

NON-DIVERGENT WIND ANALYSIS ALGORITHM
FOR THE ST. LOUIS RAPS NETWORK

by

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ABSTRACT

An objective wind analysis algorithm capable of producing non-divergent wind fields at up to ten levels in the atmospheric boundary layer for St. Louis, Missouri is described. Wind data collected during the St. Louis Regional Air Pollution Study (RAPS) and averaged over 15-minute intervals were used to construct u and v wind component fields on a 46 by 46 grid network with a grid spacing of 1 km via a scan-radius technique. The divergence across grid squares was minimized by a non-divergence algorithm.

Several analyses produced by the algorithm are illustrated. A user's guide and computer program listing are included.

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1. INTRODUCTION

The non-divergent wind field analysis procedure presented in this report utilizes modifications of techniques developed by Hovland et al. (1976) of Control Data Corporation (CDC) and Liu and Goodin (1976). The CDC objective analysis procedure generates, via a weighted scan radius technique, a horizontal wind field, which is not divergent-free. The Liu and Goodin procedure adjusts this field to produce a horizontal, divergent-free wind analysis. Divergent-free wind fields are required in most Eulerian air pollution models; Shir and Shieh's (1975) sulfur dioxide model and the Systems Applications, Inc. photochemical model (Reynolds et al., 1973) are examples.

These models treat the atmosphere as several vertically-stacked, two-dimensional layers. This implies, of course, that the vertical velocity is zero everywhere. If the two-dimensional velocity field is not divergent-free, or at least the divergence is small ($\vec{\nabla}_2 \cdot \vec{v} < 10^{-5} \text{sec}^{-1}$), the divergence will act as a source or sink term (depending on the sign of the divergence) when the pollution species conservation equations are solved by numerical techniques.

The influence of the divergence on the calculated concentrations can be explained by first examining the simplest conservation-of-species equation

$$\frac{\partial c}{\partial t} = -\vec{v} \cdot \nabla c$$

where c is the concentration of a pollutant and \vec{v} the wind. This equation can be written as

$$\frac{\partial c}{\partial t} = -\vec{v} \cdot \nabla c - c \nabla \cdot \vec{v}$$

The first term on the right represents the change in the concentration due to advection and the second term represents the change due to confluence or diffluence of the wind. If $\vec{v} \cdot \nabla > 0$ (diffluence), pollutant is lost from the system and if $\vec{v} \cdot \nabla < 0$ (confluence), pollutant is added.

The non-divergent wind fields are constructed by first analyzing the wind field using the technique developed by Hovland et al. This objective analysis technique was originally developed for the St. Louis RAPS network for a grid which was 21 by 21 grid points with a spacing of 5 km. The technique was modified so that the procedure could be employed to construct wind fields on a grid which was 46 by 46 grid points with a spacing of 1 km. The resulting wind fields are two-dimensional and are not divergent-free.

The CDC wind fields (referred to as first-guess fields) are adjusted to generate divergent-free, vertically-stacked fields in the boundary layer by the technique developed by Liu and Goodin. From Liu and Goodin's routine, the computed winds at the grid points represent an average wind and have no vertical structure. Their published technique was modified to produce smoother wind fields and a divergent-free wind field at any level or levels in the boundary layer specified by the user.

The objective analysis techniques of Hovland et al. and Liu and Goodin and the modifications made by the authors are described in Sections 2 and 3, respectively. Section 4 illustrates and discusses several examples of the resultant wind fields using 15-minute averaged RAPS data. Section 6 is a user's guide to the computer program. The final section contains a listing of the computer program.

2. MODIFIED CDC OBJECTIVE ANALYSIS PROCEDURE

The modified version of the Control Data Corporation objective analysis procedure attempts to describe the u and v wind fields across an equally-spaced grid using time-averaged data from an unequally-spaced data network with a high density of stations in the center (see Fig. 1). This is performed via an iterative process using a variable-scan-radius technique. The values computed at the grid points after m

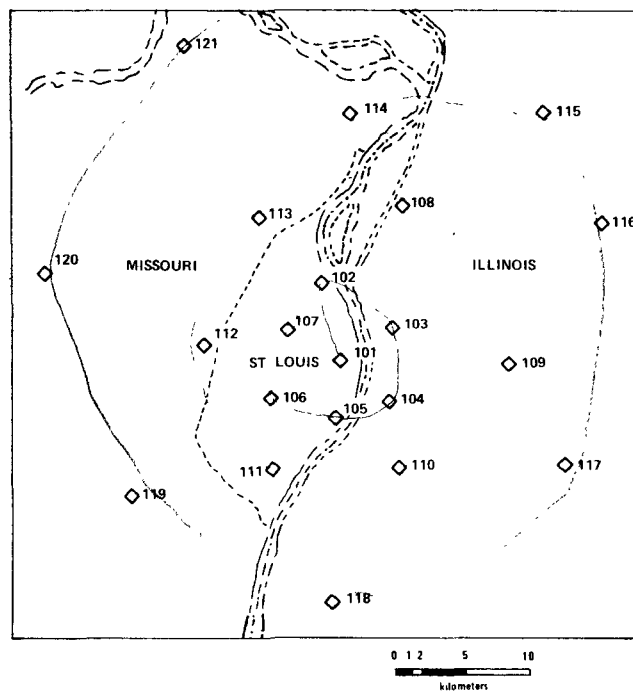


Figure 1. Analysis domain considered from a portion of the Regional Air Pollution Study (RAPS) monitoring network at St. Louis, Missouri. Winds at sites 108, 110, 114-118 were measured at the 10-meter level and at the 30-meter level elsewhere.

iterations ($x_{i,j}^m$) are based upon the observations at K data points (0^k), which lie within a circle of specified radius (R), and a weighted correction factor.

The original CDC procedure uses data from all 25 RAPS stations and a 21 by 21 grid with a 5 km grid spacing. The prescribed number of observation points and scan radii (measured in terms of grid points) used for the five iterations were 4,12,12,25,25 and 20,14,7,4,1, respectively. The number of the iterative step when data from the stations were first incorporated into the analysis is given in Fig. 2. This procedure uses data from the four outlying observation points (not within the grid domain illustrated by Fig. 1) and a large scan radius for the first iteration. With each subsequent iteration, data from additional observational points and a smaller scan radius are employed. Data from the inner-most observation points are used only when the scan radii are small.

The modified version uses a 46 by 46 grid with a grid spacing of 1 km. The grid domain does not include the four outer-most RAPS stations and the data from these stations are not used. New sets of data points and scan radii used for each iteration were established empirically. These new sets are 7,12,21,21,21, and 46,20,10,5,1, respectively. The highest numbered stations in Figure 1 are always used before the lower ones.

A rejection scheme is included to ignore data thought to be in error. Prior to the first iterative step, the standard deviations of the u and v components of the data are calculated. All components with values greater than $\pm 4\sigma$ from the mean are labeled as incorrect and

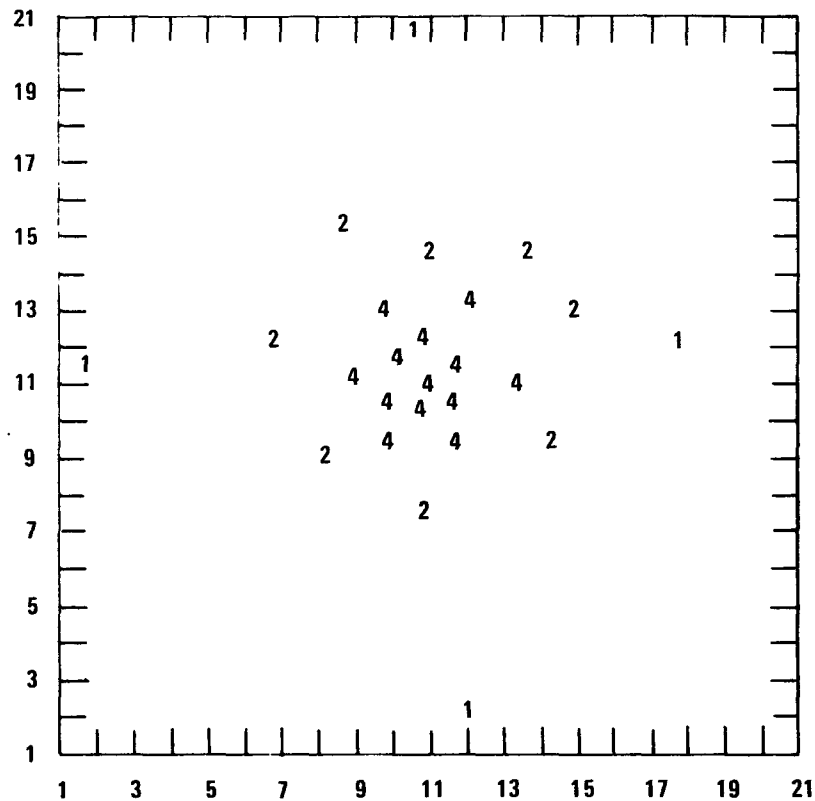


Figure 2. Analysis domain for the original CDC objective analysis technique. The numbers inside the grid boundary correspond to station locations and represent the number of the iterative step when the data value was used.

are ignored during the analysis procedure. If one component of the wind at a data point is ignored, the other component is likewise ignored.

After the gross errors in the data have been removed, the analysis begins with defining a first-guess field. The original version of the procedure used a field of zeroes, while the modified version defines the field as a uniform field of values equal to the mean of the data. In theory, the analysis would converge faster when the first-guess field is more comparable to the data.

The first-guess field is adjusted repeatedly until the values at each grid point converge. After five iterations, the values converge (tolerance of 0.1 m sec^{-1}). the grid point values are adjusted by

$$X_{i,j}^m = X_{i,j}^{m-1} + \frac{\sum_{k=1}^K W_{i,j}^k C^{k,m}}{\sum_{k=1}^K W_{i,j}^k}, \quad (1)$$

where K is the number of data points within the scan circle centered at the grid point i,j ; $W_{i,j}^k$ is a weighting factor (described later); and $C^{k,m}$ is a correction factor determined at the m^{th} iteration for each of the non-rejected observations.

The value of the correction factor ($C^{k,m}$) is determined by subtracting from the data value (O^k) the interpolated value from the previous iteration ($I_{i+p,j+q}^{k,m-1}$) at a point corresponding to the location of the station point

$$C^{k,m} = O^k - I_{i+p,j+q}^{k,m-1}, \quad (2)$$

where p and q are the distances along the x and y axes, respectively, from the observation point to the grid point (i,j) . The four-point interpolation scheme is illustrated in Fig. 3 and given by

$$I_{i+p,j+q}^{k,m} = (1-p)(1-q) X_{i,j} + p(1-q) X_{i+1,j} + q(1-p) X_{i,j+1} + pq X_{i+1,j+1}. \quad (3)$$

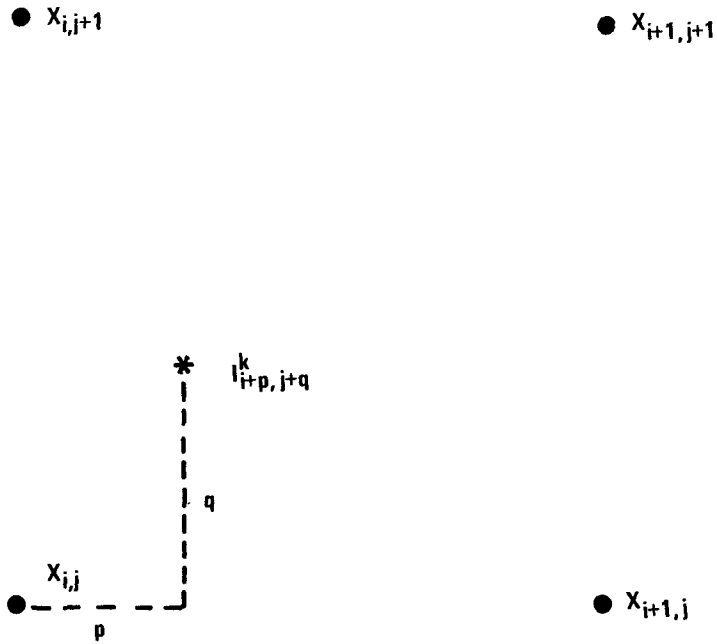


Figure 3. Illustration of the four-point interpolation scheme used to interpolate the value $I_{i+p,j+q}^k$ at a position on the grid corresponding to the location of observation point 'k' denoted by '*'. The horizontal distance is p and the vertical distance is q .

The correction factor determined at a station point is applied to those grid points within a specified distance (R) of the station point (Fig. 4). The actual correction applied to the grid point value of the previous iterative step is weighted as a function of distance (r^k) between the grid point and the station point. The values at the station points would have no direct influence on those values at grid points outside the circle of radius R ($w_{i,j}^k = 0$ when $r^k \geq R$). The weighting function, illustrated by Fig. 5, is defined as

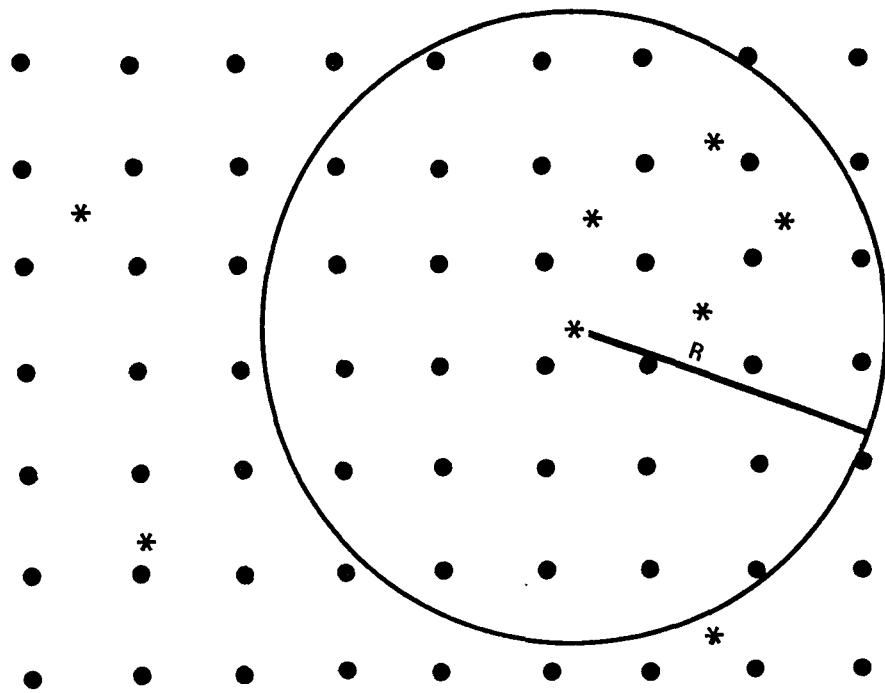


Figure 4. Scan circle centered at a station (*) enclosing 29 grid points.

