

UPCONING OF A SALT-WATER/FRESH-WATER INTERFACE BELOW
A PUMPING WELL

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UPCONING OF A SALT-WATER/FRESH-WATER
INTERFACE BELOW A PUMPING WELL

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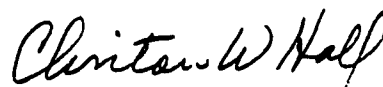
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FOREWORD

EPA is charged by Congress to protect the Nation's land, air, and water systems. Under a mandate of national environmental laws focused on air and water quality, solid waste management and the control of toxic substances, pesticides, noise, and radiation, the Agency strives to formulate and implement actions which lead to a compatible balance between human activities and the ability of natural systems to support and nurture life.

The Robert S. Kerr Environmental Research Laboratory is the Agency's center of expertise for investigation of the soil and subsurface environment. Personnel at the Laboratory are responsible for management of research programs to: (a) determine the fate, transport and transformation rates of pollutants in the soil, the unsaturated zone and the saturated zones of the subsurface environment; (b) define the processes to be used in characterizing the soil and subsurface environment as a receptor of pollutants; (c) develop techniques for predicting the effect of pollutants on ground water, soil and indigenous organisms; and (d) define and demonstrate the applicability and limitations of using natural processes, indigenous to the soil and subsurface environment, for the protection of this resource.

This project was initiated to develop an interactive computer model which could be utilized to predict the impact of density gradients on water flow. The model should be useful in regard to salt water intrusion and salt water injection problems. This model assumes idealized conditions of a homogeneous isotropic media. Care should be utilized if there is significant heterogeneity in the aquifer.



Clinton W. Hall
Director
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ABSTRACT

Analytical solutions for the upconing of an abrupt salt-water/fresh-water interface beneath a pumping well and for the concentration profile across a moving interface are developed for two types of upconing problems. The first considers the position of the interface and the salinity of the pumped water for a specified pumping rate. The second type of problem addresses the pumping schedules to prevent salinization of a well or to reach a predetermined salinity in the pumped water.

An interactive Fortran computer code has been developed to obtain solutions to both types of problems. The user is provided with options to modify the definition of a given problem, and, therefore, can gain some insight into the effects of geometry and physical properties on the rate and extent of upconing and the salinization of a well.

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INTRODUCTION

Relatively simple analytical models can often be used to solve ground-water contamination problems, depending upon the complexity of the system and the availability of field data. Analytical models can also be used to gain some insight to the expected behavior of a complex system before progressing to the application of more sophisticated numerical models. In general, relatively few input parameters are required to define a problem using an analytical model and numerical results can be calculated in a few seconds. Analytical models are well suited for interactive use, and in some instances can be programmed on hand-held calculators.

This report presents an analytical solution for the upconing of an abrupt salt-water/fresh-water interface below a pumping well. Dispersion phenomena arising from the displacement of a moving interface, or a finite transition zone between the invading and displaced fluids, can be superimposed on the analytical solution for the position of an abrupt interface. An interactive Fortran computer code has been developed which enables the user to modify input parameters and to control the computational sequence. This interactive approach enables the user to gain insight into the effects of geometry and physical properties on the rate and extent of upconing and salinization of a well.

SECTION I

Mathematical Development

McWhorter (1972) presented the equations which describe the flow in saturated aquifers which are underlain by a zone of saline water and pointed out the difficulties in obtaining solutions to these problems. The complexity of the flow phenomenon has led many investigators to idealize the system as a fresh-water zone separated from an underlying salt-water zone by a sharp interface. In other words, the two fluids are assumed to be immiscible. Schmorak and Mercado (1969) followed this approach and accounted for the mixing of the two fluids by superimposing the effects of dispersion on the transient solution for the position of an abrupt interface.

Upconing of an Abrupt Interface

The following discussion is based on the studies of Bear and Dagan as reported by Schmorak and Mercado (1969). The basic assumptions underlying the theoretical development are: (1) the porous medium is homogeneous and nondeformable, (2) the two fluids are incompressible, immiscible, and separated by an abrupt interface (a geometric surface), and (3) the flow obeys Darcy's law. The non-linear boundary condition along the interface between the two fluids constitutes the major difficulty with the immiscible formulation of the problem. Bear and Dagan used the method of small perturbations to obtain an approximate solution for the position of the interface which served as a tool for obtaining analytical solutions for cases involving small deviations from an initially steady interface.

For the case of upconing beneath a pumping well partially penetrating a relatively thick confined aquifer as shown in Figure 1, Schmorak and

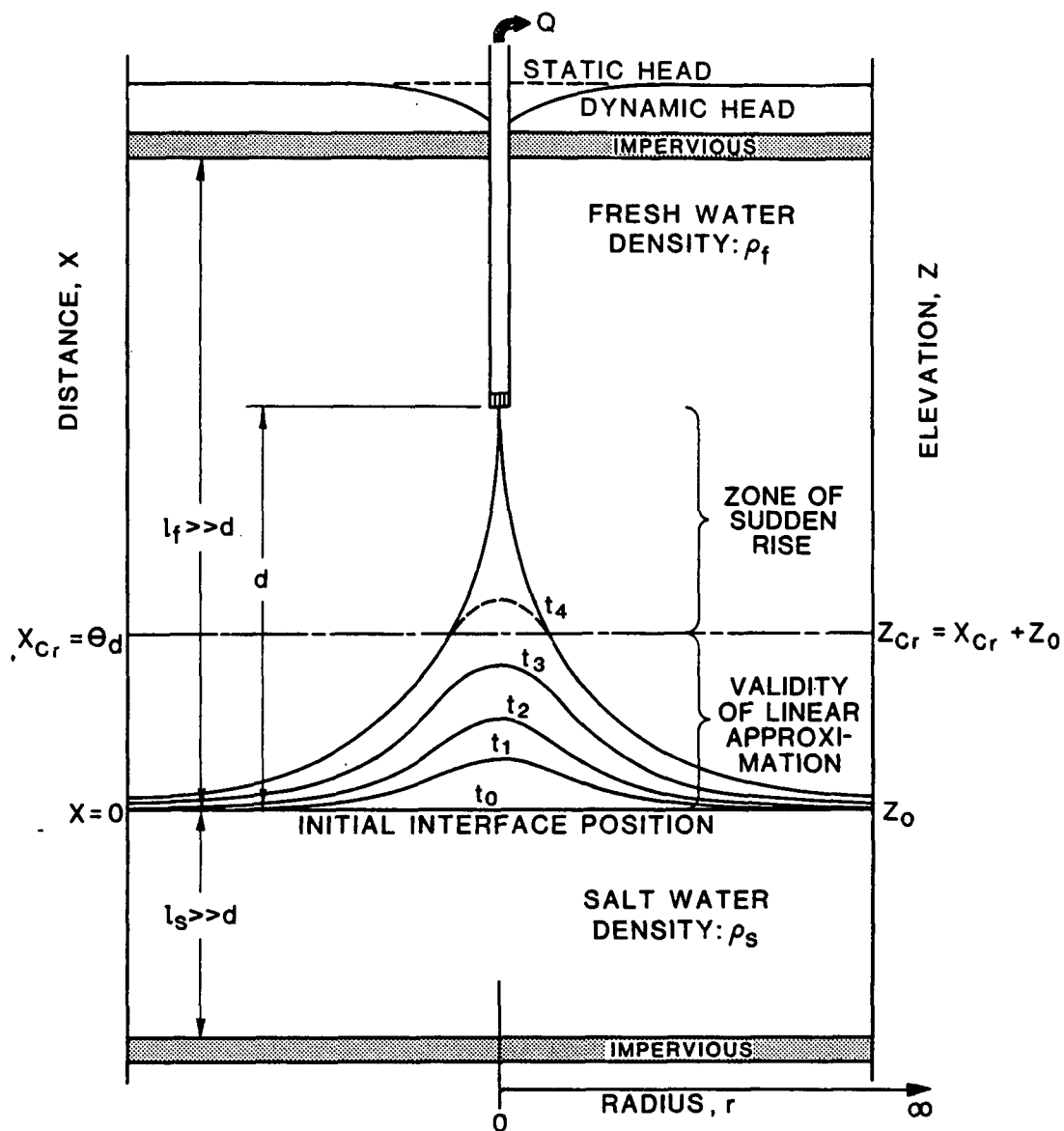


Figure 1. Upconing of an abrupt interface below a pumping well.

Mercado (1969) presented Bear and Dagan's solution for the position of the interface as a function of time and radial distance from the pumping well as

$$X(r,t) = \frac{Q}{2\pi(\Delta\rho/\rho)K_x d} \left[\frac{1}{(1 + R^2)^{1/2}} - \frac{1}{\left[(1 + \tau)^2 + R^2 \right]^{1/2}} \right] \quad (1)$$

where R and τ are dimensionless distance and time parameters defined by

$$R = \frac{r}{d} \left(\frac{K_z}{K_x} \right)^{1/2} \quad (2)$$

and

$$\tau = \frac{(\Delta\rho/\rho)K_z}{2\theta d} t \quad (3)$$

Other notations are defined as follows (also refer to Figure 1):

d	distance from the bottom of the well to the initial interface elevation (L)
K_x, K_z	horizontal and vertical permeabilities, respectively (L/t)
Q	well pumping rate (L ³ /t)
r	radial distance from well axis (L)
t	time elapsed since start of pumping (t)
X	rise of the interface above its initial position (L)
$\Delta\rho/\rho$	dimensionless density difference between the two fluids, $(\rho_s - \rho_f)/\rho_f$
θ	porosity of the aquifer.

Application of the method of small perturbations restricts changes in the interface elevation to relatively small values. In terms of the physical problem, this restriction implies $d \ll l_f$ and $d \ll l_s$. Although the governing differential equations have been formulated for a confined aquifer, the results can be applied to unconfined systems if the drawdown is negligible compared to the saturated thickness of the fresh-water zone.

The linear relationship, Equation 1, between the rise of the interface and the pumping rate is limited to a certain "critical rise," X_{cr} . This limitation arises from linear approximation of the boundary conditions. As the interface approaches this critical rise, the rate of rise increases. Above the critical rise the interface reaches the pumping well with a sudden jump. Muskat (1946) defines the zone of accelerated rise for $X/d > 0.48$ and the critical rise within the limits of $X/d \sim 0.60$ to 0.75 . Schmorak and Mercado (1966) recommend application of the linear approximation for $X/d < \sim 0.5$. Sahni (1972) investigated the zone of instability of the interface using both numerical and physical models and recommended design criteria for skimming wells.

An abrupt interface such that (1) salinization of the pumping well occurs only for $X > X_{cr} = fd$ where f is the fractional critical rise, and (2) Equation 1 is valid for $0 \leq X \leq X_{cr}$ will be assumed in this report. Thus, the maximum permissible pumping rate which will ensure salt-free water can be obtained from Equation 1.

For $r = 0$ and $t \rightarrow \infty$

$$X(0, \infty) = \frac{Q}{2\pi d(\Delta\rho/\rho)K_x} \quad (4)$$

and

$$Q_{max} = 2\theta d(\Delta\rho/\rho)K_x X_{cr} \quad (5)$$

For a decaying mound, an imaginary recharge well is superimposed at time $t = t^*$ corresponding to the end of the pumping period, and for $t > t^*$

$$X(r, t) = \frac{Q}{2\pi(\Delta\rho/\rho)K_x d} \left[\frac{1}{\left[(1+\tau_1)^2 + R^2 \right]^{1/2}} - \frac{1}{\left[(1+\tau)^2 + R^2 \right]^{1/2}} \right] \quad (6)$$

where

$$\tau_1 = \frac{(\Delta\rho/\rho)K_z}{2\theta d} (t-t^*) \quad (7)$$

Values of R and τ are evaluated using Equations 2 and 3 respectively.

Dispersion

The upconing process as treated above assumes that the two fluids are immiscible and that the interface between them is abrupt. Actually, the interface is diffuse and a transition zone exists between the two fluids in which the concentration varies from the concentration in one fluid to the concentration in the other fluid over a finite distance. This transition zone is related to dispersion processes which alter the concentration profile across the moving interface.

Bear and Todd (1960) approximated the concentration profile as a function of position, X; the "interface" position, \bar{X} ; the equivalent total distance the interface is displaced, $|\Delta\bar{X}|$, independent of direction; and the dispersivity, D_m . The correlation is given by

$$\epsilon(X) = \frac{1}{2} \text{ERFC} \left(\frac{X-\bar{X}}{2(D_m|\Delta\bar{X}|)^{1/2}} \right) \quad (8)$$

where $\epsilon(X)$ is a dimensionless, or relative, concentration defined as

$$\epsilon(X) = \frac{C - C_b}{C_x - C_b} \quad (9)$$

C = measured concentration at X

C_s = concentration of the invading fluid

C_b = background concentration of the displaced fluid.

Now, Equation 9 is a normal distribution function with a mean \bar{X} and a standard deviation

$$\sigma = (2D_m|\Delta\bar{X}|)^{1/2} \quad (10)$$

or

$$P_r \{X \geq x\} = \frac{1}{\sigma(2\pi)^{1/2}} \int_x^{\infty} \text{EXP} \left(-\frac{(X-\bar{X})^2}{2\sigma^2} \right) dx \quad (11)$$

From the definition of the error function,

$$P_r \{X \geq x\} = \frac{1}{2} \text{ERFC} \left(\frac{X-\bar{X}}{\sigma \sqrt{2}} \right) \quad (12)$$

The two-parameter distribution is completely defined once the mean, \bar{X} , and standard deviation, σ , are known.

The mean of the distribution is assumed to be the rise of the interface as determined from Equation 1, or

$$\bar{X} = X|_{\epsilon=0.5} = X(r,t) \quad (13)$$

The standard deviation is defined as

$$2\sigma = \left(X|_{\epsilon=0.841} - X|_{\epsilon=0.159} \right) \quad (14)$$

Now, the width of the transition zone is a function of the total distance traveled, $|\Delta\bar{X}|$, (independent of direction) and the dispersivity as given by Equation 10, or

$$2\sigma = 2(2D_m |\Delta\bar{X}|)^{1/2} \quad (15)$$

For an interface with an initial transition width, $2\sigma_0$, when raised by a distance, $\Delta\bar{X}$,

$$\sigma_1 = \left(\sigma_0^2 + (2D_m |\Delta\bar{X}|) \right)^{1/2} \quad (16)$$

The concentration distribution function then becomes

$$\epsilon(X) = \frac{1}{2} \text{ERFC} \left(\frac{X-\bar{X}}{\sigma_1 \sqrt{2}} \right) \quad (17)$$

or

$$\epsilon(X) = \frac{1}{2} \text{ERFC} \left(\frac{X-\bar{X}}{\left(2\sigma_0^2 + 4D_m |\Delta\bar{X}| \right)^{1/2}} \right) \quad (18)$$

Two important points should be noted concerning the preceding discussion of dispersion. First, the "initial width" of the transition zone has been defined as two standard deviations of the dimensionless concentration distribution. This definition has been adopted for convenience and serves to define the standard deviation of the concentration distribution across the initial transition zone. Secondly, the dispersion concept should be limited to the zone below the critical depth. This point will be considered in more detail in the following paragraphs.

