                                                    00087
       TEMP=R(I)+H(I)
                                                                                    00088
       IF (TEMP.GE.RM) GO TO 816
                                                                                    00089
       RM=TEMP
                                                                                    00090
       IM=I
                                                                                    00091
  816 CONTINUE
                                                                                    00092
       IF (RM.GE.0.) GO TO 890
                                                                                    00093
       DO 822 J=1.N
                                                                                    00094
       B(IM_{\bullet}J) = -B(IM_{\bullet}J)
                                                                                    00095
  822 B(J,IM) = -B(J,IM)
                                                                                    00096
      DO 824 J=1.N
                                                                                    00097
      H(J) = H(J) + 2 \cdot *B(IM \cdot J)
                                                                                    00098
  824 R(J)=R(J)+2.*8(J,IM)
                                                                                    00099
      H(IM) = -H(IM)
                                                                                    00100
      R(IM) = -R(IM)
                                                                                    00101
      KC(IM) = -KC(IM)
                                                                                    00102
      WRITE(61,830) IM
                                                                                    00103
  830 FORMAT (1H ,6X,18)
                                                                                    00104
       ITR=ITR+1
                                                                                    00105
       IF (ITR.LT.N) GO TO 811
                                                                                    00106
  890 CONTINUE
                                                                                    00107
      READ (LUN)
                      ((B(I,J),J=1,N),I=1,N)
                                                                                    00108
      REWIND 2
                                                                                    00109
      DO 870 I=1.N
                                                                                    00110
      IF (KC(I).GE.0)GO TO 870
                                                                                    00111
      DO 864 J=1.N
                                                                                    00112
      B(I,J) = -B(I,J)
                                                                                    00113
  864 B(J,I) = -B(J,I)
                                                                                    00114
  870 CONTINUE
                                                                                    00115
      GO TO 25
                                                                                    00116
                                                                                    00117
C....KOP=2...INPUT DATA AS COVARIANCE MATRIX IN FULL MATRIX FORM
                                                                                    00118
```

```
00119
С
                                                                          00120
   18 DO 20 I=1.N
                                                                          00121
     READ(60,FMT) (B(I,J),J=I,N)
                                                                          00122
      IF (I.EQ.1) WRITE (61,1195) (B(I,J),J=1,NV)
                                                                          00123
   20 CONTINUE
                                                                          00124
      GO TO 25
                                                                          00125
                                                                          00126
C....KOP=3 OR 4...INPUT DATA AS RAW NUMBERS
                                                                          00127
                                                                          00128
    7 00 8 I=1.N
                                                                          00129
      READ(60.FMT) (B(I.J).J=1.NV)
                                                                          00130
      IF(I.EQ.1)WRITE(61,1195)(B(I,J),J=1,NV)
                                                                          00131
    8 CONTINUE
                                                                          00132
      IF (KOP.EQ.4) GO TO 602
                                                                          00133
C...KOP=3...STANDARDIZE OVER COLUMNS
                                                                          00134
      DO 10 J=1.NV
                                                                          00135
      SUM=0.
                                                                          00136
      SS=0.
                                                                          00137
      DO 9 I=1.N
                                                                          00138
      SUM=SUM+B(I,J)
                                                                          00139
    9 SS=SS+B(I,J)**2
                                                                          00140
      FMEAN=SUM/FN
                                                                          00141
      FMSQ=SS/FN
                                                                          00142
      SD=SQRT (FMSQ-FMEAN**2)
                                                                          00143
      DO 10 I=1.N
                                                                          00144
   10 B(I,J) = (B(I,J) - FMEAN)/SD
C....COMPUTE DISTANCES....USING
                                                                          00145
                                                                          00146
  602 IF (N.GT.75) GO TO 14
C.....TOP OF MATRIX SINCE N LT 75
                                                                          00147
      DO 12 I=1.N
                                                                          00148
                                                                          00149
      DO 12 J=I,N
      B(I+75,J)=0.