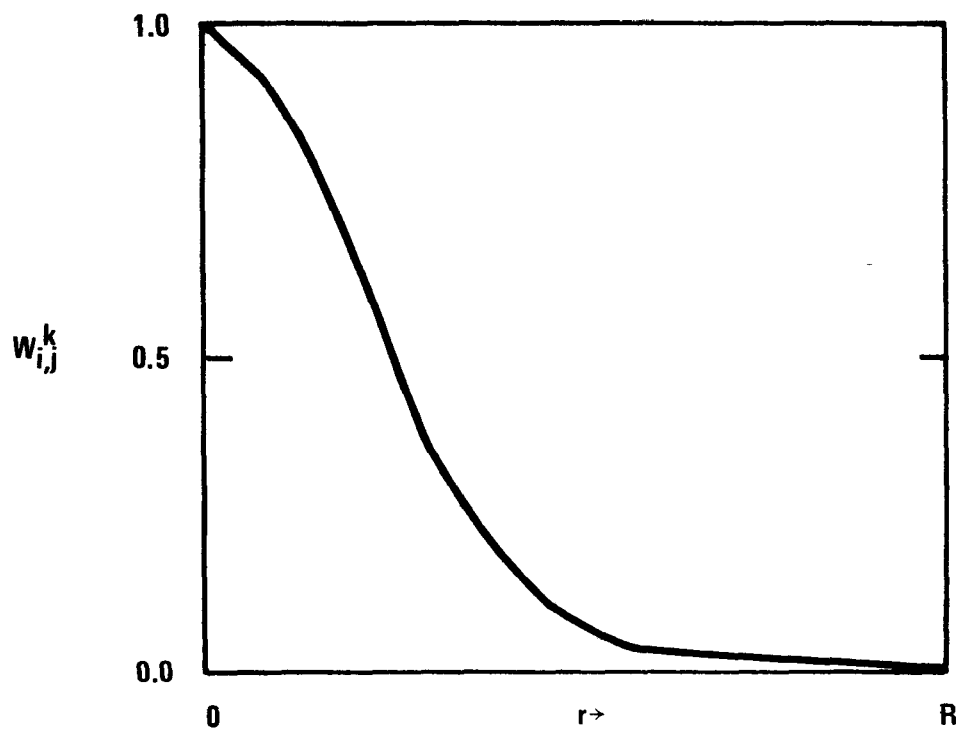


Figure 5. Depiction of weighting function, $w_{i,j}^k$, where R is the scan radius and r is the distance from grid point i,j to station (k) .

$$w_{i,j}^k = \frac{R^2 - (r_{i,j}^k)^2}{R^2 + (r_{i,j}^k)^2} \quad \begin{matrix} r_{i,j}^k \leq R \\ 0 \quad r_{i,j}^k > R \end{matrix} \quad (4)$$

Since the data points are unevenly-spaced and concentrated in the center of the grid, the number of observation points and/or the scan radius are changed with each iteration. If all the data were used in each iteration with large scan radii, the gradients observed in the center of the grid, where the density of observation points are high, would be propagated outward. Furthermore, if the scan radii were not changed with each iteration, the radii would have to be large enough to guarantee that every grid point was within R grid points of at least one data point. This would result in a very smooth, non-representative analysis.

The application of this technique requires the availability of reliable data at the outer-most observation points, since the field created using this set of data in the first iteration greatly influences the final analysis. Moreover, when data are missing or ignored from several of the data points, the data configuration is altered. For this case, the chosen set of stations and radii may not yield an acceptable analysis.

3. MODIFIED NON-DIVERGENT WIND FIELD ANALYSIS PROCEDURE

The algorithm of Liu and Goodin adjusts the wind field (generated by the technique discussed in Section II) in order to construct a divergent-free wind field. This adjustment process usually makes only small changes in the value at any grid point. Therefore, if the analysis to be adjusted by the algorithm is poor, it will most likely remain poor.

The algorithm is based upon the uniform adjustment of values at grid points $(i-1,j)$, $(i+1,j)$, $(i,j-1)$, and $(i,j+1)$ using the divergence calculated at (i,j) . The grid is scanned repeatedly until the maximum divergence meets an arbitrary value.

The simplest approximation to the continuity equation in a non-staggered grid (u,v defined at every point) is

$$D_{i,j} = \frac{u_{i+1,j} - u_{i-1,j}}{2\Delta x} + \frac{v_{i,j+1} - v_{i,j-1}}{2\Delta y} \quad (6)$$

Liu and Goodin define the following relationships (the equal signs should be interpreted as replacement operations):

$$\begin{aligned} u_{i+1,j} &= u_{i+1,j} + f_{i+1,j} \hat{u}_{i,j} , \\ u_{i-1,j} &= u_{i-1,j} - f_{i-1,j} \hat{u}_{i,j} , \\ v_{i,j+1} &= v_{i,j+1} + f_{i,j+1} \hat{v}_{i,j} , \\ v_{i,j-1} &= v_{i,j-1} - f_{i,j-1} \hat{v}_{i,j} . \end{aligned} \quad (7)$$

where $f_{i,j}$ is a weighting factor. By substituting (7) into (6), Liu and Goodin find

$$\begin{aligned}\tilde{u}_{i,j} &= -D_{i,j} \Delta x / (f_{i+1,j} + f_{i-1,j}), \\ \tilde{v}_{i,j} &= -D_{i,j} \Delta y / (f_{i,j+1} + f_{i,j-1}).\end{aligned}\quad (8)$$

Liu and Goodin's procedure is as follows: first, the divergence is calculated by (6); second, $\tilde{u}_{i,j}$ and $\tilde{v}_{i,j}$ are calculated by (8) and then new values of u and v are calculated using (7). This procedure is repeated until $D_{i,j}$ is reduced to some desired level. The results depicted in Fig. 6 show a wind field that is somewhat irregular and not very satisfactory.

If one substitutes (7) into (6) and collects terms, this yields

$$(f_{i+1,j} + f_{i-1,j}) \tilde{u}_{i,j}/2\Delta x + (f_{i,j+1} + f_{i,j-1}) \tilde{v}_{i,j}/2\Delta y + D_{i,j} = 0 \quad (9)$$

from which (8) is derived. However, a second formulation of \tilde{u} and \tilde{v} is available. If the formulation of $\tilde{u}_{i,j}$ and $\tilde{v}_{i,j}$ given by Liu and Goodin for the eight point continuity equation is used, it can be reduced to a four point form,

$$\begin{aligned}\tilde{u}'_{i,j} &= -2D_{i,j} \Delta x / (f_{i,j+1} + f_{i,j-1} + f_{i+1,j} + f_{i-1,j}), \\ \tilde{v}'_{i,j} &= -2D_{i,j} \Delta y / (f_{i,j+1} + f_{i,j-1} + f_{i+1,j} + f_{i-1,j}).\end{aligned}\quad (10)$$

Substitution of (10) into (9) shows that (10) is also a solution.

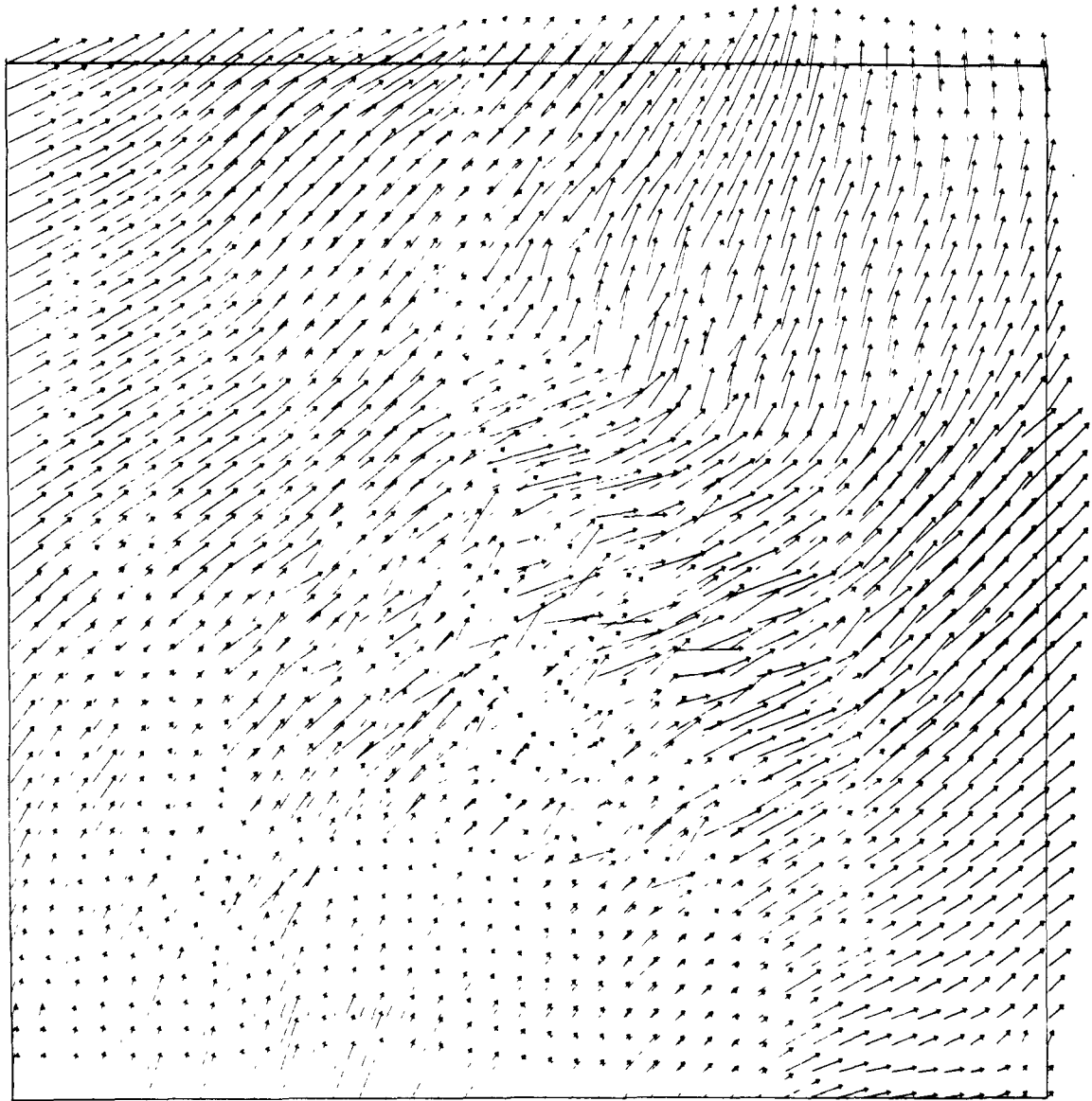


Figure 6. Analyzed wind field from the original Liu and Goodin technique.

The procedure used in this modified technique is to first calculate the divergence by (6), then $\tilde{u}'_{i,j}$ and $\tilde{v}'_{i,j}$ are calculated by (10). Finally, the new values of u and v are calculated using (7) after \tilde{u}' and \tilde{v}' are substituted for \tilde{u} and \tilde{v} . The results of using this variation of the algorithm are shown in Fig. 7.

Fig. 7 clearly shows a smoother wind field to that of Fig. 6. To see the reason that (10) is a superior formulation it is necessary to examine the grid point weighting technique used in this modified algorithm. The grid point nearest the data point is treated as the station and assigned a weight of .25. The adjacent grid points are assigned weights of .50 and all other points are given a weight of 1.00 (see Fig. 8).

It is apparent from (10) and (8) that

$$\tilde{u}_{i,j} = \tilde{u}'_{i,j} \quad , \quad (11)$$

at grid points nearest data points and

$$\tilde{u}_{i,j} = -0.8D_{i,j}\Delta x \quad \text{and} \quad \tilde{u}'_{i,j} = -0.61D_{i,j}\Delta x \quad (12)$$

at grid points located one grid length from the grid points nearest the data points. Similar relationships hold for \tilde{v} and \tilde{v}' . At a point 2 grid points away from the station,

$$\tilde{u}_{i,j} = -0.6667 D_{i,j} \Delta x \quad \text{and} \quad \tilde{u}'_{i,j} = -0.57 D_{i,j} \Delta x. \quad (13)$$

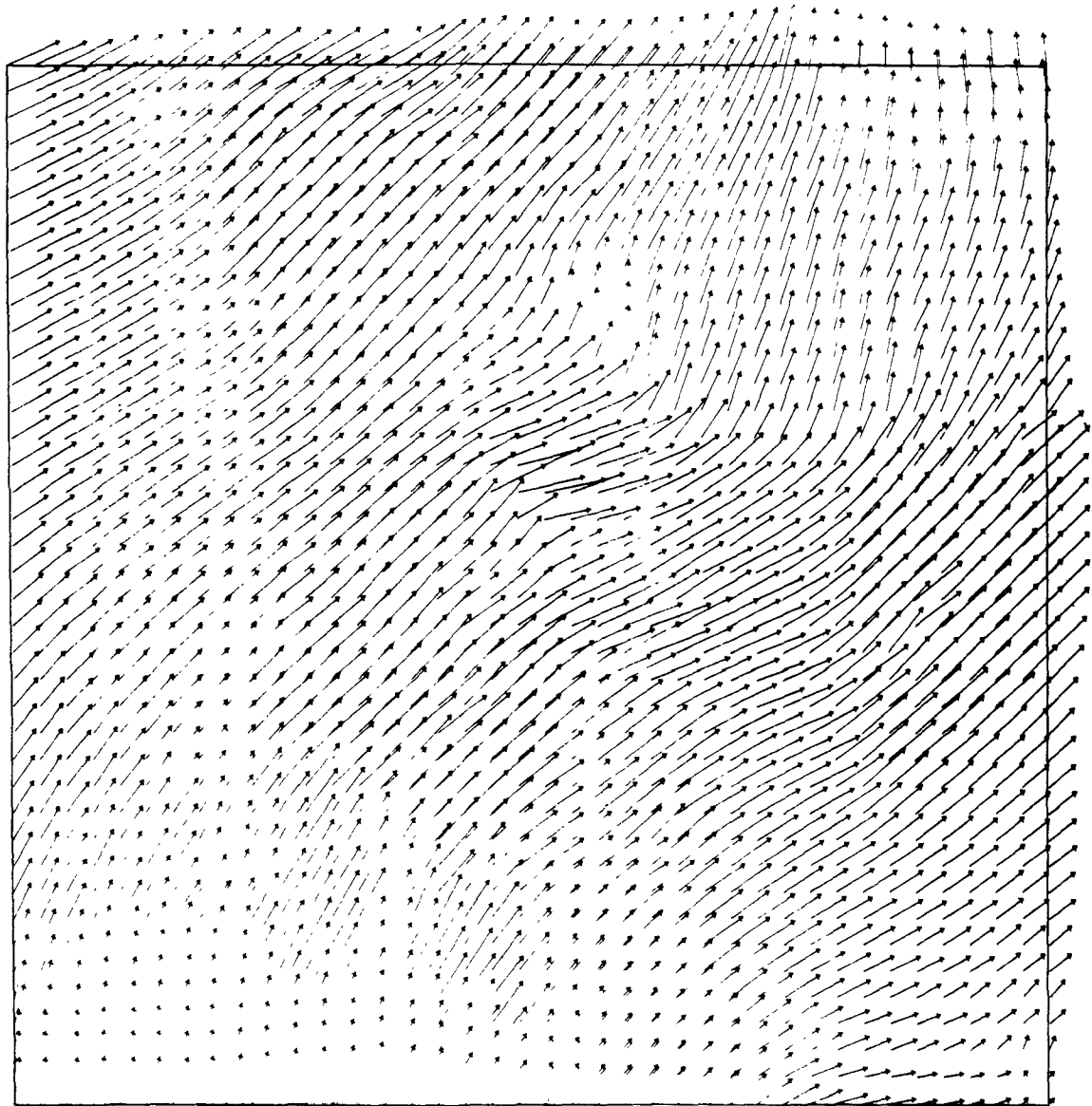


Figure 7. Analyzed wind field from the modified Liu and Goodin technique (using identical data to those in Figure 6).

