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Rates, Constants, and Kinetics Formulations in Surface Water Quality Modeling (Second Edition)

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RATES, CONSTANTS, AND KINETICS FORMULATIONS IN SURFACE WATER QUALITY MODELING (SECOND EDITION)

By

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FOREWORD

As environmental controls become more costly to implement and the penalties of judgment errors become more severe, environmental quality management requires more efficient analytical tools based on greater knowledge of the environmental phenomena to be managed. As part of this Laboratory's research on the occurrence, movement, transformation, impact, and control of environmental contaminants, the Technology Development and Applications Branch develops management or engineering tools to help pollution control officials achieve water quality goals.

Basin planning requires a set of analysis procedures that can provide an assessment on the current state of the environment and a means of predicting the effectiveness of alternative pollution control strategies. This report contains a revised and updated compilation and discussion of rates, constants, and kinetics formulations that have been used to accomplish these tasks. It is directed toward all water quality planners who must interpret technical information from many sources and recommend the most prudent course of action that will minimize the cost of implementation of a pollutant control activity and maximize the environmental benefits to the community.

> Rosemarie C. Russo Director Environmental Research Laboratory Athens, Georgia

ABSTRACT

Recent studies are reviewed to provide a comprehensive volume on stateof-the-art formulations used in surface water quality modeling along with accepted values for rate constants and coefficients. Topics covered include: dispersion, heat budgets, dissolved oxygen saturation, reaeration, CBOD decay, NBOD decay, sediment oxygen demand, photosynthesis, pH and alkalinity, nutrients, algae, zooplankton, and coliform bacteria. Factors affecting the specific phenomena and methods of measurement are discussed in addition to data on rate constants.

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Chapter 1

INTRODUCTION

1.1 BACKGROUND

The use of mathematical models to simulate ecological and water quality interactions in surface waters has grown dramatically over the past two decades. Simulation techniques offer an integrated and relatively sound course for evaluating wasteload abatement alternatives. Predictions of system behavior based upon mathematical simulation techniques may be misleading, however, particularly if the physical mechanisms involved are not accurately represented in the model. Furthermore, even where the model does faithfully describe mechanisms in the prototype, poor results may be obtained where insufficient data are available to estimate rate constants and coefficients.

Much of the work done in the water quality modeling field has been oriented toward improvement of models--toward incorporating better numerical solution techniques, toward an expanded complement of water quality constituents simulated, and toward realistic representations of modeled physical, chemical, and biological phenomena. There is, however, a need for a document that summarizes the rate constants and coefficients (e.g., nitrification rates and reaeration rates) needed in the models. This document is intended to satisfy that need.

The first edition of this document was published seven years ago (Zison <u>et al.</u>, 1978). Because an extensive body of literature on rate constants and modeling formulations has emerged since that time, the United States Environmental Protection Agency has sponsored an updating of the manual. In addition, a workshop was held to evaluate the manual, to review the

formulations and associated coefficients and rate values, and to provide further data for the final document. As a result of the literature review and workshop, a substantially new manual has been produced.

1.2 PURPOSE AND USE OF THIS MANUAL

This manual is intended for use by practitioners as a handbook--a convenient reference on modeling formulations, constants, and rates commonly used in surface water quality simulations. Guidance is provided in selecting appropriate formulations or values of rate constants for specific applications. The manual also provides a range of coefficient values that can be used to perform sensitivity analyses. Where appropriate, measurement techniques for rate constants are also discussed.

It was impossible, however, to encompass all formulations or to examine all recent reports containing rates data. It is hoped, therefore, that the user will recognize the desirability of seeking additional sources where questions remain about formulations or values. Data used from within this volume should be recognized as representing a sampling from a larger set of data. It should also be noted that there are often very real limitations involved in using literature values for rates rather than observed system values. It is hoped that this document will find its main use as a guide in the search for "the correct value" rather than as the sole source of that value.

1.3 SCOPE AND ARRANGEMENT OF MANUAL

In preparing this manual, an attempt was made to present a comprehensive set of formulations and associated constants. In contrast to the first edition (Zison <u>et al</u>.,1978), the manual has been divided into sections containing specific topics. Following this introduction, chapters are presented that discuss the following topics:

- Physical processes of dispersion and temperature
- Dissolved oxygen

- pH and alkalinity
- Nutrients
- Algae
- Zooplankton
- Coliforms

The parameters that are addressed in this manual are those that traditionally have been the focus of water quality management and the focus for control of conventional pollutants. These include temperature, dissolved oxygen, nutrients and eutrophication, and coliform bacteria. Higher organisms (fish, benthos) are not discussed, nor are the details of higher trophic levels in ecosystem models. Also, hydrodynamic processes, although important, are not dealt with in detail.

1.4 GENERAL OBSERVATIONS ON MODEL FORMULATIONS, RATE CONSTANTS, AND COEFFICIENTS

Each rate value or expression used in a model should not be chosen as an "afterthought", but should be considered as an integral part of the modeling process. A substantial portion of any modeling effort should go into selecting specific approaches and formulations based upon the objectives of modeling, the kinds and amounts of data available, and the strengths and weaknesses of the approach or formulation. Once formulations have been selected, a significant effort should be made to determine satisfactory values for parameters. Even where the parameter is to be chosen by calibration, it is clearly important to establish whether the calibrated value is within a reasonable range or not. Recent references on model calibration include Thomann (1983), National Council on Air and Stream Improvement (1982), and Beck (1983). Users should be aware that an acceptable model calibration does not imply that the model has predictive capability. The model may contain incorrect mechanisms, and agreement between model predictions and observations could have been obtained through an unrealistic choice of parameter values. Further, the future status of the prototype may be controlled by processes not even simulated in the model.

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Values of many constants and coefficients are dependent upon the way they are used in modeling formulations. For example, while pollutant dispersion is an observable physical process, modeling this process is partly a mathematical construct. Therefore, constants that are used to represent the process (i.e., dispersion coefficients) cannot be chosen purely on the basis of physics since they also depend on the modeling For example, to determine the dispersion coefficients in a approach. model application to an estuary, both the time and length scales of the model must be considered. Whether the model is tidally averaged or simulates intra-tidal variations, and whether the model is 1-, 2-, or 3dimensional, all influence the value of the appropriate dispersion coefficient for that model. Ford and Thornton (1979) discuss scale effects in ecological models, and conclude that inconsistent scales for the hydrodynamics, chemistry, and biology may produce erroneous model predictions.

Since coefficient values are never known with certainty, modelers are constantly faced with the question of how accurately rate constants should be known. The relationship between uncertainty in coefficient values and model predictions can be evaluated by performing sensitivity analyses. For models with few parameters, sensitivity analyses are generally straightforward. However, for complex models, sensitivity analyses are no longer straightforward since many dynamic interactions are involved. Sensitivity analyses are discussed in detail in Thornton and Lessem (1976), Thornton (1983), and Beck (1983).

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Chapter 2

PHYSICAL PROCESSES

2.1 INTRODUCTION

The purpose of this chapter is to give the reader an overview of how the major physical processes are incorporated into water quality and ecosystem simulations. Since a detailed review is beyond the scope of this report, the reader is encouraged to review the articles listed in Table 2-1 which represent several of the more complete and recent reviews of the state-of-the-art in physical process modeling.

Physical processes often simulated in water guality models include flow and circulation patterns, mixing and dispersion, water temperature, and the density distribution (which is a function of temperature, salinity, and suspended solids concentrations) over the water column. It is stressed that quality predictions are very dependent upon the physical processes and how well these are represented in the water quality simulations. Despite this dependence, the modeler often is forced to make a trade-off between acceptable degree of detail in water guality vs. physical process simulation due to cost or other restrictions. It is desirable from the standpoint of both the engineer and ecosystem analyst, therefore, to select the simplest model which satisfies the temporal and spatial resolution required for water quality and/or ecosystem simulation. For example, the optimum time step for dynamic simulation of a fully-mixed impoundment would be 3-6 hours for capturing diurnal fluctuations, and daily or weekly for strongly stratified impoundments which normally exhibit slowly varying conditions. In terms of spatial resolution required, the analyst should take advantage of the possible simplifications of dominate physical characteristics (i.e., physical shape, stratified layers, mixing zones, etc.).

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2.1.1 Geometric Representation

2.1.1.1 Zero-Dimensional Models

Zero-dimensional models are used to estimate spatially averaged pollutant concentrations at minimum cost. These models predict a concentration field of the form C = g(t), where t represents time. They cannot predict the fluid dynamics of a system, and the representation is usually such that an analytical solution is possible. As an example, the simplest representation of a lake is to consider it as a continuously stirred tank reactor (CSTR).

2.1.1.2 One-Dimensional Models

Most river models use a one-dimensional representation, where the system geometry is formulated conceptually as a linear network of segments or volume sections (see Figure 2-1). Variation of water quality parameters occur longitudinally (in the x-direction) as the water is transported out of one segment and into the next. The one-dimensional approach is also a popular method for simulation of small, deep lakes, where the vertical variation of temperature and other quality parameters is represented by a network of vertically stacked horizontal slices or volume segments.

2.1.1.3 Multi-Dimensional Models

Water quality models of lakes and estuaries are often two- or threedimensional in order to represent the spatial heterogeneity of the water bodies. Depending on the system, two-dimensional representations include a vertical dimension with longitudinal segmentation for deep and narrow lakes, reservoirs, or estuaries (Figure 2-2).

Three-dimensional spatial representations have been used to model overall lake circulation patterns. Part of the reason for this need is the concern with the water quality of the near-shore zone as well as deep zones of lakes. In addition, the different water quality interactions in these zones can lead to changes in the overall lake quality that cannot be predicted without this spatial definition.

2.1.2 Temporal Variation

Ecological models are distinguished on a temporal basis as being either "dynamic" or "steady-state". A strict steady-state assumption implies that the variables in the system equations do not change with time. Forcing functions, or exogenous variables, that describe environmental conditions which are unaffected by internal conditions of the system, have constant values. Inflows and outflows are discharged to and drawn from the system at

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a constant rate and any other hydrologic phenomena are also steady. Insolation, light intensity, photoperiods, extinction coefficients, and settling rates are a few examples of additional forcing functions which are held constant in a steady-state model. Constant forcing functions represent mean conditions observed in a system, and therefore the model cannot simulate cyclic phenomena.

A wide variety of planning problems can be analyzed by use of steadystate or quasi-steady (slowly varying) mathematical models which provide the necessary spatial detail for important water quality variables. Certain phenomena can achieve steady-state conditions within a short time interval and therefore can be modeled rather easily. Steady-state or quasi-steady representations are particularly useful because of their simplicity. Examples of phenomena which have been modeled on a steady-state basis are: 1) bacterial die-off, 2) dissolved oxygen concentrations (under certain conditions), and 3) nutrient distribution and recycle.



Figure 2-2. Two-dimensional geometric representation for lake systems (Baca and Arnett, 1976).

Many water quality or ecological models for rivers and lakes are concerned with the simulation of water quality variables that have substantial temporal variation and are linked to processes and variables that vary considerably. For example, the seasonal distribution of certain biological species and related abiotic substances may be of major importance. In these instances, dynamic models are required.

The process of selecting the correct time and length scales and then matching these with an appropriate model demands both an a priori understanding of the dominate physical, chemical and biological processes occurring within the system, as well as an understanding of a given model's theoretical basis and practical application limits. Proper guidance for model selection and application best comes from a thorough review of the relevant literature appropriate to the specific problem at hand. Ford and Thornton (1979), for example, present a detailed discussion of the time and length scales appropriate for the vertical one-dimensional modeling approach for reservoirs and lakes. The references presented in Table 2-1 as well as several others cited throughout this chapter discuss model compatibility requirements for various water body types and applications.

The remainder of this chapter focuses on advective transport, dispersive transport, and the surface heat budget.

2.2 ADVECTIVE TRANSPORT

The concentration of a substance at a particular site within a system is continually modified by the physical processes of advection and dispersion which transport fluid constituents from location to location. However, the total amount of a substance in a closed system remains constant unless it is modified by physical, chemical, or biological processes. Employing a Fickian type expression for turbulent mass flux, the threedimensional advection-diffusion (mass balance) equation can be written as:

$$\frac{\partial c}{\partial t} + \frac{u\partial c}{\partial x} + \frac{v\partial c}{\partial y} + \frac{w\partial c}{\partial z} - \frac{\partial}{\partial x} \left(K_x \frac{\partial c}{\partial x}\right) - \frac{\partial}{\partial y} \left(K_y \frac{\partial c}{\partial y}\right) - \frac{\partial}{\partial z} \left(K_z \frac{\partial c}{\partial z}\right) = \Sigma S \quad (2-1)$$

where	С	<pre>= mean concentration of constituent, mass/volume</pre>
	u	<pre>= mean velocity in x-direction, length/time</pre>
	v	<pre>= mean velocity in y-direction, length/time</pre>
	W	= mean velocity in z-direction, length/time
	K,,K,,K,	<pre>= eddy diffusion coefficients, length²/time</pre>
	Σŝ	= sum of source/sink rates, mass/(volume-time)
	t	= time

Difficulties exist in trying to correctly quantify the terms in this The unsteady velocity field (u,v,w) is usually evaluated equation. separately from Equation (2-1) so that the pollutant concentration, c, can be prescribed. The complete evaluation of the velocity field involves the simultaneous solution of the momentum, continuity, hydrostatic, and state equations in three dimensions (see Leendertse and Liu, 1975; Hinwood and Wallis, 1975). Although sophisticated hydrodynamic models are available, the detail and expense of applying such models are often not justified in water quality computations, especially for long term or steady-state simulations where only average flow values are required. For example, the annual thermal cycle for a strongly stratified reservoir with a relatively low inflow to volume ratio has been successfully simulated with only a crude one-dimensional, steady-state application of mass and energy conservation principles. On the other hand, simulation of large, weakly stratified impoundments dominated by wind driven circulation may require the ultimate, full representation of the unsteady velocity field in three dimensions.

The purpose of this section is to briefly familiarize the reader with the various types of approaches used to evaluate the velocity field in water quality models. Most hydrodynamic models internally calculate hydrodynamics with relatively little user control except for specification of forcing conditions such as wind, tides, inflows, outflows and bottom friction. Thus, the following paragraphs present only a summary discussion of the approaches used, organized according to the dimensional treatment of the model.

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2.2.1 Empirical Specification of Advection

This is the crudest approach, in that the advective terms of the advection-diffusion equation (Equation 2-1) are directly specified from field data. Empirical specification is quite common in water quality models for rivers, but is also often used in steady-state or slowly-varying estuary water quality models (e.g., O'Connor <u>et al</u>. (1973)). In these types of estuary models, specification of the dispersion coefficients is critical since dispersion must account for the mixing which in reality is caused by the oscillatory tidal action. Due to the highly empirical treatment of the physical processes in such models, the model "predictions" remain valid for only those conditions measured in the field. These models cannot predict water quality variations under other conditions, thus increasing the demand on field data requirements. Examples of models representative of the above approach include O'Connor et al. (1973) and Tetra Tech (1977).

2.2.2 Zero Dimensional Models for Lakes

A coarse representation of the water system as a continuously stirred tank reactor (CSTR) is often sufficient for problem applications to some lakes where detailed hydrodynamics are not required. Since in this zero-dimensional type of representation there is only a single element, no transport direction can be specified. The quantity of flow entering and leaving the system alone determines water volume changes within the element. Examples of zero-dimensional models include lake models by Anderson <u>et al</u>. (1976).

2.2.3 One-Dimensional Models for Lakes

For lake systems with long residence times and stratification in the vertical direction, vertical one-dimensional representations are common. Horizontal layers are imposed and advective transport is assumed to occur only in the vertical direction.

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Generally the tributary inflows and outflows are assumed to enter and leave the lake at water levels of equal density. Since water is essentially incompressible the inflow is assumed to generate vertical advective flow (via the continuity equation) between all elements above the level of entry. The elements below this level, containing higher density water, are assumed to be unaffected. Examples of one-dimensional lake models include Lombardo (1972, 1973), Baca <u>et al</u>. (1974), Chen and Orlob (1975), Thomann <u>et al</u>. (1975), Imberger <u>et al</u>. (1977), HEC (1974), Markofsky and Harleman (1973), and CE-QUAL-R1 (1982).

For lake or reservoir systems exhibiting complex horizontal interflows, inflows, and outflows, semi-empirical formulations have been developed to distribute inflows and to determine the vertical location from which outflows arise, depending on stratification conditions. Examples include models by U.S. Army Corps of Engineers (1974), Baca <u>et al</u>. (1976), and Tetra Tech (1976).

2.2.4 One-Dimensional Models for Rivers

Most river models represent river systems conceptually as horizontal linear networks of segments or volume elements. The process of advection is assumed to transport a constituent horizontally by movement of the parcel of water containing the constituent. In general, there are two approaches to treat the advection in river models. One approach requires field calibration of the river flow properties by measuring flows and cross sectional geometry at each model segment over a range of flow magnitudes. A power series can then be developed for each cross section to interpolate or extrapolate for other flow events. Such an approach is especially appropriate for rivers exhibiting complex hydraulic properties (i.e., supercritical flows, cascades, etc.) and when steady state solutions are of interest. Examples of such models include Tetra Tech (1977).

A second, more rigorous approach for simulating river advection involves the simultaneous solution of the continuity and momentum equations for the portion of the river under study. This approach is considered more "predictive" than the former since empirical flow data are required only for model calibration and verification. It is also more accurate and appropriate for use in transient water quality simulations. In either case, however, geometrical data on the cross-sectional shapes of the river are required. Examples of models representative of the latter approach include Brocard and Harleman (1976), and Peterson et al. (1973).

2.2.5 <u>One-Dimensional and Pseudo-Two-Dimensional Models for Estuaries</u>

A natural extension of the one-dimensional river model has been to estuary systems, either as a one-dimensional representation for narrow estuaries or as a system of multiple interconnecting one-dimensional channels for pseudo-representation of wider or multi-channeled estuaries. In either case, advection is determined through the simultaneous solution of the continuity and momentum equations together with appropriate tidal boundary conditions. These types of models are generally quite flexible in their ability to handle multiple inflows, transient boundary conditions, and complex geometrical configurations. Two primary approaches include the "link-node" network models by Water Resources Engineers (WRE) (1972), and the finite element model (Galerkin Method) by Harleman et al. (1977).

2.2.6 Two-Dimensional Vertically Averaged Models for Lakes and Estuaries

Vertically averaged, two-dimensional models have proven to be quite useful, especially in modeling the hydrodynamics and water quality of relatively shallow estuaries and wind-driven lakes. The crucial assumption of these models is the vertically well-mixed layer that allows for vertical integration of the continuity, momentum, and mass-transport equations. Such models are frequently employed to provide the horizontal advection for water quality models since they are relatively inexpensive to operate compared to the alternatives of large scale field measurement programs or fully threedimensional model treatments. There exist well over fifty models which would fit into the two-dimensional, vertically averaged classification. Examples of models that have been widely used and publicized include Wang and Connor (1975), Leendertse (1970), Taylor and Pagenkopf (1980), and Simons (1976).

2.2.7 <u>Two-Dimensional Laterally Averaged Models for Reservoirs and</u> Estuaries

In recent years, laterally averaged models have become standard simulation techniques for reservoirs or estuaries which exhibit significant vertical and longitudinal variations in density and water quality conditions. The two-dimensional laterally averaged models require the assumption of uniform lateral mixing in the cross channel direction. Although this simplification eliminates one horizontal dimension, the solution of the motion equations in the remaining longitudinal and vertical dimensions requires a much more rigorous approach than for the twodimensional vertically averaged models. In order to correctly simulate the vertical effects of density gradients on the hydrodynamics and mass transport, both the motion (continuity and momentum) and advective-diffusion equations must be solved simultaneously. In addition, such models must also treat the vertical eddy viscosity (momentum transfer due to velocity gradients) and eddy diffusivity (mass transfer due to concentration gradients) coefficients, which are directly related to the degree of internal mixing and the density structure over the water column. Mathematical treatment of vertical diffusion and vertical momentum transfer varies greatly between models, and will be discussed further in this document. Examples of laterally averaged reservoir models include Edinger and Buchak (1979) and Norton et al. (1973). Examples of laterally averaged models developed for estuaries include Blumberg (1977), Najarian et al. (1982) and Wang (1979).

2.2.8 Three-dimensional Models for Lakes and Estuaries

Fully three-dimensional and layered models have been the subject of considerable attention over the last decade. Although still a developing field, there are a number of models which have been applied to estuary, ocean, and lake systems with moderate success. As with laterally averaged two-dimensional models, the main technical difficulty in this approach is in the specification of the internal turbulent momentum transfer and mass diffusivities, which are ideally calibrated with field

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observations, thus making availability of adequate prototype data an important consideration. An additional factor of great importance is the relatively large computation cost of running three-dimensional models, especially for long-term water quality simulations. In many cases, the effort and cost of running such models is difficult to justify from purely a water quality standpoint. However, as computational costs continue to decrease and sophistication of numerical techniques increases, such models will eventually play an important role in supplying the large scale hydrodynamic regimes in water quality simulations. Examples of the more prominent three-dimensional models include Blumberg and Mellor (1978), Leendertse and Liu (1975). Sheng and Butler (1982), Simons (1976) and King (1982).

2.3 DISPERSIVE TRANSPORT

2.3.1 Introduction

The purpose of this section is to show how dispersive transport terms are incorporated into the equations of motion and continuity by temporal and spatial averaging (a detailed discussion of this subject is also given by Fischer <u>et al.</u> (1979)). A consequence of temporal averaging of either instantaneous velocity or concentration is to produce a smoothed velocity or. concentration response curve over time. Figure 2-3 illustrates both instantaneous velocity and time-smoothed curves. The velocities V and \overline{V} are related by

$$V = \overline{V} + V' \tag{2-2}$$

The velocity component V' is a random component of velocity which vanishes when averaged over the appropriate time interval (i.e., \overline{V} ' = 0).

By averaging, the stochastic components are removed from the momentum and mass conservation equations. However, cross product terms appear in the equations, such as $\overline{V'_x V'_x}$ and $\overline{V'_x V'_y}$ in the case of the momentum equation, and $\overline{V'_x C'}$ and $\overline{V'_y C'}$ in the case of the mass conservation equation (where C' is the instantaneous concentration fluctuation, and V'_x and V'_y are the random velocity deviations in the x and y directions, respectively). In the case of the momentum equation these terms are called turbulent momentum fluxes, and in the case of the mass conservation equation they are called turbulent mass fluxes. It is through these terms that eddy viscosity and eddy diffusivity enter into the momentum and mass conservation equations.

To solve the time-smoothed equations, the time averaged cross product terms are expressed as functions of time averaged variables. Numerous empirical expressions have been developed to do this. The expressions most often applied are analogous to Newton's law of viscosity in the case of turbulent momentum transport and Fick's law of diffusion in the case of turbulent mass transfer. Expressed quantitatively these relationships are of the form:



Figure 2-3. Oscillation of velocity component about a mean value (redrawn after Bird et al., 1960).

$$\overline{PV_{x}^{\dagger}V_{y}^{\dagger}} = E \frac{\partial \overline{V}_{x}}{\partial y}$$
(2-3)

$$\overline{V_{y}^{\dagger}C^{\dagger}} = K \frac{\partial \overline{C}}{\partial y}$$
(2-4)

where E = eddy viscosity, mass/(length-time) K = eddy diffusivity, length²/time \overline{V}_x = time smoothed velocity in the x direction, length/time \overline{C} = time smoothed concentration, mass/volume ρ = mass density, mass/volume

In natural water bodies the turbulent viscosity and diffusivity given by Equations (2-3) and (2-4) swamp their counterparts on the molecular level. The relative magnitude between eddy diffusivities and molecular diffusion coefficients is depicted graphically in Figure 2-4.

In addition to temporal averaging, spatial averaging is often used to simplify three dimensional models to two or one dimensions. As an illustration consider the vertically averaged mass transport equation. Before averaging, the governing three dimensional mass transport equation is typically written as:

$$\frac{\partial c}{\partial t} + \frac{\partial (uc)}{\partial x} + \frac{\partial (vc)}{\partial y} + \frac{\partial (wc)}{\partial z} = -\frac{\partial}{\partial x}(Q_x) - \frac{\partial}{\partial y}(Q_y) - \frac{\partial}{\partial z}(Q_z)$$
(2-5)

Before spatial averaging, the local concentration and velocities can be expressed by a vertically averaged term and a deviation term:


Figure 2-4. Diffusion coefficients characteristic of various environments (redrawn after Lerman, 1971).

$$c = c_{h} + c'_{h}$$

 $u = u_{h} + u'_{h}$
 $v = v_{h} + v'_{h}$ (2-6)

where c,u,v = previously defined

c_h = vertically averaged concentration, mass/volume

$$= \frac{1}{h} \int_{0}^{h} c dz$$
 (2-7)

 u_h, v_h = vertically averaged water velocities, length/time

$$= \int_{0}^{h} u dz, \quad \int_{0}^{h} v dz \qquad (2-8)$$

 u'_{h}, v'_{h} = deviation from u_{h} , v_{h} at any point in the water column, length/time

h = local water depth, length

Equation (2-5) can now be written in its vertically averaged form:

$$\frac{\partial c_{h}}{\partial t} + \frac{\partial (u_{h}c_{h})}{\partial x} + \frac{\partial (v_{h}c_{h})}{\partial y} = -\frac{\partial}{\partial x} \int_{0}^{n} (Q_{x} + u_{h}'c_{h}')dz - \frac{\partial}{\partial y} \int_{0}^{n} (Q_{y} + v_{h}'c_{h}')dz \quad (2-9)$$

It is noted that when vertical integration is performed on the threedimensional mass conservation equation, cross product terms appear in the resulting two-dimensional equation, just as they do when temporal averaging is done because vertical gradients generally exist in <u>both</u> the concentration and velocity fields. The horizontal turbulent diffusion fluxes Q_x , Q_y are usually expressed in terms of the gradients of the vertically averaged concentration and the turbulent diffusion coefficient, which in general form are written:

$$Q_{x} = -\varepsilon_{xx} \frac{\partial c_{h}}{\partial x} - \varepsilon_{xy} \frac{\partial c_{h}}{\partial y}$$
(2-10a)

$$Q_{y} = -\varepsilon_{yx} \frac{\partial^{c} h}{\partial x} - \varepsilon_{yy} \frac{\partial^{c} h}{\partial y}$$
(2-10b)

where ε_{xx} , ε_{xy} , ε_{yx} , ε_{yy} = turbulent eddy diffusion coefficients

By analogy, the horizontal transport terms, $u'_hc'_h$ and $v'_hc'_h$, associated with vertical velocity variations (i.e., differential advection), are expressed by means of the shear dispersion coefficients:

$$u'_{h}c'_{h} = -E^{d}_{xx} \frac{\partial^{c}_{h}}{\partial x} - E^{d}_{xy} \frac{\partial^{c}_{h}}{\partial y}$$
 (2-11a)

$$v_{h}'c_{h}' = -E_{yx}^{d} \frac{\partial^{c}h}{\partial x} - E_{yy}^{d} \frac{\partial^{c}h}{\partial y}$$
 (2-11b)

where $E_{xx}^{d}, E_{xy}^{d}, E_{yx}^{d}, E_{yy}^{d}$ = shear dispersion coefficients

By combining Equations (2-10) and (2-11), the final form of the vertically averaged mass transport equation can be written as:

$$\frac{\partial c_{h}}{\partial t} + \frac{\partial (u_{h}c_{h})}{\partial x} + \frac{\partial (v_{h}c_{h})}{\partial y} = \frac{\partial}{\partial x} \left(D_{xx}h \frac{\partial c_{h}}{\partial x} + D_{xy}h \frac{\partial c_{h}}{\partial y} \right)$$
$$\frac{\partial}{\partial y} \left(D_{xy}h \frac{\partial c_{h}}{\partial x} + D_{yy}h \frac{\partial c_{h}}{\partial y} \right)$$
(2-12)

where $D_{xx}^{}, D_{xy}^{}, D_{yy}^{}$ = dispersion coefficients which account for mass transport due to both concentration and velocity gradients over the vertical.

One-dimensional mass conservation equations result when a second spatial averaging is performed. The one-dimensional equations express changes along the main flow axis. As expected, the diffusion terms are again different from their two-dimensional counterparts. Consequently, the type and magnitude of the diffusion terms appearing in the simulation equations depends not only on the water body characteristics, but the model used to simulate the water body.

2.3.2 Vertical Dispersive Transport

Vertical dispersive transport of momentum and mass becomes important in lakes or estuaries characterized by moderate to great depths. In a lake environment, vertical mixing is generally caused by wind action on the surface through which eddy turbulence is transmitted to the deeper layers by the action of shear stresses. In estuaries, typically the vertical mixing is induced by the internal turbulence driven by the tidal flows, in addition to surface wind effects. Similarly, the internal mixing in deep reservoirs is primarily caused by the flow-through action. In each environment, however, the amount of vertical mixing is controlled, to a large extent, by the degree of density stratification in the water body.

Treatment of vertical mixing processes in mathematical models is generally achieved through the specification of vertical eddy viscosity (E_v) and eddy diffusivity (K_v) terms, as previously discussed. As observed by McCutcheon (1983), however, there is little consensus on what values the vertical eddy coefficients should have and how eddy viscosity and eddy diffusivity are related. At present, the procedure for estimating these coefficients is generally limited to empirical techniques that range from specifying a constant E_v and K_v to relating to some measure of stability, i.e., the Richardson number Ri. In this approach, the ratio of the coefficients for stratified flow to the coefficients for unstratified flow is expressed as a function of stability f(s):

$$E_v/E_{vo} = f_1(s),$$
 (2-13)

$$K_v/K_{vo} = f_2(s),$$
 (2-14)

and
$$E_{vo} = Pr K_{vo}$$
 (2-15)

where $E_{vo} = kzu_*(1 - z/h)$ for shear layers and Pr = the Prandtl or Schmidt number, which is generally close to unity for open-channel shear flow (Watanabe et al., 1984).

In addition

k = von Karman's constant (~0.4), dimensionless
z = distance above the bottom, length
u_{*} = shear velocity. length/time
h = depth of flow, length

A widely used formula which relates E_v/E_{vo} to stability involves the Munk and Anderson (1948) formulation (as reported by McCutcheon (1983)):

$$E_v/E_{vo} = (1 + 10 \text{ Ri})^{-1/2}$$
 (2-16)

anđ

$$K_v/K_{vo} = (1 + 3.33 \text{ Ri})^{-3/2}$$
 (2-17)

where Ri =
$$\frac{g}{\rho} \frac{\partial \rho}{\partial z} / \left(\frac{\partial u}{\partial z} \right)^2$$
, dimensionless (2-18)
 ρ = density, mass/volume
 u = the mean horizontal velocity at a point z above the bottom,
length/time
 a = accoloration of gravity length/time²

g = acceleration of gravity.length/time'

As reported by McCutcheon (1983), in a recent review of available data for stratified water flows (Delft, 1979) Equations (2-16) and (2-17) were found to fit the data better than several other similar formulations. Models by Waldrop (1978), Harper and Waldrop (1981), Edinger and Buchak (1979), O'Connor and Lung (1981), Najarian <u>et al</u>. (1982), and Heinrich, Lick and Paul (1981) use this scheme. In some models, the coefficients and exponents in Equation (2-16) and (2-17) are not adjusted, and any discrepancies between field measurements and model predictions are attributed to the inexactness of the model. In other models, the coefficients and exponents are calibrated on a site specific basis. For model simulations of mixing through and below the thermocline, the Munk and Anderson type formulas appear to be less adequate (McCutcheon, 1983). Odd and Rodger (1978) developed site specific eddy viscosity formulations for the Great Ouse Estuary in Britain:

$$E_v/E_{vo} = (1 + bRi)^{-n}$$
 for $Ri \le 1$ (2-19)

and

$$E_v/E_{vo} = (1 + b)^{-n}$$
 for Ri >1 (2-20)

where b and n are coefficients. The depth varying Ri is used if Ri increases continuously starting at the bed and extending over 75 percent or more of the depth. Where a significant peak in Ri occurs in the vertical gradient, that peak Ri is used for all depths in the equation above. McCormick and Scavia (1981) make a correction for K_v in Lake Ontario and Lake Washington studies that is similar to corrections of E_v by Odd and Rodger. Above the hypolimnion, they apply a modification of the Kent and Pritchard (1959) equation:

$$K_{\rm v} = u_{\star} / \beta R_{\rm o} \tag{2-21}$$

where
$$R_0 = -kz^2 \frac{g}{\rho} \frac{\partial \rho}{\partial z} / u_{\star}^2$$
 (2-22)

 β = constant

Below the thermocline a constant K_v was specified for Lake Ontario. In Lake Washington, Equation (2-21) and (2-22) were applied throughout the depth. In Lake Washington bottom shear was important for mixing as opposed to deeper Lake Ontario where surface wind shear dominated the mixing process.

Several other formulations for E_v and K_v have been developed which are not based on the Munk and Anderson equations. For example, Blumberg (1977), in his laterally averaged model of the Potomac River Estuary, employed an expression for K_v which uses a ratio of Ri to a critical Ri to relate K_v to stability, where:

$$K_{v} = K_{1}^{2} z^{2} \left(\frac{1-z}{h}\right)^{2} \left|\frac{u}{z}\right| \left(1 - \frac{Ri}{Ri_{c}}\right)^{1/2}$$
(2-23)

where K_1 is a turbulence constant which must be determined by calibration, and Ri_c is the critical Richardson number, which is the value of Ri at which mixing ceases due to strong stratification. Blumberg also related E_v to K_v through the following formulation:

$$E_v = K_v (1 + Ri)$$
 for $0 < Ri < Ri_c$ (2-24a)

$$E_v = K_v = 0$$
 for $Ri \ge Ri_c$ (2-24b)

Using the above formulations, Blumberg obtained reasonably good comparisons for salinity distributions in the Potomac River.

Simons (1973) based his formulation for K_v for Lake Ontario on the results of dye diffusion experiments performed by Kullenberg <u>et al</u>. (1973) where K_v is expressed as:

$$K_{v} = C \frac{W^{2}}{N^{2}} |\frac{\partial q}{\partial z}| \qquad (2-25)$$

where C = an empirical constant, $(2 \sim 8)10^{-8}$ W = wind speed, length/time N² = Brunt-Väisälä frequency, $\frac{g}{\rho} \frac{\partial \rho}{\partial z}$, time⁻² $\frac{\partial q}{\partial z}$ = vertical shear of the current, time⁻¹

Simons also assumed that the vertical eddy viscosity coefficient was based on a similar relationship.

The above formulation is a result of experiments performed in fjords, coastal and open sea areas, as well as from Lake Ontario, and is generally valid for expressing the vertical mixing in the upper 20 m for persistent winds above 4-5 m/sec. The lower value of the numerical constant refers to the lake data and the higher value to the oceanic data.

For low and varying wind speeds Equation (2-25) will not be valid (Murthy and Okubo, 1975). In these cases the internal mixing is considered to be governed by local processes, i.e., the energy source is the kinetic energy fluctuations. Kullenberg (as reported by Murthy and Okubo (1975)) proposed the following relation for weak local winds:

$$K_v = 4.1 \times 10^{-4} q'^2 (N^2)^{-1} |\frac{\partial q}{\partial z}|$$
 (2-26)

where q'² = $v_{x}'^{2} + v_{y}'^{2}$

Equation (2-26) is representative of the vertical mixing both above and below the thermocline under conditions of low wind speeds.

Tetra Tech (1975) has used the following empirical expressions for computation of the vertical eddy thermal diffusivity, K_v , in their three-dimensional hydrodynamic simulation of Lake Ontario.

$$K_{v} = 100 \frac{|\tau_{s}|}{\rho_{0}} \left(\frac{3}{1+3.3Ri}\right)^{\frac{1}{2}}$$
(2-27)

where ρ_0 = density of fresh water at 4^oC, mass/volume τ_s = surface wind stress, mass/(length-time²).

Lake systems that are represented geometrically as a series of completely mixed horizontal slices consider advective and dispersive transport processes to occur in the vertical direction alone. Baca and Arnett (1976), in their one-dimensional hydrothermal lake model, proposed the following expression for determining the one-dimensional vertical dispersion coefficient:

$$K_v = a_1 + a_2 V_w d^{-4.6z/d}$$
 (2-28)

where	K _v	=	vertical dispersion coefficient, m ² /sec
	z	=	depth, m
	Vw	=	wind speed, m/sec
	d	=	depth of thermocline, m
	^a 1' ^a 2	=	empirical constants, m^2 /sec and m respectively

The following table of values (Table 2-2) for a_1 and a_2 , as given by Baca and Arnett (1976), were obtained from previous model applications.