Superposition of Dispersion on the Upconing of an Abrupt Interface

The position of the interface as a function of time and radial distance from the well is evaluated using Equation 1, which assumes an abrupt interface between the two fluids. This elevation is assumed to correspond to $X|_{\epsilon=0.5}$, or the mean of the concentration distribution across the transition zone. In other words,

$$\bar{X} = X(r,t) = \frac{Q}{2\pi(\Delta\rho/\rho)K_x d} \left(\frac{1}{\left[(1+\tau_1)^2 + R^2 \right]^{1/2}} - \frac{1}{\left[(1+\tau)^2 + R^2 \right]^{1/2}} \right) \quad (6)$$

assuming an abrupt interface. The effect of dispersion arising from the displacement of the interface by a distance

$$|\overline{\Delta X}| = |X(r,t \leq t^*)| + |X(r,t > t^*)| \quad (20)$$

is superimposed to estimate the concentration distribution across the interface using Equation 18, or

$$\epsilon(X) = \frac{1}{2} \text{ERFC} \left(\frac{X - \bar{X}}{\left[2\sigma_o^2 + 4D_m |\overline{\Delta X}| \right]^{1/2}} \right) \quad (18)$$

The only difficulties in the approach occur for $\epsilon(X) = 0.0$ and $\epsilon(X) = 1.0$.

Since

$$\epsilon(X) = 0 \text{ for } X \rightarrow \infty$$

and

$$\varepsilon(X) = 1.0 \text{ for } X \rightarrow 0 \quad (22)$$

the transition zone would have an infinite width in theory. To overcome this physical impossibility, the width of the transition zone is arbitrarily set at five standard deviations. This range includes approximately 99 percent of the area under the concentration distribution curve. Thus

$$\varepsilon(X) \approx 0 \text{ for } X = \bar{X} + 2.5 \sigma_1 \quad (23)$$

and

$$\varepsilon(X) \approx 1 \text{ for } X = \bar{X} - 2.5 \sigma_1 \quad (24)$$

Note that these limits differ from those used to define the "initial width" of the transition zone defined by Equation 14, or

$$2\sigma_0 = \left(X|_{\varepsilon=0.841} - X|_{\varepsilon=0.159} \right) \quad (25)$$

Concentration in Pumped Water

The increase in concentration, or salinization, of pumped water is probably due to the intrusion of invading fluid above the critical depth. Data for two pumping tests on a coastal aquifer in the Ashqelon area of Israel indicated that the increase in salinity of the pumped water was approximately proportional to the average salinity above the critical depth (Schmorak and Mercado, 1969).

Previous discussion has emphasized that the linear approximation for the interface elevation is limited to elevations below the critical elevation and that the dispersion concept should be limited to the zone below the critical depth. The complex mixing and flow phenomena above the critical depth, near the well screen, and within the well pipe are approximated empirically using the approach followed by Schmorak and Mercado (1969).

The average dimensionless concentration of the transition zone above the critical rise, $\bar{\varepsilon}(X > X_{cr})$, is approximated as one-half the concentration at the critical depth, or

$$\varepsilon(X > X_{cr}) = 0.5 \varepsilon(X_{cr}) \quad (26)$$

The concentration in the pumped water, ε_w , is determined from dilution of the average transition-zone concentration above the critical depth with displaced fluid, or

$$\varepsilon_w = \phi \bar{\varepsilon}(X > X_{cr}) \quad (27)$$

where ϕ is an interception coefficient, or the fraction of transition zone fluid in the total volume pumped.

SECTION II

Applications

Two types of upconing problems are considered. The first involves the description of the expected interface elevation and the salinity of the pumped water as a function of time for a given pumping rate. The second problem addresses the maximum rate at which a well can be pumped without exceeding a specified salinity in the pumped water. Both types of problems are discussed in the following paragraphs.

Case I - Estimation of Interface Elevations for a Given Pumping Rate

Case I problems are solved in a fairly straight-forward manner. Once the physical properties of the aquifer and the initial conditions have been specified, Equation 1 or Equation 6 is solved for the position of the abrupt interface, or the mean of the transition zone, i.e.,

$$X(r,t) = X|_{\epsilon=0.5} = \bar{X} \quad (13)$$

In terms of elevations,

$$Z(r,t) = X(r,t) + Z_0 \quad (28)$$

where Z_0 is the initial interface elevation.

The concentration profile across the transition zone is evaluated using Equation 18. The salinity of the pumped water is determined from the dilution of the average transition zone salinity above the critical rise. From Equations 26 and 27

$$\epsilon_w = 0.5 \phi \epsilon(X_{cr}) \quad (29)$$

and from the definition of dimensionless concentration (Equation 9)

$$C_w = \epsilon_w (C_s - C_b) + C_b \quad (30)$$

where C_w is the concentration in the pumped water.

Case II - Estimation the Maximum Permissible Pumping Rate to Prevent Salinization of a Well

Case II problems present some difficulty as the pumping rate, Q , is unknown. Thus, the elevation of the interface, \bar{X} , and the total displacement of the interface, $|\Delta\bar{X}|$, are also unknown. Equation 18 must be solved for the maximum permissible rise in interface elevation such that

$$\epsilon(X_{cr}=fd) \leq \epsilon_{max} \quad (31)$$

where

$$\epsilon_{max} = \frac{\epsilon_w}{0.5\phi} \quad (32)$$

Assuming a constant, steady pumping rate the total displacement of the interface will be equal to the rise of the interface or

$$|\Delta\bar{X}| = \bar{X}$$

and Equation 18 can be written as

$$\epsilon_{max} = \frac{1}{2} \text{ERFC} \left[\frac{X_{cr} - \bar{X}}{\left[\frac{2}{2\sigma_o + 4D_m \bar{X}} \right]^{1/2}} \right] \quad (33)$$

Equation 33 must be solved for \bar{X} using trial-and-error procedures. The maximum permissible rise in the interface elevation,

$$X_{max} \leq X_{cr}=fd \quad (34)$$

is then corrected for the concentration profile as

$$X_{max}^* = X_{max} - (fd - \bar{X}) \quad (35)$$

and

$$Z_{max}^* = X_{max}^* + Z_o \quad (36)$$

The maximum permissible steady-state pumping rate is then obtained using Equation 5, or

$$Q_{\max}^* = 2\pi d(\Delta\rho/\rho)K_z X_{\max}^* \quad (37)$$

where X_{\max}^* depends only upon the critical rise and the dispersion pattern.

The time required to reach a predetermined salinity in the well can be estimated by rewriting Equation 1 as

$$t(C_w) = \frac{2\theta d}{(\Delta\rho/\rho)K_z} \left[\frac{1}{1 - \left(2\pi(\Delta\rho/\rho)K_z d X_{\max}^* \right) / Q} - 1 \right] \quad (38)$$

Substituting Equation 37 into Equation 38 yields

$$t(C_w) = \frac{2\theta d}{(\Delta\rho/\rho)K_z} \left[\frac{1}{1 - Q_{\max}^*/Q} - 1 \right] \quad (39)$$

which can be used to estimate the time required to reach a predetermined salinity in the pumped water for pumping rates, Q , greater than the maximum steady-state pumping rate, Q_{\max}^* .

An interactive computational code has been developed to calculate interface elevations, and concentrations for both Case I and Case II problems using the approach described above. The computer program is discussed in Section IV of this report.

Example Problem - Upconing Below a Coastal Collector Well

The application of the analytical model will be demonstrated using the field data for Test B on the coastal collector well Semadar 1 in the Ashqelon area of Israel (Schmorak and Mercado, 1969). Test B consisted of pumping Semadar 1 at a rate of $348 \text{ m}^3/\text{day}$ for a period of 84 days. The upconing and decay of the salt-water/fresh-water interface were monitored by measuring the

TABLE 1

Parameters for Semadar 1 - Test B

Fresh-water density, ρ_f	1.00 g/cm ³
Salt-water density, ρ_s	1.03 g/cm ³
Porosity, θ	0.33
Horizontal permeability, K_x	14.7 m/day
Vertical permeability, K_z	14.7 m/day
Initial interface elevation, Z_o	-30.75 m MSL
Distance from bottom of well to initial interface, d	15.5 m
Fractional critical rise, f	0.4
Chloride concentration in salt water, C_s	22,000. ppm Cl
Chloride concentration in fresh water, C_b	145. ppm Cl
Dispersivity, D_m	0.5 m
Initial width of transition zone, $2\sigma_o$	3.5 m
Interception coefficient, ϕ	0.08
Pumping rate, Q	348. m ³ /dy
Pumping period, t^*	84. dy
Observation wells:	

Identification	Radius, m
T-2	4.5
T-3	12.4
T-4	16.7
T-5	33.9

salinity profiles in four observation wells. Samples of the pumped water were collected periodically and analyzed for chlorides. The properties of the fluids and the aquifer as estimated by Schmorak and Mercado are summarized in Table 1.

Program UPCONE was used to calculate the transient interface elevations and chloride concentrations in the pumped water. The input data dialog and printed results for this problem are presented in Appendix D.

The predicted and observed interface elevations after 16, 57, and 84 days of pumping are shown in Figure 2. The observed interface elevations correspond to elevations for a 50 percent relative concentration of sea water, or

$$\epsilon = \frac{C - C_b}{C_s - C_b} = 0.5$$

The predicted and observed interface elevations match fairly well with the exception of the values for observation well T-2. Well T-2 is located 4.5 meters from the pumping well and penetrates to an elevation of 31.10 meters below MSL. However, this well is screened to an elevation of only 29.02 meters below MSL, and Schmorak and Mercado (1969) indicate that saline water was entrapped at the bottom of the well from a previous pumping test. The predicted rise of the interface at well T-2 also approaches the critical elevation for a fractional critical rise of 0.4. Thus, the observed interface elevation could be in a zone of accelerated rise. Finally, the reported concentration gradients were very steep in well T-2, and small errors in concentration measurements could lead to large errors in estimating the position of the interface.

The predicted upconing and recovery curves for each of the four observation wells are shown in Figure 3. With the exception of well T-2 the

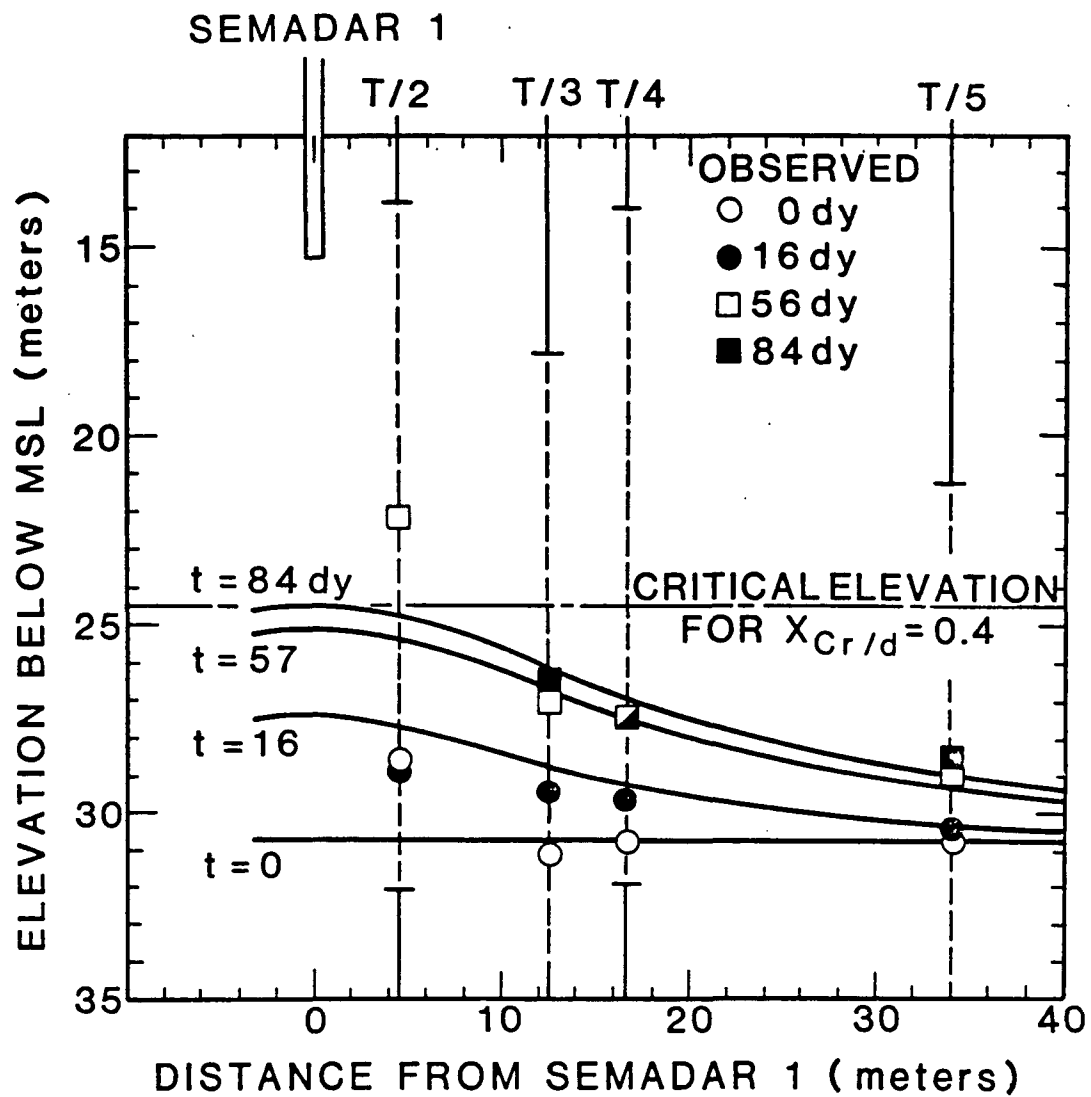


Figure 2. Predicted and observed interface elevations for Test B of Semadar 1.