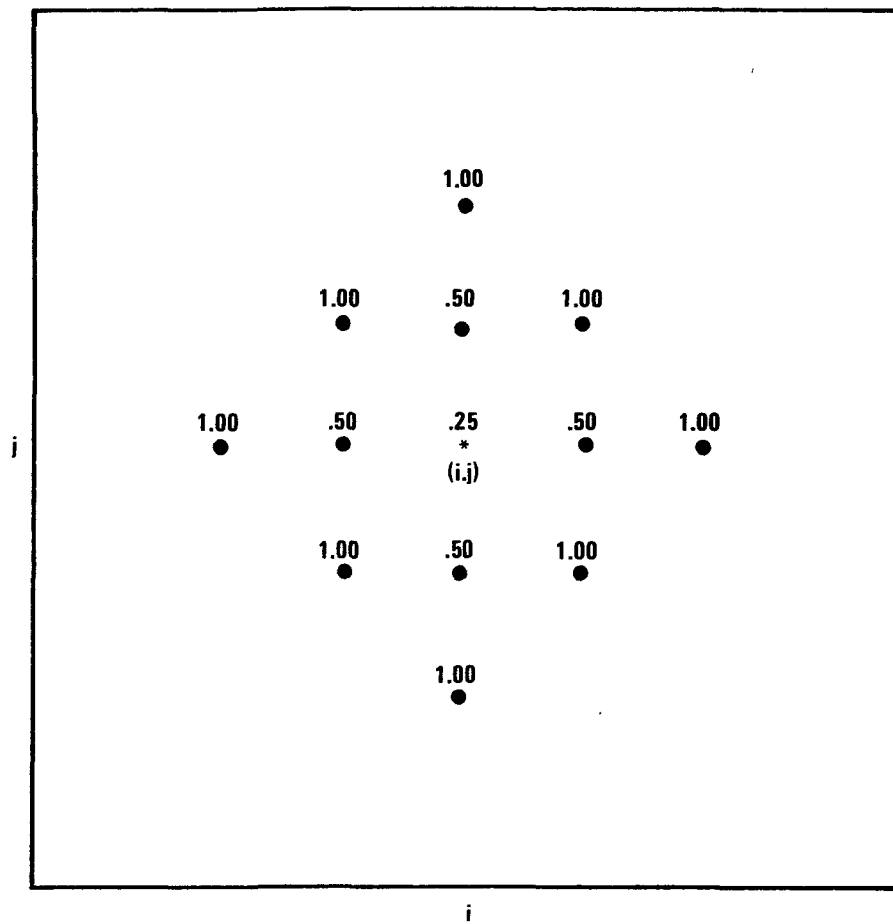


Figure 8. Weighting of grid points at and around a station denoted by '*' for the Liu and Goodin analysis procedure.

Now at a grid point 3 grid points away, it is found again that

$$\tilde{u}_{i,j} = \tilde{u}'_{i,j} \quad . \quad (14)$$

In effect, what occurs is that the correction at each iteration is smaller in the modified algorithm than the one given by Liu and Goodin resulting in a smoother analysis.

It should be noted that an iteration level does not appear in the above equations as it does in the equations in Liu and Goodin's paper. In a recent paper by Eskridge (1977), it has been shown that new values of u and v must be used as soon as they are calculated instead of maintaining two separate iterative levels as the Liu and Goodin paper implies.

In addition Eskridge (1977) demonstrates that the use of a four-point continuity equation in a non-staggered grid results in the iteration procedure acting as if there are two separate grids (Fig. 9) which do not interact or affect neighboring points at anytime. This division of the grid into two independent subgrids will result in an analysis with large oscillations of wavelength $2\Delta x$ if incorrect boundary conditions are used.

An examination of the computer code used by Liu and Goodin shows that they minimized this problem by setting the gradient at the boundary equal to zero. In other words, they connected the two independent grids at the boundary through common values. One can still expect to see some oscillation in the wind field analysis. However, it has been small and does not appear to be much of a problem.

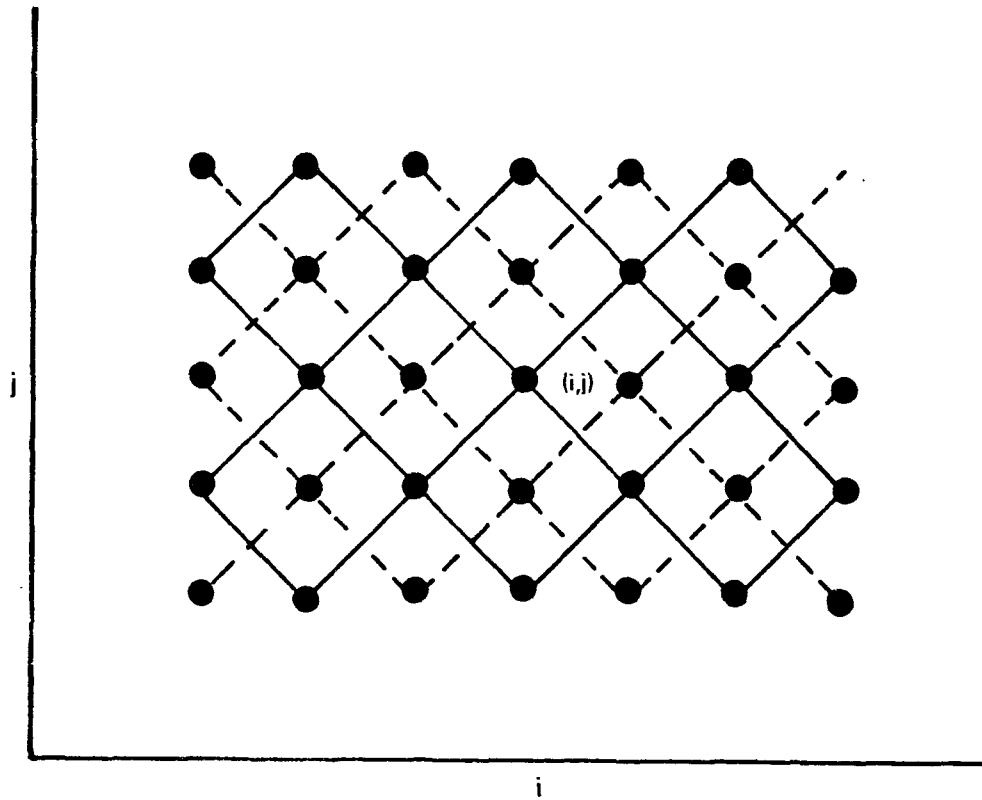


Figure 9. A portion of the computational grid showing the two independent subgrids.

4. ANALYSIS FIELDS

Both the first-guess and final wind analysis (i.e. divergent and divergent-free) fields from five different time periods are illustrated in this section. The 46 by 46 grid point fields are composed of vectors with points of origin corresponding to the grid points. These vectors point in the direction of the flow and have lengths proportional to the wind speed at the grid point. (0.6 cm vector length represents a wind speed of 1.0 m/sec).

The data used in the analyses were sampled and averaged over a 15-minute period at 20 of the 25 RAPS stations during selected periods in August of 1975. During this month station 111 was not operating. Of the periods selected, two involved cases where the wind field was relatively uniform. These two cases are discussed first.

The first-guess and final analysis fields for the first period are illustrated by Figures 10 and 11, respectively. The data used in these analyses were averaged temporally over the 15-minute period centered around 7:07 a.m. (C.S.T) of August 15. Most of the average winds during this period ranged in direction from 211 to 240° and in speeds from 1.8 to 3.2 m/sec. Those stations having average directions and speeds out of these ranges are listed in Table 1. The average winds at station 102 were noticeably different than winds measured at adjacent stations throughout the cases investigated. Although questionable, they were not rejected by the rejection criteria in the procedure.

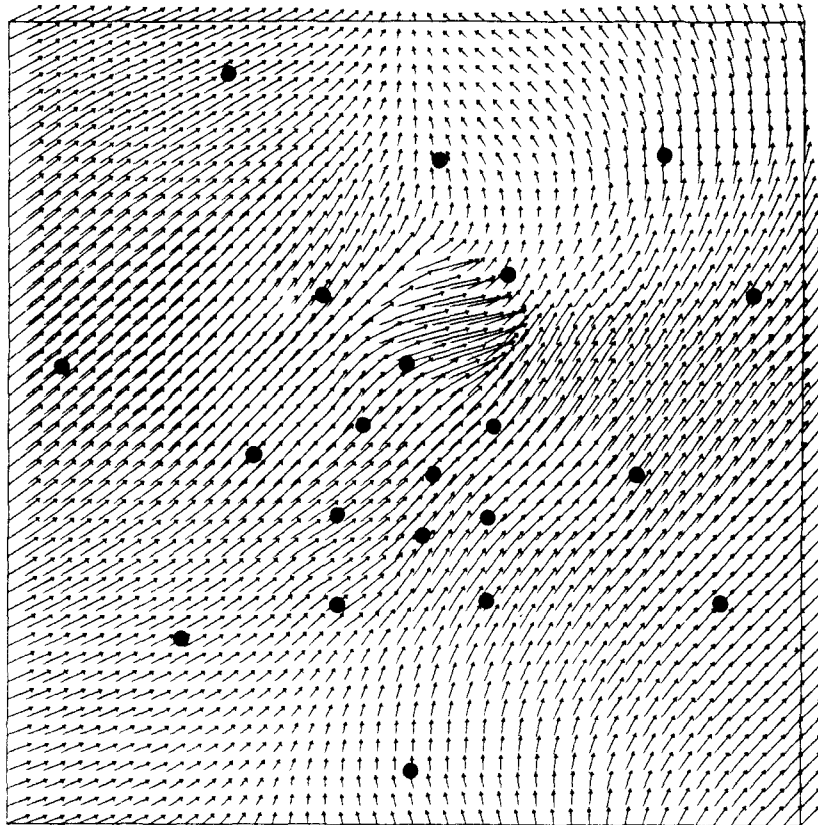


Figure 10. First-guess analysis for averaged data centered around 7:07 A.M. (C.S.T.) for August 15, 1975, St. Louis (RAPS).

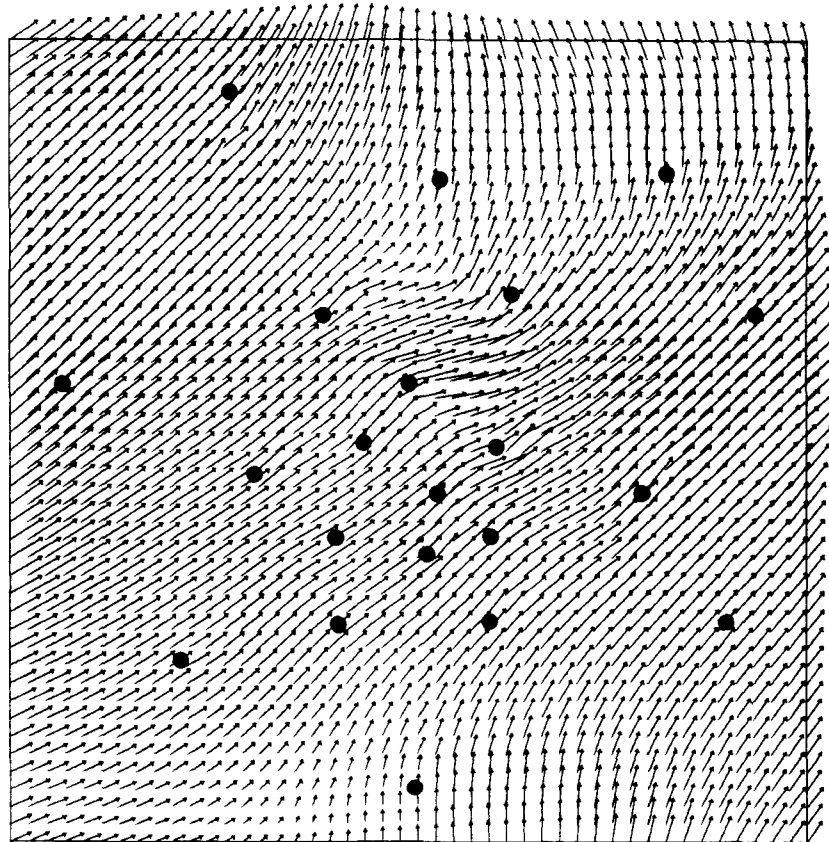


Figure 11. Non-divergent analysis for averaged data centered around 7:07 A.M. (C.S.T.) for August 15, 1975, St. Louis (RAPS).

Table 1. STATIONS HAVING AVERAGE WIND DIRECTIONS AND SPEEDS OUT OF THE RANGE 211 TO 240° AND 1.8 TO 3.2 M/SEC, RESPECTIVELY FOR THE ANALYSIS ILLUSTRATED BY FIGURES 10 AND 11

<u>Station Number</u>	<u>Average Wind Direction</u>	<u>Average Wind Speed</u>
102	260°	4.1 m/sec
108	199	0.9
114	155	0.8
115	173	1.3
118	181	1.0

The wind values listed in Table 1 were likely indications of the presence of mesoscale features of the atmosphere. By averaging the data over 15-minute periods, these features, which are significant in determining actual flow patterns, would not be ignored.

The CDC analysis (Fig 10) shows the variability in the wind near those stations listed above. As can be readily seen, especially north and northeast of St. Louis, the analysis is not divergent-free. This analysis was adjusted to minimize the divergence. The final analysis, illustrated by Figure 11, was generated by adjusting the u- and v-wind components at every grid point so that the quantity

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y}$$

was minimized by the technique described in Section 3.