		Max.		
Lake	Description	Depth (m)	a _l (m²/sec)	a ₂ (m)
American Falls	well-mixed	18	1×10^{-5}	1×10^{-4}
Lake Washington	stratified	65	1×10^{-6}	1×10^{-5}
Lake Mendota	stratified	24	5×10^{-7}	5 x 10 ⁻⁵
Lake Wingra	well-mixed	5	5×10^{-5}	2×10^{-4}
Long Lake	linearly stratified	54	5×10^{-6}	5 x 10 ⁻⁵

TABLE 2-2. VALUES FOR EMPIRICAL COEFFICIENTS a1 and a2

The vertical eddy viscosity and eddy diffusivity concepts continue to be practical and are a popular means for simplifications of the momentum and mass conservation equations. As pointed out by Sheng and Butler (1982) and McCutcheon (1983), however, a wide variety exists among the various forms of the vertical turbulence stability functions determined empirically by various investigators, and suggest that the appropriate stability function is dependent on the type of numerical scheme used and the nature of the water body under study. The wide variation in formulations is, in part, due to the attempt to fit empirical functions determined under specific field conditions to a wider range of water body types and internal mixing phenomena. Due to the possibility of applying an empirical relationship beyond its valid limits, site-specific testing of formulations for E_v and K_v will probably be required in most model applications.

The above discussion has concentrated on the eddy diffusion concept on which many models are based. However, an alternative to this approach is the mixed layer concept which has been successfully applied by numerous investigators to predict the vertical temperature regime of lakes and reservoirs. As summarized by Harleman (1982), the mixed layer or integral energy concept involves the following: the turbulent kinetic energy (TKE) generated by the surface wind stress is transported downward and acts to mix the upper water column layer. At the interface between the upper mixed layer and the lower quiescent layer, the remaining TKE, plus any that may be locally generated by interfacial shear (minus dissipation effects), is transferred into potential energy by entraining guiescent fluid from below the interface into the mixed layer. This entrainment, in addition to any vertical advective flows, determines the thickness of the mixed layer. TKE is also produced by convective currents which occur during periods of cooling, and can contribute to the mixing process. Also, the total vertical heat balance due to surface heat flux and internal absorption must be considered in evaluating the vertical density distribution and potential energy of the water column. A discussion of the mixed layer model approach can be found in Harleman (1982), French (1983) and Ford and Stefan (1980). Models based on this approach include those by Stefan and Ford (1980), Hurley-Octavio et al. (1977), Imberger et al. (1977) and CE-QUAL-R1 (1982).

2.3.3 Horizontal Eddy Diffusive Transport

Generally, horizontal eddy diffusivity is several orders of magnitude greater than the vertical eddy diffusivity (see Figure 2-4). The Journal of the Fisheries Research Board of Canada (Lam and Jacquet, 1976) reported a range of values for the horizontal diffusivity in lakes from 10^4 to 10^6 cm²/sec. Unlike diffusive transport in open-channel type flows, diffusion in open water, such as in lakes and oceanic regimes, cannot be effectively related to the mean flow characteristics (Watanabe <u>et al.</u>, 1984). Oceanic or lake turbulence represents a spectrum of different eddies resulting from

the breakdown of large-scale circulations in shore zones and by wind and wave induced circulations. Attempts to analyze this phenomenon have demonstrated that the horizontal diffusive transport, D_h depends on the length scale L of the phenomenon. The most widely used formula is the fourthirds power law:

$$D_{h} = A_{D}L^{4/3}$$
 (2-29)

where A_D is the dissipation parameter (of the order .005, with D_h in cm^2/sec). The length scale L is loosely defined depending on the nature of the diffusion phenomenon. For a waste discharge in the ocean, for example, L is often estimated based on the diffuser length, which is typically the order of a kilometer. Another example is to estimate L based on the length of the tidal excursion in estuaries or coastal areas. When using Equation (2-29) to estimate the diffusion coefficient in two or three-dimensional numerical models, the length scale is often taken as the size of the horizontal grid spacing, since this approximates the minimum scale of eddies which can be reproduced in the model.

Useful summaries of lake and ocean diffusion data are given by Yudelson (1967), Okubo (1968) and Osmidov (1968). Okubo and Osmidov (1970) have graphed the empirical relationship between the horizontal eddy diffusivity and the length scale, as shown in Figure 2-5. According to Figure 2-5:

$$\begin{split} & \mathsf{D}_{h} \approx 2 \ x \ 10^{-3} \ \mathsf{L}^{4/3} \quad \text{for } \mathsf{L} < 10^{5} \text{cm} \\ & \mathsf{D}_{h} \approx 10^{4} \qquad \qquad \text{for } 10^{5} < \mathsf{L} < 5 \ x \ 10^{5} \ \text{cm} \\ & \mathsf{D}_{h} \approx 10^{-3} \ \mathsf{L}^{4/3} \qquad \qquad \text{for } \mathsf{L} > 5 \ x \ 10^{5} \ \text{cm} \end{split} \tag{2-30}$$

where D_h is in cm²/sec and L in cm. Based on these empirical observations, it is seen that the dissipation parameter of the four-thirds law decreases at larger length scales.

A comprehensive collection of diffusion data in the ocean was presented by Okubo (1971), who proposed as best fit to all the data the relation:

$$D_{\rm h} = 0.01L^{1.15}$$
 for $10^3 \le L \le 10^8$ cm (2-31)

which is graphed in Figure 2-6. According to Christodoulou <u>et al</u>. (1976), the four-thirds law seems theoretically and experimentally acceptable for expressing the horizontal eddy diffusivity in large lakes and in the ocean, providing the length scales of interest are not of the order of the size of the energy containing eddies. In addition, the four-thirds law is not fully acceptable near the shore, due to the shoreline and bottom interference.

Two examples of the use of Equation (2-29) in lake models are in Lam and Jacquet (1976) and Lick <u>et al</u>. (1976). Lam and Jacquet obtained the following formulation for the horizontal eddy diffusivity for lakes, based on experimental results:



Figure 2-5. Dependence of the horizontal diffusion coefficient on the scale of the phenomenon (after Okubo and Osmidov (1970)).



$$D_{h} = .0056L^{1.3}$$
 (2-32)

where D_h = horizontal eddy diffusivity, cm^2/sec L = length scale of grid, cm

As reported by Lam and Jacquet, for a grid size larger than 20 km, the diffusivity is expected to be essentially constant $(10^6 \text{ cm}^2/\text{sec})$.

Lick (1976) used a similar formulation after Osmidov (1968), Stommel (1949), Orlob (1959), Okubo (1971) and Csanady (1973):

$$D_{h} = a E^{1/3} L^{4/3}$$
 (2-33)

where a = constant of proportionality, of the order 0.1

E = rate of energy dissipation per unit mass

Observations by Lick indicated values of 10^4 to 10^5 cm²/sec for D_h for the overall circulation in the Great Lakes with smaller values indicated in the near-shore regions.

The above relationships can be used as a general guide to evaluate the horizontal diffusivities in a numerical model, where the grid size may be regarded as the approximate length scale of diffusion. However, as pointed out by Murthy and Okubo (1977): (1) the data upon which these empirical relations are obtained do not represent diffusion under severe weather conditions, and thus may include a bias towards relatively mild conditions; (2) the horizontal diffusivity can vary (depending primarily upon the environmental conditions) by an order of magnitude for the same length scale of diffusion; (3) the definition of the length scale of diffusion for the horizontal diffusivity is somewhat arbitrary; and (4) the horizontal diffusivity varies by an order of magnitude between the upper and lower layers of oceans and deep lakes. Thus, to develop reliable threedimensional models the scale and stability dependence of eddy diffusivities and the large variability of the magnitude of the eddy diffusivity with depth and environmental factors (wind, waves, inflows, etc.) must somehow be incorporated into the models.

The formulations for horizontal eddy diffusivity discussed above are generally representative of empirical (physical) diffusion behavior and are most compatible with a three-dimensional approach. As previously discussed, horizontal dispersion is the "effective diffusion" that occurs in twodimensional mass transport equations that have been integrated over the depth. Thus the horizontal dispersion must account for both horizontal eddy diffusivity due to horizontal turbulence and concentration gradients, as well as the effective spreading caused by velocity and concentration variations over the vertical. In addition, any simplifications in the

velocity field used in modeling must also be accounted for in the dispersion coefficients. The less detailed the flow field is modeled, the larger the dispersion coefficient needs to be to provide for the spreading that would occur under the actual circulation (Christodoulou and Pearce, 1975). Therefore, the dispersion coefficients are characteristic not only of the flow conditions to be simulated, but more significantly of the way the process is modeled. Hence these coefficients are model-dependent and difficult to quantify in any general, theoretical manner. For example, many two-dimensional models use a constant dispersion coefficient over the whole model domain as well as over time despite the fact that dispersion changes both spatially and temporally as the circulation features change. An example of a model that uses constant dispersion coefficients is Christodoulou et al. (1976).

One two-dimensional model which utilizes variable dispersion coefficients (velocity dependent) in time and space is the finite difference model by Taylor and Pagenkopf (1981). They utilize Elder's (1959) relationship for anisotropic flow where the dispersion of a substance is proportional to the friction velocity, u_* , and the water depth, h, as follows:

$$D_r = 5.9 u_* h$$
 (2-34)

$$D_n = 0.2 u_* h$$
 (2-35)

where D_r = dispersion coefficient along the flow axis, length²/time D_n = dispersion coefficient normal to the flow axis, length²/time $u_* = \sqrt{\frac{f}{8} |\vec{U}|}$, length/time f = Darcy-Weisbach friction factor, dimensionless $|\vec{U}|$ = absolute value of mean velocity along flow axis, length/time

The above relationship is incorporated into the two dimensional mass conservation equation resulting in an anisotropic mixing process which calculates a dispersion coefficient at each time step and node as a function of the instantaneous flow conditions. The expressions used for the dispersion coefficients in the model are as follows:

$$D_{xx} = \sqrt{\frac{f}{8} (q_x^2 + q_y^2)} (5.9 - 5.7 \sin^2 \theta)$$
 (2-36)

$$D_{xy} = 11.4 \sqrt{\frac{f}{8} (q_x^2 + q_y^2)} \sin \theta \cos \theta \qquad (2-37)$$

$$D_{yy} = \sqrt{\frac{f}{8} (q_x^2 + q_y^2)} (5.9 - 5.7 \cos^2 \theta)$$
 (2-38)

where
$$D_{xx}, D_{xy}, D_{yy} = dispersion coefficients$$

 $\theta = tan^{-1} (q_y/q_x)$
 $q_x = flow in x direction$
 $q_y = flow in y direction$

The above model has been successfully tested against dye diffusion experiments in Flushing Bay. New York, and in Community Harbor, Sau di Arabia (Pagenkopf and Taylor (1985); Taylor and Pagenkopf (1981)).

A two-dimensional, finite element water quality model was developed by Chen <u>et al</u>. (1979), based on the earlier model by Christodoulou <u>et al</u>. (1976). They provided for flow-dependent anisotropic dispersion coefficients by using the following relationships:

$$D_{x} = \frac{\varepsilon_{x}^{\star} q_{x}}{H^{1/6}} + \varepsilon_{x}^{\star\star}$$
(2-39)

$$D_{y} = \frac{\varepsilon_{y}^{*} q_{y}}{H^{1/6}} + \varepsilon_{y}^{**}$$
(2-40)

where ε_x^* and ε_y^* are user-defined constants as are ε_x^{**} and ε_y^{**} , the latter being provided for additional dispersion effects such as wind and marine traffic.

Whether the two-dimensional model in question utilizes constant or flow-dependent dispersion coefficients, the dispersion mechanism is usually somewhat dependent on factors typically beyond user control, such as numerical instabilities and grid size averaging effects. It is therefore stressed that any application of a two-dimensional water quality model be verified either through site-specific salinity or dye tracer data. Naturally, when performing field tracer experiments the time and length scales of the field phenomenon should be compatible with the time and length scales to be represented in the model. For example, a dye study lasting only a few hours is not valid for verification of a model using a daily computational time step. Similarly, a dye study confined to a small portion of a large lake or estuary will not allow for verification of the model over the entire system.

2.3.4 Longitudinal Dispersive Transport in Estuaries

As previously discussed, longitudinal dispersion is the "effective diffusion" that occurs in one-dimensional mass transport equations that have been integrated over the cross sectional area perpendicular to flow. This one-dimensional approach to modeling has often been applied to tidal and nontidal rivers, and to estuaries.

The magnitude of the one-dimensional dispersion coefficient in estuaries and tidal rivers is determined in part by the time scale over which the simulation is performed. The time scale specifies the interval over which quantities that generally change instantaneously, such as tidal current, are averaged. For shorter time scales the simulated hydrodynamics and therefore water quality relationships are resolved in greater detail and hence, in such models, smaller dispersion coefficients are needed than in those which, for example, average hydrodynamics over a tidal cycle.

The magnitude of the dispersion coefficient can also be expected to change as a function of location within an estuary. Since the onedimensional dispersion coefficient is the result of spatial averaging over a cross section perpendicular to flow, the greater the deviation between actual velocity and the area-averaged velocity, and between actual constituent concentrations and area-averaged concentrations, the larger will be the dispersion coefficient. These deviations are usually largest near the mouths of estuaries due to density gradients set up by the

interface between fresh and saline water. Strong tidal currents may also result in large dispersion coefficients.

Because of the time scale and location dependency of the dispersion coefficient, it is convenient to divide the discussion of dispersion into time varying and tidally averaged time expressions, and then to subdivide these according to estuarine location, i.e. the salinity intrusion region and the freshwater tidal region. The salinity intrusion region is that portion of the estuary where a longitudinal salinity gradient exists. The location of the line of demarcation between the salinity intrusion region and the freshwater tidal region varies throughout the tidal cycle, and also depends on the volume of freshwater discharge. It should also be noted that the freshwater tidal region can contain saline water, if the water is of uniform density throughout the region (TRACOR, 1971). There is at present no analytical method for predicting dispersion in the salinity intrusion region of estuaries: However, because of the presence of a conservative constituent (salinity), empirical measurements are easily performed. In the freshwater tidal region, analytical expressions have been developed, while empirical measurements become more difficult due to the lack of a naturally occurring conservative tracer. Empirical measurements can alternatively be based, however, on dye release experiments.

2.3.4.1 Time Varying Longitudinal Dispersion

A model which is not averaged over the tidal cycle is more capable of representing the mixing phenomena since it represents the time varying advection in greater detail. However, the averaging effects of spatial velocity gradients (shear) and density gradients must still be accounted for. The specification of longitudinal dispersion coefficients is closely associated with the type of mathematical techniques used in a given model. Most of the model developments for one-dimensional representation of estuaries has occurred in the early 1970's, and the most prominent techniques are summarized below.

The "link-node" or network model developed originally by WRE (1972) and commonly known as the Dynamic Estuary Model (DEM) used the basic work of Feigner and Harris (1970) to describe the numerical dispersion in the constant density region of an estuary:

$$D_{L} = C_{1} E^{1/3} L_{e}^{4/3}$$
 (2-41)

where D_L = longitudinal dispersion coefficient, length²/time E = rate of energy dissipation per unit mass L_e = mean size of eddies participating in the mixing process C₁ = function of relative channel roughness

For computational purposes, Feigner used the following simplification:

$$D_{L} = 0.042 |u| R$$
 (2-42)

where R = hydraulic radius, ft

u = absolute value of velocity, ft/sec

There exists no corresponding formulation for the longitudinal dispersion coefficient in the salinity intrusion regions of estuaries. Rather, a careful calibration procedure is required using available salinity data to prescribe the appropriate dispersion coefficients. Obviously, this approach somewhat restricts the predictive nature of such models since a substantial amount of empirical data is necessary for proper model application.

Similar versions of the DEM exist in one form or another. Not all versions, however, include the option for specification of longitudinal dispersion. This stems from the fact that considerable numerical dispersion occurs in the DEM from the first order, explicit, finite difference treatment of the advective transport terms. Feigner and Harris (1970) gave some comparisons of different weightings of the first order differencing in terms of trade-offs between numerical mixing, accuracy. and stability. Work on this problem has been done by Bella and Grenney (1970) and a numerical

estimate of this dispersion can be given by the following equation:

$$D_{num} = \frac{V}{2} \left[(1-2\nu) \Delta x - V \Delta t \right]$$
 (2-43)

where u represents the weighting coefficient assigned to the concentrations of two adjacent nodes.

This equation shows that the numerical dispersion is a function of Δx , Δt , and the velocity, V, which is a function of location and time. This equation is useful for estimating the magnitude of numerical dispersion. It illustrates the lack of control that the modeler has over this phenomena in the DEM.

Daily and Harleman (1972) developed a network water quality model for estuaries which uses a finite element numerical technique. The hydraulics are coupled to the salinity through the density-gradient terms in the manner formulated by Thatcher and Harleman (1972). The high accuracy finite element Galerkin weighted residuals technique is relatively free of artificial numerical dispersion. The longitudinal dispersion formulation combines both the vertical shear effect and the vertical density-induced circulation effect through the following expression:

$$D(x,t) = K \left| \frac{\partial S}{\partial x} \right| + m D_{T}$$
 (2-44)

- 9 = s/s_o where s(x,t) is the spatial and temporal distribution of salinity, ppm
 - = ocean salinity, ppm
- $s_0 = oce$ x = x/L

L = length of estuary, ft (to head of tide)

- D_{T} = Taylor's dispersion coefficient in ft²/sec = 77 u nR_h^{5/6}
- u = u(x,t) tidal velocity, ft/sec

n	= Manning's friction coefficient
R _h	= hydraulic radius, ft.
ĸ	= estuary dispersion parameter in ft ² /sec = u _o L/1000
u_	= maximum ocean velocity at the ocean entrance, ft/sec
m	= a multiplying factor for bends and channel
	irregularities

One-dimensional, time varying modeling using this expression has been performed for several estuaries, a recent example being an application (Thatcher and Harleman, 1978) to the Delaware Estuary wherein the timevarying calculations were made for a period of an entire year in order to provide a model for testing different water management policies.

For real time simulations in the constant density region of estuaries and tidal rivers, the following expression has been proposed (TRACOR, 1971):

$$D_{\rm L} = 100 \, {\rm n} \, U_{\rm max} \, {\rm R}_{\rm H}^{5/6}$$
 (2-45)

The determination of real time dispersion coefficients in the salinity intrusion region requires field data on salinity distribution. Once the field data have been collected, the magnitudes of the dispersion coefficients can be found by fitting the solution of the salinity mass transport equation to the observed data. As reported in TRACOR (1971), this technique has been applied to the Rotterdam Waterway, an estuary of almost uniform depth and width. The longitudinal dispersion coefficient was found to be a function of x, the distance measured from the mouth (ft), as follows:

$$D_{L} = 13000 \left(1 - \frac{x}{L}\right)^{3}$$
 (2-46)

L = length of entire tidal region of the estuary.

At the estuary mouth, D_{L} was found to be 13,000 ft²/sec or 40 mi²/day (1.2 x 10⁷ cm²/sec) by using the technique described above. Under the same conditions in a constant density region, Equation (2-38) predicts $D_{L} = 175$ ft²/sec, or 0.5 mi²/day (1.6 x 10⁵ cm²/sec). This illustrates the large difference that can be expected between the real time dispersion coefficient in the salinity intrusion region of an estuary and in the constant density region. For more detailed discussions of real time longitudinal dispersion in estuaries, see Holley et al. (1970) and Fischer et al. (1979).

2.3.4.2 Steady State Longitudinal Dispersion

For tidally averaged or net nontidal flow simulations, the dispersion coefficients must somehow include the effects of oscillatory tidal mixing which has been averaged out of the hydrodynamics representation. No known general analytical expressions exist for this coefficient. Hence, it is cautioned and emphasized that steady-state dispersion coefficients must be determined based on observed data, or based on empirical equations having parameters that are determined from observed data. This limitation exists for both the constant density and salinity intrusion regions of the estuary.

In their one-dimensional tidally averaged estuary model, Johanson et al. (1977) used an empirical expression, comprised of three principal components (tidal mixing, salinity gradient, and net freshwater advective flow) for the dispersion coefficient. The relative location in an estuary where each of these factors is significant, and their relative magnitudes, are shown in Figure 2-7.



Figure 2-7. Factors contributing to tidally averaged dispersion coefficients in the estuarine environment (modified after Zison et al., 1977).

The expression used is:

$$D_{L} = C_{1} \left(\left| \bar{u} \right| + \sigma_{u} \right) \left(\bar{y} + \sigma_{y} \right) + C_{4} \left(\frac{\Delta S}{\Delta x} \right)$$
(2-47)

where
$$D_L$$
 = tidally averaged dispersion coefficient, ft²/sec
 C_1 = tidally-induced mixing coefficient (dimensionless)
 \bar{y} = tidally averaged depth, ft
 $|\bar{u}|$ = tidally averaged absolute value of velocity, ft/sec
 σ_u = standard deviation of velocity, ft/sec
 σ_y = standard deviation of depth, ft
 C_4 = density-induced mixing coefficient, ft³/sec/mg/l-salinity
 $\frac{\Delta S}{\Delta x}$ = salinity gradient, mg/l/ft

The first term on the right side of Equation (2-47) represents mixing brought about by the oscillatory flows associated with the ebbing and flooding of the tide. The second term represents additional mixing when longitudinal salinity gradients are present. It is noted that, in practice the above formulation requires careful calibration using field salinity data due to the high empirical dependency of this relationship.

One common method of experimentally determining the tidally averaged dispersion coefficient is by the "fraction of freshwater method," as explained by Officer (1976). The expression is:

$$D_{L} = \frac{Rs}{A(ds/dx)} = \frac{R(f-1)}{A(df/dx)}$$
(2-48)

where D_1 = tidally averaged dispersion coefficient, ft^2/sec

- s = mean salinity at a particular location averaged over depth, mg/l
- A = cross-sectional area normal to flow, ft^2
- R = total river runoff flow rate, cfs
- f = freshwater fraction = $\frac{\sigma s}{\sigma}$, unitless
- σ = normal ocean salinity of the coastal water into which the estuary empties, mg/l
- x = distance along estuary axis, ft.

 D_L can be calculated at any location within the estuary if the river flow, cross-sectional area, and salinity or freshwater fraction distributions are known.

The above method has certain pitfalls which are pointed out by Ward and Fischer (1971) in their analysis of such an application to the Delaware Estuary. They point out that the use of a dispersion coefficient relationship, i.e., a functional relationship of dispersion to distance, which is also directly related to the measured upstream freshwater inflow. neglects entirely the basic response of the waterbody to variations in freshwater inflow. Ward and Fischer show, for example, that it may take a period of months for the estuary to adjust to a short period change in freshwater discharge and that any dispersion coefficient relationship based on a simple correlation analyses may be seriously in error.

Hydroscience (1971) has collected values of tidally averaged dispersion coefficients for numerous estuaries, and these values are shown in Table 2-3.

In his book, Officer (1976) reviews studies performed in a number of estuaries throughout the world. He discusses the dispersion coefficients which have been determined, and a summary of values for these estuaries is contained in Table 2-4. Many values were developed using the fraction of freshwater method just discussed. Additional values for the longitudinal dispersion coefficient have been summarized in Fischer et al. (1979).

2.3.4.3 The Lagrangian Method

The models discussed in previous sections of this chapter have all been based on the Eulerian concept of assigning velocities and concentrations to fixed points on a spatial grid. As previously discussed, the fixed grid approach tends to introduce a fictitious "numerical" dispersion into the mass transport solution since the length scale of the diffusion process is somewhat artificially imposed depending on the grid detail. To avoid such a problem, an alternative approach termed the Lagrangian method has been used by Fischer (1972), Wallis (1974), and Spaulding and Pavish (1984) for models of estuaries and tidal waters. Briefly, the Lagrangian method establishes marked volumes of water, distributed along the channel axis, which are moved along the channel at the mean flow velocity. Numerical diffusion is almost entirely eliminated, since there is no allocation of concentrations to specific grid points; rather, the "grid" is a set of moving points which represent the centers of the marked volumes. Longitudinal dispersion between marked volumes can be set according to appropriate empirical or theoretical diffusion behavior (Fischer et al., 1979). The Lagrangian method has been primarily applied to channelized estuaries such as the Suisun Marsh (Fischer, 1977) and Bolinas Lagoon (Fischer, 1972), and more recently has been extended by Spaulding and Pavish (1984) to simulate particulate transport in three dimensions.

Estuary	Freshwater Inflow (cfs)	Low Flow Net Nontidal Velocity (fps) Head - Mouth	Dispersion Coefficient (mi ² /day)*	(ft ² /sec)
Delaware River	2,500	0.12-1.000	5	1610
Hudson River (NY)	5,000	0.037	20	6450
East River (NY)	0	0.0	10	3230
Cooper River (SC)	10,000	0.25	30	9680
Savannah River (GA, SC)	7,000	0.7-0.17	10-20	3230-6450
Lower Raritan River (NJ)	150	0.047-0.029	5	1610
South River (NJ)	23	0.01	5	1610
Houston Ship Channel (TX)	900	0.05	27	8710
Cape Fear River (NC)	1,000	0.48-0.03	2-10	645-3230
Potomac River (VA)	550	0.006-0.003	1-10	320-3230
Compton Creek (NJ)	10	0.10-0.013	1	320
Wappinger and Fishkill Creek (NY)	2	0.004-0.001	0.5-1	160-320

TABLE 2-3. TIDALLY AVERAGED DISPERSION COEFFICIENTS FOR SELECTED ESTUARIES (from Hydroscience, 1971)

 $1 \text{ mi}^2/\text{day} = 322.67 \text{ ft}^2/\text{sec.}$

2.3.5 Dispersive Transport in Rivers

2.3.5.1 Introduction

Dispersive transport in rivers is typically, but not always, modeled using a one-dimensional equation such as:

$$\frac{\partial C}{\partial t} + \frac{U \partial C}{\partial x} = \frac{\partial}{\partial x} \left(D_L \frac{\partial C}{\partial x} \right)$$
(2-49)

where C = concentration of solute, mass/length³

- U = cross-sectional averaged velocity, length/time
- D_{L} = longitudinal dispersion coefficient, length²/time
- x = longitudinal coordinate, length
- t = time

TABLE 2-4. TIDALLY AVERAGED DISPERSION COEFFICIENTS (FROM OFFICER, 1976)

Estuary	Dispersion Coefficient Range (ft2/sec)	Comments
San Francisco Bay, CA Southern Arm Northern Arm	200-2,000 500-20,000	Measurements were made at slack water over a period of one to a few days. The fraction of freshwater method was used. Measurements were taken over three tidal cycles at 25 loca- tions.
Hudson River, NY	4,800-16,000	The dispersion coefficient was derived by assuming D _L to be constant for the reach studied, and that it varied only with flow.
		A good relationship resulted be- tween D, and flow, substantiating the assumption.
Narrows of Mercey, UK	1,430-4,000	The fraction of freshwater method was used by taking mean values of salinity over a tidal cycle at different cross sections.
Potomac River, MD	65-650	The dispersion coefficient was found to be a function of dis- tance below the Chain Bridge. Both salinity distribution studies (using the fraction of freshwater method) and dye release studies were used to determine D _L .
Severn Estuary, UK	7 5-7 50	Bowden recalculated D _L values originally determined by Stommel, who had used the fraction of freshwater method. Bowden in- cluded the freshwater inflows from tributaries, which produced the larger estimates of D _L .
Tay Estuary, UK	530-1,600	The fraction of freshwater method was used. At a given location, D was found to vary with freshwater ^L inflow rate.
Thames Estuary, UK	3,640 (high flow) 600-1000 (low flow)	Calculations were performed using the fraction of freshwater method, between 10 and 30 miles below London Bridge.
Yaquina Estuary	650-9,200 (high flow) 140-1,060 (low flow)	The dispersion coefficients for high flow conditions were substan- tially higher than for low flow conditions, at the same locations. The fraction of freshwater method was used.

Because of the difficulty of accurately solving Equation (2-49) numerically, some researchers (e.g., Jobson, 1980a; Jobson and Rathbun, 1985) have chosen a Lagrangian approach, where the coordinate system is allowed to move with the local stream velocity. Using this approach, Equation (2-49) become:

$$\frac{\partial C}{\partial t} = \frac{\partial}{\partial \xi} \left(D_{L} \frac{\partial C}{\partial \xi} \right)$$
(2-50)

The numerically troublesome advective term does not appear in Equation (2-50). In general, the equation can be solved more easily and with more accuracy than Equation (2-49).

where $\xi = x - \int^t U d\tau$

A second method used to simulate dispersive transport in rivers is to consider lateral mixing in addition to longitudinal mixing. A typical form of the two-dimensional equation is:

$$\frac{\partial C}{\partial t} + u(y) \frac{\partial C}{\partial x} = \frac{\partial}{\partial x} \left(\epsilon_{\chi} \frac{\partial C}{\partial x} \right) + \frac{\partial}{\partial y} \left(\epsilon_{y} \frac{\partial C}{\partial y} \right)$$
(2-51)

where u(y) = depth averaged velocity of water, which is a function of y, and is no longer the cross-sectional averaged velocity. length/time ɛ_x = depth averaged longitudinal diffusion coefficient, length²/time ɛ_y = depth averaged lateral diffusion coefficient, length²/time y = lateral coordinate, length

Note that longitudinal dispersion coefficient, D_L, in Equation (2-49) is not the same as the longitudinal diffusion coefficient, ε_{χ} , in Equation (2-51). Typically, D_L>> ε_{χ} .

2.3.5.2 Longitudinal Dispersion in Rivers

Fischer (1966, 1967a, 1967b, 1968) has performed much of the earlier research on longitudinal dispersion in natural channels. Prior to Fischer, Taylor (1954) studied dispersion in straight pipes and Elder (1959) studied dispersion in an infinitely wide open channel. More recently Fischer <u>et al</u>. (1979) and Elhadi <u>et al</u>. (1984) have provided a comprehensive review of dispersion processes.

Researchers have shown that Equation (2-49) is valid only after some initial mixing length, often called the Taylor length or convective period. While the convective period has been a topic of active research in the literature (e.g., Fischer, 1967a and b; McQuivey and Keefer, 1976a; Chatwin, 1980), this concept is not embodied in one-dimensional water quality models in general use.

Table 2-5 summarizes references on stream dispersion. The references include information from at least one of the following areas:

- methods to predict D₁, typically for model applications
- methods to measure D₁ from field data
- data summaries of dispersion coefficients
- approaches used to simulate dispersion in, a non-Fickian manner.

Bansal (1971), Elhadi and Davar (1976), Elhadi <u>et al</u>. (1984) also provide reviews of stream dispersion.

To date, the predictive capabilities of expressions for dispersion coefficients have not been thoroughly tested. However, it is known that the Taylor (1954) or Elder (1959) formulas do not accurately predict dispersion coefficients for natural streams. Glover (1964) found that dispersion coefficients in natural streams were likely to be 10 to 40 times higher than predicted by the Taylor or Elder equations. The lateral variation in stream velocity is the primary reason for the increased dispersion not accounted for by Taylor and Elder. Fischer (1967a) quantified the contribution of the

Reference	Comments
Taylor (1954)	D _L =10.1R _p u _* ; pipe flow.
Elder (1959)	D _L = 5.93Hu _* ; lateral velocity variation not considered.
Glover (1964)	D _L = 500Ru _* ; natural streams.
Krenkel (1960)	$D_L = 6.4H^{1.24}E^{0.3}$; two-dimensional channel.
	(E = USg)
Parker (1961)	D_{L} 14.3 $R^{3/2}$ $\sqrt{2}gS$; open channel flow.
Fischer (1967a, 1967b)	$D_{L} = \frac{U^{2}}{2} \left(\frac{\sigma_{t2}^{2} - \sigma_{t1}^{2}}{t_{2} - t_{1}} \right); \text{ concentration variances}$
	Long tails may introduce some error.
	$D_{L} = \frac{-1}{A} \int_{0}^{b} q'(y) dz \int_{0}^{y} \frac{1}{\varepsilon_{y} d(y)} dy \int_{0}^{y} q'(y) dy.$
	where q'(y) $\int_{0}^{d(y)} (U(y,z)-\bar{u})dz$
	This formula considers the effects of lateral velocity changes.
	$D_{L} = \frac{1}{2} \frac{d\sigma_{x}^{2}}{dt}$
	$D_{L} = 0.3 \overline{u'}^{2} \frac{1^{2}}{Ru_{*}}$; a simplification of the integral equation above
	Fischer also discusses another method for determining D _L called the routing procedure.
Elhadi and Davar (1976)	Reviewed many methods to predict D ₁ . Found D ₁ /(Hu*) is not a constant as reported by many researchers.
Fischer (1968)	Field measurements of D ₁ were made in the Green and Duwamish Rivers.
Bansal (1971)	$\log\left(\frac{KU_{s}D_{L}}{U^{2}H}\right) = 6.45 - 0.762 \log\left(\frac{\rho_{UH}}{\mu}\right)$
	$\log\left(\frac{KU_{s}}{U} \frac{D_{L}}{u_{\star}H}\right) = 6.467 - 0.714 \log\left(\frac{\rho u_{\star}H}{\mu}\right)$
Godfrey and Frederick (1970)	Dispersion tests were summarized in five natural streams; measured dispersion coefficients were from 4 to 35 times greater than pre- dicted by Taylor's (1954) method.
Thackston (1966)	$D_L = 7.25 Hu_* \left(\frac{U}{u_*} \right)$; 2-D channels.
	(continued)

Reference	Comments
Thackston and Krenkel (1967)	The limitations of dispersion equations which do not consider lateral velocity variations are discussed. Site specific measurements of D_L are recommended.
Miller and Richardson (1974)	In laboratory experiments, D _L varied from 0.6 ft ² /sec to 66 ft ² /sec.
McQuivey and Keefer (1974)	Dispersion coefficient data were reviewed, including hydraulic data, for 17 rivers.
	$D_{L} = 0.66 \frac{U_{3}^{3}}{C} Q_{0} / (2S_{0}W_{0})$
	$D_{L} = 0.058 \frac{Q_{o}}{S_{o}W_{o}}$
McQuivey and Keefer (1976b)	Dispersion tests performed in the Mississippi River are summarized.
Liu (1977)	$D_L = \frac{\beta Q^2}{u_* R^3}$
	$\beta \simeq 0.18 \left(\frac{\sqrt{gRS}}{U}\right)^{1.5}$
	Summary of D _L values also reported.
Fischer (1975)	$D_{L} = \frac{0.0110^2 W^2}{H_{u}}$
	Liu (1977) shows this is a special case of his formula when eta = 0.011.
Hays <u>et</u> <u>al</u> . (1966)	Several conceptual models of mass exchange with dead zones are presented and the Fickian Equation is modified to include mass transfer to and from dead zones.
Thackston and Schelle (1970)	Application of Hays <u>et al</u> . (1966) dead zone model to TVA stream data.
Day (1975)	Longitudinal dispersion of fluid particles in small mountain streams in New Zealand was investigated. It was shown that the dispersion coefficient increased with distance and never approached an asymptotic value.
Day and Wood (1976)	Longitudinal dispersion of fluid particles in the Missouri River and in a small moun- tain stream was investigated. The dis- persing particles were shown to behave differently from the Taylor type model. A method to predict dispersion was developed.
Liu and Cheng (1980)	A non-Fickian model is presented to predict stream dispersion.
	(continued)

Reference	Comments
Sabol and Nordin (1978)	A modified model of stream dispersion is presented that includes the effects of storage along the bed and banks.
Valentine and Wood (1977)	Effects of dead zones on stream dispersion are addressed
Valentine and Wood (1979)	Experimental results are provided to show how dead zones modify longitudinal dis- persion.
Rutherford, Taylor, Davies (1980)	A hybrid method is discussed to predict dispersion in the Waikato River, New Zealand.
Beltaos (1980a)	Dispersion processes in streams are reviewed and it is shown that many experimental results do not comply with Fickian dispersion theory. A non-Fickian dispersion model is proposed.
Beltaos (1982)	Dispersion in steep mountain streams is examined.
Bajraktarevic - Dobran (1982)	Fischer's methods are successfully applied to predict dispersion in mountainous streams.
Beer and Young (1983)	Methods are developed to predict dispersion in rivers including the effects of dead zones, using a (j,n,m) model.
Jobson (1980a)	The Fickian Equation is solved with a Lagrangian scheme to avoid lumping numerical dispersion with actual physical dispersion. See Jobson (1980b).
Jobson (1985) and McBride and Rutherford (1984)	Determined that D _L and coefficients for nonconservative water quality constituents could be determined simultaneously during calibration. D _L determined by this method is in good agreement with literature values (Jobson) or match D _L values determined from dye studies (McBride and Rutherford).
Jobson and Rathbun (1985)	Numerical dispersion minimized with a Lagrangian routing procedure that provides more consistent estimates of D ₁ than the method of moments for pool and riffle streams. Applying this procedure to peak dye concentrations yielded D ₁ to within 10%
	of estimates based on the entire concentration-time curves.
	(continued)

Footnotes:	
A	= cross-sectional area
ь	= channel width
C	= wave velocity
d(y)	- depth of water at y
Ε	= rate of energy dissipation per unit mass of fluid
εv	= lateral turbulent mixing coefficient
н	= stream depth
к	= regional dispersion factor
1	lateral distance from location of maximum velocity
σ_{x}^{2}	- variance of distance - concentration curves
$\hat{\sigma_{t2}^2}, \sigma_{t1}^2$	= variance of time concentration curves
$\overline{t}_2, \overline{t}_1$	= mean times of passage
ρ	= mass density of water
۹ ₀	= discharge at steady base flow
q'(y)	integral of velocity deviation on depth
R	= hydraulic radius
Rp	- pipe radius
so	 slope of energy gradient at steady base flow
U	= mean velocity of flow in reach
น่	= deviation of velocity from cross-sectional mean
υ _s	<pre>= mean velocity of flow at sampling point</pre>
u*	= shear velocity
μ	 coefficient of viscosity of water
Wo	= channel width at steady base flow

lateral velocity variation on stream dispersion.