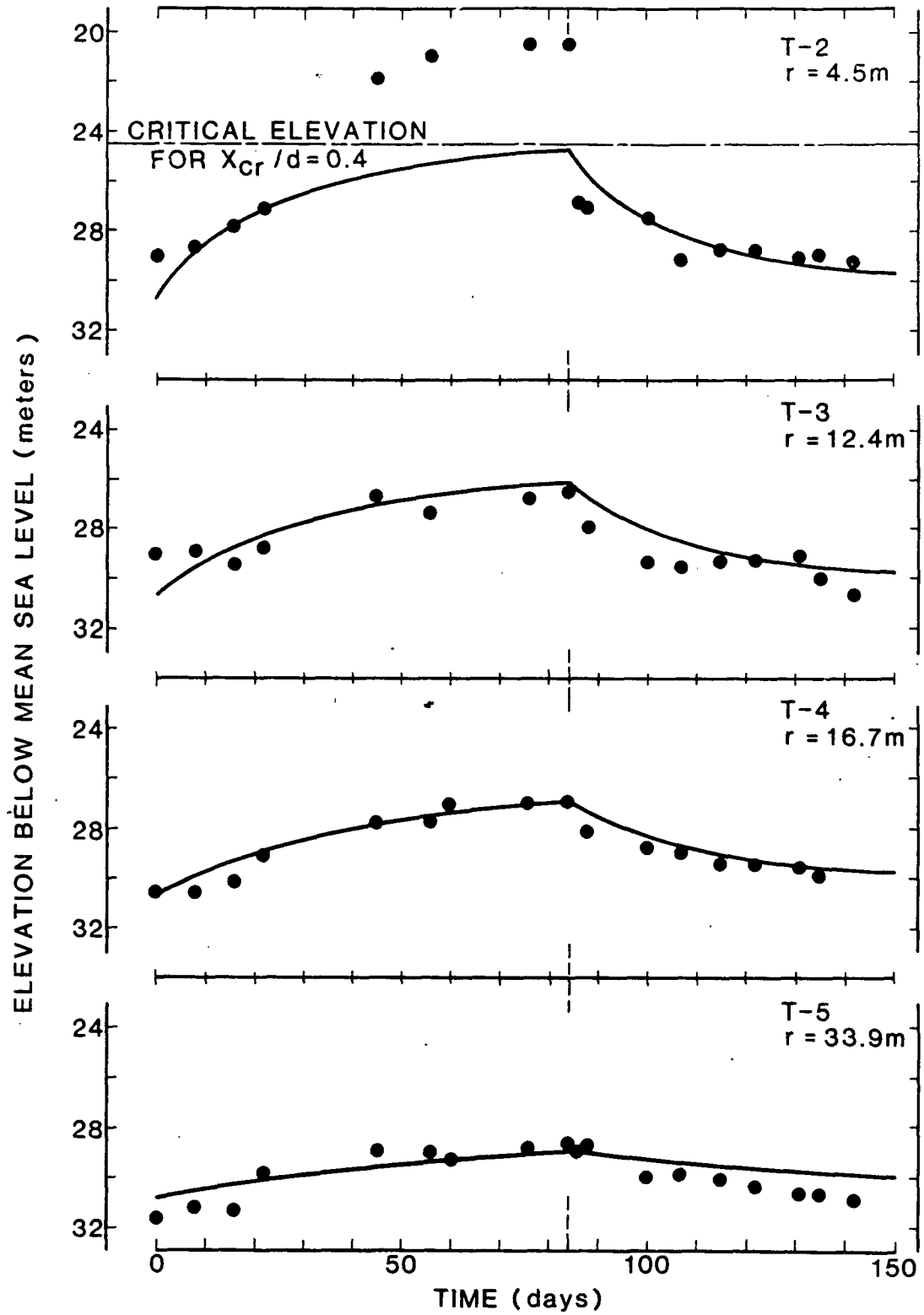


Figure 3. Predicted and observed upconing and recovery curves for Test B of Semadar 1.

predicted upconing curves follow the observed interface elevations fairly well. The recession curves for all four observation wells are also in fair agreement with the field data.

Initial observed relative concentrations for wells T-3, T-4, and T-5 are plotted on Figures 4a and 4b. The predicted concentration profile across the transition zone using an initial transition zone width, $2\sigma_0$, of 3.5 meters is also shown. This value represents an average of the widths of the transition zones at the three observation wells.

The parameters listed in Table 1 were used to predict the concentration of chlorides in the pumped water as a function of time. The results of the simulation are summarized in Figure 5 and agree very well with the observed values.

No effort has been made in this report to "optimize" model input parameters or to quantify the "goodness of fit" between observed and predicted values of elevations, concentration profiles, or salinity of the pumped water. However, a qualitative comparison of the predicted and observed values as shown in Figures 2, 3, and 5 indicate that the assumptions incorporated in the analytical model approach the field conditions.

Program UPCONE was also used to develop salinity/maximum pumping rate relationships and salinity/time relationships for Semadar 1. These relationships correspond to Case II types of problems. The corrected critical interface elevations, Z_{\max}^* , and maximum steady-state pumping rates, Q_{\max}^* , for several values of predetermined salinity in the pumped water are presented in Table 2. The time required to reach the specified salinity in the pumped water were also calculated for two optional pumping rates. These pumping rates correspond to Test A and Test B of Semadar 1.

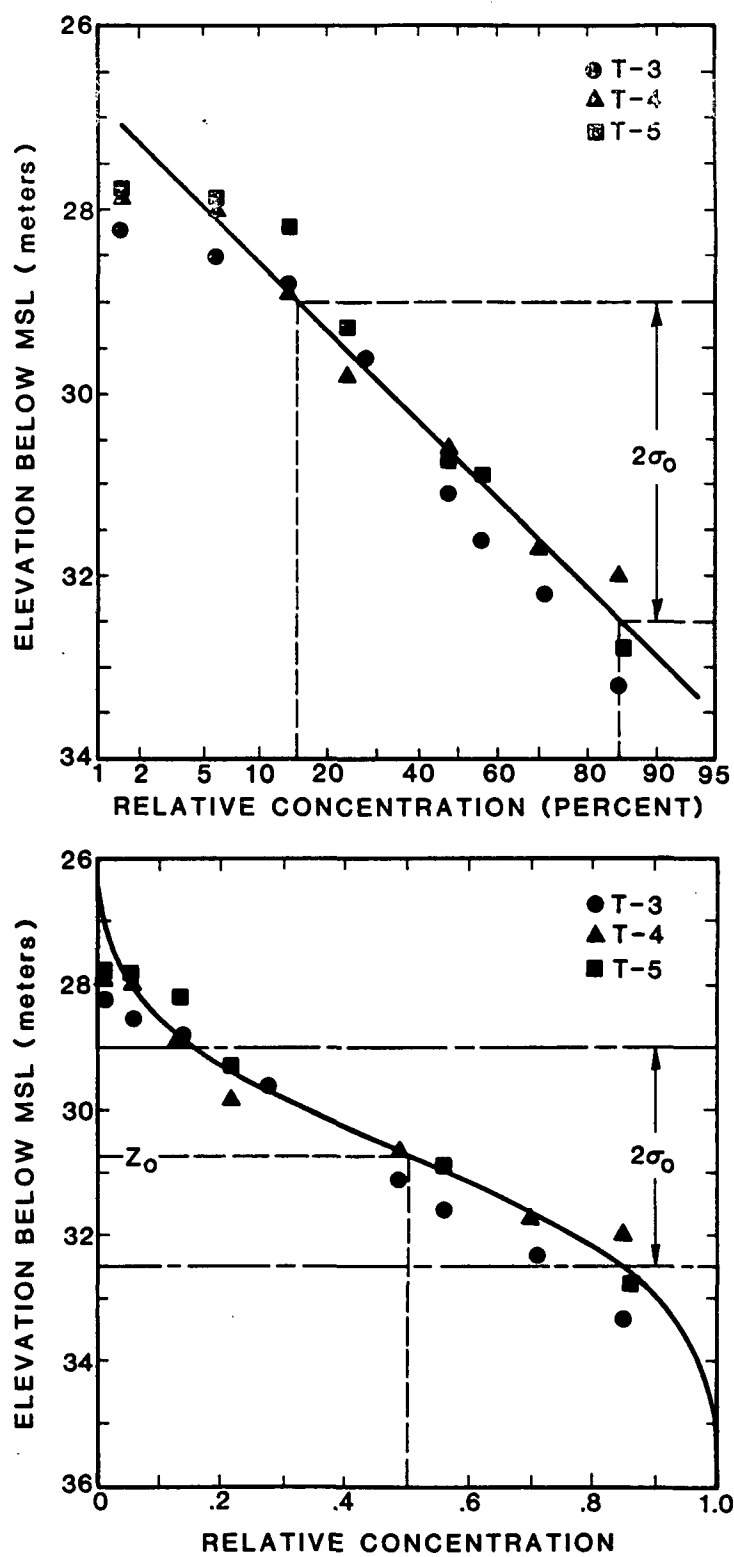


Figure 4. Concentration profile across initial transition zone.
 (a) Relative concentration on probability scale.
 (b) Relative concentration on arithmetic scale.

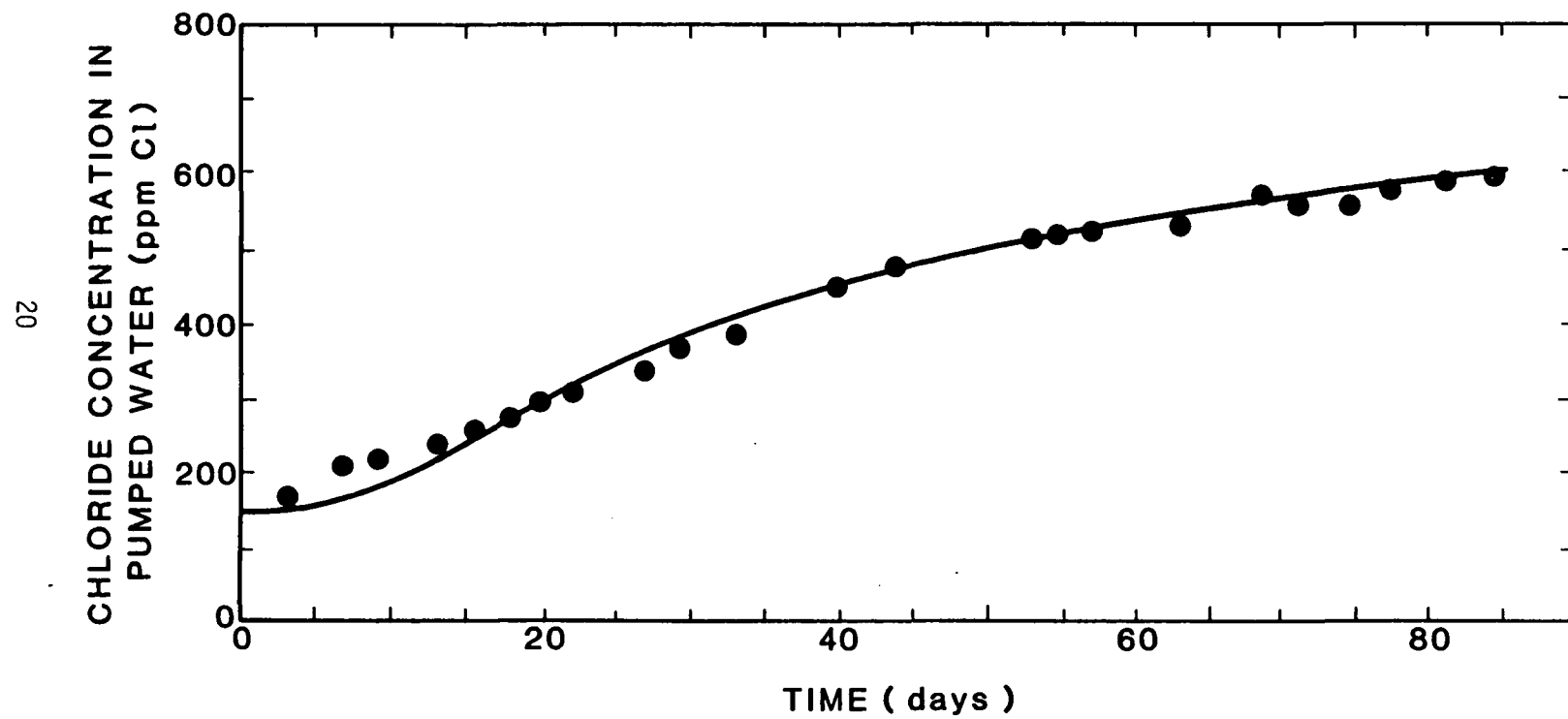


Figure 5. Predicted and observed chloride concentrations in pumped water for Test B on Semadar 1.

TABLE 2

Salinity/Maximum Pumping Rate and Salinity/Time

Relationships For Semadar 1 ($X_{cr} = 0.4d$)

	Relative Concentration of Salt Water (Dimensionless)	Chloride Concentration In Pumped Water (ppm CL)	X_{max}^* (meters)	Q_{max}^* (m ³ /day)	Time	
					Test A $Q = 575 \text{ m}^3/\text{day}$ (days)	Test B $Q = 348 \text{ m}^3/\text{day}$ (days)
21	0.001	166.85	2.85	79.57	3.73	6.88
	.003	210.56	3.73	117.40	5.95	11.81
	.005	254.27	4.30	141.66	7.58	15.92
	.010	363.55	5.36	187.34	11.21	27.05
	.020	582.10	7.20	266.28	20.01	75.59
	.030	800.65	9.49 [†]	364.76 [†]	40.25	-

(†) $X_{max}^* > X_{cr} = 6.20 \text{ meters}$

The example problems using the data for Test B of Semadar 1 described above are intended to support, in general, the validity of the theoretical approach and to demonstrate the application of the analytical model to a typical upconing problem. The reader interested in methods which might be used to develop input parameters for the model are referred to the Schmorak and Mercado (1969) discussion of the field investigation and interpretation of the field data.

SECTION III

Program UPCONE

Program UPCONE evaluates the position of an abrupt salt-water/fresh-water interface beneath a pumping well as a function of time and radial distance from the well. The program has also been written to (1) superimpose the effects of dispersion on the abrupt interface to estimate the concentration profile across the interface and the salinity of the pumped water, or (2) estimate the maximum pumping rate or time required to reach a specified salinity in the well. The program has been designed for interactive use and requires data input under two modes of operation--"Basic Input Data" and "Edit."

Basic Input Data

Basic input data are required to initiate a new problem using the UPCONE program. The data entries include the problem title, the physical properties of the aquifer and the two fluids, and the geometry of the system. The user is prompted for the required data through a series of input commands described below. Numeric data should be entered through the keyboard with decimal points, and multiple data entries should be separated by a comma(s). The first basic input command is

ENTER TITLE

?

Any valid keyboard characters can be used. The first 60 characters will be retained for further problem identification.

The next two input commands are used to define the units of all variables used in the calculations and printouts of the results. Any consistent set of units may be used. The two commands are

ENTER UNITS FOR LENGTH (2 CHARACTERS)

?

ENTER UNITS FOR TIME (2 CHARACTERS)

?

Any valid keyboard characters can be used. The first two characters will be retained for identification of length and time units.

The next series of input commands are used to specify the physical properties of the fluids and the aquifer. Input data errors which may interrupt the computational sequence are detected by the program and a command is issued to reenter the data for the appropriate variable. The series of commands are as follows:

ENTER FRESH-WATER AND SALT-WATER DENSITIES

?,?