The most noticeable adjustment occurred in the area near station 102 and 108. The flow pattern here was made less chaotic. Another noticeable adjustment occurred near the middle of the top border where the flow converged. The wind speeds were greatly increased here and, to a lesser extent, near station 114. It should be noted, with the exception of the area near station 102, that the large adjustment in the CDC analysis occurred in areas outside the data network. Moreover, the wind determined at a grid point near a station will not always be exactly what was observed.

Figure 12 shows the first-guess field of the flow using 15-minute-averaged data centered around 7:37 a.m. (C.S.T.) for August 15. These wind data were observed half an hour after the data used for the analysis in Figures 10 and 11.

All the stations, but one, had average wind speeds in the range of 1.4 to 3.4 m/sec. Station 102 had an average wind speed of 4.3 m/sec. Most of the stations had average wind directions falling into the 216 to 249° range. Those stations having average wind directions out of this range are listed in Table 2.

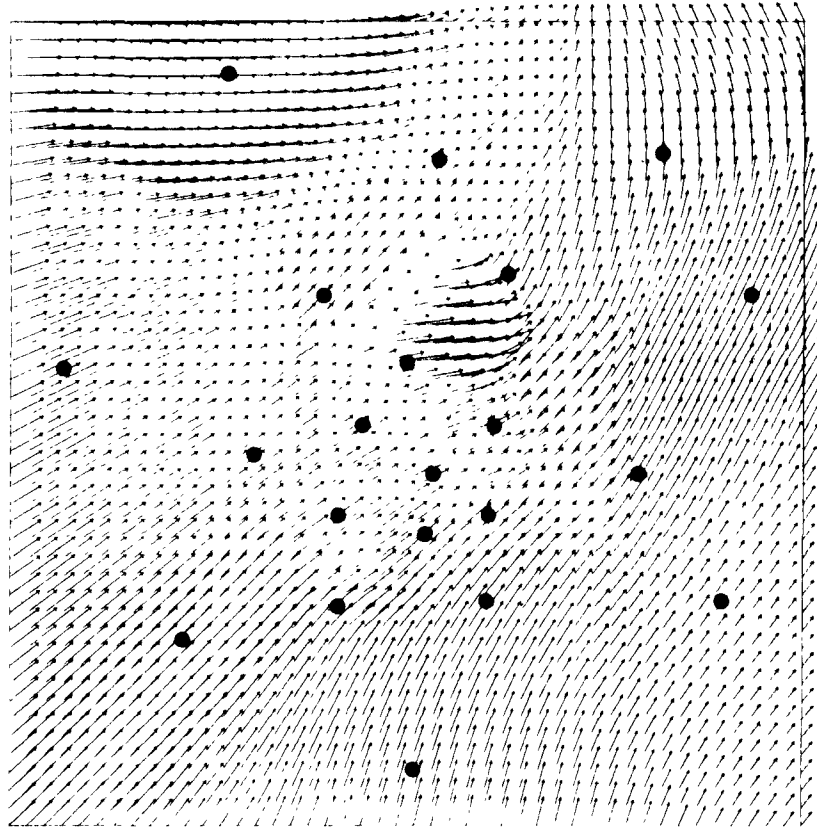


Figure 12. First-guess analysis for averaged data centered around 7:37 A.M. (C.S.T.) for August 15, 1975, St. Louis (RAPS).

Table 2. STATIONS HAVING AVERAGE WIND DIRECTIONS OUT OF THE 216 TO 249° RANGE FOR THE ANALYSIS ILLUSTRATED BY FIGURES 12 AND 13

<u>Station Number</u>	<u>Average Wind Direction</u>
102	265°
108	204
109	210
115	174
116	204
118	199
121	267

The influence of the data on the analysis from the outlying stations is illustrated in the upper-left corner of Figure 12. Many more grid point values are affected by the outlying stations than the inner stations. The average wind direction at station 121 is different than the others, but the grid point values in the corner reflect the value observed at this single station.

Figure 13 shows the non-divergent analysis after the winds were adjusted. Like the adjustment of the analysis of the previously mentioned period, the wind speeds near the top of the border of the grid were increased to compensate for the extensive convergence pattern. The analysis in the area near stations 102, 108, and 121 has been noticeably adjusted resulting in a smoother, non-divergent flow.

The next two analyses, illustrated by Figures 14 and 15, were generated using data averaged over the 15-minute period centered around

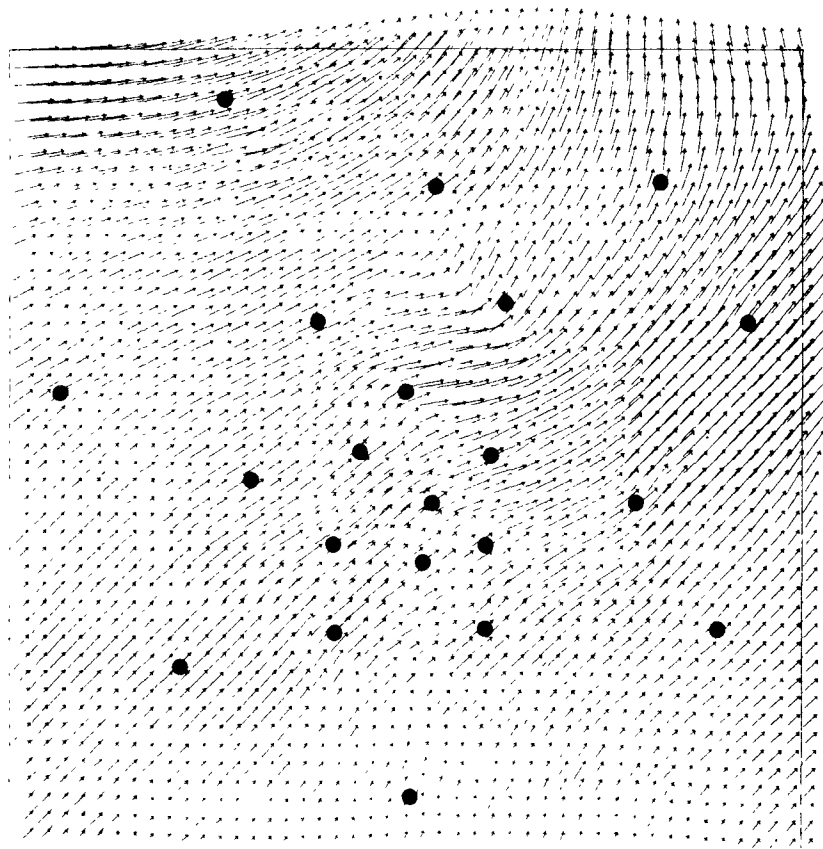


Figure 13. Non-divergent analysis for averaged data centered around 7:37 A.M. (C.S.T.) for August 15, 1975, St. Louis (RAPS).

8:22 a.m. (C.S.T) for August 15. These data were observed 45 minutes after the data analyzed in Figures 12 and 13 were observed.

Except for station 111, the set of data was complete and contained average wind directions which were more variable in the urban area than in the other sets. Most of the average wind directions ranged from 208 to 257° and the average wind speeds, with one exception, ranged from 1.7 to 3.6 m/sec. Station 102 had an average wind speed of 4.8 m/sec. Stations with average wind directions not in this range are listed in Table 3.

Table 3. STATIONS HAVING AVERAGE WIND DIRECTIONS OUT OF THE RANGE 208 to 257°, FOR THE ANALYSIS ILLUSTRATED BY FIGURES 14 AND 15

<u>Station Number</u>	<u>Average Wind Direction</u>
102	286°
105	189
114	200
121	273

The first-guess wind field analysis (Fig. 14) depicts the large variability in the wind direction. The average wind direction near stations 105 and 106 differed nearly by 60° and the average wind direction near station 102 differed by nearly 45° from the surrounding area.

The final analysis (Fig. 15) shows that the major adjustments occurred in the areas near stations 102, 108, and 106 and on the top center of the grid. The wind speeds were decreased slightly in the lower-left

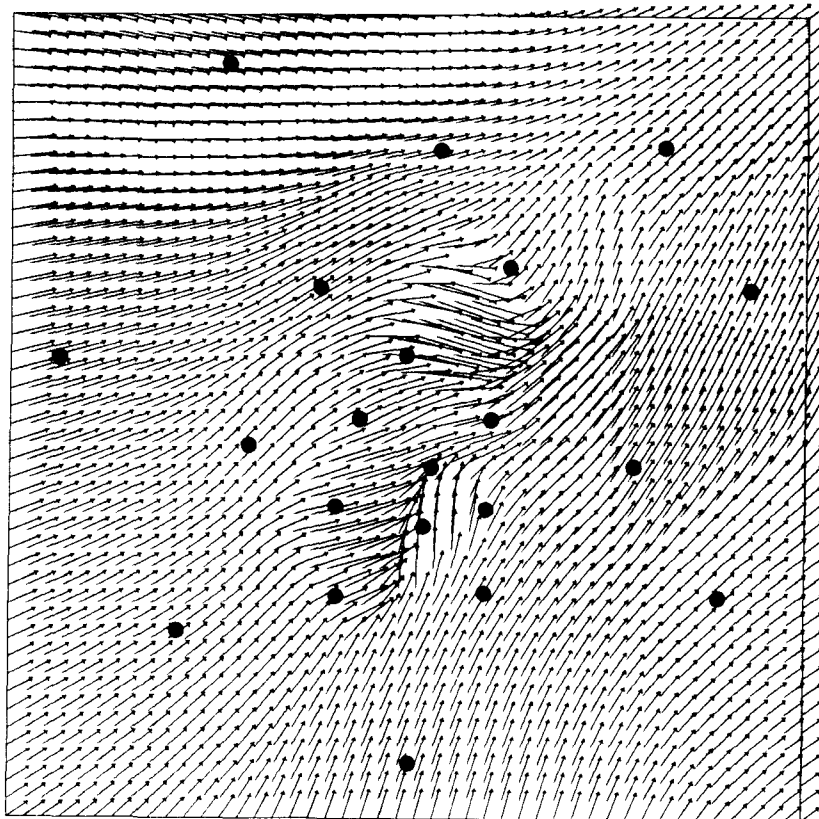


Figure 14. First-guess analysis for averaged data centered around 8:22 A.M. (C.S.T.) for August 15, 1975, St. Louis (RAPS).

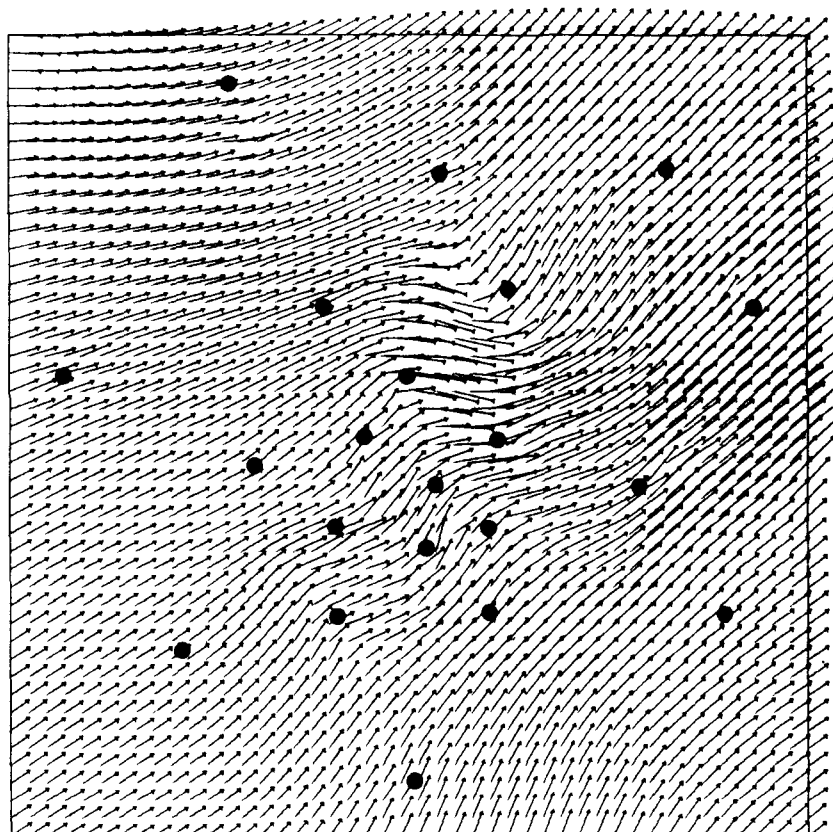


Figure 15. Non-divergent analysis for averaged data centered around 8:22 A.M. (C.S.T.) for August 15, 1975, St. Louis (RAPS).

corner and increased near the upper segment of the right border. As in this case, significant changes in the u- and v- wind components usually occurred outside the station network.

Figure 16 illustrates another analysis using data which were not uniform over the urban area. Data from stations 111 and 114 were missing during this period centered around 11:37 a.m. (C.S.T.) for August 14. The average wind direction ranged from 136 to 183°, while most of the average wind speeds fell in the 3.3 to 4.8 m/sec. range. Stations 102 and 103 had average wind speeds of 6.6 and 5.7 m/sec., respectively.

The CDC wind analysis outside the city was fairly uniform with the winds from the south southeast at approximately 4 m/sec. The wind near stations 102, 103, 112 was more southerly at about the same speed. Therefore, areas of convergence occurred over the city.

The u- and v- components of the wind in these areas were adjusted to minimize the divergence. This non-divergent analysis, illustrated by Figure 17, might not appear to be as smooth as the previously discussed analyses. Due to the higher wind speeds and gradual wind direction changes near station 102, 103, 113, the longer vectors intersect others at angles, making the field appear chaotic.

The last pair of figures (Figs 18 and 19) illustrates the analyses for the 15-minute-averaged data centered around 2:37 p.m. (C.S.T.) for August 13. At this time, a squall line was moving through St. Louis from the northwest at approximately 20 km/hr. The position of the squall line during this time period can be located at grid points with west winds.