A number of the formulas in Table 2-5 are of the type $D_L/(u_*H) = constant$. However, several researchers, including Bansal (1971). Elhadi and Davar (1976), and Beltaos (1978a) have shown that the ratio $D_L/(u_*H)$ is not a constant. Figure 2-8 shows this ratio can vary by several orders of magnitude.

Two widely used methods of predicting the longitudinal dispersion coefficients were developed by Liu (1977) and Fischer (1975) and are shown in Table 2-5. Liu showed that Fischer's method is identical to his own when β = 0.011.

Although numerous researchers (e.g., Sabol and Nordin, 1978) have shown how to include the effects of dead zones on dispersive transport, this refinement does not yet appear to be in general use in water quality models today. In fact, some water quality models do not include dispersion at all (at least physical dispersion; numerical dispersion may be present, depending on the solution technique used).

Dispersion can be neglected in certain circumstances with very little effect on the predicted concentration distributions. Thomann (1973), Li (1972), and Ruthven (1971) have investigated the influence of dispersion. Ruthven gave a particularly simple expression for a pollutant which decays at a rate k. If

$$\frac{kD_{L}}{U^{2}} < \frac{1}{23} = .04$$

then the concentration profile will be affected by no more than 10 percent if dispersion is ignored. Consider, for example, a decaying pollutant with k = 0.5/day in a stream where U = 1 fps and D_L = 500 ft²/sec. The ratio kD_L/U^2 =.003, which indicates that dispersion can be ignored. This guideline assumes that the pollutant is being continuously released and conditions are at steady state. The basic presumption is that if the concentration gradient is small enough, the dispersive transport is also small, and

- Godfrey and Frederick (1970)
- △ Glover (1964), rectangular flume
- ▲ Glover (1964), triangular flume
- Glover (1964), South Platte River
- Glover (1964), Mohawk River
- Yotsukura et. al. (1970), Missouri River
- Fischer, Sacramento River (see Sooky, 1969)
- ▽ Fischer (1968), Green-Duwamish River
- + Fischer (1967), trapezoidal flume

- Smooth, meandering flume¹
- Rough, meandering flume¹
- ♦ Smooth; meandering flume²
- * Thackston and Schnelle (1969)
- Hou and Christensen (1976)
- ¹ Width/radius of curvature = 0.28
- ² Width/radius of curvature 0.14



Figure 2-8. Dispersion coefficients in streams (Beltaos, 1978a).

perhaps negligible. On the other hand when pollutants are spilled, concentration gradients are large and dispersion is not negligible.

Thomann (1973) investigated the importance of longitudinal dispersion in rivers that received time variable waste loadings, and therefore produced concentration gradients in the rivers. His results showed that for small rivers, dispersion may be important when the waste loads vary with periods of 7 days or less. For large rivers, dispersion was found to be important whenever the waste load was time-variable.

2.3.5.3 Lateral Dispersion in Rivers

Although two-dimensional water quality models are less widely used in rivers than one-dimensional models, lateral mixing has been the topic of considerable research. Models that simulate lateral mixing are particularly useful in wide rivers where the one dimensional approach may not be applicable. Vertical mixing is rarely simulated in river modeling because the time required for vertical mixing is usually very rapid compared to the time required for lateral mixing. Thermal plumes are an exception.

An example of a model that simulates lateral mixing in rivers is the RIVMIX model of Krishnappan and Lau (1982). The model is particularly useful for delineating mixing zones or regulating the rate of pollutant discharge so that concentrations outside of the mixing zones are limited to allowable values.

When lateral and longitudinal mixing are both simulated, the x and y coordinates are generally assumed to continuously change to be oriented in the longitudinal and transverse directions. Although Equation (2-51) should rigorously contain metric factors (Fukuoka and Sayre, 1973) to account for these continuous changes, modelers typically assume the metric factors are unity.

Lateral mixing coefficients are usually presented in one of the following two forms:
$$\varepsilon_y = a H u_{\star}$$
 (2-52)

or

$$D_{y} = \frac{\beta Q^{2}}{W}$$
(2-53)

where
$$\varepsilon_y$$
 = lateral mixing coefficient, length²/time
 D_y = lateral diffusion factor, length⁵/time²
H = water depth, length
 a,β = coefficients that vary from river to river
 u_* = friction velocity. length/time
Q = stream flow, length³/time
W = width of river, length

 $D_{\rm v}$ and $\varepsilon_{\rm v}$ are related by the following formula:

$$D_{y} = H^{2} Um_{x} \varepsilon_{y}$$
 (2-54)

where m_v = average metric value in x- direction (≈ 1)

Equation (2-52) is generally the most widely used of the two formulas. Equation (2-53) is used when the two-dimensional convective-diffusion equation is expressed in terms of cumulative discharge (Yotsukura and Cobb, 1972).

Table 2-6 summarizes studies of transverse mixing in streams. Data from the literature are summarized in Tables 2-7 through 2-9. Table 2-9 contains values of β for use in Equation (2-53).

Elhadi <u>et al.</u> (1984) have recently provided a detailed review of lateral mixing in rivers. They concluded that lateral mixing coefficients can be predicted with accuracy only in relatively straight channels.

Reference	Comments
Okoye (1970)	This study presented a detailed analysis of laboratory experiments of lateral mixing.
Prych (1970)	This study detailed the effects of density differences on lateral mixing.
Yotsukura, Fischer, Sayre (1970)	A lateral dispersion coefficient of 1.3 ${\rm ft}^2/{\rm sec}$ was determined for the Missouri River.
Yotsukura and Cobb (1972)	Studies of lateral mixing were performed on the South River, Atrisco Feeder Canal, Bernardo Conveyance Channel, and the Missouri River.
Holley (1975)	A two-dimensional model of contaminant transport in rivers was developed and applied to the Missouri and Clinch Rivers. ε_y was experimentally determined using
	$\varepsilon_y = \frac{U}{2} \frac{d\sigma_y^2}{dx}$
Holley and Abraham (1973)	Transverse dispersion measurements were made in the Waal and IJssel Rivers, Holland. The change of moments method was used.
Yotsukura and Sayre (1976)	Transverse cumulative discharge was used as an independent variable replacing transverse distance in the 2-D mass transport equation.
Shen (1978)	The approach of Yotsukura and Sayre (1976) was extended to include transient mixing.
Lau and Krishnappan (1981)	Field data for transverse mixing coefficients were summarized. A further extension of the approach of Yotsukura and Sayre was made. Values of $\epsilon_y/(u_xH)$ were found to depend on depth/width ratios.
Somlyody (1982)	Tracer studies were performed in five streams to predict lateral mixing coefficients. A numerical model used in the study was an extension of the work of Yotsukura and Sayre (1976).
Gowda (1978)	Transverse mixing coefficients were measured in the Grand River.
Mescal and Warnock (1978)	A study of lateral mixing in the Ottawa River produced the expression \mathbb{S}_{y} = 0.043HU.
Benedict (1978)	This study reviewed various mixing expressions.
Henry and Foree (1979)	An approximate method of two-dimensional dispersion modeling was presented.
Beltaos (1980)	Transverse mixing characteristics of three rivers in Alberta, Canada were documented by tracer tests for open water and ice covered flow conditions.
Cotton and West (1980)	Rhodamine WT dye was used to determine the transverse diffusion coefficient on a straight reach of an open channel.
Holley and Nerat (1983)	Inclusion of secondary mixing as part of a lateral diffusion coefficient was concluded to have a limited physical basis.
Demetracopoulous and Stefan (1983)	Transverse mixing was studied in wide and shallow rivers using heated discharge as a tracer. A modified method of moments was developed to compute transverse mixing coefficients.
Webel and Schatzmann (1984)	An experimental study was conducted to investigate variations in transverse mixing coefficients in straight, rectangular channels. $\epsilon_y/(u_\star H)$ was found to be constant.

 ε_y = lateral mixing coefficient

U = cross-sectional average velocity

- σ_y^2 = variance of concentration in y-direction
- $u_{\star} = shear velocity$
- H = depth

Source	Channel and Description	W (m)	W	ຢ (ສ(ຣ)	f	o /(Hu)	Comments
		((!	Ey/(nu*)	Conkients
Glover 1964	Columbia River	305	100	1.35	.034	.74	Test results and analysis approximate
Yotsukura <u>et</u> _ <u>al.</u> , 1970	Missouri River, two mild alternating bends	183	68.7	1.74	.014	.60	Flow distribution available at only two cross sections
Yotsukura and Cobb, 1972	South River, few mild bends	18.2	46.2	.21	.284	.30	Analysis by streamtube method
Sayre and Yeh, Missouri River, sinuous, 1973 severe bends		234	59.1	1.98	.015	3.30	Analysis by numerical and analytical methods. Periodical variation of E, detected; average value indicated here
Engmann and Kellerhais, 1974	Lesser Slave River, ir- regular, almost contorted meander, no bars; sinu- osity = 2.0	43.0	17.0	.65	.045	.33	Effects of transverse advection lumped together with transverse dispersion. Reanalysis of ice covered data by streamtube method gave $\mathbb{S}_y/\mathrm{Ru}_{\star}$.16
Meyer, 1977	Mobile River, mostly straight, one mild curve	430	87.2	.30	.028	7.20	Steady-state condition unlikely
Krishnappan & Lau, 1977	Meandering laboratory flume with "equilibrium bed". Planview sinu- soidal. Meander wave- length=2 #W=1.88m	.30 .30 .30 .30 .30 .30 .30	10.5 15.9 7.6 10.2 9.0 11.6 10.0	.26 .27 .31 .30 .28 .23 .32	.162 .105 .163 .208 .271 .156	:	Evaluation of Ey by a numerical simulation method. Use of constant Eygave more consistent results than laterally variable values of Ey*
Beltaos, 1978b	Athabasca River below Fort McMurray, straight with occasional islands, bars; sinousity=1.0	373	170	.95	.028	.75	Slug-injection tests; analysis by streamtube method applied to dosage (see also Beltaos 1975)
Beltaos, 1978b	Athabasca River below Athabasca, irregular meanders with occa- sional bars, islands; sinuosity=1.2	320	156	.86	.067	.41	
Beltaos, 1978b	Beaver River near Cold Lake, reqular meanders, point bars and large dunes, sinuosity=1.3	42.7	44.6	.50	.062	1.0	Steady-state concentration tests. Analysis by stream-tube method.
Beltaos (unpublished)	North Saskatchewan River below Edmonton, nearly straight, few, very mild bends with occasional bars, islands; sinuo- sity=1.0	213	137	.58	.152	.25	By steady-state concentration and slug-injection tests. Analysis by streamtube and numerical methods respectively
Beltaos (unpublished)	Bow River at Calgary, sinuous with frequent islands; mid-channel bars diagonal bars, sinu- osity=1.1	104	104	1.05	.143	.61	

TABLE 2-7. TRANSVERSE MIXING COEFFICIENTS IN NATURAL STREAMS AND CHANNELS (FROM BELTAOS, 1978a)

A f

amplitude of meanders fraction factor hydraulic radius cross-sectionally averaged velocity width depth lateral mixing coefficient

R ม พ =

εy

TABLE 2-8.SUMMARY OF FIELD DATA FOR TRANSVERSE DISPERSION COEFFICIENTS
(LAU AND KRISHNAPPEN, 1981)

Data Source	Width, in meters	W/H	Average velocizy in meters per second	Shear Velocity in meters per second	Friction factor	Dispersion Coefficient, ^E y, in meters squared per second	€,,/u , ₩	€,∕u " H	Sinuosity S
			·····	······			J		
Yotsukura and Cobb (1972) Missourí River near Blair	183.0	66.7	1.74	0.073	0.014	0.101	7.5 x 10 ⁻³	0.50	1.1
Yotsukura and Cobb (1972) South River	18.3	46.2	0.18	0.040	0.220	0.0046	6.3 x 10 ⁻³	0.29	1.0 ^a
Yotsukura and Cobb (1972) Aristo Feeder Canal	18.3	27.3	0.67	0.062	0.069	0.0093	8.2×10^{-3}	0.22	1.0 ^ª
Yotsukura and Cobb (1972) Bernado Conveyance Channel	20.1	2 8. 7	1.25	0.061	0.020	0.013	10.6×10^{-3}	0.30	1.0 ^a
Beltaos (1978a), Athabasca below Fort McMurray	a 373.0	170.0	0.95	0.056	0.028	0.092	4.4×10^{-3}	0.75	1.0 ^a
Beltaos (1978a), Athabasca River below Athabasca	320.0	156.0	0.86	0.079	0.067	0.066	2.6 x 10^{-3}	0.41	1.2
8eltaos (1978a), North Saskatchewan River below Edmonton	213.0	137.0	0.58	0.080	0.152	0.031	1.8 × 10 ⁻³	0.25	1.0 ^a
Beltaos (1978b), Bow River at Calgary	104.0	104.0	1.05	0.139	0.143	0.085	5.9 x 10 ⁻³	0.61	1.1
Beltaos (1978b), Beaver River near Cold Lake	42.7	44.6	0.50	0.044	0.062	0.042	22.4 × 10^{-3}	1.00	1.3
Sayre and Yeh (1975) Missouri River below Cooper Generation Station	234.0	59.1	1.98	0.085	D.015	1.110	55.8 x 10 ⁻³	3.30	2.1
Lau and Krishanppan (1977) Grand River below Kitchener) 59.2	117.0	0.35	0.069	0.314	0.009	2.2×10^{-3}	0.26	1.1

		Discharge, in cubic meters	Mean width, in	Mean depth, in	Mean velocity in meters	Nondimensional diffusion
Source of data	Sallent reatures	per_second	meters	meters	per second	Tactor, p
Hamdy and Kinkead (1979) St. Clair River	12.0 km straight stretch with an island	6,800.00	819.3	10.00	0.83	5.9 x 10 ⁻⁴
Glover (1964) Columbia River near Richland	0.11 km stretch with a gradual S-curve	1,235.30	304.8	3.00	1.35	4.7 x 10 ⁻⁴
Holley and Abraham (1973)Waal River	10.0 km straight stretch	1,027.75	266.1	4.70	0.82	5.3 x 10 ⁻⁴
Yotsukura and Cobb (1972) Missouri River near Blair	10.0 km stretch with mild alter- nating curve	965.60	183.0	2.74	1.74	6.6 x 10 ⁻⁴
Beltaos (1980b) Athabasca River below Fort McMurray	17.6 km stretch with occasional bars and islands	776.00	373.0	2.20	0.95	7.8 x 10 ⁻⁴
Beltaos (1980b) Athabasca River below Athabasca	17.0 km stretch with irregular meanders, occa- sional bars and islands	566.00	320.0	2.05	0.86	8.4 x 10 ⁻⁴
Holly and Abraham (1973) Ijssel River	8.6 km stretch with three al- ternating bends	269.75	69.5	4.00	0.97	23.0 x 10 ⁻⁴
Beltaos (1980b) Beaver Ríver near Cold Lake	1.5 km stretch with regular meanders, point bars and large dunes	20.5	42.7	0.96	0.50	41.0 × 10 ⁻⁴
Yotsukura and Cobb (1972) Bernardo Conve- yance Channel	2.0 km straight stretch	17.75	20.1	0.70	1.25	81.0 × 10 ⁻⁴
Gowda (1980) Grand River below Waterloo	3.4 km stretch with two alter- nating curves	12.54	57.3	0.56	0.39	10.0 × 10 ⁻⁴
Yotsukura and Cobb (1972) Atrisco Feeder Canal near Bernalillo	2.0 km straight stretch with a channel of nearly uniform cross- section	7.42	18.3	0.67	0.67	13.0 x 10 ⁻⁴
Yotsukura and Cobb (1972) South River near the Town of Wayresboro	0.4 km stretch with a few very slight bends	1.53	18.2	0.38	0.21	25.0 x 10 ⁻⁴
Gowda (1980) Boyne River below Alliston	0.2 km straight stretch	0.82	8.85	0.43	0.22	25.0 x 10 ⁻⁴

SUMMARY OF NONDIMENSIONAL DIFFUSION FACTORS IN NATURAL STREAMS (FROM GOWDA, 1984) TABLE 2-9.

Notes:

β =

^Dy = H²U m_x ₅y

W channel width Q = flow rate H = depth U = velocity m_{χ} = average value of matrix (≈ 1) in x- direction

2.3.6 Summary

The previous sections have provided a brief review on the treatment of dispersive transport in water quality models. This has included a discussion of vertical dispersion in lakes and estuaries, and horizontal (lateral and longitudinal) dispersion in lakes, estuaries, and rivers. It is readily seen that a wide variety of numerical formulations for dispersion exist in the literature. Formulations for dispersion coefficients tend to be model-dependent and are all based to some extent on general lack of a complete understanding of the highly complex turbulence induced mixing processes which exist in natural water bodies. In all cases, due to this model and empirical dependence, it is desirable to include a careful calibration and/or verification exercise using on-site field data for any water quality modeling application.

2.4 SURFACE HEAT BUDGET

The total heat budget for a water body includes the effects of inflows (rivers, discharges), outflows, heat generated by chemical-biological reactions, heat exchange with the stream bed, and atmospheric heat exchange at the water surface. In all practicality, however, the dominant process controlling the heat budget is the atmospheric heat exchange, which is the focus of the following paragraphs. In addition, however, it is also important to include the proper boundary conditions for advective exchange (e.g., rivers, thermal discharges, or tidal flows) when the relative source temperature and rate of advective exchange is great enough to affect the temperature distribution of the water body.

The transfer of energy which occurs at the air-water interface is generally handled in one of two ways in river, lake, and estuary models. A simplified approach is to input temperature values directly and avoid a more complete formulation of the energy transfer phenomena. This approach is most often applied to those aquatic systems where the temperature can be readily measured. Alternatively, and quite conveniently, the various energy transfer phenomena which occur at the air-water interface can be considered in a heat budget formulation.

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In a complete atmospheric heat budget formulation, the net external heat flux, H, is most often formulated as an algebraic sum of several component energy fluxes (e.g., Baca and Arnett, 1976; U.S. Army Corps of Engineers, 1974; Thomann <u>et al</u>., 1975; Edinger and Buchak, 1978; Ryan and Harleman, 1973; TVA, 1972). A typical expression is given as:

$$H = Q_{s} - Q_{sr} + Q_{a} - Q_{ar} - Q_{br} - Q_{e} + Q_{c}$$
(2-55)

where H = net surface heat flux +Qς = shortwave radiation incident to water surface, 30 to 300 kcal/m²/hr = reflected short wave radiation, 5 to 25 kcal/ m^2 /hr ^{†Q}sr = incoming long wave radiation from the atmosphere, 225 to ↓Qa 360 Kcal/m²/hr = reflected long wave radiation, 5 to 15 kcal/ m^2 /hr ^{†Q}ar [†]Q_{br} = back radiation emitted by the body of water, 220 to 345 kcal/m²/hr = energy utilized by evaporation, 25 to 900 kcal/ m^2 /hr άQ_e ‡0_c = energy convected to or from the body of water, -35 to 50 $kcal/m^2/hr$ at the surface The magnitudes are typical for middle latitudes of the NOTE: United States. The arrows indicate if energy is coming

These flux components can be calculated within the models from semitheoretical relations, empirical equations, and basic meteorological data. Depending on the algebraic formulation used for the net heat flux term and the particular empirical expressions chosen for each component, all or some of the following meteorological data may be required: atmospheric pressure, cloud cover, wind speed and direction, wet and dry bulb air temperatures, dew point temperature, short wave solar radiation, relative humidity, water temperature, latitude, and longitude.

into the system (\downarrow) , out of the system (\uparrow) , or both (\updownarrow) .

Estimation of the various heat flux components has been the subject of many theoretical and experimental studies in the late 1960's and early

1970's. Most of the derived equations rely heavily on empirical coefficients. These formulations have been reviewed extensively by the Tennessee Valley Authority (1972), Ryan and Harleman (1973), Edinger <u>et al</u>. (1974), and Paily <u>et al</u>. (1974). A summary of the most commonly used formulations in water quality models is given in the following sections.

2.4.1 Measurement Units

The measurement units in surface heat transfer calculations do not follow any consistent units system. For heat flux, the English system units are BTU/ft²/day. In the metric system, the units are either Kcal/m²/hr or watt/m² (1 watt = 1 joule/sec). The Langley (abbreviated Ly), equal to 1 cal/cm², also persists in usage. The following conversions are useful in this section:

	•		0				2
1	BTU/ft ² /day	=	0.131 watt/m ²	=	0.271 Ly/day	=	0.113 kcal/m ² /hr
1	watt/m ²	=	7.61 BTU/ft ² /day	=	2.07 Ly/day	=	0.86 kcal/m ² /hr
1	Ly/day	=	0.483 watt/m ²	=	3.69 BTU/ft ² /day	=	0.42 kcal/m ² /hr
1	kcal/m ² /hr	=	1.16 watt/m ²	=	2.40 Ly/day	=	8.85 BTU/ft ² /day
1	kilopascal	Ŧ	10 mb	=	7.69 mm Hg	=	0.303 in Hg
1	mb	=	0.1 kilopascal	=	0.769 mm Hg	=	0.03 in Hg
1	mm Hg	=	1.3 mb	=	0.13 kilopascal	=	0.039 in Hg
1	in Hg	=	33.0 mb	=	25.4 mm Hg	=	3.3 kilopascal

2.4.2 Net short wave Solar Radiation, Q_{sn}

Net short wave solar radiation is the difference between the incident and reflected solar radiations $(Q_s - Q_{sr})$. Techniques are available and described in the aforementioned references to estimate these fluxes as a function of meteorological data. However, in order to account for the reflection, scattering, and absorption incurred by the radiation through interaction with gases, water vapor, clouds, and dust particles, a great deal of empiricism is involved and the necessary data are relatively extensive if precision is desired.

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One of the most common simplified formulations for net short wave solar radiation (Anderson, 1954; Ryan and Harleman, 1973) is expressed as:

$$Q_{sn} = Q_s - Q_{sr} \approx 0.94 Q_{sc} (1-0.65C^2)$$
 (2-56)

where Q_{sc} = clear sky solar radiation, kcal/m²/hr C = fraction of sky covered by clouds

As reported by Shanahan (1984), Equation (2-56) is an approximation in that it assumes average reflectance at the water surface and employs clear sky solar radiation. In certain circumstances atmospheric attenuation mechanisms are much greater than normal, even under cloudless conditions. For such situations, the more complex formulae described by TVA (1972) are required.

A number of methods are available for estimating the clear sky solar radiation. TVA (1972) presents a formula for Q_{sc} as a function of the geographical location, time of year, and hour of the day. Thackston (1974) and Thompson (1975) report methods for calculating daily average values of solar radiation as a function of latitude, longitude, month, and sky cover. Hamon <u>et al</u>. (1954) have graphed the daily average insolation as a function of latitude, day of year and percent of possible hours of sunshine, and is given in Figure 2-9.

Lombardo (1972) represents the net short wave solar radiation, Q_{sn} (langleys/day), with the following expression:

$$Q_{sn} = (1-R) Q_{s}$$
 (2-57)

where Q_s = short wave radiation at the surface (langleys/day) R = reflectivity of water = 0.03, or alternately: R = Aa^B (A,B given below in Table 2-10) = sun's altitude in degrees



Figure 2-9. Clear sky solar radiation according to Hamon, Weiss and Wilson (1954)

Cloudiness	Clear	Scattered	Broken	Overcast
А	1.18	2.20	0.95	0.35
В	-0.77	-0.97	-0.75	-0.45

TABLE 2-10. VALUES FOR SHORT WAVE RADIATION COEFFICIENTS A AND B (LOMBARDO, 1972)

The WQRRS model by the U.S. Army Corps of Engineers (1974) considers the net short wave solar radiation rate $(Q_s - Q_{sr})$ as a function of sun angle, cloudiness, and the level of particulates in the atmosphere. Chen and Orlob, as reported by Lombardo (1973), determine the net short wave solar radiation by considering absorption and scattering in the atmosphere.

A final important note on calculation of the net short wave solar radiation regards the effects of shading from trees and banks primarily on stream systems or rivers with steep banks. Shading can significantly reduce the incoming solar radiation to the water surface, resulting in water temperatures much lower than those occurring in unobstructed areas. Jobson and Keefer (1979) present a method to account for the reduction of incoming solar radiation by prescribing geometric relations of vertical obstruction heights and stream widths for each subreach of their model of the Chattahoochee River.

2.4.3 Net Atmospheric Radiation, Q_{an}

The atmospheric radiation is characterized by much longer wavelengths than solar radiation since the major emitting elements are water vapor, carbon dioxide, and ozone. The approach generally adopted to compute this flux involves the empirical determination of an overall atmospheric emissivity and the use of the Stephan-Boltzman law (Ryan and Harleman, 1973). The formula by Swinbank (1963) has been adopted by many investigators for use in various water quality models (e.g., U.S. Army Corps of Engineers, 1974; Chen and Orlob, 1975; Brocard and Harleman, 1976). This

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formula was believed to give reliable values of the atmospheric radiation within a probable error to +5 percent. Swinbank's formula is:

$$Q_{an} = Q_{a} - Q_{ar} = 1.16 \times 10^{-13} (1 + 0.17C^{2}) (Ta + 460)^{6}$$
 (2-58)
where Q_{an} = net long wave atmospheric radiation, BTU/ft²/day
C = cloud cover, fraction
 T_{a} = dry bulb air temperature, ^oF

A recent investigation by Hatfield <u>et al</u>. (1983) has found that the formula by Brunt (1932) gives more accurate results over a range of latitudes of $26^{\circ}13$ 'N to $47^{\circ}45$ 'N and an elevation range of -30m to + 3,342m. Brunt's formula is:

$$Q_{an} = 2.05 \times 10^{-8} (1+0.17 c^2) (T_a + 460)^4 (1+0.149 \sqrt{e_2})$$
 (2-59)

where $Q_{an} = net long$ wave atmospheric radiation, BTU/ft²/day $e_2 = the air vapor pressure 2 meters above the water surface, mm$ Hg $<math>T_a = air temperature 2 meters above the water surface, ^OF$

2.4.4 Long Wave Back Radiation, Q_{br}

The long wave back radiation from the water surface is usually the largest of all the fluxes in the heat budget (Ryan and Harleman, 1973). Since the emissivity of a water surface (0.97) is known with good precision, this flux can be determined with accuracy as a function of the water surface temperature:

$$Q_{\rm br} = 0.97 \ \sigma T_{\rm s}^{4}$$
 (2-60)

where
$$Q_{br} = 1$$
 ong wave back radiation, cal/m²/sec
 $T_s = surface$ water temperature, ⁰K
 $\sigma = Stefan-Boltzman$ constant =1.357 x 10⁻⁸, cal/m²/sec/⁰K⁴

The U.S. Army Corps of Engineers (1974) uses the following linearization of Equation (2-60) to express the back radiation emitted by the water body:

$$Q_{\rm br} = 73.6 + 1.17 \, \text{T}$$
 (2-61)

where $T = water temperature, {}^{O}C$

In the range of 0° to 30° C, this linear function has a maximum error of less than 2.1 percent relative to Equation (2-60).

2.4.5 Evaporative Heat Flux, Q_{p}

Evaporative heat loss occurs as a result of the change of state of water from a liquid to vapor, requiring sacrifice of the latent heat of vaporization. The basic formulation used in all heat budget formulations (e.g., Ryan and Harleman, 1973; U.S. Army Corps of Engineers, 1974; Chen and Orlob, 1975; Lombardo, 1972) is:

$$Q_{\rho} = \rho L_{W} E \qquad (2-62)$$

where Q_e = heat loss due to evaporation, kcal/m²/sec ρ = fluid density, kg/m³ L_w = latent heat of vaporization, kcal/kg or L_w = 597 - 0.57 T_s E = evaporation rate, m/sec T_s = surface water temperature, ^oC

The general expression for evaporation from a natural water surface is usually written as:

$$E = (a + bW) (e_s - e_a)$$
 (2-63)

where a,b = empirical coefficients

- W = wind speed at some specified elevation above water surface, m/sec
- e_s = saturation vapor pressure at the surface water temperature, mb

Various approaches have been used to evaluate the above expression. In a very simplified approach, the empirical coefficient, a, has often been taken to be zero, while b ranges from 1×10^{-9} to 5×10^{-9} (U.S. Army Corps of Engineers, 1974). The value of e_s is a nonlinear function of the surface water temperature. However e_s can be estimated in a piecewise linear fashion as follows:

$$e_s = a_i + \beta_i T_s$$
 (2-64)

where a_i, β_i = empirical coefficients with values as given in

Table 2-11.

 T_s = surface water temperature, ^OC

Temperature Range, ^O C	a _i	β_{i}
0-1	6.05	0.522
5-10	5.10	0.710
10-15	2.65	0.954
15-20	-2.04	1.265
20-25	-9.94	1.659
25-30	-22.29	2.151
30-35	-40.63	2.761
35-40	-66.90	3.511

TABLE 2-11. VALUES FOR EMPIRICAL COEFFICIENTS

A more convenient formula for the saturation vapor pressure, e_s , is presented by Thackston (1974) as follows:

$$e_s = \exp\left[17.62 - 9501/(T_s + 460)\right]$$
 (2-65)

where e_s = saturation vapor pressure at the surface water temperature, in Hg T_s = water temperature, ^OF

The standard error of prediction of Equation (2-55) is reported by Thackston (1974) to be 0.00335.

A large number of evaporation formula exist for a natural water surface, as demonstrated in Table 2-12 (Ryan and Harleman, 1973). Detailed comparisons of these formulae by the above authors showed that the discrepancies between these formulae were not significant. Both Ryan and Harleman (1973), and TVA (1968) recommend the use of the Lake Hefner evaporation formula developed by Marciano and Harbeck (1954), which has the best data base, and has been shown to perform satisfactorily for other water bodies. The Lake Hefner formula is written as:

$$Q_e = 17 W_2 (e_s - e_2)$$
 (2-66)

It is important to note that the Lake Hefner formula was developed for lakes and may not be universally valid for streams or open channels due to physical blockage of the wind by trees, banks, etc.; and due to differences in the surface turbulence which affects the liquid film aspects of evaporation (McCutcheon, 1982). Jobson developed a modified evaporation formula which was used in temperature modeling of the San Diego Aqueduct (Jobson, 1980) and the Chattahoochee River (Jobson and Keefer, 1981). This formula is written as:

$$E = 3.01 + 1.13 W (e_s - e_a)$$
 (2-67)

Formula in Original Form	Units*	Observation Levels	Time Increments	Water Body	Formula at sea-level Meas. Ht. Spec. Units BTU/ft2/day mph, mm Hg	Remarks
E=6.25·10 ⁻⁴ W ₈ (e _s -e ₈)	cm/3 hr knots mb	8m-wind ^{8m~e} a	3 hrs Day	Lake Hefner Oklahoma 2587 acres	12.4W ₈ (e _s -e ₈) 17.2W ₂ (e _s -e ₂)	Good agreement with Lake Mead, Lake Eucumbene, Russian Lakes.
E=.00304W ₄ (e _s -e ₂)	in./day miles/day in. Hg	4m-wind 2m-e _a	Day	Lake Hefner Oklahoma 2587 acres	15.9W ₄ (e _s -e ₂) 17.5W ₂ (e _s -e ₂)	Essentially the same as the Lake Hefner Formula.
E=[.15+.108W ₂](e _s -e ₂)	mm/day m/s mb	2m-wind 2m-e _a		Ponds and small reservoirs	(43+14W ₂)(e _s -e ₂)	Based on Russian experience. Recommended by Shulyakovskiy
E=10(1+.1W ₈)(e _s -e ₈)	in./month mph in. Hg	25 ft-wind 25 ft-e _a	Monthly	Small lakes and reservoirs	(73+7.3W ₃)(e _s -e ₈) (80+10W ₂)(e _s -e ₂)	e, is obtained daily from mean morning and evening measurements of T, R _H . Increase constants by 10% if average of maximum and minimum used.
E=(300+50W)(e _s -e _a)/p	in./month mph in. Hg	8m-wind 2m-e _a	Monthly	Class A pan	(73.5+12.2W ₈)(e _s -e ₂) (73.5+14.7W ₂ (e _s -e ₂)	Data from meteorological stations. Measurement heights assumed.
E=.771[1.4650186B]x [.44+.118W](e _s -e _a) where B=atmos. press.	in./day mph in. Hg	0.5-1 ft-wind 1 inch-e _a	Daily	Pans 85 ft diameter tank 1300 acre Reservoir	(67+10W ₂)(e _s -e ₂)	Extensive pan measurements using several types of pans. Correlated with tank reservoir data:
	Formula in Original Form $E=6.25 \cdot 10^{-4} W_8(e_s-e_8)$ $E=.00304W_4(e_s-e_2)$ $E=[.15+.108W_2](e_s-e_2)$ $E=10(1+.1W_8)(e_s-e_8)$ $E=(300+50W)(e_s-e_a)/p$ E=.771[1.4650186B]x $[.44+.118W](e_s-e_a)$ where B=atmos. press.	Formula in Original Form Units* $E=6.25 \cdot 10^{-4} W_8(e_s - e_8)$ cm/3 hr knots mb $E=.00304 W_4(e_s - e_2)$ in./day miles/day in. Hg $E=.00304 W_4(e_s - e_2)$ in./day miles/day in. Hg $E=.00304 W_4(e_s - e_2)$ in./day m/s mb $E=.00304 W_4(e_s - e_2)$ mm/day m/s mb $E=.00304 W_4(e_s - e_3)$ in./month mph in. Hg $E=.00304 W_4(e_s - e_3)/p$ in./month mph in. Hg $E=.00304 W_4(e_s - e_3)/p$ in./month mph in. Hg $E=.00304 W_4(e_s - e_3)/p$ in./month mph in. Hg $E=.771[1.4650186B] x$ [.44+.118W](e_s - e_3) in./day mph in. Hg where B=atmos. press. in./day	Formula in Original FormUnits*Observation Levels $E=6.25 \cdot 10^{-4}W_g(e_s-e_g)$ $cm/3 hrknots$ $8m-wind$ $8m-e_a$ $E=.00304W_4(e_s-e_2)$ $in./day$ miles/day in. Hg $4m-wind$ $2m-e_a$ $E=.00304W_4(e_s-e_2)$ $in./day$ m/day m/s mb $2m-wind$ $2m-e_a$ $E=[.15+.108W_2](e_s-e_2)$ mm/day m/s mb $2m-wind$ $2m-e_a$ $E=10(1+.1W_g)(e_s-e_g)$ $in./month$ mph in. Hg 25 ft-wind 25 ft-e_a $E=(300+50W)(e_s-e_a)/p$ $in./month$ mph in. Hg $8m-wind$ $2m-e_a$ $E=.771[1.4650186B]x$ $[.44+.118W](e_s-e_a)$ $in./day$ mph in. Hg $0.5-1 \text{ ft-wind}$ 1 inch-e_a where B=atmos. press. $mress$ $mress$ $mress$	Formula in Original FormUnits*Observation LevelsTime Increments $E=6.25 \cdot 10^{-4}W_8(e_s-e_8)$ $cm/3 hrknotsmb8m-wind8m-e_a3 hrsDayE=.00304W_4(e_s-e_2)in./daymiles/dayin. Hg4m-wind2m-e_aDayE=[.15+.108W_2](e_s-e_2)mm/daym/smb2m-wind2m-e_aDayE=10(1+.1W_8)(e_s-e_8)in./monthmphin. Hg2m-wind25 ft-wind25 ft-e_aMonthlyE=(300+50W)(e_s-e_a)/pin./monthmphin. Hg8m-wind2m-e_aMonthlyE=.771[1.4650186B] x[.44+.118W](e_s-e_a)in./daymphin. Hg0.5-1 ft-wind1 inch-e_aDailywhere B=atmos. press.in.Hg0.5-1 ft-wind1 inch-e_aDaily$	Formula in Original FormUnits*Observation LevelsTime IncrementsWater Body $E=6.25 \cdot 10^{-4} W_g(e_s-e_g)$ cm/3 hr knots mbBm-wind Bm-e_a3 hrs DayLake Hefner Oklahoma 2587 acres $E=.00304W_4(e_s-e_2)$ in./day miles/day in. Hg4m-wind $2m-e_a$ DayLake Hefner Oklahoma 2587 acres $E=[.15+.108W_2](e_s-e_2)$ mm/day m/s mb2m-wind $2m-e_a$ DayLake Hefner Oklahoma 2587 acres $E=10(1+.1W_g)(e_s-e_g)$ in./month mph in. Hg25 ft-wind $25 ft-e_a$ MonthlySmall lakes and reservoirs $E=(300+50W)(e_s-e_a)/p$ in./month mph in. Hg $25 ft-wind$ $2m-e_a$ MonthlyClass A pan $E=.771[1.4650186B]x(.44+.118W](e_s-e_a)$ in./day mph in. Hg $0.5-1 ft-wind$ $1 inch-e_a$ DailyPans B5 ft diameter tank 1300 acree Reservoir	Formula in Original FormUnits*Observation LevelsTime IncrementsWater BodyFormula at sea-level Meas. Ht. Spec. Units BTU/ft2/day mph, mm Hq $E=6.25 \cdot 10^{-4}W_8(e_5-e_8)$ $cm/3$ hr kmbs $Bm-wind$ $Bm-e_a$ 3 hrs DayLake Hefner Ok lahoma 2587 acres $12.4W_8(e_5-e_8)$ $E=.00304W_4(e_5-e_2)$ $in./day$ miles/day in. Hg $4m-wind$ $2m-e_a$ DayLake Hefner Ok lahoma 2587 acres $15.9W_4(e_5-e_2)$ $E=[15+.108W_2](e_5-e_2)$ m/day mb $2m-wind$ $2m-e_a$ DayLake Hefner Ok lahoma

TABLE 2-12. EVAPORATION FORMULA FOR LAKES AND RESERVOIRS (RYAN AND HARLEMAN, 1973)

*For each formula, the units are for evaporation rate, wind speed, and vapor pressure.