The densities, or specific gravities, of the two fluids may be entered in any units so long as the units are identical for both entries.

ENTER AQUIFER POROSITY

?

Enter the volume void fraction as a decimal value greater than zero and less than one.

ENTER HORIZONTAL PERMEABILITY (L/t)

?

ENTER VERTICAL PERMEABILITY (L/t)

?

Horizontal and vertical permeabilities must be entered with dimensions of L/t in the units requested. Numerical values for both entries must be greater than zero.

ENTER INITIAL INTERFACE ELEVATION (L)

?

The initial interface elevation may be either positive, zero, or negative, depending upon the location of the reference elevation with respect to the initial abrupt interface (or the elevation of the mean concentration of the transition zone). The elevation must be entered in the units requested.

ENTER DISTANCE FROM BOTTOM OF WELL TO INITIAL INTERFACE (L)

?

The entry must be positive and in the units requested.

ENTER FRACTIONAL CRITICAL RISE

?

The fractional critical rise must be a decimal value greater than zero and less than one.

The next basic input command is used to select the option of performing concentration calculations. The command is

CONCENTRATION CALCULATIONS? (Y/N)

If the user does not respond with Y, the problem title and parameters which have been specified are listed. The critical rise and the maximum steady-state

pumping rate which will maintain the interface at the critical elevation are evaluated and the results are printed. The program then enters the "Edit" mode.

If the response to the last basic input command is Y, the user will be requested for additional basic input data required to carry out the concentration calculations. The first command is

ENTER UNITS FOR CONCENTRATION (6 CHARACTERS)

?

Any valid keyboard characters can be used. The first 6 characters will be used to specify concentrations for following data entries and printed results. The following commands are:

ENTER SALT-WATER AND BACKGROUND CONCENTRATIONS (M/L^3)

?,?

The concentration of any desired component in the invading fluid and the displaced fluid are entered. If the user wishes to work in terms of dimensionless concentrations, enter a value of 1.0 for the salt-water concentration and a value of 0.0 for the background concentration.

ENTER DISPERSIVITY (L)

?

The dispersivity has dimensions of L and must be entered in the units requested. Numerical values must be greater than zero.

ENTER INITIAL WIDTH OF TRANSITION ZONE (M)

?

The width of the transition zone is defined as two standard deviations of the concentration distribution function across the transition zone, as discussed in Section II of this report. For an initially abrupt interface enter a value of zero.

ENTER INTERCEPTION COEFFICIENT

?

The interception coefficient is the fraction of transition zone water in the total volume pumped. Enter a decimal fraction greater than zero and less than one.

At this point the program will list the problem title and parameters as they are currently specified along with the critical rise and the maximum permissible pumping rate for an abrupt interface. The program then enters the "Edit" mode.

Edit Commands

Once the basic input data have been entered, the problem as currently defined is listed and the program enters the "Edit" mode. The edit commands are listed in Table 3. The request for information is

ENTER NEXT COMMAND

?

One of the responses from Table 1 should be given. If the response is incorrect or improperly formatted the statement

ERROR IN LAST COMMAND--REENTER

?

is issued. Error messages for invalid numeric data will be issued as described under Basic Input Data.

The request for information will be repeated until one of the responses EL, PR, LI, NP or DN is entered.

EL will initiate the calculation of interface elevations for a specified pumping rate. The user is given the option of calculating the concentration profile across the transition zone by responding to the following command

CONCENTRATION CALCULATIONS ? (Y/N)

If the response is Y and the data required for concentration calculations have not been entered previously, the user is prompted for the required information using "Basic Input" commands.

For the initial use of the EL edit command, the following requests for data are issued:

ENTER PUMPING RATE (CU L/t) AND PERIOD (t)

?,?

Enter the well pumping rate and the pumping period in the units requested. Both entries must be positive and separated by a comma.

Two additional requests for data are used to define the coordinates of the observation points. The first is

ENTER TFIRST, TLAST, DELTAT (t)

?,?,?

Input units for the time variables must be in the units requested. TFIRST must not be negative value. A zero entry for DELTAT will result in interface elevations at a single time. The second request is

ENTER RFIRST, RLAST, DELTAR (L)

?,?,?

The numerical values used to define the radial coordinates of the observation points may be positive or negative. The results of the calculations will be printed from RFIRST to RLAST.

The pumping rate and observation coordinate parameters are listed and a request

CONTINUE ? (Y/N)

is issued. If the response is not Y, the program returns to the edit mode. If the response is Y, the program proceeds to the computation of interface elevations at the specified times and radial distances from the well and prints the results. If concentration calculations were requested, the concentration in the pumped water and the concentration distribution across the transition zone are also evaluated and printed for the specified times.

On subsequent use of the EL edit command, the pumping rate and observation coordinate data as currently defined will be listed and a request to continue will be issued.

PR initiates the calculation of maximum permissible interface elevations and pumping rates for a specified concentration in the pumped water. If the data required for concentration have not been entered previously, the user is prompted for the required data using "Basic Input Data" dialog. The following request for information is then issued:

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (M/L^3)
?

Enter the concentration in the units requested. The numerical value must not be negative.

The program then lists the problem as currently defined and evaluates the maximum permissible interface elevation and pumping rate. The following request for information is then issued:

ENTER OPTIONAL PUMPING RATE (L^3/t)
?

If a value greater than the maximum pumping rate is entered, the time to reach the specified concentration in the pumped water will be calculated, and the command reissued. If a value less than the maximum pumping rate is entered the program returns to the edit mode.

LI will list the problem as currently defined.

NP will request a complete new problem definition using the
 "Basic Input Data" dialog.

DN will terminate the program.

Although many tests for valid input data and properly formulated edit commands have been embedded in the computer code, the user is encouraged to correct "keyboard errors" before the data are transmitted. This practice will serve to minimize the frustration of program termination as a result of fatal errors during execution of the numerical computations.

TABLE 3
Edit Commands for UPCONE

<u>Command</u>	<u>Variable Changed/Execution</u>
CO	Salt-water and background concentrations
CR	Fractional critical rise
DI	Dispersivity
DT	Depth from bottom of well to initial interface
FD	Fluid densities
IC	Interception coefficient
KX	Horizontal permeability
KZ	Vertical permeability
OB	Time and radius coordinates
PO	Porosity
QP	Pumping rate and time
RC	Radius coordinates
TC	Time coordinates
TW	Initial width of transition zone
ZO	Initial interface elevation
EL	Interface elevation calculations
DN	Terminate program
LI	List problem definition
NP	New problem
PR	Pumping rate calculations

REFERENCES

- Abramowitz, M. and I. A. Stegun. 1966. Handbook of Mathematical Functions with Formulas, Graphs, and Mathematical Tables. National Bureau of Standards Applied Mathematics Series 55, U. S. Department of Commerce, 1046 pp.
- Bear, J. and D. K. Todd. 1960. "The Transition Zone between Fresh and Salt Waters in Coastal Aquifers." Contribution No. 29, Water Resources Center, University of California, Berkeley, CA.
- Carnahan, B., H. A. Luther and J. O. Wilkes. 1969. Applied Numerical Methods. John Wiley and Sons, New York, NY.
- McWhorter, D. B. 1972. "Steady and Unsteady Flow of Fresh Water in Saline Aquifers." Water Management Technical Report No. 20, Engineering Research Center, Colorado State University, Fort Collins, CO.
- Schmorak, S. and A. Mercado. 1969. "Upconing of Fresh Water-Sea Water Interface Below Pumping Wells, Field Study." Water Resources Research, Vol. 5, No. 6, pp 1290-1311.

APPENDIX A

Example Problems

The following pages contain the documentation of the upcoming simulation used to generate the predicted interface/time and concentration/time relationships for the example problem discussed in Section II of this report.

ENTER TITLE
 ?
 SEMADAR 1 -- TEST B
 ENTER UNITS FOR LENGTH (2 CHARACTERS)
 ?
 M
 ENTER UNITS FOR TIME (2 CHARACTERS)
 ?
 DY
 ENTER FRESH-WATER AND SALT-WATER DENSITIES
 ?,?
 1.00,1.03
 ENTER AQUIFER POROSITY
 ?
 0.33
 ENTER HORIZONTAL PERMEABILITY (M /DY)
 ?
 14.7
 ENTER VERTICAL PERMEABILITY (M /DY)
 ?
 14.7
 ENTER INITIAL INTERFACE ELEVATION (M)
 ?
 -30.75
 ENTER DISTANCE FROM BOTTOM OF WELL TO INITIAL INTERFACE (M)
 ?
 15.5
 ENTER FRACTIONAL CRITICAL RISE
 ?
 0.4

 CONCENTRATION CALCULATIONS ? (Y/N)
 N

SEMADAR 1 -- TEST B

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
MAXIMUM STEADY-STATE PUMPING RATE (CU M /DY)	266.2818

ENTER NEXT COMMAND

?

EL

CONCENTRATION CALCULATIONS ? (Y/N)

N

ENTER PUMPING RATE (CU M /DY) AND PERIOD (DY)

?,?

348.,84.

ENTER TFIRST, TLAST, DELTAT (DY)

?,?,?

0.,57.,16.

ENTER RFIRST, RLAST, DELTAR (M)

?,?,?

0.,40.,5.

PUMPING RATE (CU M /DY)
PUMPING PERIOD (DY)

348.0000
84.0000

TFIRST =	.0000	TLAST =	57.0000	DELTAT =	16.0000
RFIRST =	.0000	RLAST =	40.0000	DELTAR =	5.0000

NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION IN 75.59 DY

CONTINUE ? (Y/N)

Y

PUMPING RATE: 348.00 CU M /DY FOR 84.00 DY

INTERFACE ELEVATIONS (M)

T (DY)	R (M)						
	.00	5.00	10.00	15.00	20.00	25.00	30.00
.00	-30.75	-30.75	-30.75	-30.75	-30.75	-30.75	-30.75
16.00	-27.44	-27.75	-28.42	-29.09	-29.60	-29.95	-30.18
32.00	-26.05	-26.41	-27.23	-28.08	-28.78	-29.30	-29.67
48.00	-25.29	-25.66	-26.52	-27.45	-28.22	-28.82	-29.26
57.00	-24.99	-25.37	-26.25	-27.18	-27.98	-28.60	-29.08

INTERFACE ELEVATIONS (M) (CONTINUED)

R (M)	35.00	40.00
T (DY)		
.00	-30.75	-30.75
16.00	-30.34	-30.45
32.00	-29.94	-30.13
48.00	-29.60	-29.84
57.00	-29.43	-29.70

ENTER NEXT COMMAND

?

OB

ENTER TFIRST, TLAST, DELTAT (DY)

?,?,?

0.,160.,5.

ENTER RFIRST, RLAST, DELTAR (M)

?,?,?

4.5,0.,0.

ENTER NEXT COMMAND

?

EL

CONCENTRATION CALCULATIONS ? (Y/N)

N

PUMPING RATE (CU M /DY)
PUMPING PERIOD (DY)

348.0000
84.0000

-	TFIRST =	.0000	TLAST =	160.0000	DELTAT =	5.0000
	RFIRST =	4.5000	RLAST =	.0000	DELTAR =	.0000

NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION IN 75.59 DY

CONTINUE ? (Y/N)

Y

PUMPING RATE: 348.00 CU M /DY FOR 84.00 DY

INTERFACE ELEVATIONS (M)

R (M)	T (DY)
4.50	
.00	-30.75
5.00	-29.45
10.00	-28.52
15.00	-27.81
20.00	-27.27
25.00	-26.83
30.00	-26.47
35.00	-26.18
40.00	-25.93
45.00	-25.71
50.00	-25.53
55.00	-25.36
60.00	-25.22
65.00	-25.09
70.00	-24.98
75.00	-24.88
80.00	-24.79
85.00	-25.00
90.00	-26.13
95.00	-26.94
100.00	-27.55
105.00	-28.01
110.00	-28.37
115.00	-28.67
120.00	-28.91
125.00	-29.11
130.00	-29.27
135.00	-29.41
140.00	-29.54
145.00	-29.64
150.00	-29.73
155.00	-29.81
160.00	-29.88

* NOTE: CRITICAL ELEVATION OF -24.55 M EXCEEDED AT R=0 AND T= 75.59 DY

ENTER NEXT COMMAND

?
RC
ENTER RFIRST, RLAST, DELTAR (M)
?,?,?
12.4,0.,0.

ENTER NEXT COMMAND

?
EL

CONCENTRATION CALCULATIONS ? (Y/N)
N

PUMPING RATE (CU M /DY)	348.0000	
PUMPING PERIOD (DY)	84.0000	
TFIRST = .0000	TLAST = 160.0000	DELTAT = 5.0000
RFIRST = 12.4000	RLAST = .0000	DELTAR = .0000

NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION IN 75.59 DY

CONTINUE ? (Y/N)
Y

PUMPING RATE: 348.00 CU M /DY FOR 84.00 DY

INTERFACE ELEVATIONS (M)

R (M)	
* 12.40	
T (DY) *	
* .00	-30.75
5.00	-29.99
10.00	-29.36
15.00	-28.85
20.00	-28.42
25.00	-28.06
30.00	-27.76
35.00	-27.50
40.00	-27.28
45.00	-27.08
50.00	-26.91
55.00	-26.76
60.00	-26.63
65.00	-26.51
70.00	-26.40
75.00	-26.30
80.00	-26.22
85.00	-26.30
90.00	-26.96
95.00	-27.49
100.00	-27.92
105.00	-28.28
110.00	-28.57
115.00	-28.82
120.00	-29.02
125.00	-29.20
130.00	-29.34
135.00	-29.47
140.00	-29.58
145.00	-29.68
150.00	-29.77
155.00	-29.84
160.00	-29.91

* NOTE: CRITICAL ELEVATION OF -24.55 M EXCEEDED AT R=0 AND T= 75.59 DY

ENTER NEXT COMMAND

?

RC

ENTER RFIRST, RLAST, DELTAR (M)

?,?,?

16.7,0.,0.

ENTER NEXT COMMAND

?

EL

CONCENTRATION CALCULATIONS ? (Y/N)

N

PUMPING RATE (CU M /DY)

348.0000

PUMPING PERIOD (DY)

84.0000

TFIRST = .0000 TLAST = 160.0000 DELTAT = 5.0000

RFIRST = 16.7000 RLAST = .0000 DELTAR = .0000

NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION IN 75.59 DY

CONTINUE ? (Y/N)

Y

PUMPING RATE: 348.00 CU M /DY FOR 84.00 DY

INTERFACE ELEVATIONS (M)

```
*
* R (M )
* 16.70
T (DY) *
*
.00 -30.75
5.00 -30.23
10.00 -29.76
15.00 -29.36
20.00 -29.00
25.00 -28.70
30.00 -28.44
35.00 -28.21
40.00 -28.00
45.00 -27.83
50.00 -27.67
55.00 -27.53
60.00 -27.40
65.00 -27.29
70.00 -27.19
75.00 -27.09
80.00 -27.01
85.00 -27.04
90.00 -27.48
95.00 -27.87
100.00 -28.20
105.00 -28.49
110.00 -28.73
115.00 -28.94
120.00 -29.12
125.00 -29.27
130.00 -29.41
135.00 -29.52
140.00 -29.63
145.00 -29.72
150.00 -29.80
155.00 -29.87
160.00 -29.93
```

* NOTE: CRITICAL ELEVATION OF -24.55 M EXCEEDED AT R=0 AND T= 75.59 DY

ENTER NEXT COMMAND

?