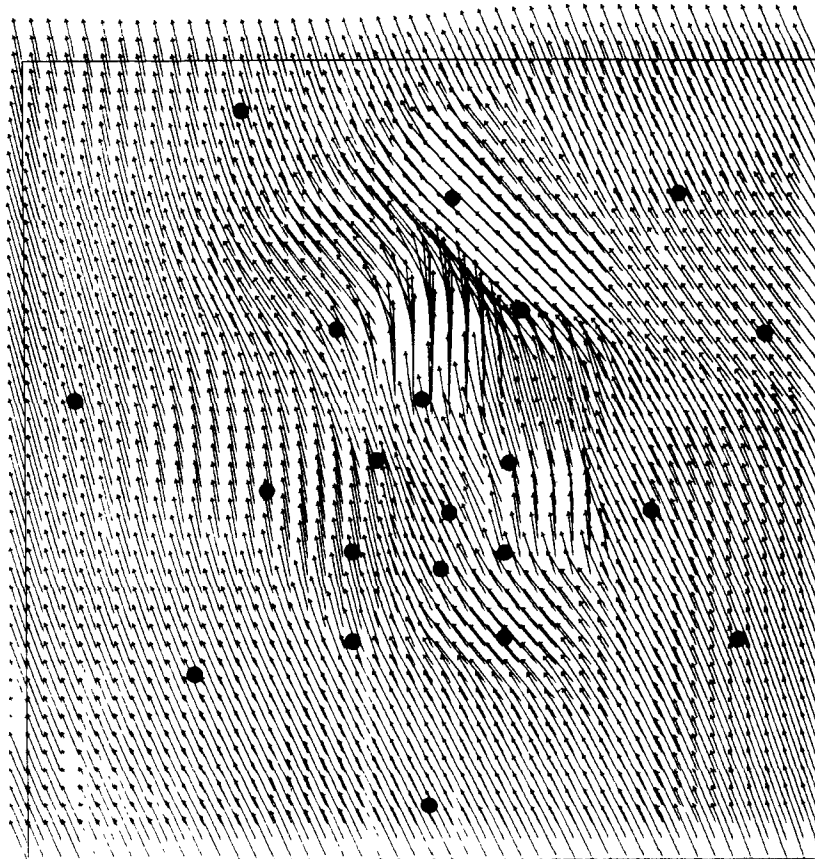


Figure 16. First-guess analysis for averaged data centered around 11:37 A.M. (C.S.T.) for August 14, 1975, St. Louis (RAPS).

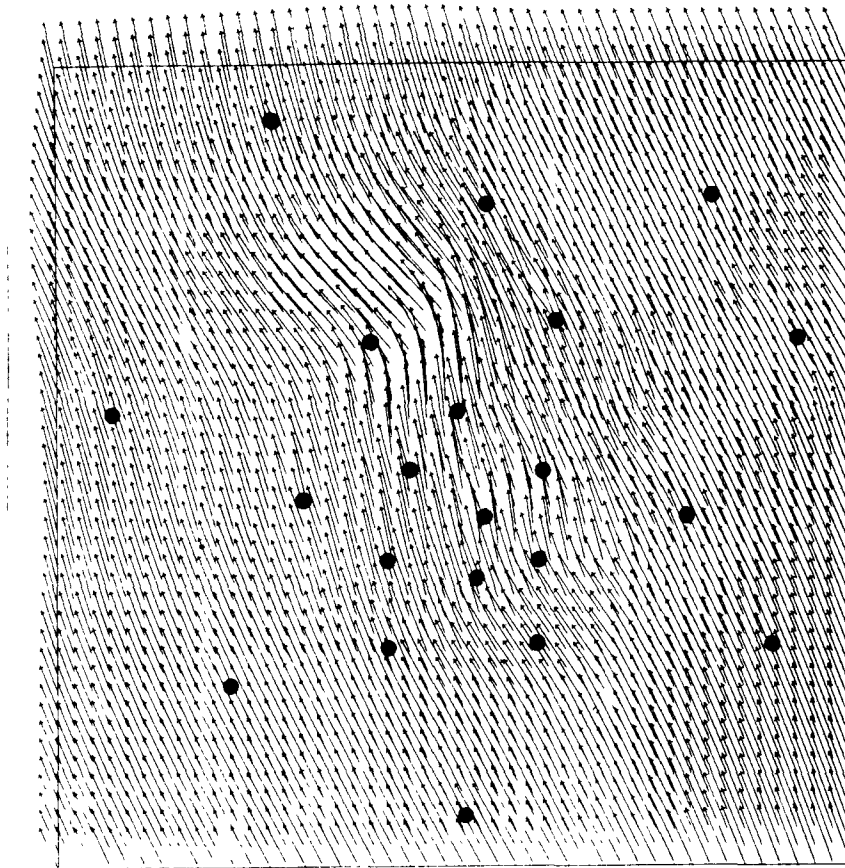


Figure 17. Non-divergent analysis for averaged data centered around 11:37 A.M. (C.S.T.) for August 14, 1975, St. Louis (RAPS).

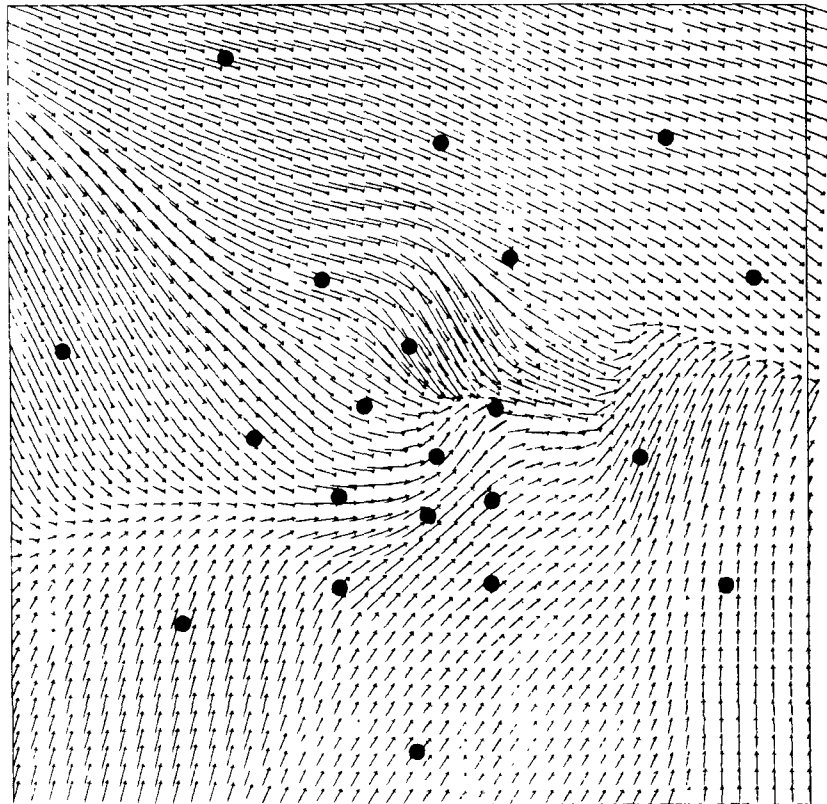


Figure 18. First-guess analysis for averaged data centered around 2:37 P.M. (C.S.T.) for August 13, 1975, St. Louis (RAPS).

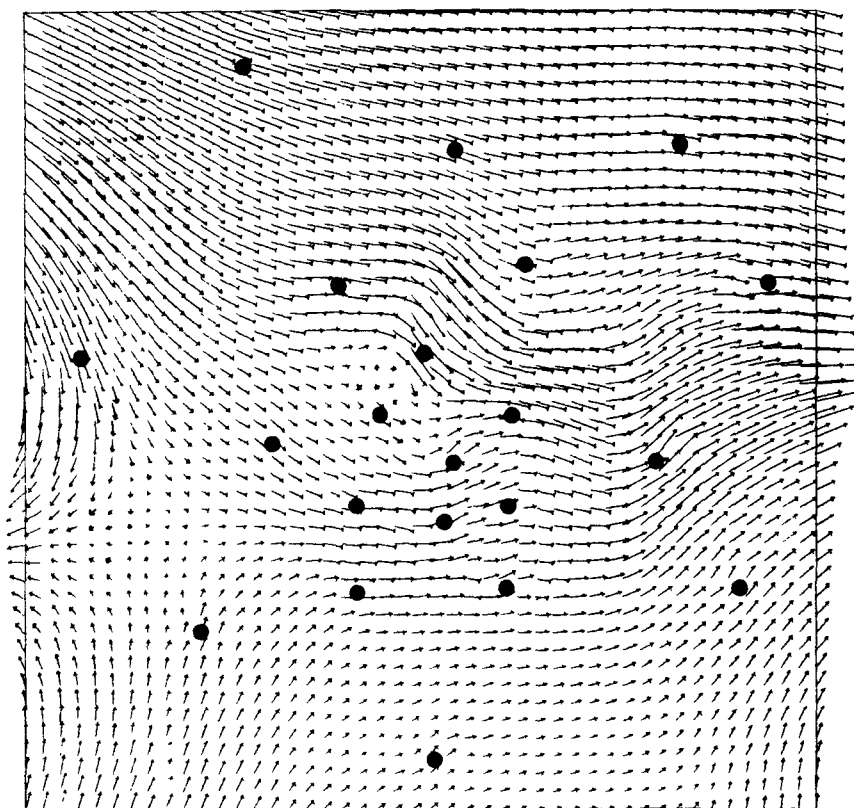


Figure 19. Non-divergent analysis for averaged data centered around 2:37 P.M. (C.S.T.) for August 13, 1975, St. Louis (RAPS).

During this period, all stations had data except for 111. The wind directions ranged from 188° at station 117 to 333° at station 120. The wind speeds ranged from 0.9 m/sec. at station 117 to 4.2 m/sec. at station 102.

This case was included to show the results of the non-divergent wind analysis routine starting from a first-guess field (Figure 18) generated from data characterized by an extensive area of strong convergence. Large adjustments were made to the first-guess field to minimize the convergence. As can be seen by Figure 19, the final analysis in some areas of the field was drastically changed.

Among the areas where changes were made, there were four areas where the winds were adjusted noticeably. These areas included the grid points near stations 107, 116, and 119. A col appeared on the final analysis field near station 119. To the left side of the col the wind directions at the grid points changed 180° .

The wind speeds at the grid points near station 107 were sharply decreased. Also, the wind speeds near 110 and 118 were decreased and the wind directions became westerly. On the right side of the grid, the wind speeds were increased sharply to minimize the convergence there.

These five cases were chosen as examples to illustrate what adjustments are made to the first-guess field by the non-divergent wind analysis procedure. The cases included data where the wind did and did not vary greatly across the field so that the extent of the adjustments for both types of cases would be known.

The CDC procedure, which generated the first-guess fields, proved to be adequate in analyzing the wind data over the St. Louis area.

Analyses proved to be very good when compared to the data at the station points.

The non-divergent wind analysis procedure used to generate the final analyses would be useful to produce wind fields for Eulerian air pollution models. In most areas of individual cases, the first-guess wind analysis is only slightly adjusted. However, there are cases when the adjustments are so extensive, that the final analyses are noticeably different.

5. SUMMARY AND CONCLUSIONS

An algorithm was created to analyze data from the RAPS network at St. Louis, Missouri. The algorithm is based on modified versions of an objective analysis technique developed by Hovland, et.al. (1976) at Control Data Corporation and a non-divergent wind analysis routine developed by Liu and Goodin (1976).

The algorithm was applied to five periods of 15-minute averaged wind data during August of 1975. The data from the first two periods showed a rather uniform wind field, while the data from the last three showed a more variable wind field. The last period involved a case where a squall line was passing through the St. Louis region.

In every case, the calculated wind values at the grid points on the first-guess field (modified CDC procedure) corresponding to station locations agreed well with the observations. It is uncertain how well the actual wind field was depicted by this field in areas far from the stations, particularly near the borders of the grid.

The final analyses (modified Liu and Goodin procedure) were generated by adjusting the u- and v- wind components from the first-guess analyses so that the divergence across grid squares was minimized. The wind was changed only slightly at most grid points. However, in areas of strong divergence, the wind speed and/or direction changed considerably. This type of analysis is desired for two-dimensional photochemical modeling, since the divergence would act as a spurious source or sink term.

There were several problems with the data used in the analyses presented in this report. The wind direction and speed at station 102 were consistently different than the winds at adjacent stations. Moreover, the winds were not measured at the same height at all stations. The wind at stations 108, 110, 114-118, and 121 were measured at 10 meters and at 30 meters at the remaining stations. No normalization of the winds was attempted in this algorithm.

6. USER'S GUIDE

The purpose of this section is to describe the format of the data set used by the algorithm and to inform the user about the multi-level capability of the algorithm. With this information, the user should be able to generate the non-divergent wind fields.

The algorithm requires input of the data summarized in Table 4. The grid parameters (number of grid points in the x and y directions and grid spacing) are defined in the context of the program, not the data set. This was done since the algorithm cannot be applied to a different grid configuration by merely changing the values of these parameters. The CDC technique, used to construct a first-guess field for the non-divergent wind analysis, employs two sets of parameters determined exclusively for a given grid configuration and data network.

Table 4. SUMMARY OF DATA INPUT TO THE NON-DIVERGENT WIND FIELD ANALYSIS ALGORITHM

	<u>Variable Name</u>	<u>Format</u>
Data card # 1	EPSI	E10.3
	IE	I3
	NPER	I3
	P	F5.2
	NLEV	I3
Data card # 2	ZK	10F5.0
Data cards # 3-23	NSTA	I3
	X	F6.2
	Y	F6.2
Data cards # 24-45 (u,v-component form)	IDAY*	I3
	IHR*	I3
	MIN*	I3
	US	F5.2,1X,F5.2
	VS	
Data cards # 24-29 (direction,speed form)	MIN	(I3,5X,I2,2X, I3,6(T21,4(4X, 2F5.1),/)
	IHR	
	IDAY	
	WDIR	
	WSPD	

* typed on data card # 24

The value of "EPSI" is compared to the average value of the divergence calculated over the grid after each iteration. When EPSI is greater than the maximum divergence value, the analysis has converged to a satisfactory degree. At this point, the iterative process is terminated. The value of 1.0×10^{-5} proved to be adequate.

Parameters "IE" and "NPER" refer to the wind data set. The total number of periods of data to be used is defined by "NPER". "IE" serves a dual purpose. First, the value selects the desired 15-minute period to use from a data set containing many periods. This is especially useful when the data is stored on a mass storage file. If the data corresponding to the fourth period of a data set is desired, the value of "IE" would be 3. The program would then skip over the first 3 data periods and start reading the data for the fourth period.

The value of "IE" also makes it possible for the program to accept averaged-wind data in two different forms. When "IE" is less than 100, the program would read the data as u and v wind components. When "IE" is greater than 100, the program would read the data in the form of wind direction and speed. In the latter case, 100 is subtracted from the value to identify the desired period to use in the algorithm.

The last two parameters on the first data card refer to the multi-level analysis section of the program. The number of the levels where wind fields are desired is defined by "NLEV", which should not exceed 10. The height of these levels, in meters, are defined on the second data card and stored into array "ZK". If only the surface analysis is desired, the value of "NLEV" would be 1 and the second card would contain the number 20.

The wind speeds at height z_k are determined by the power law equation

$$|\vec{v}_k| = |\vec{v}_1| \left(\frac{z_k}{z_1} \right)^p, \quad (15)$$

where $|\vec{v}_1|$ and $|\vec{v}_k|$ denote the wind speed (m/sec) at the level of data measurement and level k respectively. The wind direction, in meteorological coordinates, at height z_k (meters) is determined by

$$\theta_k = \theta_1 + \left(\frac{1^\circ}{30\text{m}} \right) (z_k - z_1) \quad (16)$$

The value of the exponent, p , is dependent upon ground roughness and lapse rate. In general, the exponent is small during the day and large at night (Munn, 1966). A value of 0.4 was assumed for general purposes. This value can be changed by changing the parameter "p" in the data set.