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- where E is in mm/day
 - W = wind speed at some specified elevation above the water surface, m/sec
 - e_a = vapor pressure at the same elevation as the wind, kilopascals
 - e_s = saturation vapor pressure at the water surface temperature, kilopascals

It is noted that the wind speed function of Equation (2-67) was reduced by 30 percent during calibration of the temperature model for the Chattahoochee River (McCutcheon, 1982). The original Equation (2-67) was developed for the San Diego Aqueduct which represented substantially different climactic and exposure conditions than for the Chattahoochee River. McCutcheon (1982) notes that the wind speed function is a catchall term that must compensate for a number of difficulties which include, in part:

- Numerical dispersion in some models.
- Inaccuracies in the measurement and/or calculation of wind speed, solar and long-wave radiation, air temperature, cloud cover, and relative humidity.
- Effects of wind direction, fetch, channel width, sinuosity, bank and tree height.
- Effects of depth, turbulence, and lateral velocity distribution.
- Stability of the air moving over the stream.

2.4.6 Convective Heat Flux, Q_c

Convective heat is transferred between air and water by conduction and transported away from (or toward) the air-water interface by convection associated with the moving air mass. The convective heat flux is related to the evaporative heat flux, $Q_{\rm p}$, through the Bowen ratio:

$$R = \frac{Qc}{Qe} = (6.19 \times 10^{-4}) p \left| \frac{T_s - T_a}{e_s - e_a} \right|$$
(2-68)

where R = Bowen Ratio

p = atmospheric pressure, mb
T_a = dry bulb air temperature, ^OC
T_s = surface water temperature, ^OC
e_s = saturation vapor pressure at the surface water temperature,
 mb
e_a = vapor pressure of the overlying atmosphere, mb

The above formulation is used in the surface heat transfer budget of several models (e.g., U.S. Army Corps of Engineers, 1974; Brocard and Harleman, 1976).

2.4.7 Equilibrium Temperature and Linearization

The preceding paragraphs present methods for estimating the magnitudes of the various components of heat transfer through the water surface. Several of these components are nonlinear functions of the surface water temperature, T_s . Thus, they are most appropriately used in transient water quality simulations where the need to predict temperature variations is on the time scale of minutes or hours. However, for long term water quality simulations or for steady state simulations, it is more economical to use a linearized approach to heat transfer. As developed by Edinger and Geyer (1965), and reported by Ryan and Harleman (1973), this approach involves two concepts, that of equilibrium temperature, T_E , and surface heat exchange, K, where H can now be written as:

$$H = K (T_{s} - T_{F})$$
 (2-69)

The equilibrium temperature, T_E , is defined as that water surface temperature which, for a given set of meteorological conditions, causes the surface heat flux H, to equal zero. The surface heat exchange coefficient, K, is defined to give the incremental change of net heat exchange induced by an incremental change of water surface temperature. It varies with the surface temperature and thus should be recalculated as the water temperature changes.

2.4.7.1 Equilibrium temperature, T_E

The equilibrium temperature T_E is the temperature toward which every water body at the site will tend, and is useful because it is dependent solely upon meteorological variables at a given site. A water body at a surface temperature, T_w , less than T_E , will have a net heat input and thus will tend to increase its temperature. The opposite is true if $T_w > T_E$. Thus, the equilibrium temperature embodies all the external influences upon ambient temperatures.

Certain formulations for the equilibrium temperature have been developed which require an iterative or trial and error solution approach (Ryan and Harleman, 1973). An approximate formula for obtaining T_E has been developed by Brady <u>et al</u>. (1969) which has been shown to yield fairly accurate results:

$$T_{E} = \frac{Q_{sn}}{23 + f(W) (\beta + .255)} + T_{d}$$
(2-70)

where
$$Q_{sn}$$
 = net short wave solar radiation, BTU/ft²/day
 T_d = dew point temperature of air, ^OF
f(w) = empirical wind speed relationship
= $17W_2$ (based on Lake Hefner data), BTU/ft²/day/mm Hg
 β = proportionality factor which is a furrction of
temperature, mm Hg/^OF
 W_2 = wind speed at 2 meters above surface, mph

The expression for β is written as:

$$\beta$$
 = .255 - .0085 T^{*} + .000204 T^{*2} (2-71)

where

$$T^* = \frac{1}{2} (T_w + T_d)$$
 (2-72)

2.4.7.2 Surface Heat Exchange Coefficient, K

The surface heat exchange coefficient, K, relates the net heat transfer rate to changes in water surface temperature. An expression for K developed by Brady <u>et al</u>. (1969), (and reported by Ryan and Harleman, 1973) is:

$$K = 23 + (\beta_{W} + .255) \ 17W_{2}$$
 (2-73)

where W_2 = wind speed at 2 meters, mph

and β_w is evaluated at T_w based on Equation (2-62):

$$\beta_{\rm w} = .255 - .0085 \, {\rm T}_{\rm w} + .000204 \, {\rm T}_{\rm w}^2$$
 (2-74)

Charts giving K as a function of water surface temperature and wind speed are given by Ryan and Stolzenbach (1972), assuming an average relative humidity of 75 percent. Shanahan (1984) presents a calculation procedure to determine T_E and K from average meteorological data.

2.4.8 Heat Exchange with the Stream Bed

For most lakes, estuaries, and deep rivers, the thermal flux through the bottom is insignificant. However, as reported by Jobson (1980) and Jobson and Keefer (1979), the bed conduction term may be significant in determining the diurnal variation of temperatures in water bodies with depths of 10 ft (3m) or less. Jobson (1977) presents a procedure for accounting for bed conduction which does not require temperature measurements within the bed. Rather, the procedure estimates the heat exchange based on the gross thermal properties of the bed, including the thermal diffusivity and heat storage capacity. The inclusion of this method improved dynamic temperature simulation on the San Diego Aqueduct and the Chattahoochee River.

2.4.9 Summary

The previous section has presented a brief summary of the most frequently used formulations for surface heat exchange in numerical water quality models. These formulations are widely used and have been shown to work quite well within the normal range of meteorological and surface water conditions, provided a reasonably complete data base is available on meteorological conditions at the site of interest. Meteorological data requirements include atmospheric pressure, cloud cover, and at a known surface elevation: wind speed and direction, relative humidity, and wet and dry bulb air temperatures. Shanahan (1984) presents a useful summary of meteorological data requirements for surface heat exchange computations.

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Chapter 3

DISSOLVED OXYGEN

3.1 DISSOLVED OXYGEN SATURATION

3.1.1 Introduction

Dissolved oxygen saturation, commonly symbolized as C_s and expressed in mg/l, is a basic parameter used in a great many water quality models. Since dissolved oxygen predictions are often primary reasons for developing water quality models, accurate values for C_s are needed.

Table 3-1 illustrates the equations used to calculate saturation dissolved oxygen values in a number of water quality models. The most frequently used equation is the polynomial equation developed by Elmore and Hayes (1960) for distilled water (Equation (3-1) in Table 3-1). In this equation, neither pressure nor salinity effects are considered (pressure is assumed to be 1 atm and salinity is 0 ppt).

Effects of pressure on saturation values are expressed as a ratio of site pressure to sea level (Equation (3-5)) or as a function of elevation (Equation (3-6)). Effects of salinity (relevant to estuaries and oceanic systems) are considered in the last two model equations (Equations (3-7) and (3-8)). When used in fresh water applications, the sections of the equations in which the saline term appears reduce to zero and have no effect on the dissolved oxygen saturation. Every saturation equation, whether or not modified to include non-standard pressure or salinity, evaluates dissolved oxygen saturation as a function of temperature.

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Equation Number	Model Name (or Description)	Model Reference	Equation or Method for Dissolved Oxygen Saturation C _s (mg/l)
3-1	Limnological Model for Eutrophic Lakes and Impoundments	Baca and Arnett, 1976	$C_s = 14.652 - (0.41022 T) + (0.007991 T^2) - (7.7774x10^{-5} T^3)$ T = ${}^{0}C$
3-1	EXPLORE-1	Battelle, 1973	Same as above
3-1	Level III-Receive	Medina, 1979	Same as above
3-1	Water Quality Model for Large Lakes: Part 2: Lake Erie	Di Toro and Connolly, 1980	Same as above
3-2	WRECEV	Johnson and Duke, 1976	$C_s = 14.62 - 0.3898 T + 0.006969 T^2 - 5.897 \times 10^{-5} T^3$ T = ${}^{\circ}C$
3-3	QUAL-II	Roesner, <u>et</u> <u>al</u> ., 1981	$C_s = 24.89 - 0.4259 T + 0.003734 T^2 - 1.328 \times 10^{-5} T^3$ T = ⁰ F
3-4	CE-QUAL-R1	U.S. Army COE, 1982	$C_s = (14.6)e^{(-(0.027767 - 0.00027 T + 0.000002 T^2) T)}$ T = ^o C
3-5	One Dimensional Steady State Stream Water Quality Model	Bauer, <u>et al</u> ., 1979	C _s = (14.65241022 T + 0.007910 T ² -7.7774x10 ⁻⁵ T ³) (BP/29.92) T = ^O C BP = Barometric pressure (in.Hg)
3-5	HSPF (Release 7.0)	lmhoff, <u>et</u> <u>al</u> ., 1981	Same as above
3-6	DOSAG and DOSAG3	Duke and Masch, 1973	(14.62 - (0.3898 T) + (0.006969 T2) - (5.897 x 10-5 T3)) $\begin{bmatrix} 1.0 - (6.97 x 10-6 E) \end{bmatrix}^{5.167}$ T = ^o C E = Elevation, ft.
3-7	Pearl Harbor Version of Dynamic Estuary Model (DEM)	Genet <u>et</u> <u>al</u> ., 1974	C _s = 14.553238217 T + .0054258 T ² -CL(1.665x10 ⁻⁴ -5.866x10 ⁻⁶ T + 9.796x10 ⁻⁸ T ²) T _s = 0 C CL = Chloride concentration (ppm)
3-8	RECEIV-II	Raytheon Co., 1974, and Weiss, 1970	$C_{s} = 1.4277 \exp \left[-173.492 + 24963.39/T + 143.3483 \ln(T/100.) - 0.218492 T + S(-0.033096 + 0.00014259 T - 0.00000017 T^{2})\right]$ $T = {}^{0}K = {}^{0}C + 273.15$ S = Salinity (ppt)

TABLE 3-1. METHODS USED BY SELECTED MODELS TO PREDICT DISSOLVED OXYGEN SATURATION

3.1.2 Dissolved Oxygen Saturation As Determined by the APHA

The APHA (1985) presents a tabulation of oxygen solubility in water as a function of both chlorinity and water temperature (see Table 3-2). This table is the work of Benson and Krause (1984) who collected the data and developed the equations for conditions in which the water was in contact with water saturated air at standard pressure (1.000 atm).

Since chlorinity is related to salinity, and salinity is more often measured than chlorinity, the relationship between the two quantities is of interest. The relationship, expressed here three ways, is:

Salinity (ppt or
$$^{0}/_{00}$$
) = 0.03 + 0.001805 Chlorinity (mg/l) (3-9a) or

Salinity (ppt or
$$^{0}/_{00}$$
) = 5.572 x 10^{-4} (SC) + 2.02 x 10^{-9} (SC)² (3-9b)

where SC = specific conductance in micromhos/cm

or

Salinity = 1.80655 (chlorinity as ppt) (3-9c)

where chlorinity and salinity are as defined in the footnote to Table 3-2.

Equation (3-9b) is from USGS (1981) and Equation (3-9c) is from APHA (1985).

The APHA (1985) recommends that the concentration of oxygen in water (at different temperatures and salinity) at equilibrium with water saturated air be calculated using the equation below (Benson and Krause, 1984):

$$\ln C_{s} = -139.34411 + (1.575701 \times 10^{5}/T)$$
(3-10)
-(6.642308 × 10⁷/T²) + (1.243800 × 10¹⁰/T³)
-(8.621949 × 10¹¹/T⁴)
-Ch1[(3.1929 × 10⁻²) - (1.9428 × 10/T)
+(3.8673 × 10³/T²)]

TABLE 3-2. SOLUBILITY OF OXYGEN IN WATER EXPOSED TO WATER-SATURATED AIR AT 1.000 ATMOSPHERIC PRESSURE (APHA, 1985)

			Chlorin	ity, ppt			Difference	
Temp.	0.0	5.0	10.0	15.0	20.0	25.0	per 0.1 ppt	
in ^o C		Dissolved Oxygen, mg/l						
0.0	14.621	13.728	12.888	12.097	11.355	10.657	0.016	
1.0	14.216	13.356	12.545	11.783	11.066	10.392	0.015	
2.0	13.829	13.000	12.218	11.483	10.790	10.139	0.015	
3.0	13.460	12.660	11.906	11.195	10.526	9.897	0.014	
4.0	13.107	12.335	11.607	10.920	10.273	9.664	0.014	
5.0	12.770	12.024	11.320	10.656	10.031	9.441	0.013	
6.0	12.447	11.727	11.046	10.404	9.799	9.228	0.013	
7.0	12.139	11.442	10.783	10.162	9.576	9.023	0.012	
8.0	11.843	11.169	10.531	9.930	9.362	8.826	0.012	
9.0	11.559	10.907	10.290	9.707	9.156	8.636	0.012	
10.0	11.288	10.656	10.058	9.493	8,959	8.454	0.011	
11.0	11.027	10.415	9.835	9.287	8.769	8.279	0.011	
12.0	10.777	10.183	9.621	9.089	8.586	8.111	0.011	
13.0	10.537	9.961	9.416	8.899	8.411	7.949	0.010	
14.0	10.306	9.747	9.218	8.716	8.242	7.792	0.010	
15.0	10.084	9.541	9.027	8.540	8.079	7.642	0.010	
16.0	9.870	9.344	8.844	8.370	7.922	7.496	0.009	
17.0	9.665	9.153	8.667	8.207	7.770	7.356	0.009	
18.0	9.467	8.969	8.497	8.049	7.624	7.221	0.009	
19.0.	9.276	8.792	8.333	7.896	7.483	7.090	0.009	
20.0	9.092	8.621	8.1/4	7.749	7.346	6.964	0.009	
21.0	8.915	8.456	8.021	7.607	7.214	6.842	0.008	
22.0	8./43	8.29/	7.8/3	7.470	7.087	6,/23	0.008	
23.0	8.5/8	8.143	7.730	7.337	6.963	6.609	0.008	
24.0	8.418	7.994	7.591	7.208	6.844	6.498	0.008	
25.0	8.263	7.850	/.45/	7.083	6.728	6.390	0.007	
26.0	8.113	<u>_/./11</u>	7.327	6.962	6.615	6.285	0.007	
27.0	7.968	/.5/5	7.201	6.845	6.506	6.184	0.007	
28.0	7.827	7.444	7.079	6./31	6.400	6.085	0.007	
9.0	7.691	/.31/	6.961	6.621	6.29/	5.990	0.007	
90.0	7.559	7.194	6.845	6.513	6.19/	5.890	0.007	
31.0	7.430	/ .0/3	0.733	6.409	6.100	5.800	0.006	
32.0	7.305	0.95/	0.024	6.307	0.005	5./1/	0.006	
0.0	7.183	0.843	0.518	6.208	5.912	5.631	0.006	
04.U	/.005	6.732	6 214	6.017	5.822	5.540	0.000	
	0.950	0.024	6.314	5.017	5./34	5.404	0.006	
27 0	0.83/ 6 727	6 416	6 110	5.925	5.048	5.384	0.006	
20 0	6.620	6 316	6 025	5.833	5.304	5 228	0.006	
20.0	6 515	6 217	5 022	5.660	5.401	5.220	0.005	
10.0	6 412	6 121	5.932	5.000	5.400	5.152	0.005	

DEFINITION OF SALINITY

Although salinity has been traditionally defined as the total solids in water after all carbonates have been converted to oxides, all bromide and iodide have been replaced by chloride, and all organic matter has been oxidized, the new scale used to define salinity is based on the electrical conductivity of seawater relative to a specified solution of KCl and H₂O (UNESCO, 1981). The scale is dimensionless and the traditional dimensions of parts per thousand (i.e., mg/g of solution) no longer applies.

DEFINITION OF CHLORINITY

Chlorinity is now defined in relation to salinity as follows:

Salinity = 1.80655 (Chlorinity)

Although chlorinity is not equivalent to chloride concentration, the factor for translating a chloride determination in seawater to include bromide, for example, is only 1.0045 based on the molecular weights and the relative amounts of the two ions. Therefore, for practical purposes, chloride (in mg/g of solution) is nearly equal to chlorinity in seawater. For wastewater, a knowledge of the ions responsible for the solution's electrical conductivity is necessary to correct for the ions impact on oxygen solubility and use of the tabular value or the equation is inappropriate unless the relative composition of the wastewater is similar to seawater.

- where C = equilibrium oxygen concentration, mg/l, at 1.000 atm
 (standard pressure)
 - T = temperature $({}^{0}K) = {}^{0}C+273.150$ and ${}^{0}C$ is within 0.0 to $40.0{}^{0}C$
 - Chl = chlorinity within 0.0 to 28.0, ppt

Table 3-2 replaces the older table of previous APHA Standard Methods editions. The USGS (1981) has replaced older tables based on calculations of Whipple and Whipple (1911) with tables generated from an equation by Weiss (1970) (Equation 3-8).

The APHA (1985) recommends that saturation dissolved oxygen concentration at non-standard pressure be calculated using the following equation:

$$C'_{s} = C_{s}P\left[\frac{(1-P_{wv}/P) (1-\theta P)}{(1-P_{wv}) (1-\theta)}\right]$$
(3-11)

where C = equilibrium oxygen concentration at non-standard pressure, mg/l = equilibrium oxygen concentration at 1.000 atm, mg/l Cs P = pressure, atm, and is within 0.000 to 2.000 atm Pwv = partial pressure of water vapor, atm, which may be computed $\ln P_{wv} = 11.8571 - (3840.70/T_k) - (216961/T_k^2)$ = temperature in ^{O}K T_k = 0.000975 - $(1.426 \times 10^{-5} T_c) + (6.436 \times 10^{-8} T_c^2)$ θ = temperature in ^{O}C T_c

The expressions for P $_{\rm WV}$ and θ are also from APHA (1985).

For altitudes less than approximately 4000 feet the bracketed quantity is very nearly 1 and at these altitudes multiplying C_s by P(atm) alone results in a good approximation of C_s . A more accurate calculation of C_s

can be made by using Table 3-3. The quantity in brackets from Equation (3-11) is tabulated for temperatures between 0-40^oC and for pressures from 1.1 to 0.5 atm (Benson and Krause, 1980). As an approximation of the influence of altitude, C_s decreases about 7 percent per 2,000 feet of elevation increase.

				P atm_			
「(⁰ C)	1.1	1.0	0.9	0.8	0.7	0.6	0.5
0.0	1.0005	1.0000	0.9994	0.9987	0.9977	0.9963	0.9944
5.0	1.0007	1.0000	0.9991	0.9980	0.9966	0.9946	0.9918
LO.0	1.0010	1.0000	0.9987	0.9971	0.9950	0.9922	0.9882
L5.0	1.0015	1.0000	0.9982	0.9959	0.9929	(0.9889)	(0.9833)
20.0	1.0021	1.0000	0.9974	0.9942	(0.9901)	(0.9845)	[0.9767]
25.0	1.0029	1.0000	0.9965	0.9921	(0.9864)	(0.9787)	[0.9680]
30.0	1.0039	1.0000	0.9952	(0.9892)	(0.9814)	[0.9711]	[0.9566]
35.0	1.0053	1.0000	(0.9935)	(0.9854)	(0.9750)	[0.9610]	[0.9415]
10.0	1.0071	1.0000	(0.9913	(0.9805)	[0.9665]	[0.9479]	[0.9217]

TABLE 3-3 VALUES FOR THE BRACKETED QUANTITY SHOWN IN EQUATION 3-11 TO BE USED WITH THE CORRESPONDING TEMPERATURES AND PRESSURES (BENSON AND KRAUSE, 1980)

Explanation of Interpolation Procedure:

Linear interpolation in P and T will introduce an error $\leq 0.02\%$ in the upper and left sections of table. Interpolation using numbers in parentheses will lead to errors $\leq 0.05\%$. With the numbers in brackets, interpolation errors become larger. Either temperature or pressure may be interpolated first, as illustrated for T - 3.00° C and P = 0.67 atm by the two arrays shown below.

	Temperature Interpolated First				Pressure	Interpolate	<u>d First</u>	
	0.7	0.67	0.6		0.7	0.67	0.6	
0	0.9977		0.9963	0	0.9977	0.99728	0.9963	
3	0.99704	0.9965	0.99528	3		0.9965, a	nswer	
5	0.9966	answer	0.9946	5	0.9966	0.99600	0.9946	

Earlier the APHA (1980) calculated the effects of barometric pressure on dissolved oxygen saturation as:

$$C'_{s} = C_{s} \left(\frac{P - P_{wv}}{1 - P_{wv}} \right)$$

This is equivalent to Equation (3-11) when $\theta = 0$.

3.1.3 Comparison of Methods

Table 3-4 compares the dissolved oxygen saturation values for Equations (3-1) through (3-8) and APHA (1971) against the values in Table 3-2 from the APHA (1985), Equation (3-10). The comparisons are performed at 0.0 mg/l salinity and sea level. When the values from the equations are compared with the APHA (1985) values within the temperature range $10-30^{\circ}C^{*}$ and the maximum differences examined, four "groups" of differences appear. Values from Equation (3-8) are in the group that shows the least difference from APHA (1985): 0.03 mg/l higher than the APHA (1985) predictions. Values from Equations (3-2), (3-4), (3-6) and APHA (1971) are in the second group with differences of .07 to .11 mg/l higher than APHA (1985). Values from Equations (3-1), (3-3) and (3-5) are in the third group with differences of .11 to .13 mg/l lower than APHA (1985). Equation (3-7) produced differences that comprise the fourth group with some values > 0.4 mg/l higher than APHA (1985). Generally, the maximum differences with each equation occur at higher temperatures, when dissolved oxygen depletion may contribute to serious water quality problems.

In Table 3-5 Equations (3-7), (3-8), (3-13) and APHA (1971) (those including salinity factors) are evaluated at a chloride concentration of 20,000 mg/l at 1 atm pressure and compared to APHA (1985) values.

^{*} Typically, the temperature range in which most freshwater water quality analyses take place.

TABLE 3-4. COMPARISON OF DISSOLVED OXYGEN SATURATION VALUES FROM TEN EQUATIONS AT 0.0 mg/l SALINITY AND 1 ATM PRESSURE

Temperature			Equatio	n Number F	rom Table	31			Δρηδ	APHA(1985)
°C	(3-1)	(3-2)	(3-3)	(3-4)	(3-5)	(3-6)	(3-7)	(3-8)	(1971)	3-10
0.0	14.652	14.620	14.650	14.600	14.652	14.620	14.553	14.591	14.6	14.621
1.0	12.250	14.23/	14.248	14.204	14.250	14.23/	14.1/6	13 203	14.2	14.210
3.0	13.491	13.512	13.490	13.465	13.491	13.512	13.456	13.435	13.5	13.460
4.0	13.134	13.169	13.133	13.120	13.134	13.169	13.111	13.084	13.1	13.107
5.0	12.791	12.838	12.790	12.790	12.791	12.838	12.778	12.748	12.8	12.770
6.0	12.462	12.519	12.460	12.475	12.462	12.519	12.456	12.426	12.5	12.44/
7.U 8.0	12.145	12.213	12.144	12.1/3	12.145	12.213	12.144	12,118	12.2	12.139
9.0	11.551	11.633	11.550	11.606	11.551	11.633	11.553	11.540	11.6	11.559
10.0	11.271	11.360	11.270	11.340	11.271	11.360	11.274	11.268	11.3	11.288
11.0	11.003	11.097	11.002	11.085	11.003	11.097	11.006	11.008	11.1	11.027
12.0	10./46	10.844	10./44	10.840	10./46	10.844	10./48	10./58	10.8	10.///
14.0	10.262	10.367	10.260	10.378	10.262	10.367	10.266	10.286	10.4	10,306
15.0	10.034	10.142	10.033	10.161	10.034	10.142	10.041	10.064	10.2	10.084
16.0	9.816	9,926	9.814	9.951	9.816	9.926	9.827	9.850	10.0	9.870
17.0	9.606	9.718	9.604	9.749	9.606	9.718	9.624	9.644	9.7	9.665
18.0	9.404	9.518	9.401	9.555	9.404	9.518	9.432	9.446	9.5	9.40/
20.0	9.022	9.140	9.019	9.186	9.022	9.140	9.080	9.070	9.2	9.092
21.0	8.841	8.961	8.838	9.011	8.841	8.961	8.920	8.891	9.0	8,915
22.0	8.667	8.789	8.664	8.842	8.667	8.789	8.772	8.720	8.8	8.743
23.0	8.498	8.624	8.495	8.679	8.498	8.624	8.634	8.554	8./	8.5/8
25.0	8.176	8.309	8,172	8.367	8,176	8,309	8.390	8.238	8.4	8.263
26.0	8.021	8.160	8.017	8.219	8.021	8,160	8,285	8.088	8.2	8.113
27.0	7.871	8.015	7.866	8.075	7.871	8.015	8,190	7.943	8.1	7.968
28.0	7.723	7.875	7.719	7.935	7.723	7.875	8.106	7.802	7.9	7.827
29.0	7.579	7.739	7.5/4	7.800	7.579	7.739	8.033	7.666	7.8	7.691
30.0	7.298	7.600	7.292	7.539	7.298	7.606	7 920	7.533	7.5	7.430
32.0	7.159	7.350	7.154	7.414	7.159	7.350	7.880	7.281	7.4	7.305
33.0	7.022	7.227	7.016	7.293	7.022	7.227	7.850	7.161	7.3	7.183
34.0	6.885	7.105	6.880	7.174	6.885	7.105	7.832	7.043	7.2	7.065
35.0	6.749	6.986	6.743	7.058	6.749	6.986	7.824	6.930	7.1	6.950
36.0	6.612	6.868	6.606	6.945	6.612 6.474	6.868 6.751	/.82/	6.819 6.711	-	6.83/
37.0	0.4/4	6 635	6.329	6.726	6.335	6.635	7.866	6.606	-	6.620
39.0	6.194	6.520	6.188	6.620	6.194	6.520	7,901	6.505	-	6.315
40.0	6.051	6.404	6.045	6.517	6.051	6.404	7.948	6.405	-	6.412
					.					

Equation (3-13) is based on the data of Green and Carritt (1967). From their data Hyer <u>et al</u>. (1971) developed an expression relating C_s to both temperature and salinity. C_s is given by:

$$C_s = 14.6244 - 0.367134T + 0.0044972T^2$$

- 0.0966S + 0.00205ST + 0.0002739S² (3-13)

Temperature °C	Equation (3-7)	Number from (3-8)	Table 3-1 (3-13)	APHA (1971)	APHA (1985) (3-10)
$\begin{array}{r} \text{Temperature} \\ 0.0 \\ 1.0 \\ 2.0 \\ 3.0 \\ 4.0 \\ 5.0 \\ 6.0 \\ 7.0 \\ 8.0 \\ 9.0 \\ 10.0 \\ 11.0 \\ 12.0 \\ 13.0 \\ 14.0 \\ 15.0 \\ 16.0 \\ 17.0 \\ 18.0 \\ 19.0 \\ 20.0 \\ 21.0 \end{array}$	Equation (3-7) 11.215 10.953 10.699 10.452 10.212 9.978 9.752 9.532 9.320 9.114 8.915 8.723 8.538 8.360 8.189 8.025 7.868 7.718 7.574 7.438 7.308 7.186	Number from (3-8) 11.400 11.105 10.823 10.553 10.295 10.048 9.811 9.585 9.367 9.158 8.958 8.958 8.765 8.580 8.402 8.231 8.067 7.908 7.755 7.607 7.465 7.327 7.194	Table 3-1 (3-13) 11.492 11.203 10.924 10.653 10.391 10.139 9.895 9.661 9.435 9.218 9.011 8.812 8.623 8.442 8.270 8.108 7.954 7.809 7.674 7.809 7.674 7.547 7.429 7.321	APHA (1971) 11.3 11.0 10.8 10.5 10.3 10.0 9.8 9.6 9.4 9.6 9.4 9.2 9.0 8.8 8.6 8.5 8.3 8.1 8.0 7.8 7.7 7.6 7.4 7.3	APHA (1985) (3-10) 11.354 11.067 10.790 10.527 10.273 10.031 9.801 9.575 9.362 9.156 8.957 8.769 8.586 8.411 8.077 7.922 7.770 7.624 7.482 7.347 7.215
21.0 22.0 23.0 24.0 25.0 26.0 27.0 28.0 29.0 30.0 31.0 32.0 33.0 34.0 35.0 36.0 37.0 38.0 39.0 40.0	7.186 7.070 6.961 6.859 6.764 6.676 6.595 6.521 6.454 6.394 6.340 6.294 6.254 6.221 6.196 6.177 6.165 6.160 6.162 6.171	7.194 7.066 6.942 6.822 6.594 6.594 6.485 6.379 6.277 6.177 6.081 5.987 5.896 5.808 5.722 5.638 5.722 5.638 5.557 5.477 5.400 5.325	7.321 7.221 7.130 7.049 6.976 6.912 6.857 6.812 6.775 6.747 6.729 6.719 6.718 6.726 6.743 6.726 6.743 6.726 6.743 6.770 6.805 6.849 6.902 6.965	7.3 7.1 7.0 6.9 6.7 6.6 6.5 6.4 6.3 6.1 - - - - - - - -	7.215 7.087 6.964 6.844 6.727 6.616 6.507 6.401 6.297 6.197 6.100 6.005 5.912 5.822 5.734 5.648 5.564 5.481 5.400 5.322

TABLE 3-5. COMPARISON OF DISSOLVED OXYGEN SATURATION VALUES FROM SELECTED EQUATIONS AT A CHLORIDE CONCENTRATION OF 20,000 mg/l (36.1 ppt SALINITY) AND 1 ATM PRESSURE

where T = temperature, ${}^{O}C$ S = salinity, ppt.

The values were compared over a temperature range of $5-30^{\circ}$ C. Equation (3-8), as before, agreed closely with APHA (1985) throughout the $5-30^{\circ}$ C temperature range with a maximum difference of .022 mg/l less than APHA (1985). Equation (3-7) had differences of .08 less than and .04 mg/l greater than APHA (1985) from $5-25^{\circ}$ C and near .2 mg/l higher than APHA (1985) at 30° C. The values from the APHA (1971) (reported to the nearest tenth mg/l) had a maximum difference range of 0 to .1 mg/l higher than APHA (1985) and the fourth equation, Equation (3-13), varied the most from APHA (1985) with differences in the range of approximately .03 to 0.5 mg/l higher.

3.1.4 Methods of Measurement

Elmore and Hayes (1960) have summarized the work of numerous researchers who have measured dissolved oxygen saturation. According to Elmore and Hayes, Fox in 1909 used a gasometric technique in which a known volume of pure oxygen was exposed to a known volume of water. After equilibrium had been established the volume of oxygen above the water was determined, and the solubility calculated assuming air contained 20.90 percent oxygen.

From Fox's expression, Whipple and Whipple (1911) converted their results from milliliters per liter to parts per million. These results were tabularized, circulated and used as standards by water agencies for years, and are only now being gradually replaced with tables developed from more elaborate equations.

Benson and Krause (1984) determined the solubility of oxygen in fresh and seawater over a temperature of $0-60^{\circ}$ C using an equilibrator different from the Jacobsen Worthington-type equilibrator used in previous investigations. They felt the new apparatus minimized the uncertainties associated with methods involving thin films of liquids (Benson, <u>et al.</u>, 1979). The dissolved gas values were determined with use of a mercury manometric system. The resulting data and equations were compared to previous sets of values from Carpenter (1966), Green (1965), and Murray and Riley (1969). The APHA (1985) subsequently adopted the Benson and Krause concentrations as tabulated in Table 3-2. In earlier work involving fresh water only (Benson and Krause, 1980) the new concentration values were recommended by Mortimer (1981) for use in fresh water systems.

To date there is no "standard method" recommended by APHA to measure saturated dissolved oxygen. The laboratory methods noted in the preceeding paragraphs are sophisticated methods developed and/or modified for each research effort and are not conducive to simplier laboratory environments nor are they adaptable for field use.

Calibration of popular dissolved oxygen probes is carried out under saturation conditions by methods recommended by the instrument manufacturers in conjunction with a table such as Table 3-2. The values obtained may be verified with one of the several wet chemistry iodometric methods (or "Winkler" titrations) (APHA, 1985).

3.1.5 Summary

Notable differences exist among the results obtained by various methods used to determine saturated dissolved oxygen values under specified conditions of temperature, salinity and pressure. These discrepancies may be as high as 11 percent for high saline conditions (Table 3-5). Under conditions of zero salinity observed differences are generally less than 2 percent (Table 3-4). The accuracy of the Elmore and Hayes expression, one of the most frequently used formulas, rapidly deteriorates at water temperatures exceeding 25° C. The algorithm, Equation (3-8), used in the RECEIV-II model (Weiss, 1970 and USGS, 1981) matches the APHA (1985) data better than any formula reviewed, for both saline and freshwater conditions. The algorithm, Equation (3-10), presented in APHA (1985) and its corresponding table of saturation values, Table 3-2, are based on latest research and provide the most accurate values of C_S to date. Knowing the

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possible sources of error using any other particular formulation for C_s permits the user to decide whether they are significant in a particular study.

3.2 REAERATION

3.2.1 Introduction

Reaeration is the process of oxygen exchange between the atmosphere and a water body in contact with the atmosphere. Typically, the net transfer of oxygen is from the atmosphere and into the water, since dissolved oxygen levels in most natural waters are below saturation. However, when photosynthesis produces supersaturated dissolved oxygen levels, the net transfer is back into the atmosphere.