                                                                          00150
                                                                          00151
      DO 12 K=1.NV
   12 B(I+75,J)=B(I+75,J)+B(I,K)*B(J,K)
                                                                          00152
      DO 13 I=1.N
                                                                          00153
      DO 13 J=I+N
                                                                          00154
   13 B(I,J)=B(I+75,J)
                                                                          00155
      GO TO 25
                                                                          00156
C.....USING EXTERNAL SCRATCH FILE SINCE N GT 75
                                                                          00157
   14 DO 15 J=1,NV
                                                                          00158
   15 WRITE(LUN)
                     (B(I_{\bullet}J)_{\bullet} I_{=1_{\bullet}N})
                                                                          00159
      REWIND 2
                                                                          00160
                                                                          00161
      DO 16 I=1.N
                                                                          00162
      DO 16 J=I+N
                                                                          00163
   16 B(I,J)=0.
      DO 17 K=1,NV
                                                                          00164
                    (R(I),I=1,N)
                                                                          00165
      READ (LUN)
      DO 17 I=1.N
                                                                          00166
      DO 17 J=I+N
                                                                          00167
   17 B(I,J)=B(I,J)+R(I)*R(J)
                                                                          00168
00169
               INPUT COMPLETE...INITIALIZE
                                                                          00170
00171
   25 TB=0.
                                                                          00172
      DO 26 I=1,NM1
                                                                          00173
      IP1=I+1
                                                                          00174
      DO 26 J=IP1•N
                                                                          00175
      B(I,J)=B(I,I)+B(J,J)-2.*B(I,J)
                                                                          00176
   26 TB=TB+B(I,J)
                                                                          00177
      DO 27 I=1,N
                                                                          00178
   27 B(I,I)=0.
                                                                          00179
      DO 28 I=1,NM1
                                                                          00180
```

```
00181
      IP1=I+1
      00 28 J=IP1.N
                                                                          00182
   28 B(J,I)=B(I,J)
                                                                          00183
     NRC=N
                                                                          00184
      KSH=0
                                                                          00185
     LOC=1
                                                                          00186
      IF (KRIT1.EQ.N.AND.MATOP.EQ.1) GO TO 1021
                                                                          00187
      WRITE(61,2000)
                                                                          00188
 2000 FORMAT( -SQUARED DISTANCES BETWEEN POINTS BEFORE CLUSTERING )
                                                                          00189
      GO TO 1000
                                                                          00190
 1021 CONTINUE
                                                                          00191
      IF (MATOP.EQ.3) WRITE (61,2014)
                                                                          00192
      NC=N
                                                                          00193
      NCM1=NC-1
                                                                          00194
      BMIN=0.
                                                                          00195
      TEMP=SQRT (FN)
                                                                          00196
      IF (KRIT1.LE.0) KRIT1=2.*TEMP+.5
                                                                          00197
      IF (KRIT2.LE.0) KRIT2=2
                                                                          00198
      MCL=0
                                                                          00199
      MIS=N
                                                                          00200
      DO 120 I=1.N
                                                                          00201
      C(I)=1
                                                                          00202
      KV(I)=I
                                                                          00203
  120 \text{ KC}(I) = I
                                                                          00204
00205
С
        MAIN LOOP
                                                                          00206
00207
C...FIND MINIMUM ENTRY IN OFF DIAGONAL ELEMENTS
                                                                          80200
  130 BPR=BMIN
                                                                          00209
      BMIN=1.E30
                                                                          00210
      DO 134 I=1,NCM1
                                                                          00211
      IP1=I+1
                                                                          00212
      DO 134 J=IP1.NC
                                                                          00213
      IF(B(I.J).GE.BMIN)GO TO 134
                                                                          00214
      BMIN = B(I,J)
                                                                          00215
      IM=I
                                                                          00216
      U=ML
                                                                          00217
  134 CONTINUE
                                                                          81500
      DEL=BMIN-BPR
                                                                          00219
      IF (NC.GT.KRIT1) GO TO 139
                                                                          00220
      GO TO (149,1022,135), MATOP
                                                                          00221
  135 WRITE (61,420) BMIN, IM, JM, DEL, MIS, MCL
                                                                          00222
  420 FORMAT (1H +8X+F8.3+9X+I3+1H++I3+8X+F10.3+18X+I8+15X+I10)
                                                                          00223
  139 \text{ CN=C(IM)+C(JM)}
                                                                          00224
      DO 136 K=1.NC
                                                                          00225
      B(IM,K) = AMAX1(B(IM,K),B(JM,K))
                                                                          00226
  136 B(K, IM) = B(IM, K)
                                                                          00227