Data cards 3 through 33 contain the station identification number (101-121) and the x and y coordinates of the station relative to the south west corner of the 46 by 46 km grid. There is one data card for each station.

The averaged wind data are read last. The user has an option to use averaged wind data in the form of u - v components (m/sec) or in the form of wind direction and speed (m/sec). If the u - v component form is used, a data card containing the day and time (IDAY,IHR,MIN) must precede the actual wind data card set. The average u and v components for each of the stations are listed on individual data cards according to

the format given in Table 4.

If the direction and speed form of data is chosen, the time and day (MIN,IHR,IDAY) are read from the first card containing averaged wind data in the first 15 columns. Each wind data card contains, wind direction and speed for four stations, except the last card which contains data for station #121.

All of the data input is read by the MAIN subroutine computer code. In addition, the MAIN subroutine 1) rejects wind data according to the rejection scheme described in Section II; 2) calls subroutine UVCMP1, if needed, to convert the average wind direction and speed (m/sec) input to the u and v component form; 3) calls subroutine INITIL; and 4) adjusts the wind fields generated by the modified CDC technique to produce non-divergent wind fields.

Subroutine INITIL defines the number of data points and the size of the scan radius to use in each of the five iterations in the CDC technique and calls subroutine GRID. Subroutine GRID generates wind fields from the averaged u and v -wind components at the 21 data points using the modified version of the CDC technique.

7. COMPUTER PROGRAM LISTING - FORTRAN

This section contains the FORTRAN computer code for the non-divergent wind field analysis algorithm. The code consists of a MAIN subroutine which calls subroutine UVCMP1, INITIL, and PRINT. Subroutine INITIL calls subroutine GRID. The code does not include any UNIVAC 1110 system routine.

```

1      C      DICTIONARY OF VARIABLES USED IN MAIN
2      C *****
3      C
4      C
5      C
6      C      AVGU      AVERAGE VALUE OF U-COMPONENTS
7      C      AVGV      AVERAGE VALUE OF V-COMPONENTS
8      C      DIR       THE DIRECTION OF THE WIND IN MET COORDINATES
9      C      DIV       POINT VALUE OF THE DIVERGENCE
10     C      DIVR      ARRAY CONTAINING THE DIVERGENCE VALUES
11     C      DMAX      MAXIMUM ABSOLUTE VALUE OF DIVERGENCE ACROSS A FIELD
12     C      DX        DISTANCE BETWEEN GRID POINTS IN THE X DIRECTION
13     C      DY        DISTANCE BETWEEN GRID POINTS IN THE Y DIRECTION
14     C      DZ        DISTANCE BETWEEN GRID POINTS IN THE Z DIRECTION
15     C      EPSI      A CONVERGENCE PARAMETER SET TO MUCH LESS THAN 1.
16     C      IDAY      JULIAN DAY OF DATA
17     C      IHR       HOUR OF DAY OF DATA
18     C      IE        NUMBER OF DATA SETS TO BE SKIPPED IN DATA FILE
19     C      IEND      NUMBER OF RECORDS TO BE SKIPPED IN DATA FILE
20     C      IOUT      DEVICE UPON WHICH ARRAYS ARE STORED FOR VECTOR OUTPUT;
21     C      IF IOUT = 0 , NO DEVICE USED
22     C      MIN       TEMPORAL MID-POINT OF DATA AVERAGING INTERVAL
23     C      NLEV      NUMBER OF FIELDS TO BE ANALYZED IN THE VERTICAL
24     C      NRPTS     NUMBER OF STATIONS TO BE USED IN ANALYSIS NOT GREATER THAN 25
25     C      NSKIP     DUMMY VARIABLE USED IN SKIPPING DATA SETS
26     C      NSTA      ARRAY CONTAINING STATION NUMBER
27     C      P         THE VALUE OF THE EXPONENT IN THE POWER LAW FORMULA
28     C      SIGU      STANDARD DEVIATION OF THE U-COMPONENTS
29     C      SIGV      STANDARD DEVIATION OF THE V-COMPONENTS
30     C      SPD       ARRAY CONTAINING WIND SPEED
31     C      SSU       SUM OF THE SQUARES OF THE U-COMPONENTS
32     C      SSV       SUM OF THE SQUARES OF THE V-COMPONENTS
33     C      SUMU      SUM OF THE U-COMPONENTS
34     C      SUMV      SUM OF THE V-COMPONENTS
35     C      U         ARRAY CONTAINING FINAL ANALYSIS
36     C      US        ARRAY CONTAINING U COMPONENT OF STATION REPORT
37     C      U1        ARRAY USED TO SAVE SURFACE STATION REPORTS OF U COMPONENT
38     C      V         ARRAY CONTAINING FINAL ANALYSIS OF V VELOCITY FIELD
39     C      VS        ARRAY CONTAINING V COMPONENT OF STATION REPORT
40     C      V1        ARRAY USED TO SAVE SURFACE STATION REPORTS OF V COMPONENT
41     C      X         ARRAY CONTAINING X COORDINATE OF STATION LOCATIONS
42     C      Y         ARRAY CONTAINING Y COORDINATE OF STATION LOCATIONS
43     C      Z         HEIGHT OF ANALYSIS LEVEL ABOVE SURFACE
44     C
45     C
46     C
47     C
48     C      DIMENSION NSTA(30),X(30),Y(30),US(30),VS(30),WDIR(25),VSPD(25)
49     C      DIMENSION U(46,46),V(46,46),DIR(25),SPD(25),U1(25),V1(25)
50     C      DIMENSION DIVR(46,46),F(46,46),ZK(10),UT(46,46),VT(46,46)
51     C      COMMON IDAY,IHR,MIN
52     C
53     C *****
54     C      THE ALGORITHM PARAMETERS ARE DEFINED
55     C *****

```

```

56      C      DATA PHI/3.141592654/,IOUT/8/,ALP/1./,BET/0./,KKMAX/250/
57      DATA FC/1.0/,IMAX/46/,JMAX/46/,I1/2/,J1/2/,NRPTS/21/,
58      *DX/1000./,DY/1000./
59      FX=1.0-FC
60      I2=IMAX-1
61      J2=JMAX-1
62      READ(5,6) EPSI,IE,NPER,P,NLEV
63      WRITE(6,5) NRPTS,DX,DY,EPSI,IE,NPER,P,NLEV
64      5 FORMAT(I3,2F6.0,E10.3,2I3,F5.2,I3)
65      6 FORMAT(E10.3,2I3,F5.2,I3)
66      READ(5,7) (ZK(I),I=1,NLEV)
67      7 FORMAT(10F5.0)
68      DO 15 I=1,NRPTS
69      READ(5,12) NSTA(I),X(I),Y(I)
70      12 FORMAT(I3,2F6.2)
71      15 CONTINUE
72
73      C
74      C*****
75      C      THE WIND DATA ARE READ
76      C
77      C      IE>100 FOR DATA IN THE FORM OF DIRECTION AND SPEED(M/SEC)
78      C      IE<100 FOR DATA IN THE FORM OF U AND V COMPONENTS(M/SEC)
79      C*****
80      C
81      DO 1000 NP=1,NPER
82      IF(IE .GE. 100) GO TO 27
83      IF(NP .GT. 1) GO TO 23
84      C
85      C      SKIP IE NUMBER OF PERIODS OF DATA IN THE FORM OF U AND V COMPONENTS.
86      C      (THERE ARE 22 RECORDS PER PERIOD)
87      C
88      IEND = IE * 22
89      IF(IEND .EQ. 0) GO TO 23
90      DO 22 I=1,IEND
91      READ(5,21) NSKIP
92      21 FORMAT(I1)
93      22 CONTINUE
94      23 READ(5,24) IDAY,IHR,MIN
95      24 FORMAT(' ',2I3,I2)
96      PRINT 24, IDAY,IHR,MIN
97      DO 26 K=1,NRPTS
98      READ(5,25) US(K),VS(K)
99      25 FORMAT(F5.2,1X,F5.2)
100     26 CONTINUE
101     GO TO 34
102
103     C
104     C      SKIP (IE-100) NUMBER OF PERIODS OF DATA IN THE FORM OF DIRECTION AND SPEED
105     C      (THERE ARE 7 RECORDS PER PERIOD)
106     C
107     27 CONTINUE
108     IF(NP .GT. 1) GO TO 30
109     IEND = (IE-100)*7
110     IF(IEND .EQ. 0) GO TO 30
111     DO 29 I=1,IEND
112     READ(5,28) NSKIP
113     28 FORMAT(I1)

```

```

113      29 CONTINUE
114      30 READ(5,32) MIN,INR,IDAY, (WDIR(I),WSPD(I),I=1,25)
115      32 FORMAT(I3,5X,I2,2X,I3,7(T21,4(4X,2F5.1),/))
116      WRITE(6,24) IDAY,INR,MIN
117
118      C
119      C      CONVERT DIRECTION AND WIND SPEED TO U AND V COMPONENTS
120      C
121      DO 33 K=1,NRPTS
122      CALL UVCMP(US(K),VS(K),WDIR(K),WSPD(K))
123      33 CONTINUE
124      34 WRITE(6,35)
125      35 FORMAT(' ',10X,'STA',15X,'X',17X,'Y',17X,'U',17X,'V',/)
126      DO 40 K=1,NRPTS
127      WRITE(6,37) NSTA(K),X(K),Y(K),US(K),VS(K)
128      37 FORMAT(' ',10X,I3,2(13X,F5.2),2(12X,F6.2))
129      40 CONTINUE
130
131      C
132      C*****
133      C      CALCULATE MEAN AND SIGMA OF DATA SAMPLE.
134      C      REJECT DATA WHEN VALUES ARE 4 SIGMA FROM MEAN OR GREATER THAN 20
135      C*****
136      C
137      SSU=0.0
138      SSV=0.0
139      SUMU = 0.
140      SUMV = 0.
141      ICOUNT = 0
142      DO 47 K=1,NRPTS
143      IF(US(K) .GT. 20.0 .OR. VS(K) .GT. 20.0) GO TO 47
144      SUMU = SUMU + US(K)
145      SUMV = SUMV + VS(K)
146      ICOUNT = ICOUNT + 1
147      SSU = SSU + US(K)*US(K)
148      SSV = SSV + VS(K)*VS(K)
149      47 CONTINUE
150      AVGU = SUMU/ICOUNT
151      AVGV = SUMV/ICOUNT
152      SIGU = SQRT(SSU/ICOUNT - AVGU*AVGU)
153      SIGV = SQRT(SSV/ICOUNT - AVGV*AVGV)
154      PRINT 50
155      50 FORMAT('1',35X,'STATISTICS FROM ALL DATA LESS THAN 20 M/SEC',/)
156      PRINT 65, AVGU,AVGV,SIGU,SIGV
157      SSU=0.0
158      SSV=0.0
159      SUMU = 0.
160      SUMV = 0.
161      ICOUNT = 0
162      DO 60 K=1,21
163      IF(US(K) .GT. 4*SIGU+AVGU .OR. VS(K) .GT. 4*SIGV+AVGV)
164      *WRITE(6,57) K,US(K),VS(K)
165      IF(US(K) .GT. 4*SIGU+AVGU .OR. VS(K) .GT. 4*SIGV+AVGV)
166      *US(K) = 99.0
167      IF(US(K) .GT. 4*SIGU+AVGU .OR. VS(K) .GT. 4*SIGV+AVGV)
168      *VS(K) = 99.0
169      IF(US(K) .LT. AVGU-4.*SIGU .OR. VS(K) .LT. AVGV-4.*SIGV)
170      *WRITE(6,57) K,US(K),VS(K)
171      IF(US(K) .LT. AVGU-4.*SIGU .OR. VS(K) .LT. AVGV-4.*SIGV)

```



```

170      *US(K) = 99.0
171      IF(US(K) .LT. AVGU-4.*SIGU .OR. VS(K) .LT. AVGV-4.*SIGV)
172      *VS(K) = 99.0
173      IF(US(K) .GT. 4.*SIGU+AVGU .OR. VS(K) .GT. 4.*SIGV+AVGV)
174      *GO TO 60
175      IF(US(K) .LT. AVGU-4.*SIGU .OR. VS(K) .LT. AVGV-4.*SIGV)
176      *GO TO 60
177      57 FORMAT(' ',2X,'THE FOLLOWING DATA HAVE BEEN IGNORED ',
178      *' (EXCLUDING DATA FROM STA 108-121) --SINCE THE U AND/OR V '
179      *' EXCEDE AVG + OR - 2*SIG',//,45X,I3,5X,2F6.1)
180      SUMU = SUMU + US(K)
181      SUMV = SUMV + VS(K)
182      ICOUNT = ICOUNT + 1
183      SSU = SSU + US(K)*US(K)
184      SSV = SSV + VS(K)*VS(K)
185      60 CONTINUE
186      AVGU = SUMU/ICOUNT
187      AVGV = SUMV/ICOUNT
188      SIGU = SQRT(SSU/ICOUNT - AVGU*AVGU)
189      SIGV = SQRT(SSV/ICOUNT - AVGV*AVGV)
190      PRINT 63
191      63 FORMAT(5(//),35X,'STATISTICS FROM DATA WITHIN 4*SIGMA OF MEAN'
192      *,//)
193      WRITE(6,65) AVGU,AVGV,SIGU,SIGV
194      65 FORMAT(' ',6(//),45X,'AVGU =',F7.2,10X,'AVGV =',F7.2,//,
195      *45X,'SIGU =',F7.2,10X,'SIGV =',F7.2)
196      C
197      C*****
198      C   OBJECTIVE ANALYSIS PROCEDURE FIRST FINDS A FIRST GUESS FIELD USING THE
199      C   CDC PROCEDURE (CALL INITIL) THEN USING THE LIU AND GOODIN ALGORITHM
200      C   MINIMIZES THE DIVERGENCE
201      C*****
202      C
203      DO 500 LL=1,NLEV
204      DO 70 J=1,JMAX
205      DO 70 I=1,IMAX
206      F(I,J)=1.00
207      70 CONTINUE
208      WRITE(6,71)
209      71 FORMAT('1')
210      CALL INITIL(X,Y,US,U,IMAX,JMAX,NRPTS,AVGU,SIGU)
211      CALL INITIL(X,Y,VS,V,IMAX,JMAX,NRPTS,AVGV,SIGV)
212      CALL PRINT(U,V,IMAX,JMAX,IOUT,I,ZK(LL))
213      IF(LL .GE. 2) GO TO 75
214      C
215      C*****
216      C   THE GRID POINTS NEAREST THE DATA STATIONS ARE IDENTIFIED
217      C*****
218      C
219      DO 74 K=1,NRPTS
220      I=X(K)+.5
221      J=Y(K)+.5
222      C
223      C *****
224      C   STORE SURFACE WIND VALUES FOR POWER LAW EXTRAPOLATION
225      C *****
226      C