The reaeration process is modeled as the product of a mass-transfer coefficient multiplied by the difference between dissolved oxygen saturation and the actual dissolved oxygen concentration, that is:

$$F_{c} = k_{l} (C_{s} - C) \qquad (3-14)$$

- C = dissolved oxygen concentration, mass/volume
- C_s = saturation dissolved oxygen concentration, mass/volume
- k₁ = surface transfer coefficient, length/time

For practically all river modeling applications and for vertically mixed estuaries a depth averaged flux (F_c) , is used:

$$F_{c} = \frac{F_{c}}{H} = \frac{k_{L}}{H} (C_{s}-C)$$
 (3-15)

where H = water depth, length

In Equation 3-15 the surface transfer rate and depth are typically combined into a single term, called the reaeration rate coefficient or reaeration coefficient, denoted in the literature by k_2 or k_a :

$$k_2 = \frac{k_L}{H}$$
(3-16)

3.2.2 Reaeration in Rivers

3.2.2.1 Overview

Rivers have been the focus of the majority of reaeration research in natural waters. Some of the equations that have been developed for rivers have been successfully applied to estuaries, and is indicative of the lack of estuarine reaeration research.

Table 3-6 summarizes reaeration coefficient expressions (k_2 values) for rivers. All formulas for reaeration in Table 3-6 are depth averaged values and are in units of 1/day. The table also shows the units required for the parameters in each formula, and when possible the range of conditions used in the development of the formulas. All values of k_2 are base e, and are referenced to 20° C, unless otherwise noted. Although base e values are used directly in most modeling formulations, in the earlier days of reaeration research, k_2 values were often expressed in base 10. The relationship between base e and base 10 reaeration coefficients is:

$$k_{2_{base e}} = \ln (10)k_{2_{base 10}} = 2.303 k_{2_{base 10}}$$
(3-17)

Stream reaeration research began in earnest in the late 1950's, and continues today. The formulas that are shown in Table 3-6 are based on theory, empiricism, or a combination of the two. In the late 1960's the radioactive tracer method was introduced by Tsivoglou and Wallace (1972). The tracer method, or a modification of it, forms the basis for much of the research being conducted on reaeration today.

Author(s)	k ₂ , base e(1/day at 20 ⁰ C)	Units	Applicability
O'Connor and Dobbins (1958)	<u>12.90^{0.5} н^{1.5}</u>	U-fps H-feet	Moderately deep to deep channels; 1 '≤ H≤30', 0.5≤U≤1.6 fps; 0.05≤k ≤12.2/day. 0'Connor and Dobbins also developed a second formula for shallow streams but 0'Connor (1958) showed the differences between the two formulas was insignificant, and recommended that the first formula be used.
Churchill <u>et al</u> . (1962)	<u>11.60^{0.969} н^{1.673}</u>	U-fps H-feet	Based on observed reaeration rates below dams from which oxygen deficient water was released. 2' <u>SHS</u> 1'; 1.8SUS5 fps. Churchill <u>et al</u> . also developed other formulas, but recommended this formula.
Owens <u>et</u> al. (1964)	21.70 ^{0.67} H ^{1.85}	U-fps H-feet	Oxygen recovery monitored for six streams in England following deoxygenation with sodium sulfite. 0.1≤U≤5 fps; 0.4'≤H≤11'.
Owens <u>et</u> <u>al</u> . (1964)	23.3U ^{0.73} H ^{1.75}	U-fps H-feet	This is a second formula developed by Owens <u>et</u> <u>al</u> ., and applies for 0.1≤U≤1.8 fps; 0.4'≤H 11'.
Langbein and Durum (1967)	7.6U H ^{1.33}	U-fps H-feet	Based on synthesis of data from O'Connor-Dobbins (1958), Churchill <u>et al</u> . (1962), Kremkel and Orlob (1963), and Streeter <u>et al</u> . (1936).
Isaacs and Gaudy (1968)	8.62U H ^{1.5}	U-fps H-feet	Developed using regression analyses from data collected using.a recirculating cylindrical tank. 0.6≤U≤1.6 fps; 0.5'≤H≤1.5'.
Parkhurst and Pomeroy (1972)	<u>48.4(1+0.17F²)(SU)^{3/8} H</u>	U-m∕s S-m/m H-meters	Developed from data collected in 12 sewers and in natural streams.
Negulescu and Rojanski (1969)	$10.9 \left(\frac{U}{H} \right)^{0.85}$	U-fps H-feet	Developed from a recirculating flume with depths less than 0.5 feet.
Thackston and Krenkel (1969)	$\frac{24.9(1+F^{0.5})u_{\star}}{H}$	u _★ -fps H-feet	Based on measurements made in a 2' wide flume with deoxygenated waters . 0.05's $H \leq 0.23$ '.
Lau (19726)	$2515\left(\frac{u}{u}\right)^{3}$ H	u _* -fps U -fps H-feet	Based on reanalysis of the data of Thackston and Krenkel (1969), Krenkel (1960), and Churchill et al. (1962).
		(continued)	

TABLE 3-6.	REAERATION	COFFFICIENTS	FOR	RIVERS	AND	STREAMS	
			I UN	NT V L NO	שויה	STREAMS	

Author(s)	k ₂ , base e(1/day at 20 ⁰ C)	Units	Applicability
Krenkel and Orlob (1962)	<u>234(US)-408</u> H-66	V-fps S-ft/ft H-feet	Based on 1' wide flume data. 0.08'≤H≤0.2'
Krenkel and Orlob (1962)	$\frac{8.4 \text{ D}_{\text{L}}^{1.321}}{\text{H}^{2.32}}$	D _L -ft ² /min H=feet	Experiments performed in a 1' wide flume by deoxygenating the water. Other similar formulas are also reported. The flume dispersion coefficient, D_L , was below the range expected in natural systems.
Padden and Gloyna (1971)	<u>6.90</u> 0.703 H ^{1.054}	U-fps H-feet	Regression analysis performed on data where 9.8≤k ₂ ≤28.8/day.
Cadwallader and McDonnell (1969)	<u>336(US)^{0.5} H</u>	U-fps S-ft/ft H-fe et	Based on multivariate analysis of reaeration data.
Bansal (1973)	$\frac{4.670^{0.6}}{H^{1.4}}$	U-fps H-feet	Based on reanalysis of reaeration data in numerous rivers.
Bennett and Rathbun (1972)	$\frac{10600.41350.273}{H^{1.408}}$	U-fps S-ft/ft H-feet	These two equations are based on a reanalysis of historical data, with the second equation being al most as good a predictor as the first, but not having the slope term.
	н ^{1.689}		
Dobbins (1964)	$\frac{117(1+F^{2}(US)^{0.375})}{(0.9+F)^{1.5}H} \operatorname{coth}\left[\frac{4.10(US)^{0.125}}{(0.9+F)^{0.5}}\right]$	U-fps H-feet S-ft/ft	Theory combined with measurements in natural streams, and flume data of Krenkel and Orlob (1963).
Ice and Brown (1978)	$\frac{37W^{2/3}S^{1/2}U^{7/6}g^{1/2}}{q^{2/3}}$	W-feet S-ft/ft U-fps Q-ft ³ /sec	Based on data collected in several small Oregon streams.
McCutcheon and Jennings (1982)	$\frac{-\ln\left[1-2\left(\frac{a I 24}{\pi (30.48H)^2}\right)^{\frac{1}{2}}\right]}{I}$	H-feet a=1.42 (1.1) ^{T-20} T- ^O C	Based on the Velz method (1970) and replaces the iterative technique. The expressions for the mix internal I are based on an accumulation of applications of the Velz technique.
	$I = \begin{cases} 0.0016 + 0.0005 \text{ H} & \text{H} \le 2.26 \text{ ft} \\ 0.0097 \ln(\text{H}) - 0.0052 & \text{H} > 2.26 \text{ ft} \end{cases}$		

(continued)

Author(s)	k ₂ , base e(1/day at 20 ⁰ C)	Units	Applicability
Long (1984)	<u>1.923U^{0.273}</u> H ^{0.894}	U-meters/sec H-meters	Known as the "Texas" equation. Based on data collected on streams in Texas.
Foree (1976)	0.30+0.19S ^{1/2} at 25 ^o C	S-feet/mile	Radioactive tracer technique used on small streams in Kentucky. O≤S≤42 feet/mile.
Foree (1977)	• 0.888 $(0.63+0.45^{1.15})q^{0.25}$ at $25^{\circ}C$ for $0.05 \le q \le 1$	S-feet/mile q-cfs/mi ²	Reanalysis of Foree's (1976) data.
	 0.888 (0.63+0.4 S^{1.5}) at 25°C for q>1 0.42 (0.63+0.4S^{1.15}) at 25°C for q<0.05 		
Tsivoglou and Wallace (1972)	$0.054 \frac{\Delta h}{t} \text{ at } 25^{\circ}\text{C}$	∆h-feet t-days	Based on summary of radioactive tracer applications to 5 rivers.
Tsivoglou and Neal (1976)	• $0.11 \left(\frac{\Delta h}{t}\right)$ for $1 \le Q \le 10$ cfs • $0.054 \left(\frac{\Delta h}{t}\right)$ for $25 \le Q \le 3000$ cfs	∆h-feet t-days	Based on data collected on 24 different streams using radioactive tracer method.
Grant (1976)	$0.09\left(\frac{\Delta h}{t}\right)$ at $25^{\circ}C$	∆h-feet t-days	Based on data from 10 small streams in Wisconsin using radioactive tracer techniques: $2.1 \le k_2 \le 55/day$ $1.2 \le S' \le 70$ ft/mile $0.3 \le Q \le 37$ cfs
Grant (1978)	$0.06\left(\frac{\Delta h}{t}\right)$ at $25^{\circ}C$	∆h-feet t-days	Based on radioactive tracer data developed on Rock River, Wisconsin and Illinois: $0.01 \le k_s \le 0.8/day$ $0.25 \le U^2 \le 1.6$ fps $0.2 \le S \le 3.5$ ft/mile $260 \le Q \le 1030$ cfs
		(continued)	

TABLE 3-6. (continued)

TABLE 3-6. (continued)

Shindala and Truax (1980)	• $0.08\left(\frac{\Delta h}{t}\right)$ at $25^{\circ}C$ for $Q \le 10$ cfs • $0.06\left(\frac{\Delta h}{t}\right)$ at $25^{\circ}C$	Δ h-feet t-days	Based on statistical analysis of reaeration coefficients for rivers in 7 states, where the radioactive tracer method was used to find the reaeration rates.
	fo r 10 < Q ≤ 280 cfs		
Eloubaidy and Plate (1972)	Wind effects analyzed. See text for	discussion.	
Mattingly (1977)	Wind effects analyzed. See text for	discussion.	
Gulliver and Stefan (1981)	Wind effects analyzed.		
Frexes <u>et</u> <u>al</u> . (1984)	Wind effects analyzed.		

Definitions of Symbols:

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D_1 = longitudinal dispersion coefficient
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F = Froude number
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- $\frac{1}{(gh)^{0.5}}$ g = acceleration due to gravity
- $\Delta h =$ change in stream bed elevation between two points
- q = stream discharge divided by drainage area
- R ≠ hydraulic radius

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S = slope
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- t = travel time between two points where Δh measured
- U ≠ stream velocity
- $u_{\pm} = \text{shear velocity} = \sqrt{gRS}$

W = width

3.2.2.2 Reviews of Stream Reaeration

Over the past decade, several researchers have reviewed reaeration formulas, and have tried to evaluate the performance of the formulas. One of the earlier reviews, Bennett and Rathbun (1972), is also an excellent source for reaeration theory. They describe the theories behind various conceptual models of reaeration (including film, renewal, penetration, filmpenetration, and two-film theory models), semi-empirical models, and empirical models. They also discuss methods to determine the reaeration coefficient that include dissolved oxygen balances in natural streams, dissolved oxygen balances in recirculating flumes, the distributed equilibrium technique (where sodium sulfite is usually added to the water to deoxygenate it), and the radioactive tracer technique.

Table 3-7 summarizes the Bennett and Rathbun review in addition to other studies that have compared reaeration coefficients. The studies conclude that no single formula is best for all rivers. For one set of data one formula may be best, while for another set of data another formula may appear to be best.

Figure 3-1 compares 13 reaeration coefficient expressions for a range of depths (from Bennett and Rathbun, 1972). The figure illustrates the variability between predictions for a velocity of 1.0 fps and slope of 0.0001. The range of differences between predicted values spans one to two orders of magnitude. The formulas agree with each other best within the depth range of 1 to 10 feet, typical of many rivers.

Figure 3-2 compares calculated and observed reaeration coefficients for the formulas of Dobbins (1965) and Parkhurst and Pomeroy (1972). These formula were found by Wilson and MacLeod (1974) to best fit the observed data. Notice that the spread of data is slightly less than one order of magnitude.

The data of Wilson and Macleod also show that the depth - velocity model of Bennet and Rathbun (1972) does not fit the experimental data nearly

Bennett and Rathbun (1972)

Thirteen equations were evaluated.

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- The standard error of the estimate was used as a measure of the difference between predicted values and data.
- The equation which provided the best fit to their original data set was Krenkel (1960).
- The equations which best fit the entire range of data were: O'Connor and Dobbins (1958), Dobbins (1965), Thackston and Krenkel (1969).
- Of the thirteen equations the Churchill <u>et al</u>. (1962) formula provided the best fit to natural stream data.
- The Bennett and Rathbun formula, developed from the data evaluated during their review, provided a smaller standard error for natural streams than the other 13 equations.
- There was a significant difference between predictions from equations derived from flume data and equations derived from natural stream data.
- The expected root-mean-square error from different measurement techniques is: 15 percent using the radioactive tracer technique; 65 percent using the dissolved oxygen mass balance, and 115 percent using the disturbed equilibrium method.

Lau (1972b)

- Both conceptual and empirical models were reviewed.
- Conclusions reported were similar to those of Bennett and Rathbun.
- It was found that no completely satisfactory method exists to predict reaeration.

Wilson and MacLeod (1974)

- Nearly 400 data points were used in the analysis.
- Sixteen equations were reviewed.
- The standard error of estimate and graphical results were both used in error analysis.
- It was concluded that equations which use only depth and velocity are not accurate over the entire range of data investigated.
- The methods of Dobbins (1965) and Parkhurst and Pomeroy (1972) gave the best fits to the data investigated.

Rathbun (1977)

- Nineteen equations were reviewed.
- Equation predictions were compared against radioactive tracer measurements on 5 rivers (Chattahoochee, Jackson, Flint, South, Patuxent).
- The best equations in terms of the smallest standard error estimates was Tsivoglou- Wallace (1972) (0.0528), Parkhurst-Pomeroy (1972) (0.0818), Padden-Gloyna (1971) (0.0712) and Owens <u>et al</u>. (1964), (0.0964).
- No one formula was best for all five rivers.

Rathbun and Grant (1978)

- Compared the radioactive and modified tracer techniques for Black Earth Creek and Madison Effluent Channel in Wisconsin.
- Differences in Black Earth Creek were -9% to 4% in one reach and 16% to 32% on another reach attributable to increased wind during the latter part of the test.
- Unsteady flow during the Madison Effluent Channel tests led to differences of as much as 25 to 58% in one case and -5% to 3% in another.

Shindala and Truax (1980)

- Reaeration measurements for streams in Mississippi, Wisconsin, Texas, Georgia, North Carolina, Kentucky, and New York were made using the radioactive tracer technique.
- The energy dissipation model resulted in the best correlation for reaeration coefficient prediction for small streams. The following escape coefficients (defined as the coefficients of $\frac{\Delta h}{+}$ in energy dissipation models for reaeration coefficients) were recommended:

0.0802/ft ,for Q <10 cfs 0.0597/ft ,for 10 \leq Q \leq 280 cfs

NCASI Bulletin (1982b)

- Six reaeration formulas were compared against measurements made using radioactive tracer techniques and hydrocarbon tracer techniques for a reach of the Ouachita River, Arkansas.
- The hydrocarbon tracer technique produced reaeration rates higher than both the radioactive tracer and empirical formulas.
- The O'Connor Dobbins (1958) equation was chosen as the best empirical equation.

Kwasnik and Feng (1979)

- Thirteen reaeration formulas were reviewed and compared against values measured using the modified tracer technique for two streams in Massachusetts.
- The equations of Tsivoglou-Wallace (1972) and Bennett-Rathbun (1972) gave the closest predictions to the field values.
- The study indicates that results using the modified tracer technique are reproducible.

Grant and Skavroneck (1980)

- Four modified tracer methods and 20 predictive equations were compared against the radioactive tracer methods for 3 small streams in Wisconsin.
- Compared to the radioactive tracer method the errors in the modified tracer techniques were:

11% for the propane-area method 18% for the propane-peak method 21% for the ethylene-peak method 26% for the ethylene-area method

- Compared to the radioactive tracer method, the equations with the smallest errors were:
 - 18% for Tsivoglou-Neal (1976) 21% for Negulescu-Rojanski (1969) 23% for Padden-Gloyna (1971) 29% for Thackston-Krenkel (1969) 32% for Bansal (1973)

House and Skavroneck (1981)

- Reaeration coefficients were determined on two creeks in Wisconsin using the propane area modified tracer technique and compared against 20 predictive formulas.
- The top five predictive formulas were:

Tsivoglou - Neal (1976), 34% mean error Foree (1977), 35% mean error Cadwallader and McDonnell (1969), 45%, mean error Isaacs-Gaudy (1968), 45%, mean error Langbein-Durum (1967), 49%, mean error.

Zison <u>et al</u>. (1978)

- Thirteen reaeration formulas were reviewed, but none were compared against historical data.
- Covar's method (1976) was discussed which shows how stream reaeration can be simulated by using three formulas (O'Connor-Dobbins (1958), Churchill <u>et al</u>. (1962), and Owens <u>et al</u>. (1964)), each applicable in a different depth and velocity regime.

Yotsukura <u>et</u> <u>al</u>. (1983)

- Developed a steady injection method to avoid uncertainty in dispersion corrections.
- Determined reproducibility to be 4%.
- Found negligible effect of wind where stream banks are high.

Ohio Environmental Protection Agency (1983)

- Eighteen reaeration coefficient equations were compared against data collected in 28 Ohio streams.
- The streams were divided into four groups based on slope and velocity. The best predictive equations for each group are shown below:

Group	<u>Slope (ft/mile)</u>	Flow (cfs)	Preferred Equation
1	<3	All data	Negelescu-Royanski (1969) Krenkel-Orlob (1962)
2	3-10	≤30	Parkhurst-Pomeroy (1972)
3	3-10	>30	Thackston-Krenkel (1969)
4	>10	All data	Parkhurst-Pomeroy (1972) Tsivoglou-Neal (1976)

as well (see Figure 3-3). This was the formula which Bennett and Rathbun (1972) found produced the smallest error of the formulas they reviewed.

Figure 3-4 shows the three reaeration formulas found by Rathbun (1977) to best predict observed values for the Chattahoochee, Jackson, Flint,







Figure 3-2. Comparisons of predicted and observed reaeration coefficients for the formula of Dobbins (1965) (a) and Parkhurst-Pomeroy (1972) (b).

South, and Patuxent Rivers. The range of reaeration coefficients analyzed here is considerably smaller than analyzed by Wilson and Macleod. The Tsivoglou - Wallace method is noticeably better than either the Padden-Gloyna or Parkhurst-Pomeroy methods. However, the Tsivoglou-Wallace method was originally developed using this data set, so it is not surprising that the fit is best.

Figure 3-5 shows the energy dissipation model of Shindala and Truax (1980) applied to streams with flow rates less than 280 cfs. They found that the best fit to the data was achieved when the flow rate was divided into two groups: less than 10 cfs and greater than 10 cfs.

Covar (1976), as discussed by Zison <u>et al</u>. (1978) found that the research of O'Connor-Dobbins (1958), Churchill <u>et al</u>. (1962), and Owens <u>et al</u>. (1964) could be used jointly to predict stream reaeration coefficients



Figure 3-3. Formula of Bennett and Rathbun (1972) compared against observed reaeration coefficients.

for a range of depth and velocity combinations. Figure 3-6 shows the data points collected by each investigator and the regions Covar choose to divide the applicable formulas. Figure 3-7 shows the plots of reaeration prediction. Note that the predictions approximately match at the boundaries of each region.



Figure 3-4. Calculated versus experimental reaeration coefficients for equations of (a) Tsivoglou and Wallace (1972), (b) Padden and Gloyna (1971), and (c) Parkhurst and Pomeroy (1972).



Figure 3-5. Reaeration coefficient versus energy dissipation (a) for flow rates between 10 and 280 cfs and (b) for flow rates less than 10 cfs. (Note: Curves for predicted reaeation coefficients are forced through the origin).

3.2.2.3 Measurement Techniques

Methods to determine reaeration rates based on instream data include the dissolved oxygen balance, deoxygenation by sodium sulfite, productivity measurements, and tracer techniques (both radioactive tracers and hydocarbon tracers). Today, use of tracers is the most widely accepted method. Productivity measurements are sometimes used, but because of their indirect approach could be subject to considerable error. Some of these methods are discussed in Kelly <u>et al</u>. (1975), Hornberger and Keliy (1975), and Waldon (1983). Only the tracer methods are discussed here.



Figure 3-6. Field data considered by three different investigations.

The tracer method which appears to produce the most accurate results is the radioactive tracer technique developed and reported by Tsivoglou <u>et al.</u> (1965), Tsivoglou (1967), Tsivoglou <u>et al</u>. (1968), Tsivoglou and Wallace (1972), and Tsivoglou and Neal (1976). The method involves the instantaneous and simultaneous release of three tracers: krypton-85, tritium, and a fluorescent dye. The fluorescent dye indicates when to sample the invisible radioactive tracers and provides travel time information as well. The tritium acts as a surrogate for dispersion: the



Figure 3-7. Reaeration coefficient (1/day) vs. depth and velocity using the suggested method of Covar (1976).

tritiated water disperses in the same manner as the natural water. The krypton-85 is lost to the atmosphere in a constant, known ratio compared with dissolved oxygen. The formula used is:

$$\begin{pmatrix} \frac{C_{kr}}{C_{tr B}} \\ \frac{C_{kr}}{C_{tr A}} \end{pmatrix} = \exp(-k_{kr}t)$$
 (3-18)

where $\begin{pmatrix} C_{kr} \\ C_{tr} \end{pmatrix}_{A,B}^{F}$ = concentration ratios of krypton and tritium at locations A and B when the dye peaks at each location t = travel time between A and B k_{kr} = atmospheric exchange rate of krypton

Since $\frac{k_{kr}}{k_2} = 0.83\pm0.04$, the dissolved oxygen reaeration rate, k_2 , can be found directly from k_{kr} . The ratio 0.83 was found in the laboratory and has not been proven to be constant for all conditions.

Wilhelms (1980) has applied the radioactive tracer technique to flow through a hydraulic model. The results compared favorably with results from disturbed-equilibrium tests.

Because of the costs and potential hazards of using this method, other tracer techniques have been developed which do not use radioactive tracers. These methods have been discussed by Rathbun <u>et al</u>. (1975), Rathbun <u>et al</u>. (1978), Rathbun and Grant (1978), Kwasnik and Feng (1979), Bauer <u>et al</u>. (1979), Rathbun (1979), Jobson and Rathbun (undated), Grant and Skavroneck (1980), House and Skavroneck (1981), Rainwater and Holley (1984), Wilcock (1984a). and Wilcock (1984b). Not all researchers agree on the accuracy to the modified tracer techniques. Kwasnik and Feng (1979), Grant and Skavroneck (1980), House and Skavroneck (1981) all reported successful applications of the method. However, NCASI (1982b) reported that the hydrocarbon tracer technique produced results higher than both the radioactive tracer and empirical methods. The application was on a large

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sluggish stream. Rainwater and Holley (1984) have investigated two assumptions of the hydrocarbon tracer technique (constant ratios between mass transfer coefficients and negligible absorptive losses) and found both assumptions to be valid for that particular study.

The modified tracer techniques use a hydrocarbon gas tracer and a fluorescent dye (e.g., rhodamine-WT) as the dispersion-dilution tracer. Sometimes two different tracer gases (e.g., ethylene and propane) can be used simultaneously to yield two estimates of reaeration rate. Two methods can be used: the peak concentration method and the total weight method.

Using the total-weight method the exchange rate of the tracer with the atmosphere, k_T is computed as follows:

$$k_{T} = \frac{1}{t_{d} - t_{u}} \log_{e} \left(\frac{A_{u}Q_{u}}{A_{d}Q_{d}} \right)$$
(3-19)

where A_u and A_d = areas under the gas concentration-versus-time curves at the upstream and downstream ends of the reach, respectively, and

 $Q_{\rm H}$ and $Q_{\rm d}$ = stream discharge at each end of the reach.

The reaeration coefficient k_2 is computed as:

$$k_{2} = \begin{cases} \frac{k_{T}}{.87} , \text{ ethylene} \qquad (3-20a) \\ \frac{k_{T}}{.72} , \text{ propane} \qquad (3-20b) \end{cases}$$

Recently Wilcox (1984a, b) has proposed methyl chloride as a gas tracer. At 20° C,

$$k_2 = \frac{k_T}{.707}$$
, for methyl chloride (3-20c)

The methyl chloride transfer coefficient k_T was found to exhibit a temperature dependence.

The peak concentration method is similar in form to the radioactive tracer equation:

$$k_{T} = \frac{1}{t_{d} - t_{u}} \log_{e} \frac{\left(\frac{C_{T}}{C_{D}}\right)_{u}}{\left(\frac{C_{T}}{C_{D}}\right)_{d}} \frac{\left(A_{D}\right)_{d}}{\left(A_{D}\right)_{u}}$$
(3-21)

where k_T = the base e desorption coefficient for the tracer gas; t_d-t_u = the time of travel between the peak concentrations; C_T and C_D = the peak concentrations of the tracer gas and rhodamine-WT dye, respectively $(A_D)_d$, $(A_D)_u$ = area under dye versus time curve downstream and uptream, respectively

More recently Yotsukura <u>et al</u>. (1983) have conducted tests to assess the feasibility of a steady-state propane gas tracer method as a means of estimating reaeration coefficients. The tests were conducted on Cowaselon Creek, New York. It was concluded that the steady state method, which also includes an instantaneous injection of dye tracer, is feasible and provides a reliable method of determining the reaeration coefficient.

3.2.2.4 Special Influences on Reaeration

In addition to hydraulic variables which typically appear in the expressions in Table 3-6, the reaeration coefficient can be influenced by certain special factors which include:

- surfactants
- suspended particles

- wind
- hydraulic structures, and
- water temperature

While surfactants, suspended solids, and wind can influence reaeration in rivers, in practice the effects of these factors are rarely if ever included in water quality models. Discussion of the influence of surfactants is given in Zison <u>et al</u>. (1978), Poon and Campbell (1967), and Tsivoglou and Wallace (1972). The influence of suspended solids is discussed by Holley (1975) and Alonso <u>et al</u>. (1975).

3.2.2.4.1 Wind Effects

While wind effects are typically not included in reaeration predictions in rivers, there is evidence that at high wind speeds, the reaeration rates can be significantly increased. These effects are occasionally alluded to in the literature when experimental measurements are abnormally high.

Eloubaidy and Plate (1972) performed experiments in the wind-wave facility at Colorado State University. They arrived at the following expression for the surface transfer coefficient, k_1 , in feet per day:

$$k_{L} = \frac{CU_{\star} h U_{\star}}{v} c \qquad (3-22)$$

where C = a constant of proportionality

$$v = kinematic viscosity of water, m^2/sec$$

 $U_{\star} = surface shear velocity due to wind, m/sec = 0.0185 V_w^{1.5}$
 $v_w = wind speed, m/sec$
 $U_{\star} = water shear velocity defined as $\sqrt{ghS_c}$, m/sec
 $h = normal depth$ (i.e., depth with uniform flow), m
 $S_c = pressure-adjusted channel slope, unitless, S_0 + \frac{1dp}{\rho gdx}$
 $\rho = mass density of water, kg/m^3$
 $g = gravitational constant, m/sec^2$
 $S_0 = slope of energy gradient (channel slope for uniform flow),
unitless$$

 $\frac{dP}{dx}$ = air pressure gradient in the longitudinal direction, kg/m²-sec²

From their experiments Eloubaidy and Plate found that C = .0027.

The variables comprising Equation 3-22 are readily obtainable, with the exception of the pressure gradient. The authors determined that an error on the order of 2 percent was obtained in k_2 (= k_L/h) by neglecting the pressure gradient.

A summary of the conditions under which Equation 3-22 was developed is:

channel slope:	.00043, .001
air velocity:	22, 30, 38 fps for each slope
discharge:	0.79, 0.83, 0.91 cfs at 0.001 slope
	0.58, 0.63, 0.75 cfs at 0.0043 slope
water depth:	0.385 feet

Note the extremely high wind velocities used in the experiments (greater than 22 fps). Hence the validity of the approach to lesser wind speeds typically encountered in the natural environment has not been demonstrated.

Mattingly (1977) also performed laboratory studies of the effects of wind on channel reaeration. He obtained this empirical expression:

$$\frac{k_2}{(k_2)_0} - 1 = 0.2395 \, V_w^{1.643} \tag{3-23}$$

where k_2 = reaeration coefficient under windy conditions, 1/day $\binom{k_2}{0}$ = reaeration coefficient without wind, 1/day V_w = wind velocity in meters per second in the free stream above the boundary layer near the water surface A plot of the experimental data is shown in Figure 3-8. Note the importance of wind induced reaeration at moderate to high wind speeds. Further discussion of the effects of wind are found in Gulliver and Stefan (1981) and Frexes et al. (1984).

Because wind effects are typically neglected in river and stream reaeration modeling, this approach is equivalent to assuming a zero wind velocity. For many water quality modeling applications, such as wasteload allocation, this approach is reasonable.



Figure 3-8. Ratio of reaeration coefficient under windy conditions to reaeration coefficient without wind, as a function of wind speed (based on laboratory studies).

3.2.2.4.2 Small Dams

On many rivers and streams small to moderate sized dams are present. Dams can influence reaeration by changing the dissolved oxygen deficit from 1 to 3 mg/l (typically) in a very short reach of the river. Table 3-8 summarizes various predictive equations that have been used to simulate the effects of small dams. Avery and Novak (1978) discuss limitations of these equations and aspects of oxygen transfer at hydraulic structures.

Butts and Evans (1983) have reviewed various approaches that predict the effects of small dams on channel reaeration and further collected field data on 54 small dams located in Illinois to determine their reaeration characteristics. They identified 9 classes of structures, and quantified the aeration coefficient b for use in the following formula:

$$r = \frac{C_s - C_u}{C_s - C_d} = 1 + 0.38 \text{ abh} (1 - 0.11\text{ h}) (1 + 0.046\text{T})$$
(3-24)

Figure 3-9 shows the general structural classification and the aeration coefficient, b, for each class.

The present review does not include influences of large dams, artificial reaeration, or other hydraulic structures. Cain and Wood (1981) discuss aeration over Aviemore Dam, 40 m (130 ft) in height, Banks <u>et al</u>. (1983) and NCASI (1969) discuss effects of artificial reaeration, and Wilhelms <u>et al</u>. (1981), Wilhelms (1980), and Wilhelms and Smith (1981) further discuss reaeration related to hydraulic structures.

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Reference	Predictive Equation	llnits	Source
		onres	
Gameson (1957)	r = 1+0.5abh	h, in meters	field survey
Gameson <u>et al</u> . (1958)	r = 1+0.11ab(1+0.046T)h	h, in feet	model
Jarvis (1970)	$r_{15} = 1.05 \ h^{0.434}$	h, in meters	model
Holler (1971)	r ₂₀ =1+0.91h	h, in meters	mode1
Holler (1971)	r ₂₀ - 1+0.21h	h, in meters	prototype
Department of the Environment (1973)	r = 1+0.69h(1-0.11h)(1+0.0464T)	h, in meters	model
Department of the Environment (1973)	r = 1+0.38abh(1-0.11h)(1+0.046T)	h, in meters	model
Nakasome (1975)	$\log_{e}(r_{20}) = 0.0675h^{1.28} q^{0.62} d^{0.439}$	d, h, in meters q, in m ² /hr	model
Foree (1976)	r = exp(0.1bh)	h, in feet	field survey

TABLE 3-8. EQUATIONS THAT PREDICT THE EFFECTS OF SMALL DAMS ON STREAM REAERATION

 $= \frac{C_s - C_u}{C_s - C_d}$ Symbols: r_T °s = dissolved oxygen saturation C_u , C_d = concentration of dissolved oxygen upstream and downstream of dam, respectively = measure of water quality (0.65 for grossly polluted; 1.8 for clear) a = function of weir type Ь = water level difference h d = tailwater depth below weir = specific discharge. q = water temperature, ^{O}C Т

3.2.2.4.3 Temperature Effects on Reaeration

The influence of temperature on reaeration is typically simulated using the following type of temperature dependence:

$$k_2(T) = k_2(20^{\circ}C)\theta^{T-20}$$
 (3-25)

where $T = water temperature, {}^{O}C$

 θ = temperature adjustment factor

Table 3-9 summarizes values of θ from the literature. Typically values of 1.022 to 1.024 are used in most modeling applications.

Schneiter and Grenney (1983) developed a different approach to simulate temperature corrections over the ranges 4° C to 30° C. Their approach effectively allows θ to vary as a function of temperature. However, the approach is not widely used.



Figure 3-9. Division of head loss structures by dam type.

Temperature		
Coefficient, θ	Reference	
1.047	Streeter, <u>et</u> <u>al.</u> (1926)	
1.0241	Elmore and West (1961)	
1.0226	Elmore and West (1961)	
1.020	Downing and Truesdale (1955)	
1.024	Downing and Truesdale (1955)	
1.016	Dowining and Truesdale (1955)	
1.016	Streeter (1926)	
1.018	Truesdale and Van Dyke (1958)	
1.015	Truesdale and Van Dyke (1958)	
1.008	Truesdale and Van Dyke (1958)	
1.024	Churchill <u>et al</u> (1962)	
1.022	Tsivoglou (1967)	
1.024	Committee on Sanitary Engineering Research (1960)	

TABLE 3-9. REPORTED VALUES OF TEMPERATURE COEFFICIENT

3.2.2.5 Sources of Data

Many sources of stream reaeration rates exist in the literature. Table 3-10 summarizes a number of the major sources. Many state agencies are also repositories of reaeration data.

3.2.3 Reaeration in Lakes

Simulation of reaeration in lakes is normally accomplished using the surface transfer coefficient $k_{\rm L}$ rather than the depth averaged k_2 . Most often in lake simulations the surface transfer coefficient $k_{\rm L}$ is assumed to be a function of wind speed.
TABLE 3-10. SOURCES OF STREAM REAERATION DATA

Source	Contents
Owens et al., (1964)	Reaeration coefficients using disturbed equilibrium technique for six rivers in England (Ivel, Lark, Derwent, Black Beck, Saint Sunday's Beck, Yewdale Beck), and associated hydraulic data.
O'Connor and Dobbins (1958)	Reaeration data for Clarion River, Brandywine Creek, Illinois River, Ohio River, and Tennessee River.
Churchill <u>et al</u> . (1962)	Reaeration data using dissolved oxygen balance downstream from deep impoundments for Clinch River, Holston River, French Broad River, Watauga River, Hiwassee River.
Tsivoglou and Wallace (1972)	Hydraulic properties and radioactive tracer measured reaeration coefficients for Flint, South, Patuxent, Jackson, and Chattahoochee Rivers.
Bennett and Rathbun (1972)	Summaries of data from Churchill <u>et al.</u> , (1962), Owens <u>et</u> <u>al.</u> , (1964), Gameson <u>et al</u> . (1958), O'Connor and Dobbins (1958), Tsivoglou <u>et al</u> ., (1967,1968), Negulescu and Rojanski (1969), Thackston (1966), Krenkel (1960).
Foree (1976)	Radioactive tracer measurements and reaeration hydraulic characteristics for small streams in Kentucky, and reaeration measurements for small dams in Kentucky.
Grant (1976)	Reaeration measurements and hydraulic characteristics for 10 small streams in Wisconsin.
Grant (1978)	Reaeration measurements and hydraulic characteristics for Rock River, Wisconsin.
Zison <u>et al</u> . (1978)	Summary of reaeration coefficients and hydraulic characteristics for rivers throughout the United States.
Kwasnik and Feng (1979)	Reaeration data using the modified tracer technique on selected streams in Massachusetts.
Grant and Skavroneck (1980)	Reaeration data from three small streams in Wisconsin.
House and Skavroneck (1981)	Reaeration data for two small streams in Wisconsin.
Shindala and Truax (1980)	Radioactive tracer measurements of reaeration rates and escape coefficients, plus hydraulic data, for rivers in Mississippi, Wisconsin, Texas, Georgia, North Carolina, Kentucky and New York.
Terry <u>et al</u> . (1984)	Hydrocarbon tracer measurements of k ₂ and hydraulic data for Spring Creek, Osage Creek, and Illinois River, Arkansas. Bennett-Rathbun (1972) best fit all three streams. Eight equations were tested.
Bauer <u>et</u> <u>al</u> . (1979)	Hydrocarbon tracer measurements of k, and hydraulic data for the Yampa River, Colorado best matched the Tsivoglou Neal and Thackston and Krenkel energy dissipation type equations. Lau's equation was extremely error prone. Nineteen equations were tested.
Goddard (1980)	Hydrocarbon tracer measurements of k, and hydraulic data from the Arkansas River in Colorado were used to test 19 equations. The best fitting equations were those by Dobbins, Padden and Gloyna, Langbein and Durum, and Parkhurst and Pomeroy.