      IF (JM.GE.NC) GO TO 141
                                                                          85500
C...CLOSE UP MATRIX NOW THAT WE ELIMINATED A CLUSTER
                                                                          00229
      DO 138 I=1,NC
                                                                          00230
      DO 138 J=JM+NCM1
                                                                          00231
  138 B(I,J)=B(I,J+1)
                                                                          00232
      DO 140 J=1,NCM1
                                                                          00233
      DO 140 I=JM+NCM1
                                                                          00234
  140 B(I,J)=B(I+1,J)
                                                                          00235
C...ADJUST KC TO SHOW NEW ARRANGEMENT
                                                                          00236
  141 DO 146 I=1.N
                                                                          00237
      IF(KV(I).EQ.KC(JM))KV(I)=KC(IM)
                                                                          00238
  146 CONTINUE
                                                                          00239
      KTR=1
                                                                          00240
```

```
00241
C...ADJUST NUMBER OF ISOLATED POINTS
            IF (C(IM) .LE.1)KTR=KTR+1
                                                                                                                                                            00242
                                                                                                                                                            00243
            IF (C(JM).LE.1)KTR=KTR+1
                                                                                                                                                            00244
            GO TO (311,314,313), KTR
                                                                                                                                                            00245
    311 MCL=MCL-1
                                                                                                                                                            00246
            GO TO 314
                                                                                                                                                            00247
    313 MCL=MCL+1
    314 MIS=NCM1-MCL
                                                                                                                                                            00248
                                                                                                                                                            00249
            IF (JM.GE.NC) GO TO 321
                                                                                                                                                            00250
C...CLOSE UP COUNTER ARRAYS
                                                                                                                                                            00251
            DO 148 J=JM,NCM1
                                                                                                                                                           00252
            C(J) = C(J+1)
    148 KC(J)=KC(J+1)
                                                                                                                                                           00253
                                                                                                                                                           00254
    321 C(IM)=CN
                                                                                                                                                           00255
            NC=NCM1
                                                                                                                                                           00256
            NCM1=NC-1
                                                                                                                                                           00257
            GO TO 130
00258
            OUTPUT SECTION
                                                                                                                                                           00259
C_5 and the same and an end an end and an end an end an end and an end an
                                                                                                                                                           00260
   149 WRITE(61,2006)
                                                                                                                                                           00261
  2006 FORMAT (1H1 , 44HMAXIMUM SQUARED DISTANCE BETWEEN CLUSTERS
                                                                                                                                                           00262
          1 53HMAXIMUM SQUARED DISTANCE WITHIN CLUSTERS IN DIAGONALS)
                                                                                                                                                           00263
                                                                                                                                                           00264
            NRC=NC
            KSH=75
                                                                                                                                                           00265
            FOC= 5
                                                                                                                                                           00266
              LOWER TRIANGULAR MATRIX PRINTOUT
                                                                                                                                                           00267
  1000 DO 1002 JL=1,NRC,15
                                                                                                                                                           00268
            JU=JL+14
                                                                                                                                                           00269
            IF (JU.GT.NRC) JU=NRC
                                                                                                                                                           00270
            WRITE(61,1010)(J,J=JL,JU)
                                                                                                                                                           00271
  1010 FORMAT (1H0,2X,15I8)
                                                                                                                                                           00272
            DO 1014 I=JL, NRC
                                                                                                                                                           00273
            リレニリリし
                                                                                                                                                           00274
            IF (JUU.GT.I) JUU=I