RC

ENTER RFIRST, RLAST, DELTAR (M)

?,?,?

33.9

ENTER NEXT COMMAND

?

EL

CONCENTRATION CALCULATIONS ? (Y/N)

N

PUMPING RATE (CU M /DY)
PUMPING PERIOD (DY)

348.0000
84.0000

TFIRST = .0000 TLAST = 160.0000 DELTAT = 5.0000
RFIRST = 33.9000 RLAST = .0000 DELTAR = .0000

NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION IN 75.59 DY

CONTINUE ? (Y/N)

Y

PUMPING RATE: 348.00 CU M /DY FOR 84.00 DY

INTERFACE ELEVATIONS (M)

```
*
* R ( M )
*      33.90
T (DY) *
*
.00 -30.75
5.00 -30.62
10.00 -30.48
15.00 -30.34
20.00 -30.20
25.00 -30.07
30.00 -29.94
35.00 -29.82
40.00 -29.70
45.00 -29.59
50.00 -29.49
55.00 -29.40
60.00 -29.31
65.00 -29.23
70.00 -29.15
75.00 -29.08
80.00 -29.02
85.00 -28.98
90.00 -29.05
95.00 -29.14
100.00 -29.23
105.00 -29.32
110.00 -29.41
115.00 -29.49
120.00 -29.58
125.00 -29.65
130.00 -29.72
135.00 -29.79
140.00 -29.85
145.00 -29.91
150.00 -29.96
155.00 -30.01
160.00 -30.05
```

* NOTE: CRITICAL ELEVATION OF -24.55 M EXCEEDED AT R=0 AND T= 75.59 DY

```
ENTER NEXT COMMAND
?
OB
ENTER TFIRST, TLAST, DELTAT (DY)
?,?,?
0.,84.,5.
ENTER RFIRST, RLAST, DELTAR ( M )
?,?,?
0.
```

```
ENTER NEXT COMMAND
?
EL
```

```
CONCENTRATION CALCULATIONS ? (Y/N)
Y
ENTER UNITS FOR CONCENTRATION (6 CHARACTERS)
?
PPM CL
ENTER SALT-WATER AND BACKGROUND CONCENTRATIONS (PPM CL)
?,?
22000.,145.
ENTER DISPERSIVITY ( M )
?
0.5
ENTER INITIAL WIDTH OF TRANSITION ZONE ( M )
?
3.5
ENTER INTERCEPTION COEFFICIENT
?
0.08
```

SEMADAR 1 -- TEST B

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
MAXIMUM STEADY-STATE PUMPING RATE (CU M /DY)	266.2818

CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

PUMPING RATE (CU M /DY)	348.0000
PUMPING PERIOD (DY)	84.0000

TFIRST =	.0000	TLAST =	84.0000	DELTAT =	5.0000
RFIRST =	.0000	RLAST =	.0000	DELTAR =	.0000

NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION IN 75.59 DY

CONTINUE ? (Y/N)

Y

PUMPING RATE: 348.00 CU M /DY FOR 84.00 DY

INTERFACE ELEVATIONS (M)

```
*
* R (M )
*      .00
T (DY) *
*
.00 -30.75
5.00 -29.31
10.00 -28.31
15.00 -27.57
20.00 -27.00
25.00 -26.55
30.00 -26.18
35.00 -25.88
40.00 -25.62
45.00 -25.40
50.00 -25.22
55.00 -25.05
60.00 -24.91
65.00 -24.78
70.00 -24.66
75.00 -24.56
80.00 -24.47*
84.00 -24.40*
```

* NOTE: CRITICAL ELEVATION OF -24.55 M EXCEEDED AT R=0 AND T= 75.59 DY

CONCENTRATION IN WELL AND PROFILES BENEATH WELL (PPM CL)

T (DY)	C (WELL) E (WELL)	ELEVATION FOR C/(E) (M)					
		145.0 (.0)	2330.5 (.1)	4516.0 (.2)	6701.5 (.3)	8887.0 (.4)	11072.5 (.5)
.00	145.17 (.0000)	-26.4	-28.5	-29.3	-29.8	-30.3	-30.8
5.00	155.81 (.0005)	-24.0*	-26.6	-27.5	-28.2	-28.8	-29.3
10.00	192.67 (.0022)	-22.4*	-25.3	-26.3	-27.1	-27.7	-28.3
15.00	244.28 (.0045)	-21.3*	-24.4*	-25.5	-26.3	-26.9	-27.6
20.00	297.22 (.0070)	-20.5*	-23.7*	-24.8	-25.6	-26.3	-27.0
25.00	345.51 (.0092)	-19.8*	-23.1*	-24.3*	-25.1	-25.9	-26.5
30.00	387.60 (.0111)	-19.3*	-22.6*	-23.9*	-24.7	-25.5	-26.2
35.00	423.69 (.0128)	-18.8*	-22.3*	-23.5*	-24.4*	-25.2	-25.9
40.00	454.52 (.0142)	-18.5*	-22.0*	-23.2*	-24.1*	-24.9	-25.6
45.00	480.92 (.0154)	-18.2*	-21.7*	-23.0*	-23.9*	-24.7	-25.4
50.00	503.65 (.0164)	-17.9*	-21.5*	-22.7*	-23.7*	-24.5*	-25.2
55.00	523.35 (.0173)	-17.7*	-21.3*	-22.6*	-23.5*	-24.3*	-25.1
60.00	540.53 (.0181)	-17.4*	-21.1*	-22.4*	-23.3*	-24.2*	-24.9
65.00	555.62 (.0188)	-17.3*	-20.9*	-22.2*	-23.2*	-24.0*	-24.8
70.00	568.94 (.0194)	-17.1*	-20.8*	-22.1*	-23.1*	-23.9*	-24.7
75.00	580.79 (.0199)	-17.0*	-20.7*	-22.0*	-23.0*	-23.8*	-24.6
80.00	591.38 (.0204)	-16.8*	-20.6*	-21.9*	-22.9*	-23.7*	-24.5*
84.00	599.06 (.0208)	-16.7*	-20.5*	-21.8*	-22.8*	-23.6*	-24.4*

* NOTE: THE DISPERSION CONCEPT SHOULD BE LIMITED TO THE ZONE BELOW
THE CRITICAL ELEVATION OF -24.5500 M

CONCENTRATION IN WELL AND PROFILES BENEATH WELL (PPM CL)

T (DY)	C (WELL) E (WELL)	ELEVATION FOR C/(E) (M)					
		11072.5 (.5)	13258.0 (.6)	15443.5 (.7)	17629.0 (.8)	19814.5 (.9)	22000.0 (1.0)
.00	145.17 (.0000)	-30.8	-31.2	-31.7	-32.2	-33.0	-35.1
5.00	155.81 (.0005)	-29.3	-29.9	-30.4	-31.1	-32.0	-34.6
10.00	192.67 (.0022)	-28.3	-28.9	-29.5	-30.3	-31.3	-34.2
15.00	244.28 (.0045)	-27.6	-28.2	-28.9	-29.7	-30.8	-33.8
20.00	297.22 (.0070)	-27.0	-27.7	-28.4	-29.2	-30.3	-33.5
25.00	345.51 (.0092)	-26.5	-27.2	-28.0	-28.8	-30.0	-33.3
30.00	387.60 (.0111)	-26.2	-26.9	-27.6	-28.5	-29.7	-33.1
35.00	423.69 (.0128)	-25.9	-26.6	-27.4	-28.2	-29.5	-32.9
40.00	454.52 (.0142)	-25.6	-26.3	-27.1	-28.0	-29.3	-32.8
45.00	480.92 (.0154)	-25.4	-26.1	-26.9	-27.8	-29.1	-32.7
50.00	503.65 (.0164)	-25.2	-26.0	-26.8	-27.7	-29.0	-32.5
55.00	523.35 (.0173)	-25.1	-25.8	-26.6	-27.5	-28.8	-32.5
60.00	540.53 (.0181)	-24.9	-25.7	-26.5	-27.4	-28.7	-32.4
65.00	555.62 (.0188)	-24.8	-25.5	-26.4	-27.3	-28.6	-32.3
70.00	568.94 (.0194)	-24.7	-25.4	-26.3	-27.2	-28.5	-32.2
75.00	580.79 (.0199)	-24.6	-25.3	-26.2	-27.1	-28.5	-32.2
80.00	591.38 (.0204)	-24.5*	-25.2	-26.1	-27.0	-28.4	-32.1
84.00	599.06 (.0208)	-24.4*	-25.2	-26.0	-27.0	-28.3	-32.1

* NOTE: THE DISPERSION CONCEPT SHOULD BE LIMITED TO THE ZONE BELOW
THE CRITICAL ELEVATION OF -24.5500 M

ENTER NEXT COMMAND
?
NP

ENTER TITLE
 ?
 SEMADAR 1 SALINITY/TIME RELATIONSHIPS
 ENTER UNITS FOR LENGTH (2 CHARACTERS)
 ?
 M
 ENTER UNITS FOR TIME (2 CHARACTERS)
 ?
 DY
 ENTER FRESH-WATER AND SALT-WATER DENSITIES
 ?,?
 1.00,1.03
 ENTER AQUIFER POROSITY
 ?
 0.33
 ENTER HORIZONTAL PERMEABILITY (M /DY)
 ?
 14.7
 ENTER VERTICAL PERMEABILITY (M /DY)
 ?
 14.7
 ENTER INITIAL INTERFACE ELEVATION (M)
 ?
 -30.75
 ENTER DISTANCE FROM BOTTOM OF WELL TO INITIAL INTERFACE (M)
 ?
 15.5
 ENTER FRACTIONAL CRITICAL RISE
 ?
 0.4

 CONCENTRATION CALCULATIONS ? (Y/N)
 Y
 ENTER UNITS FOR CONCENTRATION (6 CHARACTERS)
 ?
 PPM CL
 ENTER SALT-WATER AND BACKGROUND CONCENTRATIONS (PPM CL)
 ?,?
 22000.,145.
 ENTER DISPERSIVITY (M)
 ?
 0.5
 ENTER INITIAL WIDTH OF TRANSITION ZONE (M)
 ?
 3.5
 ENTER INTERCEPTION COEFFICIENT
 ?
 0.08

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
MAXIMUM STEADY-STATE PUMPING RATE (CU M /DY)	266.2818

CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

ENTER NEXT COMMAND
?
PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)
?
166.85

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	166.8500
MAXIMUM RELATIVE CONCENTRATION	.0010
MAXIMUM INTERFACE ELEVATION (M)	-28.8973
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	79.5689

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

348.

PUMPING RATE (CU M /DY)	348.0000
TIME TO REACH CMAX (DY)	6.8762

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

575.

PUMPING RATE (CU M /DY)	575.0000
TIME TO REACH CMAX (DY)	3.7256

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

0.

ENTER NEXT COMMAND

?

PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)

?

210.56

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	210.5600
MAXIMUM RELATIVE CONCENTRATION	.0030
MAXIMUM INTERFACE ELEVATION (M)	-28.0165
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	117.4009

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

348.

PUMPING RATE (CU M /DY)	348.0000
TIME TO REACH CMAX (DY)	11.8100

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

575.

PUMPING RATE (CU M /DY)	575.0000
TIME TO REACH CMAX (DY)	5.9515

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

0.

ENTER NEXT COMMAND

?

PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)

?

245.27

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	245.2700
MAXIMUM RELATIVE CONCENTRATION	.0046
MAXIMUM INTERFACE ELEVATION (M)	-27.5565
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	137.1553

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
348.

PUMPING RATE (CU M /DY)	348.0000
TIME TO REACH CMAX (DY)	15.0899

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
575.

PUMPING RATE (CU M /DY)	575.0000
TIME TO REACH CMAX (DY)	7.2666

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
0.

ENTER NEXT COMMAND
?
PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)
?
363.55

SEMADAR 1 SALINITY/TIME, RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	363.5500
MAXIMUM RELATIVE CONCENTRATION	.0100
MAXIMUM INTERFACE ELEVATION (M)	-26.3880
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	187.3442

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
348.

PUMPING RATE (CU M /DY)	348.0000
TIME TO REACH CMAX (DY)	27.0509

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
575.

PUMPING RATE (CU M /DY)	575.0000
TIME TO REACH CMAX (DY)	11.2107

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
0.

ENTER NEXT COMMAND
?
PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)
?
582.1

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	582.1000
MAXIMUM RELATIVE CONCENTRATION	.0200
MAXIMUM INTERFACE ELEVATION (M)	-24.5511
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	266.2366

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

348.

PUMPING RATE (CU M /DY)	348.0000
TIME TO REACH CMAX (DY)	75.5346

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

575.

PUMPING RATE (CU M /DY)	575.0000
TIME TO REACH CMAX (DY)	20.0023

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

0.

ENTER NEXT COMMAND

?

PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)

?

800.65

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	800.6500
MAXIMUM RELATIVE CONCENTRATION	.0300
MAXIMUM INTERFACE ELEVATION (M)	-22.2571*
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	364.7604

* NOTE: THE DISPERSION CONCEPT SHOULD BE LIMITED TO THE ZONE BELOW
THE CRITICAL ELEVATION OF -24.5500 M
(MAXIMUM CONCENTRATIONS IN PUMPED WATER LESS THAN 582.10 PPM CL)

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
575.

PUMPING RATE (CU M /DY)	575.0000
TIME TO REACH CMAX (DY)	40.2467

ENTER OPTIONAL PUMPING RATE (CU M /DY)
?
0.