Source	Contents		
Hren (1983)	Radioactive tracer measurements for the North Fork Licking River, Ohio.		
Rathbun <u>et</u> <u>al</u> . (1975)	Hydrocarbon tracer measurements for West Hobolochitts Creek, Mississippi.		
NCASI (1982c)	Radioactive tracer measurements for Ouachita River, Arkansas, and Dugdemona River, Louisiana.		
Parkhurst and Pomeroy (1972)	Reaeration coefficients were determined by a deoxygenation method in 12 sewers in the Los Angeles County Sanitation District.		
Ice and Brown (1978)	Reaeration coefficients were determined using sodium sulfite to deoxygenate the water in small streams in Oregon.		
Ohio Environmental Protection Agency (1983)	Reaeration coefficients were determined for 28 different streams in Ohio using predominantly the modified tracer technique, and in one case the radioactive tracer technique.		
Long (1984)	Reaeration coefficients, hydraulic data, and time of travel data collected on 18 streams in Texas.		

Since many lakes are not vertically well-mixed, multiple layers are often used to simulate dissolved oxygen dynamics. Atmospheric reaeration occurs only through the surface layer, and then dissolved oxygen is dispersed and advected to layers lower in the water body.

Table 3-11 summarizes various methods that have been used to simulate reaeration in lakes. With the exception of the method of Di Toro and Connolly (1980), all formulas include a wind speed term. Di Toro and Connolly applied a constant surface transfer coefficient to Lake Erie. They found that the surface layer of the lake remained near saturation so that the value of $k_{\rm L}$ used was not important as long as it was sufficiently high to maintain saturated dissolved oxygen levels in the surface layer.

All the surface transfer coefficients shown in Table 3-11 should be viewed as empirical; the researchers have simply hypothesized that the suggested formulas are adequate to simulate reaeration. The coefficients (a and b) are of limited validity, and should be treated as calibration parameters. O'Connor (1983) has analyzed from a more theoretical point of view the effects of wind on the surface transfer coefficient.

Author(s)	Surface Transfer Rate, k _L (m/day)
Di Toro and Connolly (1980)	k _L 2.0
Chen <u>et al</u> ., (1976)	$k_{L} = \frac{86400D}{(200-60\sqrt{V})10^{-6}}$ D molecular diffusion coefficient of oxygen in water, m ² /sec V = wind speed, m/sec
Banks (1975)	$k_{L} = 0.362 V^{1/2}$ for $0 \le V \le 5.5$ m/sec $k_{L} = 0.0277V^{2}$ for $V > 5.5$ m/sec
Baca and Arnett (1976)	k_{L} a + bV a 0.005 - 0.01 m/day b = 10 ⁻⁶ - 10 ⁻⁵ m ⁻¹ V = wind speed, m/day
Smith (1978)	k _L a + bV ² a = 0.64 m/day b - 0.128 sec ² m ⁻¹ day ⁻¹ V = wind speed, m/s
Liss (1973)	k _L 0.156 $V^{0.63}$ V \leq 4.1 m/sec k _L 0.0269 $V^{1.9}$ V > 4.1 m/sec V wind speed, m/sec
Downing and Truesdale (1955)	k _L = 0.0276V ^{2.0} V = wind speed, m/sec
Kanwisher (1963)	k _L 0.0432V ² V = wind speed, m/sec
Broecker <u>et</u> <u>al</u> . (1978)	k _L 0.864V V = wind speed, m/sec
Yu <u>et al</u> . (1977)	k _L - 0.319V V wind speed, m/sec
Broecker and Peng (1974)	k _L = 0.0449V ² V - wind speed, m/sec

TABLE 3-11 . REAERATION COEFFICIENTS FOR LAKES

Author(s)	Surface Transfer Rate, k _L (m/day)		
Weiler (1975)	k _i = 0.398 V <1.6 m/sec k _i = 0.155V ² V ≥1.6 m/sec V = wind speed, m/sec		

TABLE 3-11. (Cont'd)

Notes:

1. Elevation of wind speed measurements is not always reported.

2. a and b are empirically determined.

Some limited research has addressed the influence of rainfall on reaeration (Banks <u>et al</u>., 1984; Banks and Herrera, 1977). Rainfall effects are more of theoretical interest rather of practical concern.

3.2.4 Reaeration in Estuaries

The present state of reaeration simulation in estuaries combines concepts used in river and lake approaches. Very little original research on estuarine reaeration has been completed to date.

Table 3-12 summarizes different formulations that have been used to predict reaeration in estuaries. The different approaches include both $k_{\rm L}$ (surface transfer) and k_2 (depth averaged) reaeration terms. In some models, k_2 can be specified (e.g., Genet <u>et al.</u>, 1974 and MacDonald and Weismann, 1977). O'Connor <u>et al</u>. (1981) specified the surface transfer rate to be 1 m/day in their two-layered model of the New York Bight. One of the more widely used approaches is the O'Connor (1960) formula, which has subsequently been modified to include wind speed terms (Thomann and Fitzpatrick, 1982).

Few field studies have been performed for the purpose of directly measuring reaeration in estuaries. Baumgartner <u>et al</u>., (1970) used Krypton-85 to measure the range of reaeration in the Yaquina River Estuary. However, no predictive formulas were developed.

Reference	Reaeration Rate
0'Connor (1960)	<pre>k₂ = \frac{(D_U_0)^{1/2}}{H^{3/2}} (1/day) U_0 = mean tidal velocity over a complete cycle, m/day D_L - molecular diffusivity of oxygen, m²/day H - average depth, m</pre>
Genet <u>et</u> <u>al</u> ., (1974)	k ₂ = user specified
O'Connor <u>et al</u> ., (1981)	k _L = 1 m/day
MacDonald and Weisman (1977)	k ₂ ≖ user specified
Harleman <u>et al</u> ., (1977)	$k_{2}^{a} = 10.86 \frac{\gamma^{0.6} HW_{T}}{H^{1.4} A} (1/day)$ V = tidal velocity, ft/sec H = depth, ft W_{T} = top width, ft A = cross-sectional area, ft
Thomann and Fitzpatrick (1982)	$k_{2} = \frac{13V^{0.5}}{H^{1.5}} + \frac{3.281}{H} (0.728W^{0.5} - 0.317W + 0.0372W^{2}) (1/day)$ V = depth averaged velocity, fps H = depth, ft W = wind speed, m/sec
Ozturk (1979)	$k_2 = \frac{4.56V^{4/3}}{H} (1/day)$ $V = mean tidal velocity, m/sec$ $H = mean depth, m$

^aThe coefficient 10.86 is the recommended value, but can be changed as discussed by Harleman et al. (1977).

Tsivoglou (1980) has discussed the application of radioactive tracer techniques to small estuaries within the Chesapeake Bay. Special discussion was given to the Ware River Estuary.

3.2.5 Summary

The most common method of simulating reaeration in rivers is to use the depth averaged k_2 approach, while in lakes the surface transfer rate k_L is typically used. In estuaries either k_2 or k_L is used, depending on the importance of stratification. Very little research on reaeration has been done in either lakes or estuaries. In lakes, reaeration is typically specified to be a constant or to be a function of wind speed. Little information is available on how to select parameters in the wind speed functions. Site specific calibration of the parameters may be required.

In contrast to lakes and estuaries much research has been conducted on reaeration in rivers. Thirty-one formulas were shown earlier in Table 3-6. The formulas have been developed based on hydraulic parameters, most often depth and velocity. Consequently, the variables in reaeration expressions are generally not of concern in distinguishing among the utility of the formulas. One exception is formulas that contain longitudinal dispersion coefficients, which are difficult to quantify.

Considerable evidence shows that reaeration formulas are most applicable over the range of variables for which they were developed, and outside of that range, errors might be quite large. This suggests that reaeration rates developed from laboratory flume data may be quite limited for natural stream applications. Some research supports this supposition (Bennett and Rathbun, 1972).

Previous reviews of stream reaeration (see Table 3-7) have shown that no one formula is best under all conditions, and depending on the data set used, the range of the reaeration coefficients in the data set, and the error measurement selected, the "best" formula may change. Some of the reaeration rate expressions which have been judged "best" during past reviews are:

• The O'Connor and Dobbins (1958), Dobbins (1964), and Thackston and Krenkel (1969) formulas best fit the entire range of data reviewed by Bennett and Rathbun (1972).

- The Churchill <u>et al</u>. (1962) formula provided the best fit to natural stream data in the Bennett and Rathbun review.
- The methods of Dobbins (1964) and Parkhurst and Pomeroy (1972) gave the best fits to the data reviewed by Wilson and MacLeod (1974).
- The Tsivoglou-Wallace and Parkhurst-Pomeroy methods were best in the review by Rathbun (1977).
- The energy dissipation model produced the best correlation for small streams based on the study of Shindala and Truax (1980).

From previous reviews, one of the more popular and more accurate methods for reaeration rates prediction is the energy dissipation method of Tsivoglou. The method requires knowledge of the escape coefficient, which appears to depend on streamflow. Typical values of the escape coefficient are 0.08/ft for flow rates less than 10 cfs, and 0.06/ft for flow rates between 10 and 280 cfs.

The method of Covar (1976), which combines the O'Connor-Dobbins, Churchill <u>et al.</u>, and Owens <u>et al.</u>, formulas, has merit in that it attempts to limit the use of the three formulas to within the depth-velocity range for which they were developed. However, for relatively small and shallow streams, the method of Owens <u>et al.</u>, tends to overestimate reaeration, so that the energy dissipation method, which appears to perform well in small streams, could be used to supplement the method.

The radioactive tracer method appears to be the best method for measuring stream reaeration coefficients. Even so, the coefficients that are predicted are valid only for the particular flow condition existing at the time of sampling. Thus to completely characterize the range of values of the reaeration coefficient would require numerous sampling events or use of an acceptable predictive equation. Sampling methods which require indirect knowledge of parameters that are difficult to quantify should be avoided. The gas tracer method has been used with at least partial success, but applications do not yet appear widespread. When stream reaeration rates are being measured the wind should be light or calm; otherwise wind effects can produce atypical reaeration rates.

In deep, slowly moving backwater regions of rivers reaeration can either be simulated using a river formula or lake formula. The O'Connor-Dobbins method is probably the most appropriate stream formula to use, although for very slowly moving backwater regions the predicted reaeration coefficient can be between 0.01 to 0.05/day, which is below the range of k_2 values used in the development of the formula. If a lake reaeration formula is used, the reaeration rate coefficient can exceed the range predicted using the O'Connor-Dobbins formula. Under these conditions, wind and not depth and velocity can control the rate of reaeration.

3.3 CARBONACEOUS DEOXYGENATION

3.3.1 Introduction

Biochemical oxygen demand (BOD) is the utilization of dissolved oxygen by aquatic microbes to metabolize organic matter, oxidize reduced nitrogen, and oxidize reduced mineral species such as ferrous iron. The term BOD is also applied to the substrate itself. Concentrations of reduced minerals in waste streams are usually inconsequential, and so BOD is commonly divided into two fractions: that exerted by carbonaceous matter (CBOD) and that exerted by nitrogenous matter (NBOD). In domestic wastewaters, CBOD is typically exerted before NBOD, giving rise to the well-known two-stage BOD curve (although the processes can be simultaneous in natural systems and certain industrial effluents). Because wastewaters are potentially high in BOD, and because dissolved oxygen concentration is used as a principal determinant of the health of an aquatic system, BOD is a widely applied measure of aquatic pollution. This section discusses dissolved and

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suspended CBOD; Section 3.4 deals with NBOD and Section 3.5 treats benthic oxygen demand or sediment oxygen demand (SOD). All are related processes.

Figure 3-10 shows the major sources and sinks of carbonaceous BOD in natural waters. Anthropogenic inputs include point sources and nonpoint sources such as urban runoff and feedlot runoff. Autochthonous sources derived from the aquatic biota (particularly algae) can be important in some systems. Also, re-entrainment of oxygen-demanding material from benthic deposits may occur. Removal of CBOD from the water column occurs through sedimentation, microbial degradation and the sorption to or uptake by the benthic flora. Some components of BOD may also volatilize from the water column. Carbonaceous material which has settled or been sorbed becomes part of the benthic oxygen demand.

It is important that the analyst distinguish in the modeling process between both the sources of BOD and the instream removal mechamisms. Waste load allocation decisions based upon models which consider CBOD as a "lumped" quantity may not accurately or fairly assess the water quality impact of the point sources.

Efforts to characterize CBOD kinetics have focused chiefly on water-column decay processes, and that is the major emphasis of this section. A general expression for BOD decay is:

BOD + BACTERIA +
$$O_2$$
 + GROWTH FACTORS (NUTRIENTS)
 \longrightarrow CO_2 + H_2O + MORE BACTERIA + ENERGY

3.3.2 <u>Water Quality Modeling Needs</u>

Nearly all water quality models characterize CBOD decay with first order kinetics represented by:

$$\frac{dL}{dt} = -k_d L \qquad (3-26)$$

This equation when coupled with stream dissolved oxygen kinetics becomes the classic Streeter-Phelps equation:

$$D = \frac{k_{d}L}{k_{2}-k_{d}} \left[e^{-k_{d}t} e^{-k_{2}t} \right] + D_{0} e^{-k_{2}t}$$
(3-27)



Figure 3-10. Sources and sinks of carbonaceous BOD in the aquatic environment.

where D = dissolved oxygen deficit, mg/l
 k₂ = stream reaeration rate, 1/day, base e
 D₀ = initial stream deficit, mg/l

This equation in principle is similar in nearly all state-of-the-art water quality models.

In using this representation of BOD/DO for waste load allocation modeling, the analyst may require measurement or estimation of three independent factors which include:

- (a) the magnitude of <u>ultimate</u> CBOD of the point sources and the resulting instream spatial distribution,
- (b) the magnitude and spatial distribution of the instream CBOD removal rate, and
- (c) the ratio of point source ultimate CBOD to 5-day CBOD (if compliance is to be based upon $CBOD_{5}$).

It is important to note that the water quality model is based upon ultimate CBOD and not $CBOD_5$. Some models internally convert from 5 day to ultimate using an assumed ratio. In the case of the QUAL-II model (NCASI, 1982a), this ratio is 1.46 and is <u>not</u> user specified. This assumption has significant implications to water quality modeling because recent experience has shown that this ratio is both wasteload and receiving water specific. Ultimate to 5 day ratios as high as 30 have been reported for some paper industry wastewaters (NCASI, 1982d). Since first order kinetics are assumed in most models, the ultimate to 5 day ratio is not independent of the decay rate, k_d . Consequently, analysts should be certain that the river water ultimate to 5 day BOD is not assigned independently of the rate, k_d .

3.3.3 Nomenclature

Since microbial degradation is not the only process contributing to the observed depletion of CBOD in a water body (see Figure 3-10), laboratory rates of carbonacous deoxygenation must be distinguished from those which

occur in the field. The following terms are used herein to maintain these distinctions:

k₁ = laboratory-derived CBOD decay rate, k_d = CBOD decay rate in natural waters k_s = CBOD settling rate k_R = overall rate of CBOD removal from water column

By these definitions,

$$k_{\rm R} = k_{\rm d} + k_{\rm s} \tag{3-28}$$

$$k_d \ge k_1$$
, typically (3-29)

Note that uptake/sorption by the benthic biota is not explicitly dealt with. In practice, the effects of instream deoxygenation and benthic biological CBOD removal are difficult to distinguish. Thus reported k_d values may incorporate both processes. Unless otherwise specified, all rate coefficients discussed in this section are corrected to 20^oC, are to the base e, and are in units of inverse days.

3.3.4 Factors Affecting CBOD Removal

A number of factors are known to influence the rate at which CBOD is removed from the water column. Chief among these are water temperature, hydraulic factors, stream geometry and the nature of the carbonaceous material. The influence of these factors has been described by both theoretical and empirical formulations.

Like all biochemical processes, CBOD decay occurs at a rate which increases with increasing temperature up to the point where protein denaturation begins. This temperature dependence is generally formulated for a limited range of temperature as:

$$k_{\rm T} = k_{20} \theta^{(\rm T-20)}$$
 (3-30)

where k_{T_r} = rate constant at temperature T k_{20} = rate constant at $20^{\circ}C$ θ = an empirical coefficient.

This formulation is based on the Arrhenius equation which incorporates the energy of activation of the overall decay reaction. Arrhenius proposed the relationship:

$$\frac{d \ln k}{dT} = -\frac{E}{RT^2}$$
(3-31)

where T = absolute temperature, ^OK
 R = universal gas constant
 E = activation energy of the reaction
 k = rate constant

Integrating Equation (3-31) results in

$$\ln \frac{k}{k_{0}} = \frac{-E (T-T_{0})}{R T_{0} T}$$
(3-32)

where T_0 = arbitarily chosen reference temperature, ${}^{O}K$ k_0 = rate constant at temperature T_0

Equation (3-32) can be rewritten as

$$k = k_{o} \exp\left(\frac{-E (T-T_{o})}{R T_{o} T}\right)$$
(3-33)

Equations (3-30) and (3-33) are identical if θ is defined as

$$\theta = \exp\left(\frac{-E}{RT_0T}\right)$$
(3-34)

Note that whether $T-T_0$ is in units of ^OC or ^OK is of no concern. Thus θ , which is assumed to be independent of temperature in Equation (3-30), really has some slight temperature dependence.

Table 3-13 shows values of θ which have been used for CBOD decay. The value 1.047 is very widely used and corresponds to an energy of activation of 7900 calories per mole measured by Fair <u>et al</u>. (1968). There are limits to the applicability of this approach because the activation energy is not actually constant. Studies by Schroepfer <u>et al</u>. (1964) indicate that the value of 1.047 for θ is valid between 20^oC and 30^oC, but higher values are appropriate at lower temperatures. Fair <u>et al</u>. (1968) suggest θ values of 1.11 and 1.15 for 10^oC and 5^oC, respectively. Few water quality models incorporate a varying temperature dependence for CBOD degradation. Some impose temperature limits, generally 5-30^oC, outside of which the reaction is considered not to occur. The model SSAM-IV (Grenney and Kraszewski, 1981) adjusts the BOD decay rate for temperature via the expression:

$$k_{\rm T} = {}^{r}k_{20}$$
 (3-35)

where
$$\tau = \frac{0.1393 \exp(0.174(T-2))}{0.9 + 0.1 \exp(0.174(T-2))}$$

This is equivalent to varying the value of θ with temperature.

The 1.047 value originated from the work of Phelps and Theriault (Phelps, 1927, Theriault, 1927). The θ value of 1.047 was an average value obtained from three separate studies with a reported standard deviation of 0.005. Moore noted in 1941 that the correlation of the CBOD decay rate with temperature using the Arrenhius model was not strong, since correlation coefficients of 0.56 to 0.78 were obtained (Moore, 1941).

Water turbulence is hypothesized to influence the rate of BOD depletion in a receiving water in several ways. It influences k_s by controlling such processes as scour and sedimentation. Increased turbulence may enhance contact between BOD and the benthic biological community. It also influences the carbonacous deoxygenation rate, so that laboratory samples which are agitated during incubation yield higher k_1 values than quiescent samples (see Morrissette and Mavinic, 1978, for example). This confounds the use of k_1 values from static laboratory tests in place of field values

θ , Temperature	Temperature	
Correction Factor	Limits (^O C)	Reference
1.047		Chen(1970)
		Harleman <u>et al</u> . (1977)
		Medina (1979)
		Genet <u>et</u> <u>al</u> . (1974)
		Bauer <u>et</u> <u>al</u> . (1979)
		JRB (1983)
		Bedford <u>et</u> <u>al</u> . (1983)
		Thomahn and Fitzpatrick (1982)
		Velz (1984)
		Roesner <u>et</u> <u>al</u> . (1981)
1.05		Crim and Lovelace (1973)
		Rich (1973)
1.03-1.06	(0-5)-(30-35)	Smith (1978)
1.075		Imhoff <u>et al</u> . (1981)
1.024		Metropolitan Washington Area
		Council of Governments (1982)
1.02-1.06		Baca and Arnett (1976)
		Baca <u>et</u> <u>al</u> . (1973)
1.04		Di Toro and Connolly (1980)
1 05 1 15		
1.05-1.15	5-30	Fair <u>et</u> <u>al</u> . (1968)

TABLE 3-13 VALUES OF THE TEMPERATURE COMPENSATION COEFFICIENT USED FOR CARBONACEOUS BOD DECAY

of k_d . To more closely duplicate natural conditions, some investigators used stirring during laboratory incubations (NCASI, 1982a). This particular experiment showed <u>no</u> effect of stirring on the reaction kinetics.

Adjustment factors based on stream characteristics have also been used in BOD calculations. Bosko (1966) expressed k_d in terms of k_1 for streams by the expression:

$$k_{d} = k_{1} + n(V/D)$$
 (3-36)

where V = stream velocity, length/time

D = stream depth, length

n = coefficient of bed activity, dimensionless

The coefficient of bed activity is a step function of stream gradient; values are given in Table 3-14. This expression has been used in a version of QUAL-II applied to rivers in New England (JRB, 1983; Van Benschoten and Walker, 1984; Walker, 1983), by Terry <u>et al</u>. (1984) on the Illinois River, Arkansas, and by Chen and Goh (1981).

TABLE 3-14. COEFFICIENT OF BED ACTIVITY AS A FUNCTION OF STREAM SLOPE (from BOSKO, 1966)

Stream Slope (ft/mi)	n	
2.5	.1	
5.0	.15	
10.0	.25	
25.0	.4	
50.0	.6	

Stream hydraulic factors may also account for differences between the deoxygenation rate k_d and the overall BOD removal rate k_R . Table 3-15 shows examples of such differences in six U.S. rivers. Higher values of k_R are attributable to settling of particulate BOD. Bhargava (1983) observed rapid settling of particulate BOD just downstream from sewage outfalls in two

Indian rivers, where k_R was several times greater than farther downstream. He modeled this effect by considering the BOD to be composed of two fractions, using the expression:

$$L_{t} = L_{1}(1 - \frac{V_{s}}{D}t) + L_{2}exp(-k_{d}t)$$
 (3-37)

where $L_t = BOD$ remaining at downstream travel time t $L_1 = portion of original BOD$ removed by settling $L_2 = portion of original BOD$ subject to in-stream degradation $V_s = settling$ velocity of particulate BOD D = average stream depth

River	Flow (cfs)	Temp. (^O C)	BOD ₅ (mg/1)	k _d (day ⁻¹)	* k _R (day ⁻¹)
Elk	5	12	52	3.0	3.0
Hudson	620	22	13	0.15	1.7
Wabash	2800	25	14	0.3	0.75
Willamette	3800	22	4	0.2	1.0
Clinton	33			.1413	2.5
Tittabawassee				0.05	0.5

TABLE 3-15.	DEOXYGENATION RATES FOR SELECTED U.S.	RIVERS
	(ECKENFELDER AND O'CONNOR, 1961)	

*Note: These data are over 20 years old. It is likely that advances in waste treatment have altered the BOD kinetics in these waterways.

Some modelers distinguish between benthic and water-column CBOD removal, and assign rate coefficients to each type. For example, the sum of

settling and benthic biological CBOD uptake is widely portrayed as a firstorder process (Baca and Arnett, 1976; Grenney and Kraszewski, 1981; Duke and Masch, 1973; Orlob, 1974):

$$\frac{\partial L}{\partial t} = -(k_d + k_3)L \qquad (3-38)$$

where k_d = water-column deoxygenation rate k_3 = total removal rate to the benthos by settling and sorption

The settling rate alone may be derived from the particle settling velocity and mean depth of the water column:

$$k_{s} = \frac{V_{s}}{D}$$
(3-39)

The effects of scour are often incorporated into the benthic removal coefficient k_3 . This may be done implicitly, or by calculating k_3 as the sum of two first-order coefficients having opposite sign (Bauer <u>et al.</u>, 1979). Scour of benthic BOD is also treated as a zero-order process (e.g., Baca <u>et al.</u>, 1973):

$$\frac{\partial L}{\partial t} = -k_{R}L + L_{a}$$
(3-40)

where L_a = rate of BOD re-entrainment by scour, mg/(1-day).

The nature of the oxygen-demanding material also affects the rate of its removal from a receiving water. Particulate BOD, while it may be susceptable to settling, is more refractory than soluble BOD. Also two waters having the same ultimate BOD may show very different BOD depletion profiles. For in-stream BOD arising from a wastewater inflow, the degree of treatment of the wastewater is important. In general, the higher the degree of treatment, the greater the degree of waste stabilization, and the lower the deoxygenation rate will be. Fair <u>et al</u>. (1968) cite deoxygenation rates of 0.39, 0.35 and 0.12-0.23 per day for raw wastewater, primary and secondary effluent, respectively.

Martone (1976) observed a similar trend with paper industry wastewaters. Following biological treatment, rates as low as 0.02 per day, base e were observed. This low rate was attributed to the refractory humic material remaining in the wastewater. Similar low rates were also noted in receiving streams (NCASI, 1982a).

The U.S. Environmental Protection Agency (1983), using the data of Hydroscience (1971) and Wright-McDonnell (1979) has derived a relationship between stream depth and CBOD removal. This is shown in Figure 3-11. Note that the predicted decay rate corresponds to the sum of water column and benthic deoxygenation. Should SOD data be available, modelers are cautioned when using this figure to avoid double counting of SOD in the oxygen balance.

To this point, depletion of dissolved oxygen caused by CBOD decay has been implicitly considered to depend only on the concentration of substrate, i.e., CBOD. However, at low dissolved oxygen concentrations, oxygen may be limiting to the reaction. Provision for this "oxygen inhibition" is incorporated into many water quality models as discussed below.

Autochthonous sources may be a major influence on BOD dynamics. In lakes, carbon fixed by phytoplankton may become the predominant source of CBOD. Investigators have dealt with the input of autochthonous CBOD in several ways. Modeling Onondaga Lake in New York, Freedman <u>et al</u>. (1980) considered the biological contribution to water-column CBOD to be equivalent to the mass rate of phytoplankton production of organic material. Baca and Arnett (1976) considered the death rates of phytoplankton and zooplankton separately. These affected BOD according to the expression:

$$\frac{\partial L}{\partial t} = -k_d L + \alpha (F_p P + F_z Z)$$
(3-41)

where α = stoichiometric coefficient, mgO₂/mgC F_z = death rate of zooplankton from fish predation, 1/day F_p = death rate of phytoplankton from zooplankton grazing, 1/day

- P = phytoplankton concentration, mg-C/l
- Z = zooplankton concentration, mg-C/l

A Potomac Estuary Model by Thomann and Fitzpatrick (1982) considers the "non-predatory" death rate of phytoplankton to augment water-column CBOD:

$$\frac{\partial L}{\partial t} = -k_d L + \alpha k_{1D} P_c / BOD_{u5}$$
(3-42)



Benthic Deoxygenation Component



- where k_{1D} = death rate of phytoplankton other than from grazing, 1/days
 - P_c = phytoplankton carbon, mg/l BOD_{u5} = ratio of ultimate to 5-day CBOD, taken as 1.85 for phytoplankton

3.3.5 Predictive Expressions for Deoxygenation

The carbonaceous deoxygenation rate is determined in two general ways. Most investigators base their measures of k_d on the results of field or laboratory experiments that monitor dissolved oxygen or ultimate CBOD. In stream modeling, this traditional approach has recently been augmented by efforts to quantify k_d as a function of hydraulic parameters.

It is important to note that these correlations relied upon published values of k_d (such as Figure 3-11). No distinction was made as to how k_d was obtained; and in these correlations, observed instream values have equal weight with measured laboratory values. Thus, considerable ambiguity exists in the published literature with regard to the meaning of k_d and the resulting correlation may be of limited value.

Bansal (1975) attempted to predict deoxygenation rates based on the Reynolds number and the Froude number. This approach was found to have limited applicability (Novotny and Krenkel, 1975). More commonly, k_d is found as a function of flow rate, hydraulic radius or average stream depth. Wright and McDonnell (1979) utilized data from 36 stream reaches in the U.S. to derive the expression:

$$k_{d} = (10.3)Q^{-0.49}$$
 (3-43)

where $Q = flow rate, ft^3/sec$

They found that above flow rates of about 800 ft^3/sec , k_d is not a function of flow rate. The lower limit of the applicability of this expression is approximately 10 ft^3/sec . Below this flow rate, deoxygenation

rates were noted to consistently fall in the range 2.5-3.5 per day, independent of streamflow. For this same range of flowrates (between 10 and 800 cfs), an expression based on channel wetted perimeter was also found successful in predicting k_d :

$$k_d = 39.6P^{-0.84}$$
 (3-44)

where P = wetted perimeter, feet

The deoxygenation rate coefficient has also been expressed as an exponential function of stream depth (Hydroscience, 1971; Medina, 1979) and hydraulic radius (Grenney and Kraszewski, 1981).

Regardless of how carbonaceous deoxygenation rate coefficients are derived, they are widely applied in only two ways: first-order decay and simultaneous first-order decay. In the latter case, the CBOD is partitioned into more than one fraction; each fraction is degraded at a specific rate according to first-order kinetics. The first-order approximation for CBOD decay has been widely criticized, and multi-order or logarithmic models have been used by individual investigators (see Hunter, 1977 for a review).

Martone (1976), in a study of BOD kinetic models, observed that first order kinetics did not universally describe observed BOD data. In a few cases, a two-stage carbonaceous BOD model resulted in a better statistical fit (McKeown <u>et al.</u>, 1981). The Wisconsin Department of Natural Resources included this alternative formulation in its QUAL-III model (Wisconsin DNR, 1979). However, no alternative formulation has been shown to be universally superior, and oxygen-sag computations are comparatively easily performed for first-order decay. Hence, this is the pre-eminent model in use today.

Table 3-16 shows the expressions used by water quality modelers to describe the consumption of oxygen as a function of water column CBOD decay. Note that nonoxidative processes such as settling, where CBOD is removed from or added to the water column, do not contribute to dissolved oxygen

TABLE 3-16. EXPRESSIONS FOR CARBONACEOUS OXYGEN DEMAND USED IN WATER QUALITY MODELS

Depletion Rate of Dissolved Oxygen by CBOD Decay, $\frac{\partial DO}{\partial t}$	Model and Reference
-k _d L	MIT-DNM (Harleman <u>et al.</u> , 1977) Dynamic Estuary Model (DEM) (Genet <u>et al.</u> , 1974) EXPLORE-I (Baca <u>et al.</u> , 1973) USGS river model (Bauer <u>et al.</u> , 1979) HSPF (Inhoff <u>et al.</u> , 1981) DOSAG3 (Duke and Masch, 1973) DIURNAL (Deb and Bowers, 1983) QUAL-II (Roesner <u>et al.</u> , 1981) O'Connor <u>et al</u> . (1981)*
$-k_{d}L \frac{0_{2}}{k_{0_{2}} + 0_{2}}$	Lake Erie Model* (Di Toro and Connolly, 1980) Potomac Estuary Model (PEM) (Thomann and Fitzpatrick, 1982)
– ոն ^b ւ	Level III-Receiving (Medina, 1979)
-aQ ^b L	Wright and McDonnell (1979) Rinaldi (1979)
$-a0^{b}L = \frac{0_{2}}{k_{0_{2}} + 0_{2}}$	Bedford <u>et</u> <u>al</u> . (1983)
- ^k 1 ^L sol - ^k 2 ^L det	WQRRS (Smith, 1978) CE-QUAL-R1* (Corps of Engineers, 1982) Chen <u>et al</u> .* (1974)
$-k_{d}^{L} (depth, D > 2.44m) - \left(\frac{D}{2.44}\right)^{-0.434} k_{d}^{L} (D < 2.44m) $	RECEIV-II (Raytheon, 1974) WRECEV (Johnson and Duke, 1976)
-c ₁ (R _h ^c ₂) _L	SSAM-IV (Grenney and Kraszewski, 1981)
-κ _d φ _c L	Freedman <u>et al</u> . (1980)

****L*** represents a fraction of organic carbon, soluble and/or detrital, rather than CBOD.

Definition of symbols:

k _d	field CBOD oxidation rate
	carbonaceous BOD concentration concentration of dissolved oxygen
k_0,	half-saturation constant for oxygen
a,b,C ₁ ,C ₂	empirically-determined coefficients
D Q k ₁ , k ₂	water depth stream flow rate oxidation rates for two CBOD fractions
L _{sol} Ldet	soluble CBOD (<u>or</u> , dissolved organic carbon) particulate CBOD (particulate organic carbon)
R _h	steam hydraulic radius
φc	nonlinear O ₂ inhibition coefficient

depletion, and are not included in the expressions. In cases where k_d is calculated within the model using a hydraulic expression, that expression is included in the table. As shown, the rate expressions do not include temperature correction coefficients. Some of the models listed (starred references) do not treat CBOD per se, but organic carbon or carbonaceous detritus. The effect of low dissolved oxygen concentration is generally handled through a Michaelis-Menten formulation. A representative value of k_{02} , the half-saturation coefficient for oxygen uptake, is 0.5 mg/l. Some models partition oxygen-demanding matter into soluble and particulate fractions, with different rate coefficients. In limnological models, the particulate or detrital fraction may be determined as a function of the death of phytoplankton and zooplankton, with no additional particulate CBOD present.

3.3.6 Values of Kinetic Coefficients

Table 3-17 is a compilation of deoxygenation rate coefficients and the methods by which they were determined. Unless otherwise specified, the coefficient is k_d . In some cases, investigators reported k_R values as such; in other cases, rates reported as deoxygenation were actually observations of total removal (k_R) and they are cited as such. Most of the data are from rivers, although some lake and estuary values have been reported. The range of values reported as in-stream deoxygenation rates is wide, spanning more than two orders of magnitude.

3.3.7 Measurement of Ultimate BOD Decay Rate

In laboratory studies using BOD bottles, BOD exertion is found as the difference between sample and control dissolved oxygen depletion. Respirometry studies and reaerated stirred-reactor studies involve essentially continuous monitoring of oxygen usage. The results of these laboratory experiments produce cumulative oxygen demand-vs-time relationships.

A number of methods have been used to derive k_{\parallel} from these curves. Among these are:

Location	kg (1/days @ 20 ⁰ C, base e)	Method of Determining Coefficient	Reference
Potomac Estuary 1977 1978	0.14 ± 0.023 0.16 ± 0.05	field study	US EPA (1979a) US EPA (1979b)
Willamette River, OR	0.1-0.3		Baca <u>et al</u> . (1973)
Chattahoochee River, GA	0.16		Bauer <u>et al</u> . (1979)
Ganga River, India Yamuna River, India	3.5-5.6 (k _R) 1.4	field study	Bhargava (1983)
S. Fork, Shenandoah River	0.4(k _R)	field study	Deb and Bowers (1983)
Merrimack River, Mass	0.01-0.1	field study	Camp (1965)
Gray's Creek, Louisana	1.44 (k _R)	model calibration	Crane and Malone (1982)
Onondaga Lake, New York	0.10	model calibration	Freedman <u>et al</u> . (1980)
Yampa River, Colorado	0.40	model calibration	Grenney and Kraszewski (1981)
Skravad River, Denmark	0.15 0.90 (k _R)	field study	Hvitved-Jacobsen (1982)
S en eca Creek	0.008		Metropolitan Washington Council of Governments (1982)
Kansas (6 rivers) Michigan (3 rivers) Truckee River, Nevada Virginia (3 rivers) N. Branch, Potamac, WV South Carolina (3 rivers) New York (2 rivers) New Jersey (3 rivers) Houston Ship Channel, TX Cape Fear R. Estuary, NC	0.02-0.60 0.56-3.37 0.36-0.96 0.30-1.25 0.4 0.3-0.35 0.125-0.4 0.2-0.23 0.25 0.23	various methods	Reported by Bansal (1975)
Holston River, Tenn	0.4-1.5	model calibration	Novotny and Krenkel (1975)
New York Bight	0.05-0.25		0'Connor <u>et al</u> . (1981)
White River, Arkansas	0.004-0.66 (k ₁)	laboratory	Terry et al. (1983)

TABLE 3-17. VALUES OF KINETIC COEFFICIENTS FOR DECAY OF CARBONACEOUS BOD

study N. Fork Kings River, CA 0.2 Tetra Tech (1976) Lake Washington, WA 0.2 Chen and Orlob (1975) 0.15 0.17 (k_R) 0.02 (k_l) Ouachita River, Arkansas calibration Hydroscience (1979) laboratory NCASI (1982a) study 36 U.S. river reaches plus laboratory flume 0.08-4.24 field studies Wright and McDonnell (1979) San Francisco Bay Estuary 0.2 Chen (1970) Boise River, ID 0.75 Chen and Wells (1975) W. Fork, Trinity River, TX Jennings <u>et al</u>. (1982) 0.06-0.30 laboratory study

Location	k _d (1/days @ 20 ⁰ C, base e)	Method of Determining Coefficient	Reference
Willamette River, OR Arkansas River, CO	0.07-0.14 1.5	lab and field field study	McCutcheon (1983)
Lower Sacramento River, CA	0.41		Hydroscience (1972)
Delaware River Estuary Wappinger Creek Estuary, NY	0.31 0.31		
Potomac Estuary	0.16,0.21		Thomann and Fitzpatrick (1982)
Speed River, Ontario	1.0	field study	Gowda (1983)

- 1. The linear least-squares technique of Reed and Theriault
- 2. Thomas' graphical slope method
- 3. The moment method of Moore (1941)
- 4. Orford and Ingram's logarithmic method
- 5. Rhame's two-point method
- 6. Nemerow's general laboratory method (graphical)
- 7. The daily difference method of Tsivoglou (1958)
- 8. The rapid ratio method of Sheehy (1960)
- 9. Nonlinear regression method of NCASI (1982d).