```

```

227      UI(K)=U(I,J)
228      VI(K)=V(I,J)
229      74 CONTINUE
230      75 CONTINUE
231  C
232      DO 80 K=1,NRPTS
233      I=X(K) + 0.5
234      J=Y(K) + 0.5
235      IF(US(K) .GE. 99. .OR. VS(K).GE. 99.) GO TO 80
236  C
237  C *****
238  C SET WEIGHTINGS FOR STATIONS AND SURROUNDING POINTS IF US OR VS IS GREATER
239  C THAN 99. THIS MEANS THE DATA FROM THE STATION WAS REJECTED IN
240  C
241  C THE FIRST PART OF THE ANALYSIS AND MUST BE IGNORED IN THE SECOND
242  C PART
243  C *****
244  C
245      F(I,J)=.25
246      F(I+1,J)=.500
247      F(I-1,J)=.500
248      F(I,J+1)=.500
249      F(I,J-1)=.500
250  C WRITE(6,77) NSTA(K),X(K),Y(K),US(K),VS(K)
251  C 77 FORMAT(' ',10X,I3,10X,2F10.2,10X,2F10.2)
252      80 CONTINUE
253  C
254  C *****
255  C ITERATE TO REDUCE THE DIVERGENCE KKNAX TIMES OR UNTIL THE MAXIMUM
256  C DIVERGENCE IS LESS THAN EPSI.
257  C THE ITERATIONS BEGIN IN THE CENTER OF THE GRID SO THAT THE ERRORS
258  C PROPAGATE OUTWARD. THE FOUR-POINT APPROXIMATION OF THE CONTINUITY
259  C EQUATION IS USED.
260  C *****
261  C
262      DO 115 KK=1,KKNAX
263      DNAX=0.
264      DO 100 MM=1,44
265      IF(MOD(MM,2) .EQ. 1) J=24+MM/2
266      IF(MOD(MM,2) .EQ. 0) J=24-MM/2
267      DO 100 NN=1,2
268      IF(MOD(NN,2) .EQ. 0) IA=23
269      IF(MOD(NN,2) .EQ. 0) IB=11
270      IF(MOD(NN,2) .EQ. 0) IC=-1
271      IF(MOD(NN,2) .EQ. 1) IA=24
272      IF(MOD(NN,2) .EQ. 1) IB=12
273      IF(MOD(NN,2) .EQ. 1) IC=1
274      DO 100 I=IA,IB,IC
275      IM=I-2
276      IPP=I+2
277      JMM=J-2
278      JPP=J+2
279      IM=I-1
280      IP=I+1
281      JMM=J-1
282      JP=J+1
283      DIVR(I,J)=FC*(U(I+1,J)-U(I-1,J))/(2.*DX)+FX*(U(I+2,J)-U(I-2,J))

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284          1          )/(4.*DX)+FC*(V(I,J+1)-V(I,J-1))/(2.*DY)+FX*(
285          2          V(I,J+2)-V(I,J-2))/(4.*DY)
286          DIV=DIVR(I,J)
287          IF(ABS(DIV).GT.DMAX) DMAX=ABS(DIV)
288          UT(I,J)=-2.*DIVR(I,J)*DX/(F(I+1,J)+F(I-1,J)+F(I,J+1)+F(I,J-1))
289          VT(I,J)=UT(I,J)
290          U(IP,J)=U(I+1,J)+F(I+1,J)*UT(I,J)
291          U(IM,J)=U(I-1,J)-F(I-1,J)*UT(I,J)
292          V(I,JP)=V(I,J+1)+F(I,J+1)*VT(I,J)
293          V(I,JM)=V(I,J-1)-F(I,J-1)*VT(I,J)
294          100 CONTINUE
295          C
296          C*****
297          C THE BOUNDARY VALUES ARE SET USING A ZERO GRADIENT CONDITION.
298          C THIS CONDITION JOINS THE TWO SEPARATE SUBGRIDS WHEN THE FOUR-
299          C POINT APPROXIMATION IS USED.
300          C*****
301          C
302          DO 104 L=2,J2
303          U(1,L)=U(2,L)
304          U(IMAX,L)=U(I2,L)
305          V(1,L)=V(2,L)
306          V(IMAX,L)=V(I2,L)
307          104 CONTINUE
308          DO 106 L=2,I2
309          U(L,1)=U(L,2)
310          U(L,JMAX)=U(L,J2)
311          V(L,1)=V(L,2)
312          V(L,JMAX)=V(L,J2)
313          106 CONTINUE
314          C
315          C*****
316          C DEFINE THE CORNER POINTS OF THE GRID AS THE AVERAGE BETWEEN
317          C THE TWO ADJACENT BOUNDARY VALUES.
318          C*****
319          C
320          U(1,1)=.5*(U(2,1)+U(1,2))
321          V(1,1)=.5*(V(2,1)+V(1,2))
322          U(1,JMAX)=.5*(U(2,JMAX)+U(1,J2))
323          V(1,JMAX)=.5*(V(2,JMAX)+V(1,J2))
324          U(IMAX,1)=.5*(U(I2,1)+U(IMAX,2))
325          V(IMAX,1)=.5*(V(I2,1)+V(IMAX,2))
326          U(IMAX,JMAX)=.5*(U(I2,JMAX)+U(IMAX,J2))
327          V(IMAX,JMAX)=.5*(V(I2,JMAX)+V(IMAX,J2))
328          C
329          C*****
330          C CHECK TO SEE IF THE WIND FIELD HAS CONVERGED
331          C*****
332          C
333          IF(DMAX.LT.EPSI) GO TO 120
334          115 CONTINUE
335          C
336          C*****
337          C PRINT THE U AND V FIELDS ONTO COMPUTER PAPER
338          C*****
339          C
340          120 CALL PRINT(U,V,IMAX,JMAX,IOUT,2,ZK(LL))

```

```

341      PRINT 200
342      200 FORMAT('1')
343      IF(NLEV.EQ. 1) GO TO 1000
344
345      C*****
346      C      SPEED AND DIRECTION AT LEVELS ABOVE THE SURFACE ARE DETERMINED BY
347      C      ASSUMING THAT THE WIND TURNS 10 DEGREES EVERY 304 METERS AND USING
348      C      A POWER LAW PROFILE
349      C*****
350      C
351      Z=ZK(LL)
352      PRINT 248,LL,Z,P
353      248 FORMAT(20X,'LEVEL NUMBER ',I2,10X,'HEIGHT (M) =',F7.2,
354      *10X,'P =',F7.4)
355      DO 260 H=1,NRPTS
356      IF(US(H) .GT. 20.0 .OR. VS(H) .GT. 20.0) GO TO 260
357      CALL UVCNPI(US(H),VS(H),DIR(H),SPD(H))
358      DIR(H)=DIR(H)+PHI*1.822688831E-4*Z
359      SPD(H)=SQRT(U1(H)**2+V1(H)**2)*(Z/20.)**P
360      260 CONTINUE
361      PRINT 211
362      211 FORMAT(3(/),20X,'STA',T34,'U',T45,'V',T55,'DIR',T65,
363      *'SPD',/)
364      DO 270 H=1,NRPTS
365      IF(US(H) .GT. 20.0 .OR. VS(H) .GT. 20.0) GO TO 270
366      NST = 100+H
367      CALL UVCNPI(US(H),VS(H),DIR(H),SPD(H))
368      PRINT 215,NST,US(H),VS(H),DIR(H),SPD(H)
369      215 FORMAT(20X,I3,T32,F6.2,T42,F6.2,T53,F6.2,T64,F5.2)
370      270 CONTINUE
371      500 CONTINUE
372      1000 CONTINUE
373      STOP
374      END

```

```

1      SUBROUTINE PRINT(U,V,IMAX,JMAX,IOUT,IN,Z)
2      C
3      C
4      C      THIS SUBROUTINE PRINTS THE ENTIRE 46 BY 46 ANALYSIS FIELD ONTO
5      C      FOUR SHEETS OF COMPUTER PAPER (FIRST : UPPER LEFT * SECOND :
6      C      LOWER LEFT * THIRD : UPPER RIGHT * FOURTH : LOWER RIGHT) AND
7      C      RECORDS THE U AND V ARRAYS ON A MASS STORAGE OR TAPE FILE
8      C
9      C
10     C
11     C
12     C *****
13     C      DICTIONARY OF VARIABLES USED IN PRINT
14     C *****
15     C
16     C
17     C
18     C      IDAY   THE JULIAN DAY OF THE YEAR OF THE DATA SET
19     C      IHR    THE HOUR OF THE DAY OF THE DATA SET (0 = MIDNIGHT)
20     C      IMAX   THE NUMBER OF GRID POINTS IN THE X DIRECTION
21     C      IN     VARIABLE USED IN TITLE OUTPUT
22     C      IOUT   THE UNIT NUMBER OF THE MASS STORAGE OR THE TAPE FILE.
23     C             IF NO MASS STORAGE OR TAPE FILE RECORDING IS DESIRED,
24     C             SET IOUT=0 IN THE DATA STATEMENT IN THE MAIN SUBROUTINE
25     C      JMAX   THE NUMBER OF GRID POINTS IN THE Y DIRECTION
26     C      K      THE NUMBER OF THE PRINTED PAGE
27     C      MIN    THE TEMPORAL MID-POINT OF THE 15 MINUTE AVERAGING INTERVAL
28     C      Z      THE HEIGHT OF THE LEVEL AT WHICH WINDS WERE COMPUTED
29     C
30     C
31     C
32     C
33     C      DIMENSION U(46,46),V(46,46)
34     C      COMMON IDAY,IHR,MIN
35     C      K2=4
36     C      112 IF(IMAX .LE. 20 .OR. JMAX .LE. 20) K2=1
37     C      DO 131 K=1,K2
38     C      II=1
39     C      IF=23
40     C      JI=1
41     C      JF=23
42     C      IF(K .EQ. 2 .OR. K.EQ.4) JI=24
43     C      IF(K .EQ. 2 .OR. K.EQ.4) JF=JMAX
44     C      IF(K .EQ. 3 .OR. K.EQ.4) II=24
45     C      IF(K .EQ. 3 .OR. K.EQ.4) IF=IMAX
46     C      WRITE(6,11)
47     C      11 FORMAT('1')
48     C      IF(IN .EQ. 1) WRITE(6,117) Z,K
49     C      IF(IN .EQ. 2) WRITE(6,118) Z,K
50     C      117 FORMAT(' ',10X,'FIRST GUESS',23X,F5.0,'-M U-FIELD (M/SEC)',30X,
51     C      *'PAGE ',I2,/)
52     C      118 FORMAT(' ',10X,'FINAL ANALYSIS',20X,F5.0,'-M U-FIELD (M/SEC)',30X,
53     C      *'PAGE ',I2,/)
54     C      WRITE(6,119) (I,I=II,IF)
55     C      119 FORMAT(5X,23I5,/)

```

```

56      DO 130 JJ=JI,JF
57      J=JMAX-JJ+1
58      WRITE(6,120) J,(U(I,J),I=II,IF)
59      120 FORMAT(' ',13,3X,23F5.1,/)
60      130 CONTINUE
61      131 CONTINUE
62      IF(IMAX .LE. 20 .OR. JMAX .LE. 20) K2=1
63      DO 151 K=1,K2
64      II=1
65      IF=23
66      JI=1
67      JF=23
68      IF(K .EQ. 2 .OR. K .EQ. 4) JI=24
69      IF(K .EQ. 2 .OR. K .EQ. 4) JF=JMAX
70      IF(K .EQ. 3 .OR. K .EQ. 4) II=24
71      IF(K .EQ. 3 .OR. K .EQ. 4) IF=IMAX
72      WRITE(6,11)
73      IF(IN .EQ. 1) WRITE(6,132) Z,K
74      IF(IN .EQ. 2) WRITE(6,133) Z,K
75      132 FORMAT(' ',10X,'FIRST GUESS',23X,F5.0,'-M V-FIELD (M/SEC)',30X,
76      *'PAGE ',12,/)
77      133 FORMAT(' ',10X,'FINAL ANALYSIS',20X,F5.0,'-M V-FIELD (M/SEC)',30X,
78      *'PAGE ',12,/)
79      WRITE(6,119) (I,I=II,IF)
80      DO 150 JJ=JI,JF
81      J=JMAX-JJ+1
82      WRITE(6,120) J,(V(I,J),I=II,IF)
83      150 CONTINUE
84      151 CONTINUE
85      IF(IOUT .EQ. 0) RETURN
86
87      C *****
88      C RECORD ONTO MASS STORAGE OR TAPE FILE
89      C *****
90      C
91      WRITE(IOUT,180) IDAY,IHR,MIN
92      180 FORMAT(3I4)
93      WRITE(IOUT,190) U
94      WRITE(IOUT,190) V
95      190 FORMAT(10F8.3)
96      RETURN
97      END