                                                                                                                                                           00275
  1014 WRITE(61,1016)I,(B(I,J),J=JL,JUU)
                                                                                                                                                           00276
  1002 CONTINUE
                                                                                                                                                           00277
  1016 FORMAT(1H , 14, 15F8.3)
                                                                                                                                                           00278
            GO TO (1021,1022), LOC
                                                                                                                                                           00279
  1022 CONTINUE
                                                                                                                                                           00280
            WRITE(61,2008)
                                                                                                                                                           00281
  2008 FORMAT(1H-, 22X, PTS INCLUDED IN CLUSTER,
                                                                                                                                                           00282
                    (ORIGINAL NUMBERING OF DATA) )
                                                                                                                                                           00283
            DO 156 I=1.NC
                                                                                                                                                           00284
            K=0
                                                                                                                                                           00285
            DO 152 J=1,N
                                                                                                                                                           00286
            IF (KV(J).NE.KC(I))GO TO 152
                                                                                                                                                           00287
            K=K+1
                                                                                                                                                           00288
            IOUT(K)=J
                                                                                                                                                           00289
    152 CONTINUE
                                                                                                                                                           00290
    156 WRITE(61,160)I,C(I),(IOUT(J),J=1,K)
                                                                                                                                                           00291
    160 FORMAT( CLUSTER ,14,1H:,14, PTS ,2015/(21X,2015/))
                                                                                                                                                           00292
            WRITE(61,2014)
                                                                                                                                                           00293
  2014 FORMAT (1HO ,7X, 22HNEXT CLUSTER. MAXIMUM ,11X,
                                                                                                                                                           00294
          1 17HCHANGE IN MAXIMUM , 11X , 9HNUMBER OF
                                                                                                                                                           00295
          2 14X,17HCLUSTERS WITH TWO/1H ,7X,26HSQUARED DISTANCE, LOCATION,
                                                                                                                                                           00296
          3 16HSQUARED DISTANCE, 12X ; 15HISOLATED POINTS, 8X.
                                                                                                                                                           00297
          4 14HOR MORE POINTS//)
                                                                                                                                                           00298
            IF (NC.GT.KRIT2) GO TO 135
                                                                                                                                                           00299
           WRITE(61,420)
                                                               BMIN, IM, JM, DEL, MIS, MCL
                                                                                                                                                           00300
C....RETURN TO GET ANOTHER CASE OR EXIT
                                                                                                                                                           00-301
            GO TO 2
                                                                                                                                                           00302
    216 CALL UNEQUIP(LUN)
                                                                                                                                                           00303
           END
                                                                                                                                                           00304
```

TE (Please read Ins	CHNICAL REPORT DAT tructions on the reverse before	A e completing)			
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This study evaluates the Earth Resources Technology Satellite One (ERTS-1; i.e., LAND-SAT-1) multispectral scanner (MSS) as a means of estimating lacustrine trophic state. Numerical classificatory methods are employed to ascertain the trophic character of 100 lakes in Minnesota, Wisconsin, Michigan, and New York. Principal components analysis is used to derive a multivariate trophic state index (PC1) using the trophic indicators chlorophyll a, conductivity, inverse of Secchi depth, total phosphorus, an algal assay yield, and total organic nitrogen. A binary masking technique is used to extract lakerelated MSS data from digital tapes (CCTs). MSS color ratio models are developed which give good estimates of Secchi depth and fair estimates of chlorophyll a levels. phic state, as defined by lake position on the first principal component axis (PC1), is predicted using MSS color ratio regression models. Each date of LANDSAT-1 coverage has its unique model. An automatic image processing technique is employed to classify a group of Wisconsin lakes. The utility of the LANDSAT-1 MSS is most apparent when the seasonal contrasts between lakes at different points on the trophic scale are at a Periods of excessive cloud cover, frames with faulty or missing MSS data, and maximum. the need for some ground truth, impair, but do not preclude its use in lake monitoring and classification. The use of CCTs in conjunction with digital image processing techniques is essential if the maximum benefits are to be derived from the LANDSAT-1 MSS.

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