The first six methods are discussed by Nemerow (1974). Gaudy <u>et al</u>. (1967) review and compare a number of calculation methods. Some of the techniques assume a particular kinetic model for the data, while others do not. The linear least-squares method can be used with a first or second-order BOD dependency, with somewhat different calculations. Orford and Ingram's method assumes that cumulative BOD exertion varies with the logarithm of elapsed time, and no limiting value is approached. The nonlinear regression technique has the advantage of flexibility in evaluating alternative BOD models.

Barnwell (1980) developed a nonlinear least-squares technique for fitting laboratory CBOD progressions. It is based upon the first-order decay model, and is suitable for implementation on programmable calculators or microcomputers. It allows computation of confidence contours for the estimates of k_1 and ultimate CBOD. The nonlinear regression technique also provides estimates of the confidence contours. Further discussion of BOD measurement techniques are contained in Stover and McCartney (1984) and Stamer et al. (1983).

Estimates of the length of time necessary to evaluate the BOD parameters have been provided by Berthouex and Hunter (1971). They determined, using statistical arguments, that this length of time is a function of the anticipated decay rate, k_1 . The time computed from $4/k_1$ is suggested as the maximum value. Barnwell (1980) and NCASI (1982d) have shown that the estimate of the confidence contours is directly related to the length of time the BOD experiment was conducted. As the length of time increases, the confidence contours get smaller.

In field estimation of deoxygenation rates, water samples from along the stream reach are collected, and their ultimate CBOD values are determined in the laboratory. Graphical methods are then used to find the CBOD decay rate. These techniques are based on a mass balance for BOD in the stream. Note that if unfiltered water samples are used, the rate calculated is k_R , not k_d . It may be that the two rates are essentially equivalent. An unvarying profile of suspended solids along the reach may indicate the validity of these measurements to estimate k_d . Alternatively, filtered samples may be incubated, and the contribution of particulate matter to BOD assumed to be insignificant.

The calculation methods described herein are based upon simplified forms of the BOD mass-balance equations. The user should assess carefully whether the necessary simplifying assumptions can reasonably be applied to the study system.

One simple and commonly used technique is for streams influenced by continuous point sources. The stream reach under study should have a relatively constant cross section, constant flow rate, and a single pointsource BOD loading. The BOD concentration downstream from the source is given by:

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$$L = L_{o} exp\left(\frac{-k_{R}X}{V}\right)$$
(3-45)

where X = distance downstream from source, length

 $L_0 = BOD$ concentration immediately downstream from source, at

X = 0, mass/volume

V = average stream velocity, length/time

A graph of the logarithm of BOD concentration versus distance downstream should show a straight-line relationship with a slope of $-k_R/V$ if decay is first order. Sometimes the slope may be more steep for the first few miles below a point source, where settling of BOD as well as decay is occurring (Deb and Bower, 1983). The slope may be found graphically or by linear regression. Figure 3-12 is an example of this type of computation. If the slope is determined by regression, the <u>natural</u> log of BOD should be regressed on distance. If the slope is found graphically from a semi-log plot, it must be multiplied by 2.3 (to convert from base-10 to base-e) for model applications.

The same approach is possible for tidally influenced rivers, as discussed in Zison <u>et al</u>. (1978). However, the tidally averaged dispersion coefficient is required as an additional piece of information and will add some degree of uncertainty to the predicted k_d value.

3.3.8 Summary and Recommendations

Although its shortcomings have been widely discussed, the first-order model is still the common method for simulating instream CBOD kinetics. Relative ease of computation, a long history of use and the absence of alternative formulations which are superior over a range of conditions are probably responsible for this precedent.

In estimating k_d, there is increasing use of various stream hydraulic parameters. Estimates based on flow rate seem to be most successful,



Figure 3-12. Example computation of $k_{\mbox{R}}$ based on BOD measurements of stream water.

although stream geometric parameters such as hydraulic radius and depth are also used. The use of hydraulic characteristics for k_d prediction has limits, since deoxygenation is independent of flow rate at both high and low flow. These predictive equations should be used with caution.

To assess CBOD fluxes based on site-specific data, it is essential to have some familiarity with the water body under study. A reconnaissance survey can help elucidate the possible importance of CBOD sedimentation or resuspension, as well as the magnitude of aquatic biological processes. The survey is also an opportunity to assess what assumptions can reasonably be made about the system to simplify calculations.

For those river waters and effluents which contain significant concentrations of NBOD, the analyst must consider an appropriate procedure for the separation of NBOD from CBOD in the ultimate BOD test. Currently, two techniques are used which include: the use of nitrification inhibitors such as TCMP and others, and the monitoring of nitrogen series with time during the test to define the NBOD. There is currently no consensus as to which technique is best. Nitrification inhibitors have been observed to have an unpredictable inhibition effect on the CBOD kinetics as well (Martone, 1976). For large modeling projects, the monitoring of nitrogen species in the BOD bottle tests can create significant additional laboratory expense. Though likely to be more expensive, the latter technique provides more information regarding the CBOD and NBOD kinetics and is recommended by NCASI (1982b).

The investigator should exercise caution in using deoxygenation coefficients obtained for other water bodies. The wide range of values in Table 3-17 indicates substantial variation in rate estimation and reporting procedures. Unfortunately, many investigators automatically equate k_1 or k_R with k_d , and do not fully consider the different meanings of these rates. Some report k_d and k_R values without stating whether these apply to total BOD or CBOD, are temperature-corrected, are to base e or base 10, etc.

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One way to handle these uncertainities is to conduct sensitivity analyses of model predictions. Such analyses are beyond the scope of many projects; however, results are available for many widely-used models either in the model documentation or in the final reports of large-scale projects. Examples of sensitivity analyses for deoxygenation rate coefficients are Crane and Malone (1982), Thomann and Fitzpatrick (1982) and NCASI (1982a).

In addition, it is possible to quantitatively evaluate the uncertainity associated with an estimated coefficient. Barnwell's (1980) and NCASI's (1982b) calculation techniques allow computation of confidence limits for an estimated k_1 value. Jaffe and Parker (1984) provide a procedure for estimating the uncertainty of k_d values as influenced by the field sampling scheme. Chadderton <u>et al</u>. (1982) evaluate the relative contributions to uncertainty of the parameters of the Streeter-Phelps equation.

3.4 NITROGENOUS BIOCHEMICAL OXYGEN DEMAND

3.4.1 Introduction

The transformation of reduced forms of nitrogen to more oxidized forms (nitrification) consumes oxygen. Although nitrification is also a nutrient transformation process, this section addresses the oxygen consumption aspects, since numerous models simulate nitrogenous biochemical oxygen demand (NBOD) without detailing nitrogen transformations.

Nitrification is a two-stage process. The first stage is the oxidation of ammonia to nitrite by <u>Nitrosomononas</u> bacteria:

$$NH_4^+ + 1.5 \ 0_2^- \rightarrow NO_2^- + H_2^- 0 + 2H^+$$
 (3-46)
(14 gm) (48 gm)

Stoichiometrically 48/14 or 3.43 gm of oxygen are consumed for each gram of ammonia-nitrogen oxidized to nitrite-nitrogen. During the second stage of nitrification <u>Nitrobacter</u> bacteria oxidize nitrite to nitrate:

$$NO_{2}^{-} + 1/2 O_{2}^{-} NO_{3}^{-}$$
 (3-47)
(14 gm) (16 gm)

Stoichiometrically 16/14 = 1.14 gm of oxygen are consumed per gram of nitrite-nitrogen oxidized. If the two reactions are combined, the complete oxidation of ammonia can be represented by:

 $NH_4^+ + 2 O_2 \longrightarrow NO_3^- + H_2O + 2H^+$ (3-48) (14 gm) (64 gm)

As expected, 64/14 = 4.57 gm of oxygen are required for the complete oxidation of one gram of ammonia.

In the reactions above, the organic-nitrogen form does not appear, since organic-nitrogen is hydrolyzed to ammonia, and does not consume oxygen in the process. However, organic nitrogen will eventually contribute to the NBOD, as the following equation shows:

$$NBOD = 4.57 (N_0 + N_1) + 1.14 N_2$$
(3-49)

where N_0 = organic-nitrogen concentration, mass/volume N_1 = ammonia-nitrogen concentration, mass/volume N_2 = nitrite-nitrogen concentration, mass/volume

The stoichiometric coefficients of 3.43, 1.14, and 4.57 in the equations above are actually somewhat higher than the total oxygen requirements because of cell synthesis. Some researchers (e.g., Wezernak and Gannon, 1967 and Adams and Eckenfelder, 1977) have suggested that the three coefficients be reduced to 3.22, 1.11, and 4.33, respectively.

3.4.2 Modeling Approaches

Modelers use both the two-stage and one-stage approach to simulate NBOD decay, as shown by Table 3-18. First order kinetics is the predominant

method used to simulate the process. Oxygen limitation is used by some modelers (e.g., O'Connor <u>et al</u>., 1981; Thomann and Fitzpatrick, 1982; and Bedford <u>et al</u>., 1983).

Relatively few modelers explicitly simulate the effects of benthic nitrification (exceptions are Williams and Lewis, 1984 and Mills, 1976). The models of Williams and Lewis, and Mills were developed for relatively shallow streams where bottom effects could be important. Of these two, only Mills looks at the details of oxygen and nitrogen transfer from the water column into an attached nitrifying biofilm. Several studies (Kreutzberger and Francisco, 1977; Koltz, 1982) have confirmed that nitrifying bacteria can thrive in the beds of shallow streams, and that, in the streams they investigated, nitrification occurred primarily in the bed, and not in the water column. Denitrification has been shown to occur in stream sediments

TABLE 3-18. EXPRESSIONS FOR NITROGENOUS BIOCHEMICAL OXIDATION RATES USED IN A VARIETY OF WATER QUALITY MODELS

Expression for Nitrogenous Oxidation Rate. 0D0/0t	Model and/or Reference
$-a_1 k_{n_1} N_1 - a_2 k_{n_2} N_2$	WQRRS (Smith, 1978)
1 2	Bauer <u>et</u> <u>al</u> . (1979)
	QUAL-II (Roesner <u>et al</u> ., 1981)
	SSAM IV (Grenney and Kraszewski, 1981)
	CE-QUAL-R1 (U.S. Army COE, 1982)
	RECEIV II (Raytheon, 1974)
	NCASI (1982d)
	Baca and Arnett (1976)
	MIT Transient Water Quality Model (Harleman <u>et</u> <u>al</u> ., 1977)
	DOSAG3 (Duke and Masch, 1973)
	HSPF (Imhoff <u>et</u> <u>al</u> ., 1981)
	Genet <u>et</u> <u>al</u> . (1974)
-kn Ln	DIURNAL (Deb and Bowers, 1983)
	Gowda (1983)
	EXPLORE-1 (Baca <u>et al</u> ., 1973)
	Bauer <u>et</u> <u>al</u> . (1979)
	Di Toro and Matystik, 1980

Expression for Nitrogenous Oxidation

Rate, ØD0/Øt		Model and/or Reference			
- $a_3 k_n \frac{0_2}{0_2 + K_{nit}} N_1$		O'Connor <u>et al</u> . (1981) Thomann and Fitzpatrick (1982)			
$-a_3 a_4 q^b \frac{0_2}{0_2 + K_{nit}} N_1$		Bedford <u>et al</u> . (1983)			
Time Shifted First Order (time delayed) Lagged First Order (nonoxidative step followed by an oxidative step)		NCASI (1982d) NCASI (1982d)			
Benthic N	itrification:				
- a ₃ S _n (zero order kinetics)		Williams and Lewis (1984) Bauer <u>et al</u> . (1979)			
- J _C (Monod kinetics)		Mills	(1976)		
Definition kn1 kn2 kn a1 a2 a3	of Symbols: ammonia to nitrite oxidation rate nitrite to nitrate oxidation rate NBOD decay rate 3.43, typically 1.14, typically 4.57, typically	0 ₂ K _{NIT} Sn J _c	dissolved oxygen concentration half-saturation constant zero order benthic nitrification rate benthic oxygen flux rate by nitrifying organisms growing in an attached biofilm		
3 α ₄ , b Ν ₁ Ν ₂ L _n	unspecified NH $\frac{4}{4}$ -N NO $\frac{2}{2}$ -N nitrogenous BOD				

as well (Wyer and Hill, 1984). Denitrification is discussed in more detail in Chapter 5.

The most straightforward method of including the effects of organic nitrogen on the potential depletion of dissolved oxygen is to simulate the conversion of organic nitrogen to ammonium nitrogen (a rate of 0.1/day is typically used). The increased ammonia concentration is then available to exert an oxygen demand. However, it is not clear that all the models in Table 3-18 simulate the organic nitrogen to ammonia conversion. Some models appear to combine ammonia and organic nitrogen together into a single term.

While first order kinetics is the most popular approach for simulating nitrification in natural systems, Monod and zero-order kinetics are often used to simulate nitrification in wastewater treatment processes (Hall and Murphy, 1980; Charley <u>et al.</u>, 1980; Rittmann and McCarty, 1978). Figure 3-13 shows how nitrification is simulated using Monod kinetics. At the high level of reduced nitrogen compounds found in wastewater, nitrification can proceed at its maximum rate, and thus is zero order (independent of substrate concentration). At lower reduced nitrogen competence.



REDUCED NITROGEN CONCENTRATION

Figure 3-13. Effect of Reduced Nitrogen Concentration on Nitrification Rate as Reported by Borchardt (1966).

Several researchers (e.g., Wild <u>et al.</u>, 1971; Kiff, 1972; Huang and Hopson, 1974) have established concentration ranges of ammonia nitrogen when zero order kinetics appear to be followed. The range is quite wide, from 1.6 mg/1 to 673 mg/1. Concentrations of ammonia-nitrogen in natural waters can exceed the lower end of the scale reported, and indicate that zero order or Monod kinetics may be appropriate in these circumstances (e.g., see Wilber <u>et al.</u>, 1979).

3.4.3 Factors That Affect Nitrification

Table 3-19 summaries studies that have investigated factors that influence the rate of nitrification. The factors include pH, temperature, ammonia and nitrite concentrations, dissolved oxygen, suspended solids, and organic and inorganic compounds. Sharma and Ahlert (1977) also provide a review of previous studies.

Many of the studies have been carried out in controlled environments, and not in natural waters. Also, the concentration of organic substances which have inhibitory effects on nitrification are often, but not always, well above 1 mg/1 (Wood <u>et al.</u>, (1981)), so that the compounds are not likely to be inhibitory in natural waters.

Modelers typically consider only the temperature effect on nitrification, although a few do model dissolved oxygen limitations (see Table 3-18). Other inhibitory or stimulatory effects are assumed to be included in the "reference" rate (typically at 20° C) measured or otherwise selected for the modeling applications.

Researchers have found that within the temperature range of 10° C to 30° C temperature effects can be simulated by the following expression:

$$k_n = k_{n20} \theta^{T-20}$$
 (3-50)

where k_{n20} = nitrification rate coefficient at 20^oC

 θ = temperature correction factor
TABLE 3-19. SUMMARY OF FACTORS THAT INFLUENCE NITRIFICATION

Reference	Factors Investigated	Comments
Sharma and Ahlert (1977)	Temperature, pH, Nitrogen Concentrations, Dissolved Oxygen, Organic Compounds	In reviews of previous studies found: 12 studies for dissolved oxygen, 15 studies for pH, 14 studies for the effect of ammonia levels on nitrification, 11 studies of effects of nitrate levels on nitrification, 34 studies on substances that are required or stimulate nitrification; 47 studies on substances that inhibit nitrification.
Stenstrom and Poduska (1980)	Dissolved Oxygen	In this literature review of the effects of dissolved oxygen concentrations on nitrification, the lowest concentration where nitrification occurred is approximately 0.3 mg/l. However, the dissolved oxygen level required for no oxygen inhibition varied to as high as 4.0 mg/l, while other researchers found only 0.5 mg/l is required.
Wild, Sawyer, and McMahon (1971)	pH, Temperature, Ammonia- nitrogen	Studies were conducted in a pilot nitrification unit receiving trickling filter effluent. Ammonia nitrogen did not inhibit nitrification at concentrations less than 60 mg/l. Optimum pH for nitrification was found to be 8.4. The rate of nitrification increased with temperature in the range 5 °C to 30° C.
Kholdebarin and Oertli (1977a)	pH, Ammonia-nitrogen	For water samples collected from the Whitewater River, California, the optimum pH for nitrification of ammonia and nitrite was 8.5. Nitrite oxidation was stimulated by the addition of 3 mg/l ammonium.
Kholdebarin and Oertli (1977b)	Suspended Solids	In water from the Whitewater River in California, suspended solids were found to have a stimulatory effect on nitrification, presumably caused by the physical support provided by the solids.
Bridle, Climenhage, Stelzig (1979)	pH, Temperature, Ammonia- nitrogen, Copper	In batch reactors ammonia nitrification was not inhibited for TKM levels up to 340 mg/l. The optimum pH for nitrification was 8.5. The nitrification rate increased approximately 2.5 fold for each 10°C increase. Copper concentrations of 3000 mg/l produced no adverse effect; concentrations of 6000 mg/l were inhibitory.
Quinlan (1980)	Temperature	Temperature for optimal ammonia and nitrite oxidation was found to depend on nitrogen concentrations. At low nitrogen concentra- tions the optimum temperatures were 35.4°C for ammonia oxidation and 15.4°C for nitrite oxidation.
Wood, Hurley, Matthews (1981)	Organic Compounds	Laboratory studies were conducted using filtered liquor from return activated sludge. Approximately 20 compounds were tested in concentrations from 10 to 330 mg/1. Approximately half the compounds had no inhibitory effects.
Hockenbury and Grady (1977)	Organic Compounds	This study reviewed previous work on the influence of organic compounds on nitrification. Additionally, they found that many compounds did not inhibit nitrification at concentrations as high as 100 mg/l, while other compounds inhibited nitrification at concentrations less than 1 mg/l.

Values of the temperature correction factor are reported in Table 3-20. Temperature correction values are slightly higher for ammonia oxidation than for nitrite oxidation. The mean temperature correction values are 1.0850 for ammonia oxidation and 1.0586 for nitrite oxidation. Many models use temperature correction factors slightly lower than these values. Typically modelers use only one temperature correction coefficient, and do not distinguish between temperature corrections for ammonia and nitrite oxidation. Example of temperature correction factors used in selected models are:

- 1.05, EXPLORE-1 (Baca et al., 1973)
- 1.065, MIT Nitrogen model (Harleman et al., 1977)
- 1.08, New York Bight model (O'Connor <u>et</u> <u>al.</u>, 1981)
- 1.047, QUAL-II (Roesner <u>et al.</u>, 1981), USGS Steady State Model (Bauer <u>et al.</u>, 1979)
- 1.045. Potomac Estuary Model (Thomann and Fitzpatrick, 1982)

TABLE 3-20

TEMPERATURE CORRECTION FACTOR, θ , FOR NITRIFICATION

Reference Am	monia Oxidation	Nitrite Oxidation
Stratton (1966); Stratton and McCarty (1967)	1.0876	1.0576
Knowles <u>et al</u> . (1965)	1.0997	1.0608
Buswell <u>et al</u> . (1957)	1.0757	-
Wild <u>et al</u> . (1971)	1.0548	-
Bridle <u>et al</u> . (1979)	1.1030	-
Sharma and Ahlert (1977)	1.069	1.0470
Laudelout and Van Tichelen (19	60) -	1.0689
Mean	1.0850	1.0586

- 1.02-1.03, WQRRS (Smith, 1978)
- 1.08, Lake Erie model (Di Toro and Connolly, 1980)

While Equation (3-44) can provide adequate temperature correction up to approximately 30° C, beyond this temperature the nitrification rate is inhibited by the high temperature, so the relationship no longer holds. Figure 3-14 illustrates the effect of temperature on nitrification and shows that the rate rapidly decreases at temperatures beyond 30° C.



Figure 3-14. Effect of Temperature on Nitrification as Reported by Borchardt (1966).

The influence of pH on rates of nitrification is also quite important. If pH is outside of the range 7.0 to 9.8, significant reduction in nitrification rates can occur. Table 3-19 indicated that the optimal pH for nitrification is approximately 8.5 and at pH values below about 6.0, nitrification is not expected to occur. Figure 3-15 shows the effect of pH on ammonia and nitrite oxidation. A more thorough review of pH effects is contained in Sharma and Ahlert (1977).

Effects of solid surfaces have frequently been documented as being important for nitrification (e.g., Kholdebarin and Oertli, 1977). The following section discusses this effect more fully through a number of case studies.



3.4.4 Case Studies and Nitrification Rates

Table 3-21 summaries case studies of nitrification in natural waters. These studies are intended to show how various researchers have determined nitrification rates in natural waters, some of the complications that can occur in doing so, and what the rates are.

Except for Slayton and Trovato (1978, 1979) all the case studies are for streams or rivers. Note the high variability in nitrification rates from study to study. For rivers, documented first order nitrification rates varied from 0.0/day to 9.0/day. For the two Potomac estuary studies, the nitrification rates were fairly small and constant (0.1 to 0.14/day). The nitrification rate was often determined from plots of TKN or NBOD versus distance or travel time. Figure 3-16 shows an example. A number of the studies (e.g., Koltz (1982) and Ruane and Krenkel (1978)) emphasized that algal uptake of ammonia can be an important transformation and should be accounted for in the rate determination. The increase of nitrate nitrogen can be monitored, as well as the decrease in ammonia nitrogen for more conclusive evidence that nitrification is occurring. Bingham <u>et al</u>. (1984) show how the nitrification rate constant is changed in a QUAL-II application when algae is simulated compared to when algae is not simulated.

Several of the case studies have enumerated nitrifying bacteria present in the water column and in the sediments (e.g., Kreutzberger and Francisco (1977)). Far more nitrifying organisms are typically present in the sediments than in the water column. Case studies on the following rivers have reached the same conclusion:

- Kanawha River, West Virginia (U.S. EPA, 1975)
- Tame and Trent Rivers, England (Curtis <u>et al.</u>, 1975)
- North Buffalo Creek, North Carolina (Williams and Lewis, 1984)
- Willamette River, Oregon (Rinella <u>et al.</u>, 1981)
- Chattahoochee River, Georgia (Jobson, undated)

TABLE 3-21. CASE STUDIES OF NITRIFICATION IN NATURAL WATERS

					*
Reference	Study Area	Purpose of Study	Reported Nitrification Rates	Methods of Determining Nitrification Rates	Comments
Wezernak and Gannon (1968) Stratton and McCarty (1969) Blain (1969)	Clinton River, Michigan, a shallow stream with velocities of 1-2 fps	To mathematically model nitrifica- tion in a stream (This was one of the earlier modeling attempts)	ammonia oxidation: 3.1-6.2/day nitrite oxidation: 4.3-6.6/day	Measurements of ammonia, nitrite, and nitrate at three locations within the stream	The nitrogen balance developed indicated that nitrification was primary mechanism responsible for observed nitrogen transformations.
Gowda (1983)	Speed River, Canada, a relatively shallow river with velocities from 0.3 to 1.5 fps	To determine the affects of nitrifica- tion on dissolved oxygen levels within the river	0.2-4.41/day	Plots of TKN versus travel time	NBOD predicted to be much more important on the dissolved oxygen deficit than CBOD.
Curtis (1983)	Still River, Connecticut	To determine the fate of ammonia in the river by simulating oxidative and non- oxidative transforma- tions	0.0-0.4/day	Comparison of total ammonia decrease to nitrate increase	
Deb and Bowers (1983)	South Fork of Shenandoah River	To simulate the dissolved oxygen of the river using the DIURNAL model	0.2-1.25/day	Plots of NBOD versus travel time	
Deb, Klafter-Snyder, and Richards (1983)	Leatherwood, Creek, Arkansas	To simulate the dissolved oxygen dynamics of a small surface-active stream for wasteload allocation purposes	1.1-7.1/day	Plots of TKN versus travel time	
Ruane and Krenkel (1978)	Holston River, Tennessee	To examine the various nitrogen transformations that occur in the river	0.15-0.3/day	Rate of ammonia reduction and rate of nitrate increase	The complexity of the nitrogen cycle in the Holston River is discussed including the effects of ammonia transformations other than caused by nitrification.
Koltz (1982)	Iowa and Cedar Rivers, Iowa	To determine the locations and rates of nitrification down- stream from two waste- water treatment plants	0.5-9.0/day (continued)	Rate of ammonia reduction and rate of nitrate increase	Algal assimilation of ammonia appeared to be an important transformation process. Labora- tory rates of nitrification varied from 0.02-0.35/day.

Reference	Study Area	Purpose of Study	Reported Nitrification Rates	Methods of Determining Nitrification Rates	Comments
Kreutzberger and Francisco (1977)	Morgan Creek, Ruin Creek, and Little Lick Creek; three shallow streams in North Carolina	To determine the distributions of nitrifying organisms, and to examine the nitrogen transformation occurring in the streams	-	-	Counts of nitrifying organisms were enumerated in the water column and in the top 1 cm of sediments. The populations were much larger in the sediments, which indicated that nitrifica- was occurring predominantly in the sediments and not in water column.
Cirello <u>et</u> <u>al</u> . (1979)	Passaic River, New Jersey	To determine whether nitrification was a significant process in the Passaic River	-	-	There were high ammonia nitrogen concentrations in the river with relatively little nitrification occurring. The potential for nitrification appeared high, and was expected to be exerted if water quality within the river improved.
Finstein and Matulewich (1974)	Passaic River, New Jersey	To determine the distribution of nitrifying bacteria in the river	-	-	Nitrifying bacteria were found to be from 21 to 140,000 times more abundant volumetrically in sedi- ments than in the water column.
Slayton and Trovato (1978, 1979)	Potomac Estuary	To determine factors important in the oxygen balance within the estuary	0.10-0.14/day	Thomas Graphical Method	-

TABLE 3-21. (continued)



Additional nitrification rates are shown in Table 3-22. Bansal (1976) has documented nitrification rates in numerous rivers throughout the United States, and developed a method to predict nitrification rate based on hydraulic data. His method has been criticized by Gujer (4977) and Brosman (1977) and is not reported.

Relatively few nitrification rates were found for lakes or estuaries. The few data in Table 3-22 for lakes and estuaries are generally in the range 0.1/day to 0.5/day.

River	Maximum	Average	Minimum	Reference
Grand River, Michigan	3.9	2.6	1.9	Courchaine (1968)
Clinton River, Michigan	15.8 4.0	5.7 1.9	2.2 0.4	Wezernak and Gannon (1968)
Truckee River, Nevada	2.4	1.9		O'Connell and Thomas (1965)
South Chickamaugo Creek, Tennessee	1.9		1.1	Tennessee Valley Authority Ruane and Krenkel (1978)
Oostanaula Creek, Tennessee	0.8		0.1	Tennessee Valley Authority Ruane and Krenkel (1978)
Town Branch, Alabama		0.7		Tennessee Valley Authority Ruane and Krenkel (1978)
Chattahoochee River, Georgia		0.44		Stamer <u>et</u> <u>al</u> . (1979)
Willamette River, Oregon	0.7		0.4	Rinella <u>et</u> <u>al</u> . (1981)
Flint River, Michigan	2.5	1.4	0.1	Bansal (1976)
Upper Mohawk River, New York	0.3	0.25	0.25	Bansal (1976)
Lower Mohawk River, New York	0.3	0.3	0.3	Bansal (1976)
Bange Canal near Upper Mohawk River, New York	0.25	0.25	0.25	Bansal (1976)
Ohio River	0.25	0.25	0.25	Bansal (1976)
Big Blue River, Nebraska	0.25	0.11	0.03	Bansal (1976)
Delaware River Estuary	0.54	0.3	0.09	Bansal (1976)
Willamette River, Oregon		0.75* 1.05**		Alvarez-Montalvo, <u>et al</u> . undated
Ouachita River, Arkansas and Louisiana		0.1* 0.5**		NCASI (1982c)
Potomac Estuary		0.09-0.13		Thomann and Fitzpatrick, 1982
Lake Huron and Saginaw Bay		0.20		Di Toro and Matystik, 1980
New York Bight		0.025		0'Connor <u>et al</u> . 1981

Note: Nitrification rates are in units of 1/day.

Ammonia Oxidation
 Nitrite Oxidation

3.4.5 Summary

Typically modelers simulate nitrification by first order kinetics, either the single stage or two stage approach. Most nitrification rate data have been collected in streams and rivers, where the rates can be quite variable due to bottom effects. Instream rates can differ significantly from laboratory or bottle rates. However, for large bodies of water (typically lakes or estuaries) the relative importance of the bottom is diminished, and nitrification rates tend to approach bottle rates. Available data suggest nitrification rates between 0.1 to 0.3/day are often appropriate for large lakes, large rivers, or estuaries.

In flowing waters, instream nitrification rates are often determined based on TKN versus travel time. Care should be taken that the assumptions of the approach are met, and that processes that transform nitrogen other than nitrification are assessed (i.e., the other components of the nitrogen cycle).

Because benthic nitrification can be important in small streams, it is important not to "doubly count" oxygen sinks in modeling applications. A component of the sediment oxygen demand would include benthic nitrification, so the two processes need to be accounted for in a mutually exclusive way for modeling applications.

Very few studies actually try to measure populations of nitrifiers in natural systems. This, however, is the most conclusive method to confirm that nitrification is occurring.

3.5 SEDIMENT OXYGEN DEMAND (SOD)

3.5.1 Concept of SOD

Oxygen demand by benthic sediments and organisms can represent a large fraction of oxygen consumption in surface waters. Benthal deposits at any• given location in an aquatic system are the result of the transportation and deposition of organic material. The material may be from a source outside the system such as leaf litter or wastewater particulate BOD (allochthonous material), or it may be generated inside the system as occurs with plant growth (autochthonous material). In either case, such organic matter can exert a high oxygen demand under some circumstances. In addition to oxygen demand caused by decay of organic matter, resident invertebrates can generate significant oxygen demand through respiration (Walker and Snodgrass, 1984). The importance of this process to water quality modeling is reflected in a recent symposium (Hatcher and Hicks, 1984). This same symposium also reviewed measurement techniques and a concensus favoring <u>in</u> <u>situ</u> measurement was reached.

It is generally agreed (e.g., Martin and Bella, 1971) that the organic matter oxygen demand is influenced by two different phenomena. The first is the rate at which oxygen diffuses into the bottom sediments and is then consumed. The second is essentially the rate at which reduced organic substances are conveyed into the water column, and are then oxidized. Traditional measurement techniques, whether they are performed <u>in situ</u> or in the laboratory, do not differentiate between the two processes but measure, either directly or indirectly, the gross oxygen uptake. Hence, in modeling dissolved oxygen, a single term in the dissolved oxygen mass balance formulation is normally used for both processes. If the two phenomena are modeled separately (e.g., see Di Toro, 1984), then additional modeling complexity is necessary.

The process is usually referred to as sediment oxygen demand (SOD) because of the typical mode of measurement: enclosing the sediments in a chamber and measuring the change in dissolved oxygen concentration at several time increments. This technique is used in the laboratory or in situ. The oxygen utilized per unit area and time (gO_2/m^2-day) is the SOD. The technique measures oxygen consumption by all of the processes enclosed in the chamber: chemical reactions, bacterially mediated redox reactions, and respiration by higher organisms (e.g., benthic worms, insects, and molluscs). Background water column respiration is then subtracted from this rate to compute the component due solely to the

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sediment interface. SOD is usually assumed to encompass the flux of dissolved constituents such as DO to sediment and reduced chemicals to the water column. However, solid particle flux as BOD or sediment entrainment or settling is modeled separately.

The major factors affecting SOD are: temperature, oxygen concentration at the sediment water interface (available oxygen), makeup of the biological community, organic and physical characteristics of the sediment, current velocity over the sediments, and chemistry of the interstitial water. Each of these factors is a resultant of other interacting processes occurring elsewhere in the aquatic system. For example, temperature and available oxygen can be changed as a result of transport and biochemical processes in the water column or system boundaries. Temperature and oxygen are usually modeled explicitly, and can be used as input variables to the SOD process equations. Another important linkage is that the biological community will change with the water quality (e.g., oxygen and nutrient concentrations) and productivity of the system. The organic characteristics will change over the long term due to settling of organic matter (detritus, fecal matter, phytoplankton) and its subsequent degradation and/or burial by continued sedimentation. The biological community and the organic and physical characteristics of the bottom sediments are usually treated as a composite characteristic of the particular system. Recently, techniques have been developed for investigating these factors; however, the usual technique is to measure the SOD directly rather than the underlying factors that control the processes of SOD.

At least two major factors affecting SOD are usually neglected in SOD modeling. Current velocity is often neglected despite the fact that it has a major effect on the diffusive gradient of oxygen beginning just below the sediment-water interface. Most measurement techniques provide mixing.by internal mixing or by recirculating or flow-through systems to minimize the effect of concentration gradients. However, the velocity of such systems may be insufficient (Whittemore, 1984a) or may be so vigorous as to cause scour and resuspension. Interstitial water chemistry affects substrates for biochemical and non-biochemical oxidation-reduction reactions and their

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reaction rates. This factor is also usually neglected in SOD measurements and kinetic formulations.

3.5.2 Kinetics

The generalized equation for sediment oxygen demand is:

$$\frac{dC}{dt} = \frac{-SOD}{H} = f(dissolved oxygen, temperature, organisms, substrate) (3-51)$$

where H = water depth, m
SOD = sediment oxygen demand (as measured), g02/m²-day
t = time
C = oxygen concentration in the overlying water, mg/l

3.5.2.1 Dissolved Oxygen

The benthic oxygen consumption has been hypothesized to depend on the dissolved oxygen concentration in the overlying waters (e.g., Edwards and Rolley, 1965; McDonnell and Hall, 1969):

$$SOD = a C^{b}$$
(3-52)

where a,b = empirically determined constants

In the McDonnell and Hall (1969) study, b was found to be 0.30 and a to vary from 0.09 to 0.16, primarily as a function of the population density of benthic invertebrates.

Lam <u>et al</u>. (1984) use a Michaelis-Menten relationship to express the effects of oxygen on SOD:

$$\frac{dC}{dt} = -\frac{k_s A_s}{V} \frac{C}{K_{0_2} + C}$$
(3-53)

where
$$k_s$$
 = rate constant for SOD in Lake Erie, 0.1 g $0_2/m^2$ -day
 A_s = area of the sediment, m^2
 V = volume of water layer, m^3
 K_{0_2} = oxygen half saturation constant (1.4 mg/l)
 C = oxygen concentration, mg/l

Walker and Snodgrass (1984) divided SOD in Hamilton Bay in Lake Ontario into two fractions: chemical-microbial (CSOD) and biological (BSOD). The chemical fraction was defined as a first-order function of oxygen:

$$CSOD = k_1(T) C \qquad (3-54)$$

2

where $k_1(T)$ = temperature-adjusted rate constant for biochemical SOD, 1/day

The biological fraction was estimated to be 20-40 percent due to macroinvertebrates in Hamilton Bay sediments but still followed a Michaelis-Menten relationship:

BSOD = u(T)
$$\frac{C}{K_{0_2} + C}$$
 (3-55)

where u(T) = temperature-adjusted rate constant for biological SOD (obtained by measurement: range = 0.58 to 5.52 g $0_2/m^2$ day), 1/day K_{0_2} = oxygen half-saturation constant (1.4 mg/1)

It is interesting to note the similarity between the two estimates of K_{O_2} (Lam et al., 1984; Walker and Snodgrass, 1984).