```

```

1      SUBROUTINE GRID(NDATA,XCOORD,YCOORD,STNVAL,GRDVAL,SUNWT,SUMCOR,
2      1      ISTART,IEND,JSTART,JEND,NSCANS,RSCAN,CRIT)
3      C
4      C
5      C      GRID IS A CDC SUBROUTINE CALLED BY SUBROUTINE INITIL.
6      C      GRID WILL TRANSFORM UNEQUALLY SPACED STATION DATA TO EQUALLY
7      C      SPACED GRID POINT DATA. WHEN GRID IS CALLED THERE MUST BE A
8      C      VALUE FOR EACH GRID POINT. THE FIRST GUESS FIELD MAY BE A
9      C      PREVIOUS ANALYSIS, A FORECAST, OR SIMPLY A CONSTANT. THE GRID
10     C      MUST BE ARRANGED SO THAT GRID POINTS SURROUND EACH DATA POINT.
11     C
12     C
13     C
14     C
15     C
16     C *****
17     C      DICTIONARY OF VARIABLES USED IN GRID
18     C *****
19     C
20     C
21     C
22     C      CRIT      CONVERGENCE CRITERION
23     C      ERROR    SUM OF SQUARES OF THE DIFFERENCES BETWEEN OBSERVATIONS
24     C                AT THE STATIONS AND INTERPOLATED VALUES ON THE FIELD.
25     C                USED IN THE CONVERGENCE TESTING.
26     C      GRDVAL   ARRAY CONTAINING GRID POINT VALUES
27     C      IEND     NUMBER OF GRID POINTS IN THE X DIRECTION
28     C      INDEX1   I-VALUE OF GRID POINT ON SCAN CIRCLE AND TO LEFT OF STATION
29     C      INDEX2   I-VALUE OF GRID POINT ON SCAN CIRCLE AND TO RIGHT OF STATION
30     C      INDEX3   J-VALUE OF GRID POINT ON SCAN CIRCLE AND BELOW THE STATION
31     C      INDEX4   J-VALUE OF GRID POINT ON SCAN CIRCLE AND ABOVE THE STATION
32     C      JEND     NUMBER OF GRID POINTS IN THE Y DIRECTION
33     C      NDATA    NUMBER OF STATIONS WITH DATA USED IN A PARTICULAR
34     C                ITERATION. EXACT NUMBER DEFINED IN SUBROUTINE INITIL.
35     C      NPTS     COUNTER USED IN THE CONVERGENCE TESTING
36     C      RSCAN    RADIUS OF SCAN CIRCLE IN GRID UNITS. EXACT VALUE DEFINED
37     C                IN SUBROUTINE INITIL
38     C      RSQ      SQUARE OF SCAN RADIUS
39     C      STNVAL   ARRAY CONTAINING STATION OBSERVATIONS
40     C      SUMCOR   TEMPORARY STORAGE ARRAY CONTAINING CUMULATIVE CORRECTIONS
41     C                AT EACH GRID POINT WITHIN A SCAN CIRCLE OF THE STATIONS
42     C                DURING AN ITERATION
43     C      SUNWT    TEMPORARY STORAGE ARRAY CONTAINING CUMULATIVE WEIGHTINGS
44     C                AT EACH GRID POINT WITHIN A SCAN CIRCLE OF THE STATIONS
45     C                DURING AN ITERATION
46     C      XCOORD   X-COORDINATE OF A STATION
47     C      YCOORD   Y-COORDINATE OF A STATION
48     C
49     C
50     C
51     C
52     C      DIMENSION XCOORD(NDATA),YCOORD(NDATA),STNVAL(NDATA)
53     C      DIMENSION GRDVAL(IEND,JEND),SUNWT(IEND,JEND),SUMCOR(IEND,JEND)
54     C      DIMENSION SUIFF(25),RSCAN(NSCANS)
55     C      DATA NPTS/0/,ERROR/0/

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56      R(5) = 1
57      C
58      C *****
59      C      INVERT SOR,XI, AND YI ARRAYS TO FORM S,X, AND Y ARRAYS.
60      C      THIS IS DONE SO THAT THE DATA FROM THE OUTER STATIONS WILL
61      C      BE USED FIRST.
62      C *****
63      C
64      DO 10 J=1,NRPTS
65      I=NRPTS - J + 1
66      S(1) = SOR(J)
67      X(1) = XI(J)
68      Y(1) = YI(J)
69      C      PRINT 2,I,X(1),Y(1),S(1)
70      C      2 FORMAT(5X,I5,3F10.1)
71      10 CONTINUE
72      C
73      C *****
74      C      USE A FIELD OF VALUES EQUAL TO AVG AS A FIRST GUESS FIELD
75      C      FOR THE CDC ANALYSIS
76      C *****
77      C
78      DO 20 J=1,JF
79      DO 20 I=1,IF
80      G(I,J)=AVG
81      W(I,J)=0
82      C(I,J)=0
83      20 CONTINUE
84      C
85      C *****
86      C      ITERATE ITMAX TIMES
87      C *****
88      C
89      PRINT 23
90      DO 60 IT=1,ITMAX
91      C      PRINT 23
92      23 FORMAT('1')
93      CALL GRID(N(11),X,Y,S,G,W,C,1,IF,1,JF,1,R(IT),0)
94      PRINT 35,N(IT)
95      35 FORMAT(/11X,'NUMBER OF STATIONS =' ,I3/)
96      GO TO 60
97      C
98      C      PRINT OUT EVERY OTHER GRID VALUE
99      C
100     PRINT 40,(I,I=1,IF,2)
101     40 FORMAT('0 ',3X,23I5,/)
102     DO 45 JJ=1,JF,2
103     J=JF-JJ
104     PRINT 50, J,(G(I,J),I=1,IF,2)
105     45 CONTINUE
106     50 FORMAT(' ',1X,I2,1X,23F5.1)
107     60 CONTINUE
108     RETURN
109     END

```



```

1      SUBROUTINE INITIL(X1,Y1,SOR,C,IF,JF,NRPTS,AVG,SIG)
2      C
3      C
4      C      THIS SUBROUTINE COMPUTES A WIND FIELD FROM 15-MINUTE AVERAGED RAPS WIND
5      C      DATA USING THE OBJECTIVE ANALYSIS PROCEDURE DEVELOPED BY CDC.
6      C      THE VALUES OF N AND R WERE BASED UPON EXPERIMENTATION AND
7      C      INFORMATION PROVIDED BY CDC.
8      C
9      C
10     C
11     C *****
12     C      DICTIONARY OF VARIABLES USED IN INITIL
13     C *****
14     C
15     C
16     C
17     C      AVG      THE AVERAGE VALUE OF THE U OR V COMPONENTS FOR A GIVEN PERIOD
18     C      C        ARRAY STORING THE CUMULATIVE CORRECTIONS FOR THE GRID VALUES
19     C      G        ARRAY STORING THE CALCULATED GRID VALUES
20     C      IF       NUMBER OF GRID POINTS IN THE X DIRECTION
21     C      ITHAX    NUMBER OF ITERATIONS TO BE PERFORMED FOR THE CDC PROCEDURE
22     C      JF       NUMBER OF GRID POINTS IN THE Y DIRECTION
23     C      N        ARRAY STORING NUMBER OF STATIONS TO BE USED IN EACH ITERATION
24     C      NRPTS    MAXIMUM NUMBER OF STATIONS TO BE USED IN ANY ITERATION
25     C      R        ARRAY STORING SIZE OF SCAN RADIUS TO BE USED IN EACH ITERATION
26     C      S        ARRAY STORING STATION NUMBERS IN DESCENDING ORDER
27     C      SIG      STANDARD DEVIATION OF U OR V COMPONENTS
28     C      SOR      ARRAY STORING STATION NUMBERS IN ASCENDING ORDER
29     C      W        ARRAY STORING CUMULATIVE WEIGHTINGS FOR EACH GRID POINT
30     C      X        ARRAY STORING X COORDINATES OF STATIONS IN DESCENDING ORDER
31     C      X1       ARRAY STORING X COORDINATES OF STATIONS IN ASCENDING ORDER
32     C      Y        ARRAY STORING Y COORDINATES OF STATIONS IN DESCENDING ORDER
33     C      Y1       ARRAY STORING Y COORDINATES OF STATIONS IN ASCENDING ORDER
34     C
35     C
36     C
37     C
38     C      DIMENSION X(25),Y(25),S(25),G(IF,JF),W(46,46),C(46,46),R(6),N(6)
39     C      *,SOR(25),X1(25),Y1(25)
40     C      DATA ITHAX/5/
41     C
42     C *****
43     C      DEFINE THE NUMBER OF STATIONS AND THE SIZE OF THE SCAN RADIUS
44     C      TO BE USED IN EACH ITERATION
45     C *****
46     C
47     C      N(1)=7
48     C      N(2)=12
49     C      N(3)=NRPTS
50     C      N(4)=NRPTS
51     C      N(5)=NRPTS
52     C      R(1)=46
53     C      R(2)=20
54     C      R(3)= 10
55     C      R(4)= 5

```

```

56
57      DO 10 I=ISTART,IEND
58      DO 10 J=JSTART,JEND
59      SUMWT(I,J)=0
60      10  SUMCOR(I,J)=0
61      ITER=0
62      11  ITER=ITER+1
63      IF(ITER.GT.NSCANS)GO TO 99
64      RSQ=RSCAN(ITER)*RSCAN(ITER)
65      ERROR=0
66      NPTS=0
67      NREJ=0
68      C
69      C *****
70      C   CALCULATE THE CORRECTIONS AT EACH GRID POINT WITHIN A SCAN
71      C   CIRCLE CENTERED AT THE STATIONS. THE CORRECTIONS ARE BASED
72      C   UPON THE WEIGHTED DIFFERENCES BETWEEN THE OBSERVATION AT THE
73      C   STATIONS AND THE INTERPOLATED VALUE ON THE FIELD.
74      C *****
75      C
76      DO 50 NDT=1,NDATA
77      SDIFF(NDT)=99.
78      IF(STNVAL(NDT).EQ.99.0)GO TO 50
79      C
80      C   FIND INDICES OF NEAREST GRID POINT IN DIRECTION OF (1,1)
81      C
82      I=XCOORD(NDT)+1.
83      J=YCOORD(NDT)+1.
84      C
85      C   FIND X AND Y DISTANCE FROM GRID POINT (I,J)
86      C
87      P=XCOORD(NDT)-(I-1)
88      Q=YCOORD(NDT)-(J-1)
89      C
90      C   USE FOUR POINT BILINEAR FORMULA TO INTERPOLATE A VALUE AT
91      C   THE STATION LOCATION FROM FOUR SURROUNDING GRID POINTS.
92      C   IF A VALUE CANNOT BE INTERPOLATED, THE STATION IS SKIPPED.
93      C
94      IF(I.LT.ISTART)GO TO 50
95      IF(I+1.GT.IEND)GO TO 50
96      IF(J.LT.JSTART)GO TO 50
97      IF(J+1.GT.JEND)GO TO 50
98      STNINT=GRDVAL(I,J)*(1.-P)*(1.-Q)
99      1   +GRDVAL(I+1,J)*P*(1.-Q)
100     2   +GRDVAL(I,J+1)*Q*(1.-P)
101     3   +GRDVAL(I+1,J+1)*P*Q
102      C
103      C   FIND THE DIFFERENCE BETWEEN THE INTERPOLATED AND OBSERVED
104      C   VALUES AT THE STATIONS.
105      C
106      DIFF=STNVAL(NDT)-STNINT
107      SDIFF(NDT)=DIFF
108      C
109      C   THE MEAN SQUARED DIFFERENCE IS USED BELOW
110      C
111      ERROR=DIFF*DIFF+ERROR
112      NPTS=NPTS+1

```

```

113 C
114 C A CORRECTION IS NOW COMPUTED FOR EACH GRID POINT WITHIN A CIRCLE
115 C OF RADIUS RSCAN(ITER) CENTERED AT THE STATIONS.
116 C
117 INDEX1=XCOORD(NDT)+1.-RSCAN(ITER)
118 IF(INDEX1.LT.ISTART)INDEX1=ISTART
119 INDEX2=XCOORD(NDT)+1.+RSCAN(ITER)
120 IF(INDEX2.GT.IEND)INDEX2=IEND
121 INDEX3=YCOORD(NDT)+1.-RSCAN(ITER)
122 IF(INDEX3.LT.JSTART)INDEX3=JSTART
123 INDEX4=YCOORD(NDT)+1.+RSCAN(ITER)
124 IF(INDEX4.GT.JEND)INDEX4=JEND
125
126 DO 30 M=INDEX1,INDEX2
127 DO 30 N=INDEX3,INDEX4
128 C
129 C FIND DISTANCE SQUARED FROM STATION TO GRID POINT (M,N).
130 C
131 DX=XCOORD(NDT)-(M-1)
132 DY=YCOORD(NDT)-(N-1)
133 DSQ=DX*DX+DY*DY
134 C
135 C GENERATE WEIGHT. IF XNUM IS NEGATIVE, GRID
136 C POINT (M,N) IS OUTSIDE THE SCAN CIRCLE.
137 C
138 XNUM=RSQ-DSQ
139 IF(XNUM.L1.0)GO TO 30
140 XDEN=RSQ+DSQ
141 WT=XNUM/XDEN
142 WT = WT * WT
143 WT = WT * WT
144 C
145 C CORRECTIONS ARE NOT APPLIED NOW SINCE A GIVEN
146 C GRID POINT MAY GET CORRECTIONS FROM SEVERAL DATA POINTS.
147 C
148 SUMWT(M,N)=SUMWT(M,N)+WT
149 SUMCOR(M,N)=SUMCOR(M,N)+WT*DIFF
150 30 CONTINUE
151 50 CONTINUE
152 C
153 C END OF LOOP FOR DATA POINTS.
154 C
155 RMS =0
156 CORMAX =0
157 I101 =0
158 IMAX =0
159 JMAX =0
160 C
161 C *****
162 C APPLY THE CUMULATIVE CORRECTIONS TO THE GRID POINTS.
163 C *****
164 C
165 DO 70 M=ISTART,IEND
166 DO 70 N=JSTART,JEND
167 IF(SUMWT(M,N).EQ.0)GO TO 70
168 GRDVAL(M,N)=GRDVAL(M,N)+SUMCOR(M,N)/SUMWT(M,N)
169 COR=SUMCOR(M,N)/SUMWT(M,N)

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170      RMS=COR*COR+RMS
171      ITOT=ITOT+1
172      IF(ABS(COR).LE.ABS(CORMAX))GO TO 69
173      CORMAX=COR
174      IMAX=M
175      JMAX=N
176 69    CONTINUE
177      SUMWT(M,N)=0
178      SUMCOR(M,N)=0
179 70    CONTINUE
180  C
181  C      IF THE MEAN SQUARED CORRECTION IS SMALL ENOUGH, STOP ITERATING.
182  C
183      ERROR=ERROR/NPTS
184      PRINT 75,ITER,ERROR,RSCAN(ITER)
185 75    FORMAT(5X,'      FOR ITERATION',I3,' THE MEAN SQUARED'
186      1' DIFFERENCE AT THE STATIONS IS',F8.2,5X,'SCAN CIRCLE',
187      2' RADIUS =',F8.2)
188      IF(ITOT.GT.0)RMS=SQRT(RMS/ITOT)
189      PRINT 80,RMS,CORMAX,IMAX,JMAX
190 80    FORMAT(/11X,'RMS CHANGE AT GRID POINTS IS',F8.3,5X,
191      1'MAXIMUM CHANGE IS',F7.2,' AT GRID POINT',2I5)
192      IF(ERROR.GT.CRIT)GO TO 11
193
194 99    RETURN
195      END

```

```

1      SUBROUTINE UVCMP1(U,V,WDA,WSP)
2      DEG = 180. / 3.141592654
3      IF(U .LE. 0. .AND. V .LE. 0.) GO TO 5
4      IF(U .LT. 0. .AND. V .GE. 0.) GO TO 10
5      IF(U .GE. 0. .AND. V .GT. 0.) GO TO 15
6      IF(U .GT. 0. .AND. V .LE. 0.) GO TO 20
7      5 WDA = ATAN(U/V)*DEG
8      GO TO 90
9      10 WDA = -ATAN(V/U)*DEG + 90.
10     GO TO 90
11     15 WDA = ATAN(U/V)*DEG + 180.
12     GO TO 90
13     20 WDA = -ATAN(V/U)*DEG + 270.
14     90 WSP = SQRT(U*U+V*V)
15     RETURN
16     END

```

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