ENTER NEXT COMMAND
?
PR

ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED WATER (PPM CL)
?
1019.2

SEMADAR 1 SALINITY/TIME RELATIONSHIPS

DENSITY OF FRESH WATER	1.0000
DENSITY OF SALT WATER	1.0300
AQUIFER POROSITY	.3300
HORIZONTAL PERMEABILITY (M /DY)	14.7000
VERTICAL PERMEABILITY (M /DY)	14.7000
INITIAL INTERFACE ELEVATION (M)	-30.7500
DISTANCE FROM BOTTOM OF WELL TO INTERFACE (M)	15.5000
FRACTIONAL CRITICAL RISE	.4000
CRITICAL RISE (M)	6.2000
CRITICAL ELEVATION (M)	-24.5500
CONCENTRATION IN SALT WATER (PPM CL)	22000.0000
BACKGROUND CONCENTRATION (PPM CL)	145.0000
INITIAL WIDTH OF TRANSITION ZONE (M)	3.5000
DISPERSIVITY (M)	.5000
INTERCEPTION COEFFICIENT	.0800

MAXIMUM CONCENTRATION IN PUMPED WATER (PPM CL)	1019.2000
MAXIMUM RELATIVE CONCENTRATION	.0400
MAXIMUM INTERFACE ELEVATION (M)	-13.1997*
MAXIMUM PERMISSIBLE PUMPING RATE (CU M /DY)	753.7639

* NOTE: THE DISPERSION CONCEPT SHOULD BE LIMITED TO THE ZONE BELOW
THE CRITICAL ELEVATION OF -24.5500 M
(MAXIMUM CONCENTRATIONS IN PUMPED WATER LESS THAN 582.10 PPM CL)

ENTER OPTIONAL PUMPING RATE (CU M /DY)

?

0.

ENTER NEXT COMMAND

?

DN

Stop - Program terminated.

C>

APPENDIX B

Description of Program UPCONE

Program UPCONE has been written in an unextended Fortran computer code in an effort to make the program transportable between computer systems. The code consists of a main program and two function subroutines. The program has been documented internally through the liberal use of comment statements.

The main program is divided into three sections. Section I provides for the "Basic Input Data" as described in Section III of this report. The numerical evaluation of interface elevations, concentrations, and maximum pumping rates is accomplished in Section II of the main program which contains the computational algorithms for Case I and Case II types of problems. Section III provides for problem redefinition and control of execution under the "Edit" mode.

Two function subroutines are required to calculate the concentration distribution across the transition zone or to evaluate the maximum pumping rate for a specified salinity of the pumped water. Function ERFC (Z) is a rational approximation of the complimentary error function of the argument Z.

Function IERFC (X, Z, ZMIN, ZMAX) uses a *regula falsi* root finding technique to find the argument, Z, for a specified value of the complimentary error function, X. The last two arguments, ZMIN and ZMAX, define the lower and upper limits of the initial search interval.

APPENDIX C

Listing of Program UPCONE

C	PROGRAM UPCONE	UPCNO01
C	VERSION 1.0	UPCNO02
C	JAN WAGNER	UPCNO03
C	SCHOOL OF CHEMICAL ENGINEERING	UPCNO04
C	OKLAHOMA STATE UNIVERSITY	UPCNO05
C	STILLWATER, OK 74078	UPCNO06
C	TELEPHONE (405) 624-5280	UPCNO07
C		UPCNO08
C	JANUARY, 1982	UPCNO09
C		UPCNO10
	DIMENSION A(30),C(11),CW(51),E(11),EW(51),IC(20),KFLG(11),	UPCNO11
	1R(26),T(51),Z(26,26)	UPCNO12
	REAL*4 KX,KZ	UPCNO13
	DATA KHAR1,KHAR2,NY/ ' ','*','Y'/	UPCNO14
	DATA IC/'FD','PO','KX','KZ','ZO','DT','CR','CO','DI','WT','IC',	UPCNO15
	1'OB','TC','RC','QP','LI','EL','PR','NP','DN'/	UPCNO16
C		UPCNO17
C	READ DEVICE: NI=1 WRITE DEVICE: NO=1	UPCNO18
	NI = 1	UPCNO19
	NO = 1	UPCNO20
C		UPCNO21
C	MAXIMUM NUMBERS OF OBSERVATION POINTS FOR TIME AND RADIUS	UPCNO22
C	HAVE BEEN SET AT 50 AND 25, RESPECTIVELY	UPCNO23
C	DIMENSION CW(M),EW(M),R(N),T(N),Z(M,N)	UPCNO24
C	-- WHERE M=MAXTIM+1 AND N=MAXPTS+1	UPCNO25
	MAXTIM = 50	UPCNO26
	MAXPTS = 25	UPCNO27
C		UPCNO28
C	INITIALIZE PROGRAM FLOW PARAMETERS	UPCNO29
	1 IEDIT = 1	UPCNO30
	KCON = 1	UPCNO31
	KELE = 1	UPCNO32
C		UPCNO33
C	***** SECTION I -- BASIC INPUT DATA	UPCNO34
C		UPCNO35
C	READ TITLE	UPCNO36
	WRITE(NO,5)	UPCNO37
	5 FORMAT('1',3X,'ENTER TITLE',/,3X,'?')	UPCNO38
	READ(NI,10) (A(I),I=1,30)	UPCNO39
	10 FORMAT(30A2)	UPCNO40
C		UPCNO41
C	DEFINE UNITS	UPCNO42
	WRITE(NO,15)	UPCNO43
	15 FORMAT(3X,'ENTER UNITS FOR LENGTH (2 CHARACTERS)',/,3X,'?')	UPCNO44
	READ(NI,20) IL	UPCNO45
	20 FORMAT(A2)	UPCNO46
	WRITE(NO,25)	UPCNO47
	25 FORMAT(3X,'ENTER UNITS FOR TIME (2 CHARACTERS)',/,3X,'?')	UPCNO48
	READ(NI,20) ITU	UPCNO49
C		UPCNO50
C	FLUID DENSITIES	UPCNO51
	29 WRITE(NO,30)	UPCNO52
	30 FORMAT(3X,'ENTER FRESH-WATER AND SALT-WATER DENSITIES',/,3X,'?.?.')	UPCNO53
	READ(NI,35) RHOF,RHOS	UPCNO54
	35 FORMAT(2F10.0)	UPCNO55
	40 IF(RHOS.GT.0.0) GO TO 55	UPCNO56
	WRITE(NO,45)	UPCNO57
	45 FORMAT(3X,'SALT-WATER DENSITY MUST BE GREATER THAN ZERO',	UPCNO58
	1' -- REENTER',/,3X,'?')	UPCNO59
	READ(NI,50) RHOS	UPCNO60
	50 FORMAT(F10.0)	UPCNO61
	GO TO 40	UPCNO62
	55 IF(RHOF.GT.0.0.AND.RHOF.LT.RHOS) GO TO 69	UPCNO63
	WRITE(NO,60)	UPCNO64
	60 FORMAT(3X,'FRESH-WATER DENSITY MUST BE GREATER THAN ZERO',	UPCNO65
	1/,6X,'AND LESS THAN SALT-WATER DENSITY -- REENTER',/,3X,'?')	UPCNO66
	READ(NI,50) RHOF	UPCNO67
	GO TO 55	UPCNO68
	69 GO TO (70,700), IEDIT	UPCNO69
C		UPCNO70

C	POROSITY	UPCNO71
	70 WRITE(NO,75)	UPCNO72
	75 FORMAT(3X,'ENTER AQUIFER POROSITY',/,3X,'?')	UPCNO73
	80 READ(NI,50) PO	UPCNO74
	IF(PO.GT.O.O.AND.PO.LT.1.O) GO TO 89	UPCNO75
	WRITE(NO,85)	UPCNO76
	85 FORMAT(3X,'POROSITY MUST BE GREATER THAN ZERO AND LESS THAN',	UPCNO77
	1' ONE -- REENTER',/,3X,'?')	UPCNO78
	GO TO 80	UPCNO79
	89 GO TO (90,700), IEDIT	UPCNO80
C		UPCNO81
C	HORIZONTAL PERMEABILITY	UPCNO82
	90 WRITE(NO,95) IL,ITU	UPCNO83
	95 FORMAT(3X,'ENTER HORIZONTAL PERMEABILITY ('',A2,'/'',A2,'') ',	UPCNO84
	1/,3X,'?')	UPCNO85
	100 READ(NI,50) KX	UPCNO86
	IF(KX.GT.O.O) GO TO 110	UPCNO87
	WRITE(NO,105)	UPCNO88
	105 FORMAT(3X,'HORIZONTAL PERMEABILITY MUST BE GREATER THAN',	UPCNO89
	1' ZERO -- REENTER',/,3X,'?')	UPCNO90
	GO TO 100	UPCNO91
	110 GO TO (111,700), IEDIT	UPCNO92
C		UPCNO93
C	VERTICAL PERMEABILITY	UPCNO94
	111 WRITE(NO,112) IL,ITU	UPCNO95
	112 FORMAT(3X,'ENTER VERTICAL PERMEABILITY ('',1A2,'/'',A2,'') ',	UPCNO96
	1/,3X,'?')	UPCNO97
	114 READ(NI,50) KZ	UPCNO98
	IF(KZ.GT.O.O) GO TO 119	UPCNO99
	WRITE(NO,115)	UPCNO100
	115 FORMAT(3X,'VERTICAL PERMEABILITY MUST BE GREATER THAN ZERO',	UPCNO101
	1' -- REENTER',/,3X,'?')	UPCNO102
	GO TO 114	UPCNO103
	119 GO TO (120,700), IEDIT	UPCNO104
C		UPCNO105
C	INITIAL INTERFACE ELEVATION	UPCNO106
	120 WRITE(NO,125) IL	UPCNO107
	125 FORMAT(3X,'ENTER INITIAL INTERFACE ELEVATION ('',A2,'')',/,3X,'?')	UPCNO108
	READ(NI,50) ZO	UPCNO109
	GO TO (129,700), IEDIT	UPCNO110
C		UPCNO111
C	DISTANCE FROM BOTTOM OF WELL TO INITIAL INTERFACE	UPCNO112
	129 WRITE(NO,130) IL	UPCNO113
	130 FORMAT(3X,'ENTER DISTANCE FROM BOTTOM OF WELL TO INITIAL ',	UPCNO114
	1' INTERFACE ('',A2,'')',/,3X,'?')	UPCNO115
	135 READ(NI,50) D	UPCNO116
	IF(D.GT.O.O) GO TO 144	UPCNO117
	WRITE(NO,140)	UPCNO118
	140 FORMAT(3X,'DISTANCE MUST BE GREATER THAN ZERO -- REENTER',/,	UPCNO119
	13X,'?')	UPCNO120
	GO TO 135	UPCNO121
	144 GO TO (145,700), IEDIT	UPCNO122
C		UPCNO123
C	FRACTIONAL CRITICAL RISE	UPCNO124
	145 WRITE(NO,150)	UPCNO125
	150 FORMAT(3X,'ENTER FRACTIONAL CRITICAL RISE',/,3X,'?')	UPCNO126
	155 READ(NI,50) THETA	UPCNO127
	IF(THETA.GT.O.O.AND.THETA.LT.1.O) GO TO 164	UPCNO128
	WRITE(NO,160)	UPCNO129
	160 FORMAT(3X,'FRACTION MUST BE GREATER THAN ZERO AND LESS THAN',	UPCNO130
	1' ONE -- REENTER',/,3X,'?')	UPCNO131
	GO TO 155	UPCNO132
	164 XCR = THETA*D	UPCNO133
	ZCR = XCR + ZO	UPCNO134
C	MAXIMUM STEADY-STATE PUMPING RATE	UPCNO135
	QMAXSS = 6.283185*((RHOS-RHOF)/RHOF)*KX*D*XCR	UPCNO136
	165 GO TO (169,700), IEDIT	UPCNO137
C		UPCNO138
C		UPCNO139
C	DATA FOR CONCENTRATION CALCULATIONS	UPCNO140

169	WRITE(NO,170)	UPCN141
170	FORMAT('O',2X,'CONCENTRATION CALCULATIONS ? (Y/N)')	UPCN142
	READ(NI,175) ICON	UPCN143
175	FORMAT(A1)	UPCN144
C	IF(ICON.NE.NY) GO TO 275	UPCN145
C		UPCN146
176	KCON = 2	UPCN147
	WRITE(NO,180)	UPCN148
180	FORMAT(3X,'ENTER UNITS FOR CONCENTRATION (6 CHARACTERS)',	UPCN149
	1/,3X,'?')	UPCN150
	READ(NI,185) IM1,IM2,IM3	UPCN151
185	FORMAT(3A2)	UPCN152
C		UPCN153
C	SALT-WATER AND BACKGROUND CONCENTRATIONS	UPCN154
188	IF(KCON.EQ.2) GO TO 189	UPCN155
	WRITE(NO,180)	UPCN156
	READ(NI,185) IM1,IM2,IM3	UPCN157
189	WRITE(NO,190) IM1,IM2,IM3	UPCN158
190	FORMAT(3X,'ENTER SALT-WATER AND BACKGROUND CONCENTRATIONS (',	UPCN159
	13A2,') ',/,3X,'?,?')	UPCN160
	READ(NI,35) CO,CB	UPCN161
195	IF(CO.GE.1.0) GO TO 205	UPCN162
	WRITE(NO,200)	UPCN163
200	FORMAT(3X,'SALT-WATER CONCENTRATION MUST BE GREATER THAN',	UPCN164
	1' OR EQUAL TO ONE -- REENTER',/,3X,'?')	UPCN165
	READ(NI,50) CO	UPCN166
	GO TO 195	UPCN167
205	IF(CB.GE.0.0.AND.CB.LT.CO) GO TO 214	UPCN168
	WRITE(NO,210)	UPCN169
210	FORMAT(3X,'BACKGROUND CONCENTRATION MUST BE GREATER THAN',	UPCN170
	1' OR EQUAL TO ZERO',/,6X,'AND LESS THAN SALT-WATER',	UPCN171
	2' CONCENTRATION -- REENTER',/,3X,'?')	UPCN172
	READ(NI,50) CB	UPCN173
	GO TO 205	UPCN174
214	GO TO (215,700,215,215), IEDIT	UPCN175
C		UPCN176
C	DISPERSIVITY	UPCN177
215	WRITE(NO,220) IL	UPCN178
220	FORMAT(3X,'ENTER DISPERSIVITY (',A2,') ',/,3X,'?')	UPCN179
225	READ(NI,50) DM	UPCN180
	IF(DM.GT.0.0) GO TO 234	UPCN181
	WRITE(NO,230)	UPCN182
230	FORMAT(3X,'DISPERSIVITY MUST BE GREATER THAN ZERO -- REENTER',	UPCN183
	1/,3X,'?')	UPCN184
	GO TO 225	UPCN185
234	GO TO (235,700,235,235), IEDIT	UPCN186
C		UPCN187
C	INITIAL WIDTH OF TRANSITION ZONE	UPCN188
235	WRITE(NO,240) IL	UPCN189
240	FORMAT(3X,'ENTER INITIAL WIDTH OF TRANSITION ZONE (',A2,') ',	UPCN190
	1/,3X,'?')	UPCN191
245	READ(NI,50) SO2	UPCN192
	IF(SO2.GE.0.0) GO TO 254	UPCN193
	WRITE(NO,250)	UPCN194
250	FORMAT(3X,'INITIAL WIDTH MUST BE GREATER THAN ZERO -- REENTER',	UPCN195
	1/,3X,'?')	UPCN196
	GO TO 245	UPCN197
254	GO TO (255,700,255,255), IEDIT	UPCN198
C		UPCN199
C	INTERCEPTION COEFFICIENT	UPCN200
255	WRITE(NO,260)	UPCN201
260	FORMAT(3X,'ENTER INTERCEPTION COEFFICIENT',/,3X,'?')	UPCN202
265	READ(NI,50) PHI	UPCN203
	IF(PHI.GT.0.0.AND.PHI.LT.1.0) GO TO 274	UPCN204
	WRITE(NO,270)	UPCN205
270	FORMAT(3X,'COEFFICIENT MUST BE GREATER THAN ZERO AND LESS THAN',	UPCN206
	1' ONE -- REENTER',/,3X,'?')	UPCN207
	GO TO 265	UPCN208
274	GO TO (275,700,275,510), IEDIT	UPCN209
		UPCN210

C		UPCN211
C	LIST PROBLEM DEFINITION	UPCN212
C		UPCN213
	275 CONTINUE	UPCN214
	WRITE(NO,280) (A(I),I=1,30), RHOF,RHOS,PO,IL,ITU,KX,IL,ITU,KZ	UPCN215
	280 FORMAT('1',3X,30A2,/,	UPCN216
	16X,'DENSITY OF FRESH WATER',25X,F10.4,/,	UPCN217
	26X,'DENSITY OF SALT WATER',26X,F10.4,/,	UPCN218
	36X,'AQUIFER POROSITY',31X,F10.4,/,	UPCN219
	46X,'HORIZONTAL PERMEABILITY ('A2,')',15X,F10.4,/,	UPCN220
	56X,'VERTICAL PERMEABILITY ('A2,')',17X,F10.4)	UPCN221
	WRITE(NO,281)IL, ZO,IL,D,THETA,IL,XCR,IL,ZCR	UPCN222
	281 FORMAT('O',	UPCN223
	15X,'INITIAL INTERFACE ELEVATION ('A2,')',14X,F10.4,/,	UPCN224
	26X,'DISTANCE FROM BOTTOM OF WELL TO INTERFACE ('A2,')',F10.4,/,	UPCN225
	36X,'FRACTIONAL CRITICAL RISE',22X,F10.4,/,	UPCN226
	46X,'CRITICAL RISE ('A2,')',28X,F10.4,/,	UPCN227
	56X,'CRITICAL ELEVATION ('A2,')',23X,F10.4)	UPCN228
C		UPCN229
	WRITE(NO,285) IL,ITU,QMAXSS	UPCN230
	285 FORMAT('O',5X,'MAXIMUM STEADY-STATE PUMPING RATE (CU 'A2,')',	UPCN231
	1A2,')',F10.4,/, 'O',/, 'O')	UPCN232
C		UPCN233
	IF(ICDN.NE.NY.OR.KCON.EQ.1) GO TO 700	UPCN234
C		UPCN235
	WRITE(NO,290) IM1,IM2,IM3,CO,IM1,IM2,IM3,CB,IL,SO2,IL,DM,PHI	UPCN236
	290 FORMAT('O',5X,'CONCENTRATION IN SALT WATER ('3A2,')',10X,F10.4,/,	UPCN237
	16X,'BACKGROUND CONCENTRATION ('3A2,')',13X,F10.4,/,	UPCN238
	26X,'INITIAL WIDTH OF TRANSITION ZONE ('A2,')',9X,F10.4,/,	UPCN239
	36X,'DISPERSIVITY ('A2,')',29X,F10.4,/,	UPCN240
	46X,'INTERCEPTION COEFFICIENT',23X,F10.4,/, 'O',/, 'O')	UPCN241
C		UPCN242
	GO TO (700,700,301), IEDIT	UPCN243
C		UPCN244
C		UPCN245
C	***** SECTION II -- NUMERICAL EVALUATION OF INTERFACE ELEVATIONS	UPCN246
C		UPCN247
C		UPCN248
C	CASE I PROBLEMS -- EVALUATE INTERFACE ELEVATIONS AND CONCENTRATION	UPCN249
C		UPCN250
C		UPCN251
	300 CONTINUE	UPCN252
	IEDIT = 3	UPCN253
		UPCN254
C	PARAMETERS FOR INTERFACE ELEVATION CALCULATIONS	UPCN255
	301 IF(KELE.EQ.2) GO TO 329	UPCN256
	KELE = 2	UPCN257
C		UPCN258
C	PUMPING RATE AND PERIOD	UPCN259
	302 WRITE(NO,305) IL,ITU,ITU	UPCN260
	305 FORMAT('O',2X,'ENTER PUMPING RATE (CU 'A2,')',A2,') AND',	UPCN261
	1' PERIOD ('A2,')',/,3X,'?',?)	UPCN262
	READ(NI,35) Q,TPUMP	UPCN263
	306 IF(Q.GT.O.O) GO TO 308	UPCN264
	WRITE(NO,307)	UPCN265
	307 FORMAT(3X,'PUMPING RATE MUST BE GREATER THAN ZERO -- REENTER',	UPCN266
	1/,3X,'?')	UPCN267
	READ(NI,50) Q	UPCN268
	GO TO 306	UPCN269
	308 IF(TPUMP.GT.O.O) GO TO 310	UPCN270
	WRITE(NO,309)	UPCN271
	309 FORMAT(3X,'PUMPING PERIOD MUST BE GREATER THAN ZERO -- REENTER',	UPCN272
	1/,3X,'?')	UPCN273
	READ(NI,50) TPUMP	UPCN274
	GO TO 308	UPCN275
	310 GO TO (700,700,312), IEDIT	UPCN276
C		UPCN277
C	COORDINATES OF OBSERVATION POINTS -- TIME AND RADIUS	UPCN278
	311 IEDIT = 1	UPCN279
	312 WRITE(NO,313) ITU	UPCN280

313	FORMAT(3X,'ENTER TFIRST, TLAST, DELTAT (' ,A2,') ' ,/,3X,'? ,? ,?')	UPCN281
	READ(NI,315) TF,TL,DELT	UPCN282
315	FORMAT(3F10.0)	UPCN283
	DELT = ABS(DELT)	UPCN284
316	IF(TF.GE.O.O.AND.DELT.LE.1.OE-06) GO TO 320	UPCN285
	IF(TF.GE.O.O) GO TO 318	UPCN286
	WRITE(NO,317)	UPCN287
317	FORMAT(3X,'TFIRST MUST NOT BE LESS THAN ZERO -- REENTER',	UPCN288
	1/,3X,'?')	UPCN289
	READ(NI,50) TF	UPCN290
	GO TO 316	UPCN291
318	IF(TL.GE.O.O) GO TO 321	UPCN292
	WRITE(NO,319)	UPCN293
319	FORMAT(3X,'TLAST MUST NOT BE LESS THAN ZERO -- REENTER',	UPCN294
	1/,3X,'?')	UPCN295
	READ(NI,50) TL	UPCN296
	GO TO 318	UPCN297
320	TL = TF	UPCN298
321	GO TO (322,700,322), IEDIT	UPCN299
C		UPCN300
322	WRITE(NO,323) IL	UPCN301
323	FORMAT(3X,'ENTER RFIRST, RLAST, DELTAR (' ,A2,') ' ,/,3X,'? ,? ,?')	UPCN302
	READ(NI,325) RF,RL,DELR	UPCN303
325	FORMAT(3F10.0)	UPCN304
	DELR = ABS(DELR)	UPCN305
	GO TO (700,700,329), IEDIT	UPCN306
C		UPCN307
329	WRITE(NO,330) IL,ITU,Q,ITU,TPUMP,TF,TL,DELT,RF,RL,DELR	UPCN308
330	FORMAT('O',5X,'PUMPING RATE (CU ' ,A2,' /' ,A2,') ' ,23X,F10.4,/,	UPCN309
	16X,'PUMPING PERIOD (' ,A2,') ' ,27X,F10.4,/,	UPCN310
	26X,'TFIRST = ' ,F10.4,3X,'TLAST = ' ,F10.4,3X,'DELTAT = ' ,F10.4,/,	UPCN311
	36X,'RFIRST = ' ,F10.4,3X,'RLAST = ' ,F10.4,3X,'DELTAR = ' ,F10.4)	UPCN312
	IF(Q.LE.QMAXSS) GO TO 332	UPCN313
	TCR = ((2.*PO*D)/(((RHOS-RHOF)/RHOF)*KZ))*((1./(1.-QMAXSS/Q))-1.)	UPCN314
	WRITE(NO,331) TCR,ITU	UPCN315
331	FORMAT('O',2X,'NOTE: INTERFACE WILL RISE TO CRITICAL ELEVATION',	UPCN316
	1' IN',F10.2,A3)	UPCN317
332	WRITE(NO,333)	UPCN318
333	FORMAT('O',2X,'CONTINUE ? (Y/N)')	UPCN319
	READ(NI,175) JFLOW	UPCN320
	IF(JFLOW.NE.NY) GO TO 700	UPCN321
C		UPCN322
C	RADIUS COORDINATES	UPCN323
335	CONTINUE	UPCN324
	IR = 1	UPCN325
	R(IR) = RF	UPCN326
	IF(DELR.LE.1.OE-06) GO TO 345	UPCN327
	DIF = RL - RF	UPCN328
	IF(ABS(DIF).LE.1.OE-06) GO TO 345	UPCN329
	IF(DIF.LE.O.O) DELR = -DELR	UPCN330
	NPTS = DIF/DELR	UPCN331
	REM = DIF - DELR*FLOAT(NPTS)	UPCN332
	TOL = 1.OE-06*ABS(DIF)	UPCN333
	NPTS = NPTS + 1	UPCN334
	IF(NPTS.LE.MAXPTS) GO TO 337	UPCN335
	WRITE(NO,336) NPTS,MAXPTS	UPCN336
336	FORMAT(3X,I3,' RADIUS OBSERVATION POINTS EXCEED MAXIMUM OF',I4)	UPCN337
	GO TO 700	UPCN338
337	CONTINUE	UPCN339
	DO 340 IR=2,NPTS	UPCN340
	R(IR) = R(IR-1) + DELR	UPCN341
340	CONTINUE	UPCN342
	IR = NPTS	UPCN343
	IF(ABS(REM).LT.TOL) GO TO 345	UPCN344
	IR = IR + 1	UPCN345
	R(IR) = RL	UPCN346
345	CONTINUE	UPCN347
C		UPCN348
C	TIME COORDINATES	UPCN349
	IT = 1	UPCN350

T(IT) = TF	UPCN351
IF(DELT.LE.1.OE-06) GO TO 355	UPCN352
DIF = TL - TF	UPCN353
IF(ABS(DIF).LE.1.OE-06) GO TO 355	UPCN354
IF(DIF.LE.0.0) DELT = -DELT	UPCN355
NPTS = DIF/DELT	UPCN356
REM = DIF - DELT*FLOAT(NPTS)	UPCN357
TOL = 1.OE-06*ABS(DIF)	UPCN358
NPTS = NPTS + 1	UPCN359
IF(NPTS.LE.MAXTIM) GO TO 347	UPCN360
WRITE(NO,346) NPTS,MAXTIM	UPCN361
346 FORMAT(3X,I3,' TIME OBSERVATION POINTS EXCEED MAXIMUM OF',I4)	UPCN362
GO TO 700	UPCN363
347 CONTINUE	UPCN364
DO 350 IT=2,NPTS	UPCN365
T(IT) = T(IT-1) + DELT	UPCN366
350 CONTINUE	UPCN367
IT = NPTS	UPCN368
IF(ABS(REM).LT.TOL) GO TO 355	UPCN369
IT = IT + 1	UPCN370
T(IT) = TL	UPCN371
355 CONTINUE	UPCN372
TMAX = TL	UPCN373
IF(TF.GT.TL) TMAX=TF	UPCN374
C	UPCN375
C	UPCN376
COEF = Q/(6.2832*((RHOS-RHOF)/RHOF)*KX*D)	UPCN377
CONR = SQRT(KZ/KX)/D	UPCN378
CONT = ((RHOS-RHOF)/RHOF)*KZ/(2.0*PO*D)	UPCN379
DO 365 I=1,IT	UPCN380
TAU = CONT*T(I)	UPCN381
TAU1 = CONT*(T(I)-TPUMP)	UPCN382
IF(T(I).LE.TPUMP) TAU1=0.0	UPCN383
XRO = COEF*(1.0/(1.0+TAU1) - 1.0/(1.0+TAU))	UPCN384
ZRO = XRO + ZO	UPCN385
DO 360 J=1,IR	UPCN386
RDIM = CONR*R(J)	UPCN387
Z(I,J) = COEF*((1.0/SQRT((1.0+TAU1)**2 + RDIM**2))	UPCN388
1	UPCN389
360 CONTINUE	UPCN390
IF(ZRO.GT.ZCR) IPR=2	UPCN391
365 CONTINUE	UPCN392
370 IT = I	UPCN393
C	UPCN394
C	UPCN395
PRINT INTERFACE ELEVATIONS	UPCN396
WRITE(NO,375) Q,IL,ITU,TPUMP,ITU,IL,IL	UPCN397
375 FORMAT('1',18X,'PUMPING RATE:',F12.2,' CU ',A2,'/',A2,' FOR',	UPCN398
1F10.2,A3,'/',O',18X,'INTERFACE ELEVATIONS ('',A2,'') ',//,	UPCN399
23X,' *',/,3X,' * R ('',A2,'')')	UPCN400
LIM1 = 1	UPCN401
LIM2 = 7	UPCN402
380 IF(LIM2.GT.IR) LIM2=IR	UPCN403
WRITE(NO,385) (R(L),L=LIM1,LIM2)	UPCN404
385 FORMAT(3X,' * ',7F9.2)	UPCN405
WRITE(NO,390) ITU	UPCN406
390 FORMAT(3X,'T ('',A2,'') *',/,12X,'**')	UPCN407
DO 400 I=1,IT	UPCN408
DO 393 L=LIM1,LIM2	UPCN409
KFLG(L) = KHAR1	UPCN410
IF(Z(I,L).GT.ZCR) KFLG(L)=KHAR2	UPCN411
393 CONTINUE	UPCN412
WRITE(NO,395) T(I),(Z(I,L),KFLG(L),L=LIM1,LIM2)	UPCN413
395 FORMAT(5X,F8.2,1X,7(F8.2,A1))	UPCN414
40AX.GE.TCR)	UPCN415
1	UPCN416
405 FORMAT('O',2X,'* NOTE: CRITICAL ELEVATION OF',F8.2,A3,	UPCN417
1' EXCEEDED AT R=O AND T=',F8.2,A3)	UPCN418
IF(LIM2.EQ.IR) GO TO 415	UPCN419
LIM1 = LIM1 + 7	UPCN420
LIM2 = LIM2 + 7	

WRITE(NO,410) IL,IL	UPCN421
410 FORMAT('1',18X,'INTERFACE ELEVATIONS ('',A2,'') (CONTINUED)',/,/,	UPCN422
13X,'*',/,3X,' * R ('',A2,'')')	UPCN423
GO TO 380	UPCN424
415 CONTINUE	UPCN425
IF(ICON.NE.NY) GO TO 700	UPCN426
C	UPCN427
C CONCENTRATION PROFILES	UPCN428
SO = SO2/2.0	UPCN429
E(1) = 0.0	UPCN430
C(1) = CB	UPCN431
DO 420 K=2,11	UPCN432
E(K) = E(K-1) + 0.1	UPCN433
C(K) = E(K)*(CO-CB) + CB	UPCN434
420 CONTINUE	UPCN435
C	UPCN436
UP = CONT*TPUMP	UPCN437
XBAR1 = COEF*(1.0-1.0/(1.0+TAUP))	UPCN438
TAU1 = CONT*(T(I)-TPUMP)	UPCN439
XTOT = COEF*((1.0/(1.0+TAU1)) - (1.0/(1.0+TAU)))	UPCN440
XBAR2 = XBAR1 - XTOT	UPCN441
XBAR = XBAR1 + XBAR2	UPCN442
GO TO 440	UPCN443
435 XTOT = COEF*(1.0 - 1.0/(1.0+TAU))	UPCN444
XBAR = XTOT	UPCN445
440 CONTINUE	UPCN446
S1 = SQRT(SO**2 + 2.0*DM*XBAR)	UPCN447
ARG = 10.0	UPCN448
IF(S1.GT.0.0) ARG = (XCR-XTOT)/(1.414214*S1)	UPCN449
EZCR = 0.5*ERFC(ARG)	UPCN450
EW(I) = 0.5*EZCR*PHI	UPCN451
CW(I) = EW(I)*(CO-CB) + CB	UPCN452
Z(I,1) = XTOT + 2.5*S1 + ZO	UPCN453
Z(I,11) = XTOT - 2.5*S1 + ZO	UPCN454
XLIM1 = 2.0	UPCN455
XLIM2 = 0.0	UPCN456
DO 445 K=2,5	UPCN457
CERF = 2.0*E(K)	UPCN458
CALL IERFC(CERF,ARG,XLIM1,XLIM2)	UPCN459
DIST = 1.41421*S1*ARG	UPCN460
Z(I,K) = XTOT + DIST + ZO	UPCN461
L = 12-K	UPCN462
Z(I,L) = XTOT - DIST + ZO	UPCN463
445 CONTINUE	UPCN464
Z(I,6) = XTOT + ZO	UPCN465
446 CONTINUE	UPCN466
LIM1 = 1	UPCN467
LIM2 = 6	UPCN468
IN WELL AND PROFILES BENEATH WELL',	UPCN469
1' ('',3A2,'')',/,11X,'T C(WELL)',14X,'ELEVATION FOR C/(E) ('',	UPCN470
2A2,'')',/,9X,'('',A2,'') E(WELL)')	UPCN471
WRITE(NO,430) (C(K),K=LIM1,LIM2),(E(K),K=LIM1,LIM2)	UPCN472
430 FORMAT(24X,6(F8.1,1X),/,24X,6('',F3.1,''))	UPCN473
431 DO 455 I=1,IT	UPCN474
DO 449 K=LIM1,LIM2	UPCN475
KFLG(K) = KHAR1	UPCN476
IF(Z(I,K).GT.ZCR) KFLG(K) = KHAR2	UPCN477
449 CONTINUE	UPCN478
WRITE(NO,450) T(I),CW(I),(Z(I,K),KFLG(K),K=LIM1,LIM2),EW(I)	UPCN479
450 FORMAT(/,6X,F8.2,F9.2,1X,6(F8.1,A1),/,16X,('',F6.4,''))	UPCN480
455 CONTINUE	UPCN481
WRITE(NO,457) ZCR,IL	UPCN482
457 FORMAT('O',2X,'* NOTE: THE DISPERSION CONCEPT SHOULD BE LIMITED',	UPCN483
1' TO THE ZONE BELOW',/,11X,' THE CRITICAL ELEVATION OF',F12.4,A3)	UPCN484
IF(LIM2.EQ.11) GO TO 700	UPCN485
LIM1 = 6	UPCN486
LIM2 = 11	UPCN487
GO TO 447	UPCN488
C	UPCN489
C	UPCN490

NCENTRATION IN PUMPED WATER	UPCN491
C	UPCN492
500 CONTINUE	UPCN493
IEDIT = 4	UPCN494
IF(KCON.NE.2) GO TO 176	UPCN495
510 WRITE(NO,515) IM1,IM2,IM3	UPCN496
515 FORMAT('O',2X,'ENTER MAXIMUM PERMISSIBLE CONCENTRATION IN PUMPED',	UPCN497
1' WATER ('',3A2,'')',/,3X,'?')	UPCN498
516 READ(NI,50) CMAX	UPCN499
IF(CMAX.GE.CB.AND.CMAX.LT.CO) GO TO 518	UPCN500
WRITE(NO,517)	UPCN501
517 FORMAT(3X,'CONCENTRATION MUST BE GREATER THAN OR EQUAL TO CB',/,	UPCN502
13X,'AND LESS THAN CO -- REENTER',	UPCN503
2/,3X,'?')	UPCN504
GO TO 516	UPCN505
518 CONTINUE	UPCN506
C	UPCN507
C	UPCN508
SO = SO2/2.0	UPCN509
EMAX = (CMAX-CB)/(CO-CB)	UPCN510
EXCR = EMAX/(0.5*PHI)	UPCN511
ELIM = 0.0	UPCN512
IF(SO.GT.0.0) ELIM = 0.5*ERFC(XCR/(1.1414214*SO))	UPCN513
CINIT = 0.5*PHI*ELIM*(CO-CB) + CB	UPCN514
IF(EXCR.LT.ELIM) GO TO 550	UPCN515
IF(EXCR.LE.0.0.OR.EXCR.GE.1.0) GO TO 520	UPCN516
CERF = 2.0*EXCR	UPCN517
XLIM1 = 3.0	UPCN518
XLIM2 = 0.0	UPCN519
CALL IERFC(CERF,ARG,XLIM1,XLIM2)	UPCN520
B = -4.0*ARG*ARG*DM - 2.0*XCR	UPCN521
CON = -2.0*ARG*ARG*SO*SO + XCR*XCR	UPCN522
GO TO 521	UPCN523
520 B = -12.5*DM - 2.0*XCR	UPCN524
CON = -6.25*SO*SO + XCR*XCR	UPCN525
521 CONTINUE	UPCN526
ROOT = B*B - 4.0*CON	UPCN527
IF(ROOT.LT.0.0) GO TO 650	UPCN528
XBAR1 = (-B-(ROOT**0.5))/2.0	UPCN529
XBAR2 = (-B+(ROOT**0.5))/2.0	UPCN530
XBAR = XBAR1	UPCN531
IF(EXCR.GT.0.5) XBAR=XBAR2	UPCN532
ZMAX = XBAR + ZO	UPCN533
JFLG = KHAR1	UPCN534
IF(ZMAX.GT.ZCR) JFLG=KHAR2	UPCN535
QMAX = 6.283185*((RHOS-RHOF)/RHOF)*KX*D*XBAR	UPCN536
C	UPCN537
WRITE(NO,280) (A(I),I=1,30),RHOF,RHOS,PO,IL,ITU,KX,IL,ITU,KZ	UPCN538
WRITE(NO,281) IL,ZO,IL,D,THETA,IL,XCR,IL,ZCR	UPCN539
WRITE(NO,290) IM1,IM2,IM3,CO,IM1,IM2,IM3,CB,IL,SO2,IL,DM,PHI	UPCN540
WRITE(NO,525) IM1,IM2,IM3,CMAX,EMAX,IL,ZMAX,JFLG,IL,ITU,QMAX	UPCN541
525 FORMAT('O',5X,'MAXIMUM CONCENTRATION IN PUMPED WATER ('',3A2,'')',	UPCN542
11X,F10.4,/,	UPCN543
26X,'MAXIMUM RELATIVE CONCENTRATION',17X,F10.4,/,	UPCN544
36X,'MAXIMUM INTERFACE ELEVATION ('',A2,'')',15X,F10.4,A1,/,	UPCN545
46X,'MAXIMUM PERMISSIBLE PUMPING RATE (CU '',A2,'/'',A2,'')',4X,	UPCN546
5F10.4)	UPCN547
IF(ZMAX.LE.ZCR) GO TO 530	UPCN548
WRITE(NO,457) ZCR,IL	UPCN549
CLIM = 0.5*(0.5*PHI)*(CO-CB) + CB	UPCN550
WRITE(NO,527) CLIM,IM1,IM2,IM3	UPCN551
527 FORMAT(3X,'(MAXIMUM CONCENTRATIONS IN PUMPED WATER LESS THAN',	UPCN552
1F10.2,A3,2A2,'')',/,,'O')	UPCN553
C	UPCN554
530 WRITE(NO,535) IL,ITU	UPCN555
535 FORMAT('O',2X,'ENTER OPTIONAL PUMPING RATE (CU '',A2,'/'',A2,'')',	UPCN556
1/,3X,'?')	UPCN557
READ(NI,50) QP	UPCN558
IF(QP.LE.QMAX) GO TO 600	UPCN559
TIME = ((2.*PO*D)/(((RHOS-RHOF)/RHOF)*KZ))*((1./(1.-QMAX/QP))-1.)	UPCN560

WRITE(NO,545) IL,ITU,QP,ITU,TIME	UPCN561
545 FORMAT('O',2X,'PUMPING RATE (CU ',A2,'/',A2,')',6X,F10.4,/ 1	UPCN562
GO TO 530	UPCN563
C	UPCN564
550 WRITE(NO,555) SO2,IL,CINIT,IM1,IM2,IM3	UPCN565
555 FORMAT('O',2X,'CMAX EXCEEDED FOR AN INITIAL TRANSITION ', 1'ZONE WIDTH OF',F10.4,A3,/, 23X,'INITIAL CONCENTRATION IN PUMPED WATER IS',F10.4,A3,2A2)	UPCN566
600 CONTINUE	UPCN567
GO TO 700	UPCN568
C	UPCN569
650 WRITE(NO,655)	UPCN570
655 FORMAT(3X,'IMAGINARY ROOT OBTAINED FOR XMAX')	UPCN571
GO TO 700	UPCN572
C	UPCN573
C	UPCN574
C ***** SECTION III -- PROBLEM REDEFINITION AND CONTROL OF EXECUTION	UPCN575
C	UPCN576
C	UPCN577
700 CONTINUE	UPCN578
IEDIT = 2	UPCN579
XCR = THETA*D	UPCN580
ZCR = XCR + ZO	UPCN581
QMAXSS = 6.283185*((RHQS-RHOF)/RHOF)*KX*D*XCR	UPCN582
WRITE(NO,705)	UPCN583
705 FORMAT(//,3X,'ENTER NEXT COMMAND',/,3X,'?')	UPCN584
710 READ(NI,715) NEXT	UPCN585
715 FORMAT(A2)	UPCN586
C	UPCN587
DO 720 I=1,20	UPCN588
IF(NEXT.EQ.IC(I)) GO TO 730	UPCN589
720 CONTINUE	UPCN590
WRITE(NO,725)	UPCN591
725 FORMAT(3X,'ERROR IN LAST COMMAND -- REENTER',/,3X,'?')	UPCN592
GO TO 710	UPCN593
730 GO TO (29,70,90,111,120,129,145,188,215,235,255, 1311,312,322,302,275,300,500,1,1000),I	UPCN594
C	UPCN595
1000 STOP	UPCN596
END	UPCN597
	UPCN598
	UPCN599
	UPCN600
	UPCN601

APPENDIX D

Listing of Function Subroutines

	FUNCTION ERFC(Z)	ERFC001
C	RATIONAL APPROXIMATION OF THE COMPLIMENTARY ERROR FUNCTION	ERFC002
C	SEE SECTION 7.1 OF: ABRAMOWITZ AND STEGUN (1966)	ERFC003
	IF (ABS(Z).GT.7.5) GO TO 30	ERFC004
C	THE FOLLOWING IDENTITIES ARE USED TO HANDLE NEGATIVE ARGUMENTS	ERFC005
C	ERFC(Z) = 1 - ERF(Z)	ERFC006
C	ERFC(-Z) = -ERFC(Z) = 1 + ERF(Z)	ERFC007
C		ERFC008
	X = Z	ERFC009
C	NEGATIVE ARGUMENTS	ERFC010
	IF (Z.LT.0.0) X = -Z	ERFC011
	ERFC = 1.0/((1.0 + 0.070523*X + 0.042282*(X**2)	ERFC012
1	+ 0.009270*(X**3) + 0.000152*(X**4)	ERFC013
2	+ 0.000276*(X**5) + 0.000043*(X**6))**16)	ERFC014
C	NOTE: 2-ERF(X) = ERFC(-X) = ERFC(Z) FOR Z<0	ERFC015
	IF (Z.LT.0.0) ERFC = 2.0 - ERFC	ERFC016
	RETURN	ERFC017
C		ERFC018
C	FOR Z>7.5, ERFC(Z)<2.32E-22 AND IS SET TO 0	ERFC019
30	ERFC = 0.0	ERFC020
C	FOR Z < -7.5 ERFC(Z) IS SET TO 2.0	ERFC021
	ERFC = 2.0	ERFC022
	RETURN	ERFC023
	END	ERFC024

C	INVERSE COMPLIMENTARY ERROR FUNCTION	IERFO01
	SUBROUTINE IERFC(CERF,X,XLH,XRH)	IERFO02
C	INVERSE COMPLIMENTARY ERROR FUNCTION .	IERFO03
C	A REGULA FALSI ROOT-FINDING TECHNIQUE IS USED TO	IERFO04
C	LOCATE X FOR A SPECIFIED VALUE OF CERF. XLH AND	IERFO05
C	XRH DEFINE THE INITIAL SEARCH INTERVAL.	IERFO06
C	SEE CARNAHAN, LUTHER AND WILKES (1969) FOR A	IERFO07
C	DISCUSSION OF THE METHOD.	IERFO08
	FLH = CERF - ERFC(XLH)	IERFO09
	FRH = CERF - ERFC(XRH)	IERFO10
10	XEST = (XLH*FRH - XRH*FLH)/(FRH - FLH)	IERFO11
	FEST = CERF - ERFC(XEST)	IERFO12
	IF(ABS(FEST).GT.1.OE-04) GO TO 20	IERFO13
	X = XEST	IERFO14
	RETURN	IERFO15
20	IF(FEST.GT.O.O.AND.FRH.GT.O.O) GO TO 30	IERFO16
	XLH = XEST	IERFO17
	FLH = CERF - ERFC(XLH)	IERFO18
	GO TO 10	IERFO19
30	XRH = XEST	IERFO20
	FRH = CERF - ERFC(XRH)	IERFO21
	GO TO 10	IERFO22
	END	IERFO23