The direct effects of dissolved oxygen on the rate constant are generally neglected except in a few models. For example, in the HSPF model (Johansen <u>et al.</u>, 1981), dissolved oxygen concentration affects the rate of sediment oxygen utilization exponentially:

$$\frac{dC}{dt} = -\frac{k_T}{H} (1 - e^{-1.22 C})$$
(3-56)

where $k_T = the temperature adjusted rate constant, mg/m²-day$

3.5.2.2 Temperature

Temperature effects on SOD are most commonly modeled using the van't Hoff form of the Arrhenius relationship:

$$k_{T} = k_{Tr} \theta^{(T-Tr)}$$
(3-57)

where k_T = the rate at ambient temperature T k_{Tr} = the rate at a reference temperature (usually Tr=20^OC) θ = the temperature coefficient for adjusting the rate (Table 3-23)

Although this form of the relationship is the most common and gives equivalent results to the Arrhenius equation, it is not preferred in standard nomenclature (Grau et al., 1982).

The exceptions to use of Equation (3-57) are RECEIV-II (Raytheon, 1974), HSPF (Johanson <u>et al.</u>, 1981), and SSAM-IV (Grenney and Kraszewski, 1981). RECEIV-II apparently does not provide a temperature correction for the SOD rate coefficient although other rate coefficients in the model are adjusted according to Equation (3-57) with $\theta = 1.047$ for CBOD. HSPF uses a linear function for adjusting the SOD for temperature:

$$k_{\rm T} = 0.05 \, {\rm T_w} k_{20}$$
 (3-58)

Mode 1	θ	Q10(20 ⁰ C)*	Reference
DOSAG-3	1.047	1.58	Duke & Masch (1973)
QUAL-II	1.047	1.58	Roesner <u>et al</u> . (1977)
Vermont QUALII	1.047	1.58	JRB (1983)
Lake Erie Model	1.08	2.16	Di Toro & Connolly (1980)
WASP	1.08	2.16	Thomann & Fitzpatrick (1982)
WASP	1.1	2.59	0'Connor <u>et al</u> . (1981)
LAKECO	1.02	1.22	Chen & Orlob (1972, 1975)
WQRRS	1.02-1.04	1,22-1,48	Smith (1978)
ESTECO	1.02-1.04	1.22-1.48	Brandes (1976)
DEM	1.04	1.48	Genet <u>et</u> <u>al</u> . (1974)
EAM	1.02	1.22	Bowie <u>et al</u> . (1980)
EAM	1.047	1.58	Tetra Tech (1980), Porcella <u>et al</u> . (1983)
USGS-Steady	1.065	1.88	Bauer <u>et al</u> . (1979)
AQUA-IV	1.02-1.09	1.22	Baca & Arnett (1976)
EXPLORE-I	1.05	1.63	Baca <u>et al</u> . (1973)
Laboratory/Field Studies	1.040-1.130	1.5-3.4	Zison <u>et al</u> . (1978); Whittemore (1984b)

TABLE 3-23. SOME TYPICAL VALUES OF THE TEMPERATURE COEFFICIENT FOR SOD RATE COEFFICIENTS USED IN WATER QUALITY MODELS

* Q10(20⁰C) = ratio of k_2/k_1 at $k_2/k_1 = \theta^{10}$.

Grenney and Kraszewski (1981) used a modification of the Thornton and Lessem (1978) equation for SSAM-IV to provide, essentially, a continuously variable adjustment coefficient (θ) for the rate constants in biological processes. The equation adjusts over a temperature range of 5 to 30^oC which is similar to using Equation (3-51) with a variable θ coefficient:

$$\tau_{11} = N \frac{\kappa_1 e^{\gamma(T-T_1)}}{1-\kappa_1(1-e^{\gamma(T-T_1)})}$$
(3-59)

where τ_{11} = a multiplier applied to the rate at the optimum temperature, dimensionless

- N = an adjustment coefficient for rate processes, dimensionless
- y = specific rate coefficient, $1/{}^{0}C$
- T = environmental temperature, $^{\circ}C$
- T_1 = lower threshold temperature, ^OC

The coefficient au_{11} is multiplied times the SOD (or benchic loading rate) directly in SSAM-IV.

Although many models use the same formulation (Equation (3-57)) of the temperature correction equation for the SOD rate constant, the value of the constant θ is in dispute. Whittemore (1984b) reviewed literature values as well as his laboratory values in an attempt to determine measurement uncertainty. For analysis of his data, Whittemore chose $\theta = 1.08$ with an estimate of uncertainty of ± 0.01 . Then performing a sensitivity analysis for the range of $\theta = 1.07-1.09$ (1.08 ± 0.01), Whittemore showed that SOD would increase 12 percent when θ is increased by 0.01 for a temperature range of 12° C (20 to 32° C). He cautions that complete physical, chemical, and biological descriptions of SOD measurements are needed, both for <u>in situ</u> and studies measurements. Even in his own studies where a single method was used, the measured mean SOD using a stirred <u>in situ</u> respirometer had a standard deviation of 44 percent of the mean (Whittemore, 1984b).

Additional field experience and the use of divers to place the respirometers should measurably improve these results.

3.5.2.3 Biological Effects on SOD

The biological component is usually neglected when modeling SOD. because of the complexity of modeling benthic microorganisms and macroinvertebrates. The spatial and seasonal variability in SOD caused by sediment biological processes and communities results in variation in SOD that modelers appear to account for by varying the temperature coefficient. Some investigators have attempted to incorporate this variation directly in the model (Grenney and Kraszewski, 1981), or have suggested that the value of the temperature coefficient changes with season (e.g., Bradshaw <u>et al</u>., 1984) or with location downstream (e.g., Mancini <u>et al</u>.,1984). Other models (LAKECO, ESTECO, WQRRS, EAM) incorporate a benthic organisms compartment and may be able to evaluate the effects of benthos on SOD directly. However, no verification studies have been discovered that demonstrate this to be a useful technique.

3.5.2.4 Substrate Variability

The process describing the substrate utilized is where most models differ (Table 3-24). In the first water quality models that were widely used (DOSAG-3, QUAL-II), the decay of substrate is assumed to balance continued settling resulting in a steady-state sediment concentration of oxygen-demanding substrate. The resulting equation is:

$$\frac{\mathrm{dC}}{\mathrm{dt}} = -k_{\mathrm{T}}/\mathrm{H}, \qquad (3-60)$$

where k_T = temperature adjusted rate constant SOD, gO_2/m^2 -day H = mean water depth, m

As shown in Table 3-24, most models have followed this approach.

Formulation	Units	Description	Model (Reference)
k/A	k,mg0 ₂ /m day A,m ²	SOD rate normalized by bottom area	DOSAG-3 (Duke & Masch, 1973) QUAL-11 (Roesner <u>et al</u> . (1977)
k/H	k,mgO ₂ /m ² day H,m	SOD rate normalized by mean depth	Vermont QUAL-II (JRB, 1983) USGS-Steady (Bauer <u>et a</u> l. 1979) AQUA-IV (Baca & Arnett, 1976) WASP (O'Connor <u>et al</u> . 1981) RECEIV-II (Raytheon, 1974) DEM (Genet <u>et al</u> . 1974) HSPF (Johanson <u>et al</u> . 1981)
a k SED	a,mgO ₂ /mg Sed k,1/day SED, mg Sed/m ³	Conversion factor Decay rate Sediment areal concentration	LAKECO* (Chen & Orlob, 1972, 1975) WQRRS* (Smith, 1978) EAM* (Bowie <u>et al.</u> , 1980; Tetra Tech, 1980; Porcella <u>et al.</u> , 1983) EXPLORE-I (Baca <u>et al</u> ., 1973)

TABLE 3-24.	MODEL	FORMULATIONS	COMMONLY	USED	ΙN	SOD	COMPUT	ATI0	NS
				~~~~	~ ` ` `				

*NOTE: Additional SOD occurs due to respiration by the benthic organism compartment, which is modeled separately from sediment oxygen demand.

Substrate has been incorporated directly into ESTECO, LAKECO, WQRRS, EAM, and EXPLORE-I. Different settling rates of oxygen-demanding organic materials can lead to different amounts of sediment materials, and consequently different SOD rates calculated according to:

$$\frac{dC}{dt} = - a k SED$$
(3-61)

- where a = stoichiometric conversion factor relating oxygen to organic sediment, mg 0₂/mg sediment
  - k = sediment decay rate constant, 1/day
  - SED = sediment substrate that is subject to decay

In EXPLORE-I, only carbonaceous BOD is simulated as the substrate (SED), which in turn is affected by scour or settling from the water column. In the other models, all of the nutrient elements (C, N, P) are transformed according to a first-order reaction (k SED) but sediment oxygen demand is exerted only by carbon. Values of the conversion factor for sedimented organic carbon to  $O_2$  lie in the range of 1.2 to 2.0 mg $O_2$ /mg sediment. Nitrogen decays to ammonium and is released to the overlying waters where nitrification can take place (see Section 3.4). Other nutrients also enter the overlying waters as a result of similar transformations.

In some versions of the WASP model (Di Toro and Connolly, 1980; Thomann and Fitzpatrick, 1982), the oxygen-demanding materials in the sediment are divided into multiple compartments. First, the decay processes of sediment organic matter generate concentrations of CBOD and NBOD constituents in interstitial waters. Then both CBOD and NBOD are released to the water column where they subsequently decay in the appropriate compartments. In addition to CBOD release, oxygen utilization in the interstitial water is computed as oxygen equivalents, and diffusion into the interstitial water compartment is determined. If oxidation in excess of the amount available from diffusion occurs, these excess "oxygen equivalents" continue to represent a potential demand on the dissolved oxygen system. Finally, a deep oxygen demand has been hypothesized in an attempt to account for the measured oxygen demand. These concepts are described Di Toro and Connolly, 1980. More recently, Di Toro (1984) has provided an additional correction to SOD from denitrification of nitrate, although he suggests that this correction is usually negligible.

#### 3.5.3 Measurement Techniques

Essentially three types of measurement techniques have been used to estimate SOD rates: model calibration to estimate SOD, <u>in situ</u> measurements using respiration chambers, and laboratory respiration chamber measurement using cores or dredged samples. However, all three methods have severe disadvantages and the uncertainty of calculating SOD rates is so great that the simple formulations in the model equations (Table 3-24) are very appealing to model users. Unfortunately, these simple formulations will not result in credible models with good predictive capability when single values are used for rates and coefficients.

It would be expected that considerable spatial and temporal variation would occur in SOD. Spatially, the bed sediments of streams, lakes, and estuaries vary in their physical and chemical characteristics, rates of deposition, and other factors. For example, a stream may have fine sediments in low velocity areas and coarse cobble or boulders in steep gradient-high velocity reaches. Depth and velocity can vary significantly in any one cross-section. Reservoirs have deposition zones near inlets and at dam structures. Estuaries like streams and lakes vary considerably in substrate type and water velocity but are influenced by the salinity gradient and an added factor of coagulation and rapid settling in zones where fresh and saline waters mix.

Another source of variation is temperature. Temperature varies seasonally but that is accounted for in use of the van't Hoff or similar relationships. However, temperature and season both cause a shift in benthic community composition. Macroinvertebrate populations, especially emergent insects, change dramatically with life stage. Also, it would be expected that considerable variation in microbial community characteristics would occur in response to temperature changes.

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These spatial and seasonal characteristics suggest that a large number of SOD measurements would be required to estimate and obtain sufficient variation in rate coefficients. This has led to the development of <u>in situ</u> and laboratory methods for measuring SOD that will be site-specific and seasonal for SOD. SOD mapping strategies may be necessary. Ideally, <u>in situ</u> methods would provide the best approach, but considerable variation in results occurs because of problems associated with field sampling:

- Horizontal and longitudinal non-homogeneity of stream bottom materials. Areas of cobble, soft sediments, logs, and bedrock, increase the cost of measurement because more samples are needed. Soft, flocculent sediments are very difficult to evaluate with <u>in situ</u> methods. In some streams, an inaccurate characterization of reach-averaged SOD will be obtained.
- Difficulties in placement of respiration chamber. For example, obtaining a complete seal in cobbled and bouldered areas or where significant interaction with the ground water system occurs is essentially impossible.
- Mixing in the respiration chamber may not be modeled correctly nor simulate natural conditions and this is reflected in the wide variance in results from measurements. For example, the Institute of Paper Chemistry reported on a comparison of 5 <u>in situ</u> samplers of two basic types (recirculating and internally mixed) and found the results to be markedly different (Parker, 1977).

Laboratory measurements suffer from similar problems. They would appear to work reasonably well for aquatic systems of relatively uniform sediment characteristics, but heterogeneous sediments often lead to measurement variability. Some practices improve laboratory measurement: correcting of results for varying sediment depth is usually unnecessary when depths exceed 5-10 cm; undisturbed core samples are preferred over dredge samples even though they are more costly to collect; storage of samples and acclimation of samples to laboratory temperatures is discouraged because of potential changes in benthos or substrate; divers may help to improve precision.

In regard to the effect of variability in oxygen-demanding materials, there appears to be no strong relationship between SOD and various measures of organic matter (NCASI, 1978), but this may have been due to inaccurate measurement techniques. Improper mixing (i.e, velocity too high or too low), inadequate oxygen supply, storage or improper pretreatment of samples in the laboratory, and inappropriate laboratory temperatures may lead to errors that prevent the derivation of SOD/substrate relationships. However, Gardiner <u>et al</u>. (1984), using a laboratory chamber, showed that SOD was related to chemical oxygen demand (COD) of the sediments in Green Bay, a large gulf in the northwest corner of Lake Michigan, according to the following equation:

$$SOD = 7.66 COD/(156.5 + COD)$$
 (3-62)

As further evidence, the higher SOD values coincided with areas of summer dissolved oxygen depletion in Green Bay.

Given the many sources of measurement error, it is not surprising that Whittemore (1984b) was unable to correlate literature SOD values obtained in simultaneous field and laboratory measurements. He obtained a low  $r^2$  value of 0.58. But even more significant, the <u>in situ</u> SOD values were consistently higher than laboratory derived values at low SOD concentrations and the reverse observed at high SOD concentrations. This systematic error indicates the need for better methods of estimating SOD as well as developing a better understanding of the component SOD mechanisms.

The model calibration approach to estimating SOD is essentially a determination of the SOD rate by calibration subject to the constraint of a

reasonable range of SOD values. Thomann (1972) used literature SOD rates and modeling experience to suggest SOD ranges for certain environments (Table 3-25). The model approach (e.g., Terry and Morris, 1984; Draper et al., 1984), by itself, contains considerable variance because there are uncertainties in the other processes (reaeration, nitrification, respiration, photosynthesis, flow) as well as the considerable spatial and temporal variation expected in most aquatic environments. Lam <u>et al</u>. (1984) suggest that variation in dissolved oxygen load to Lake Erie owing to

	Uptake (g O ₂ /m ² -day) <u>@ 20⁰C</u>		
Bottom Type and Location	Range	Average	
<u>Sphaerotilus</u> - (10 gm dry wt/m ² )	-	7	
Municipal Sewage Sludge- Outfall Vicinity	2-10.0	4	
Municipal Sewage Sludge- "Aged" Downstream of Outfall	1-2	1.5	
Estuarine mud	1-2	1.5	
Sandy bottom	0.2-1.0	0.5	
Mineral soils	0.05-0.1	0.07	

# TABLE 3-25. AVERAGE VALUES OF OXYGEN UPTAKE RATES OF RIVER BOTTOMS (AFTER THOMANN, 1972)

hydrologic fluctuations could easily mask the effects of SOD on water column oxygen.

# 3.5.4 Summary

There is a diversity of modeling and measurement techniques used for predicting oxygen consumption by sediments. This diversity reflects the need for better process descriptions and measurement techniques. Simple zero-order model formulations have been used, but first-order multicomponent reactions with a separate benthic organism component may be needed to accurately model sediment oxygen demand (SOD). Consequently, it is suggested that modelers use site-specific SOD rates. In situ methods such as described in Whittemore (1984a) and Markert <u>et al</u>. (1983) are more useful and credible than laboratory methods at this time.

As an aid to estimating SOD rates and establishing reasonable ranges for calibration, the SOD literature values in Tables 3-26, 3-27, and 3-28 are presented for rivers and streams, lakes and reservoirs, and estuaries and marine environments, respectively. These should be considered only as order of magnitude estimates.

#### 3.6 PHOTOSYNTHESIS AND RESPIRATION

#### 3.6.1 Introduction

Photosynthetic oxygen production (P) and respiration (R) can be important sources and sinks of dissolved oxygen in natural waters. Many models simulate these processes directly in terms of algal growth and respiration. For example, net algal growth is simulated with the QUAL-II model (Roesner et al., 1981) using:

$$\frac{\partial A}{\partial t} = (\mu - \rho - \sigma)A \qquad (3-63)$$

where A = algal concentration, mass/volume

 $\mu$  = specific growth rate of algae, 1/time

- $\rho$  = algal respiration rate, 1/time
- $\sigma$  = algal settling rate, 1/time

The net algal oxygen production minus consumption is simulated by QUAL-II as:

$$\frac{\partial C}{\partial t} = (a_1 \mu - a_2 \rho) A \qquad (3-64)$$

where C = dissolved oxygen concentration, mass/volume

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- a₁ = oxygen production per unit of algal mass, mass oxygen/mass algae
- $a_2$  = oxygen uptake per unit of algal mass, mass oxygen/mass algae

The stoichiometric coefficients  $a_1$  and  $a_2$  relate algal growth and death to oxygen production and consumption. Tables 3-29 and 3-30 summarize values of these coefficients used in different models.

SOD, gO ₂ /m ² day	Environment	Experimental Conditions	References
0.022-0.92	Upper Wisconsin River	60-hour laboratory core incubation, periodic mixing, 4 ⁰ C, dark	Sullivan <u>et</u> <u>al</u> . (1978)
0.09±0.02 (012 ⁰ C) 0.15±0.04 (020 ⁰ C) 0.20±0.03 (028 ⁰ C) 0.18±0.05 (012 ⁰ C) 0.55±0.22 (020 ⁰ C) 0.60±0.28 (028 ⁰ C) 0.87±0.23 (036 ⁰ C)	Eastern U.S. River Southeastern U.S. River	45 day incubation of 0.6 liters sediment in 3.85 liters BOD dilution water, light	NCASI (1981)
3.2-5.7 0.52-3.6	Fresh shredded tree bark Aged shredded tree bark	10-liter incubations in aged tap water, room temperature, light	NCASI (1971)
2-33	Four eastern U.S. rivers downstream of paper mill	<u>In-situ</u> chamber respirometers, 22-27 ⁰ C, light,	NCASI (1978)
0.9-14.1	discharges	stirred at varying rates; open-ended tungel respirometer, <u>in-situ</u> , 22-27 [°] C, dark	
<0.1-1.4(@20 ⁰ C)	Eastern U.S. river downstream of paper mill discharge	In-situ respirometer stirred a $\pm$ various rates 9-16°C, dark, $\theta$ = 1.08	NCASI (1979)
0.27-9.8	Northern Illinois rivers (N = 89 stations)	In-situ respirometry, dark, $\overline{T} = 5^{\circ} - 31^{\circ}C$ time $1\frac{1}{2} - 3$ hours	Butts & Evans (1978)
0.10-5.30 (@20 ⁰ C)	Six stations in eastern Michigan rivers	In-situ respirometry in stirred chambers, 15-27 hours dark, 19-25°C, $\theta$ = 1.08	Chiaro & Burke (1980)
1.1-12.8	New Jersey rivers (10 stations)	<u>In-situ</u> respirometer, dark, 30 minutes-8 hours, stirred. Temperature unknown	Hunter <u>et</u> <u>al</u> . (1973)
0.3-1.4	Swedish rivers	<u>In-situ</u> respirometer, light, stirred, 0-10 ⁰	Edberg & Hofsten (1973)
0.20-1.2	Swedish rivers	Laboratory incubations, stirred, dark, 5-10°C	Edberg & Hofsten (1973)
1.7-6.0	Spring Creek, PA	Laboratory incubators in dark, stirred, 20°C	McDonnell & Hall (1969)
1.5-9.8	74 samples from from 21 English rivers	Laboratory incubation of cores; 15°C	Rolley & Owens (1967)
4.6-44.	Streams	Oxygen mass balance	James (1974)

# TABLE 3-26. MEASURED VALUES OF SEDIMENT OXYGEN DEMAND IN RIVERS AND STREAMS

SOD, gO ₂ /m ² day	Environment	Experimental Conditions	References
1-7	Green Bay, Lake Michigan	Lab incubation in darkness, 20 ⁰ C	Gardiner <u>et al</u> . (1984)
0-2.2	Fish culture ponds	<u>In situ</u> respirometry with 100-cm Tong plexiglass columns (dark pvc), over 47 days. Temperature unknown	Shapiro & Zur (1981)
0.4-2.6	Swedish lakes	<u>In situ</u> respirometer, light stirred, 5-18	Edberg & Hofsten (1973)
0.21-1.5	Swedish lakes	Laboratory incubations, stirred, dark, 10-13 C	Edberg & Hofsten (1973)
5.5 (31-32.5 ^o C) 5.1 (22.5-25.6 ^o C) 2.1 (13.2-16.1 ^o C)	Horseshoe Lake, IL	<u>In situ</u> respirometry, dark, stirred about 1 hour	Butts & Evans (1979)
0.84-3.3	Lake Apopka, FL	Laboratory incubation of	Belanger (1981)
0.4-3.6	Lake Apopka, FL	cores at room temperature, 2-3 hours, light. No stirring. Laboratory flow-through system (closed, 100 l volume)	
0.40-0.45 0.27	Hyrum Reservoir, UT Lake Powell	3-phase microcosms, 25°C, dark	Medine <u>et al</u> . (1980)
0.12-0.22	Shagawa Lake	<u>In-situ</u> chambers (1m ² ), at 7-12 m depths; 12-14°C (est.)	Sonzogni <u>et</u> al. (1977)
0.47-0.92	Swedish Lakes	Laboratory measurement with undisturbed cores; used <u>in situ</u> temperatures	Graneli (1977)
0.72-8.40	Lakes	0xygen mass balance	James (1974)
0.6-3.6	Hamilton Harbor, Lake Ontario	<u>In situ</u> chambers, 11-16 ⁰ C	Polak & Haffner (1978)
1.7-8.9	Lake Mohegan, NY	Measurement based on mass balance, continuous flow lab chamber, 22-32°C	Fillos (1977)
0,17-0.5	Swedish lakes	<u>In situ</u> & laboratory measurements, winter temperatures	Edberg (1977)
0.54-0.71	Swedish lakes	Laboratory incubation of undisturbed cores, 8°C	Andersen (1977)
0.3-1.0	Lake Hartwell, SC	Laboratory chambers, 18 ⁰ C	Brewer <u>et al</u> . (1977)
0.076-0.48	Marion Lake, BC	Laboratory incubation of undisturbed cores, no mixing, 15 ⁰ C	Hargrave (1969)
0.004-0.012	Lake Superior	Laboratory incubation of undisturbed cores, 4 ⁰ C	Glass & Podolski (1975)

# TABLE 3-27. MEASURED VALUES OF SEDIMENT OXYGEN DEMAND IN LAKES AND RESERVOIRS

In addition to algal respiration, respiration from zooplankton and nekton can contribute to oxygen depletion, and would be included in Equation (3-64), along with additional equations to describe their growth and death. Models that simulate algae and zooplankton (such as those in Tables 3-29 and 3-30) are discussed in detail in Chapters 6 and 7 of this report. This section describes methods to predict P-R without simulating algal growth or respiration. The methods pertain largely to streams and rivers, and are useful in that they simplify the modeling approach. It should be mentioned that some water quality models do not simulate photosynthesis and algal respiration. This approach is valid where P=O and R=O. Other models simulate only daily average photosynthetic oxygen production ( $\overline{P}$ ) and daily average respiration ( $\overline{R}$ ). If, on a daily average basis,  $\overline{P}-\overline{R}\approx 0$ , these models would predict little effect of algal activity on dissolved oxygen. However, if  $\overline{P}$  and  $\overline{R}$  are both large numbers, then actual dissolved oxygen levels will be higher during the day and lower at night than predicted by the models.

# 3.6.2 Methods

Table 3-31 summarizes the methods reviewed to predict photosynthetic oxygen production and respiration without simulating algal growth. The methods consist of either single station methods or two-station methods. Odum (1956) appears to be one of the first researchers to use this approach.

SOD, gO ₂ /m ² day	Environment	Experimental Conditions	References
0.10±0.03 (@12 ⁰ C) 0.20±0.05 (@20 ^o C) 0.22±0.09 (@28 ^o C) 0.37±0.15 (@36 ^o C)	A North Carolinian estuary	45 day incubation of 0.6 liters sediment in 3.85 liters BOD dilution water, light	NCASI (1981)
2.32±0.16	Buzzards Bay near raw sewage outfall	<u>In-situ</u> dark respirometers, stirred, I-3 days. Temperature unknown	Smith <u>et al</u> . (1973)
1.88±0.018	Buzzards Bay control		
0.14-0.68 ( 5 [°] C) 0.20-0.76 (10 [°] C) 0.30-1.52 (15 [°] C)	Puget Sound sediment cores	Laboratory incubations	Pamatmat <u>et al</u> . (1973)
0.05-0.10	San Diego Trough (deep marine sediments)	<u>In-situ</u> respirometry for 5-13 hours, 4 ⁰ C, light	Smith (1974)
1.25-3.9	Yaquina River estuary, Oregon	Dark laboratory incubators, stirred, 20°C	Martin & Bella (1971)
0.02-0.49	Eastern tropical Pacific	Shipboard incubations, 15 ⁰ C stirred, dark	Pamatmat (1971)
0.9-3.0	The Baltic Sea	<u>In-situ</u> light respirometer, stirred, 10 C	Edberg & Hofsten (1973)
0.4-0.71	The Baltic Sea	Laboratory incubations, stirred, dark, 10°C	Edberg & Hofsten (1973)
0-10.7	Delaware Estuary (22 stations)	In-situ dark respir <b>ometry,</b> 13-14 ⁰ C	Albert (1983)
0.3-3.0	Fresh & brackish waters, Sweden	In-situ respirometry, 0-18 ⁰ C Laboratory cores, 5-13 ⁰ C	Edberg & Hofsten (1973)

TABLE 3-28	<ol> <li>MEASURED</li> </ol>	VALUES	OF SEDIM	ENT OXY	GEN DEMAND
	IN ESTUAR	IES AND	MARINE S	YSTEMS	

Model	Value	Reference
DOSAG3	1.4 - 1.8 <u>mg O₂</u> mg algae (D.W.)	Duke & Masch (1973)
QUAL-II	1.4 1.8 mg 0 ₂ mg algae (D.W.)	Roesner <u>et al</u> . (1977)
WASP	2. <b>67</b> mg 0 ₂ /mg C	Di Toro & Connolly (1980)
WASP	2.66 mg 0 ₂ /mg C	0'Connor <u>et</u> <u>al</u> . (1981)
	.133 mg 0 ₂ /mg Chl- <u>a</u>	0'Connor <u>et al</u> . (1981)
WASP	2.67 mg 0 ₂ /mg C	Thomann & Fitzpatrick (1982)
LAKE ECO	1.6 mg O ₂ /mg algae (D.W.)	Chen & Orlob (1975)
WQRRS	1.6 mg O ₂ /mg algae (D.W.)	Smith (1978)
AQUA-IV	1.6 - 2.66 mg 0 ₂ /mg C	Baca & Arnett (1976)
ESTECO	1.6 - 1.8 mg O ₂ /mg algae (D.W.)	Brandes (1976)
EAM	1.24 mg O ₂ /mg algae (D.W.)	Porcella <u>et al</u> . (1983)
EAM	1.6 mg O ₂ /mg algae (D.W.)	Bowie <u>et</u> <u>al</u> . (1980)
EAM	1.24mg 0 ₂ /mg algae (D.W.)	Tetra Tech (1980)
DEM	1.6 mg O ₂ /mg algae (D.W.)	Feigner & Harris (1970)
Vermont- QUAL-II	1.4 1.8 mg O ₂ /mg algae (D.W.)	JRB (1983)

TABLE	3-29.	OXYGEN	PRODUCED	PER	MASS	0F	ALGAE
		••••••••••••••••••••••••••••••••••••••			,		

Note:

D.W. dry weight

Both numerical and analytical techniques have since been developed. The light-dark bottle technique and benthic chamber method are also included in the table.

As shown in Table 3-31, O'Connell and Thomas (1965) applied a total derivative approach for P-R calculation, and compared the results against a

second procedure using a submerged algal chamber. Respiration was corrected for oxygen consumption by bacterial oxidation. Figure 3-17 compares the two methods for a station on the Truckee River, and shows good agreement.

O'Connor and Di Toro (1970) use a half cycle sine wave or a Fourier series to find the time varying photosynthetic oxygen production rate. In

Mode 1	Value	Reference
DOSAG 3	1.6 - 2.3 mg 0 ₂ /mg algae (D.W.)	Duke & Masch (1973)
QUAL-II	1.6 - 2.3 mg 0 ₂ /mg algae (D.W.)	Roesner <u>et al</u> . (1977)
WASP	1.87 mg O $_2/$ mg C 1	Di Toro & Connolly (1980)
WASP	2.0 mg O ₂ /mg C	Thomann & Fitzpatrick (1982)
WASP	2.0 mg 0 ₂ /mg C	O'Connor <u>et al</u> . (1981)
	.10 mg 0 ₂ /mg Chl- <u>a</u>	0'Connor <u>et</u> <u>al</u> . (1981)
LAKE ECO	1.6 mg O ₂ /mg algae (D.W.)	Chen & Orlob (1975)
WQRRS	1.6 2.0 mg 0 ₂ /mg algae (D.W.)	Smith (1978)
AQUA-IV	1.6 2.66 mg 0 ₂ /mg C	Baca & Arnett (1976)
ESTEC0	1.6 - 1.8 mg O ₂ /mg algae (D.W.)	Brandes (1976)
EAM	.95 mg O ₂ /mg algae (D.W.)	Porcella <u>et</u> <u>al</u> . (1983)
EAM	1.6 mg O ₂ /mg algae (D.W.)	Bowie <u>et al</u> . (1980)
EAM	.95 mg O ₂ /mg algae (D.W.)	Tetra Tech (1980)
DEM	1.6 mg O ₂ /mg algae (D.W.)	Feigner & Harris (1970)
Vermont QUAL-II	1.6 - 2.3 mg O ₂ /mg algae (D.W.)	JRB (1983)

TABLE 3-30. OXYGEN CONSUMED PER MASS OF ALGAE

¹ This is multiplied by an oxygen limitation factor,  $\frac{0_2}{K + 0_2}$ , where K is a half-saturation constant equal to 0.1 mg/l. <u>Note</u>: D.W. = dry weight

# TABLE 3-31. SUMMARY OF METHODS TO PREDICT PHOTOSYNTHETIC OXYGEN PRODUCTION AND RESPIRATION WITHOUT SIMULATING ALGAL GROWTH AND DEATH

Source	Equations	Symbols	Comments
Odum (1956)	see comments	see comments	<ol> <li>Photosynthetic oxygen production was based on a graphical procedure. Either two stations or single station approaches could be used. A method was also presented to find the reaeration coefficient.</li> </ol>
O'Connell and Thomas (1965)	$P - R = \frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} - k_2 \{C_s - C\} + k_1 L + k_n N$	<pre>U = stream velocity k₂ = reaeration rate C = dissolved oxygen C_S = dissolved oxygen saturation k₁ = CBOD decay rate L = CBOD k_n = nitrification rate N = NBOD</pre>	<ol> <li>P-R was found in two independent ways. In the first, all terms in the dissolved oxygen mass-balance were found independently and then P-R was found as the only remaining term in the oxygen balance. In the second method, an algal chamber was placed on the river bed.</li> <li>The two methods gave comparable results.</li> <li>The approach was used on the Truckee River, where attached algae were abundant.</li> </ol>
O'Connor and Di Toro (1970)	$\frac{\text{Half cycle sine wave:}}{F = \begin{cases} P_m \sin \left\{\frac{\pi}{p} (t-t_s)\right\} t_s \le t \le t_s + p \\ 0 \text{ when } t_s + p \le t \le t_s + 1 \end{cases}}$ $\frac{\text{Fourier series extension:}}{P = P_m \left\{\frac{2p}{\pi} + \sum_{n=1}^{\infty} b_n \cos \left[2\pi n (t-t_s - p/2)\right]\right\}}$ where $b_n = \cos (n\pi p) \frac{4\pi/p}{(\pi/p)^2 - (2\pi n)^2}$	P = rate of photosynthetic oxygen production, mg/(1-day) P _m (x) = maximum rate of photosynthetic oxygen production, mg/(1-day) t _s = time of day when source begins p = fraction of day when source is active	<ol> <li>This approach is found in DIURNAL, a stream model developed by O'Connor and Di Toro.</li> <li>The approach is potentially applicable to any vertically mixed water body.</li> <li>The method of Erdmann (1979a) was used to evaluate P and R for a wasteload allocation application on the Shenondoah River (Deb and Bowers, 1983) and on Leatherwood Creek, Arkansas (Deb <u>et al.</u>, 1983).</li> <li>O'Connor and Di Toro (1970) applied the method to the Grand, Clinton, and Flint rivers in Michigan, the Truckee River ir Nevada, and the Ivel River in Great Britain. They used a trial and error procedure to determine Pm, ts, P and R to best fit observed diurnally varying</li> </ol>

Source	Equations	Symbols	Comments
Kelly, Hornberger, Cosby (1975)	$P - R = \frac{A_0}{2} + \sum_{n=1}^{\infty} A_n \cos(n\omega t)$	A _n = unknown coefficients ω = 2π/48	<ol> <li>A 48-hour cycle was used so that values at the beginning and end of a day are not constrained to be identical.</li> </ol>
		The A _n are determined based on measurements of dissolved oxygen at either one of two locations	<ol> <li>R is total respiration, including both algal respiration and bacterial decay.</li> </ol>
		in a stream. They are chosen to give a "best fit" between predicted and observed dissolved oxygen values.	<ol> <li>The single station analysis can be used when the dissolved oxygen concentrations at the upstream and downstream stations are approximately the same.</li> </ol>
Hornberger and Kelly (1972)	P - R = $\frac{\partial C}{\partial t}$ + U $\frac{\partial C}{\partial x}$ - k ₂ (C _s -C)	C = dissolved oxygen concentration	<ol> <li>Three methods were examined to predict P-R: a finite difference method, an</li> </ol>
		U = stream velocity	analytical solution assuming P-R remains constant over the time interval, and a
		k ₂ = reaeration rate	varies linearly over a time step.
		C _s = dissolved oxygen saturation	<ol> <li>The analytical methods were preferred over the numerical approach from a conceptual point of view, and because time steps smaller than the residence time through the stream reach could be used.</li> </ol>
Erdmann (1979a)	$P - R = k_2(C_s - C) - \frac{DC}{Dt}$ where:	C = concentration of dissolved nm oxygen at station m and time n	<ol> <li>Respiration is first computed at night when P = 0. Then P is computed during the day using known R.</li> </ol>
	$\frac{DC}{Dt} = 1/2 \begin{cases} \frac{c_{21} - c_{11} + c_{22} - c_{12}}{t_{12} - t_{12}} + \frac{c_{12} - c_{11}}{t_{12}} \end{cases}$	+C ₂₂ -C ₂₁ t ₂ = time of sample at downstream station	<ol> <li>The method was applied to Charles River, Massachusetts.</li> </ol>
		t ) t ₁ = time of sample at upstream station	<ol> <li>R is total oxygen consumption rate by both algae and bacteria.</li> </ol>
		t ≖ travel time between two r stations	
		k ₂ = reaeration rate	
		C = dissolved oxygen s saturation	
		C = dissolved oxygen	
		(continued)	

Source	Equations	Symbols المر	Comments
Erdmann (1979b)	$\overline{P} = (\Delta C_u + \Delta C_d)$	₱ = daily average photosynthesis	I. The method is a simplification of Erdmann (1979a) and is used to predict daily
	$\overline{R} = k_2 \left(\frac{u + b_d}{2}\right) + (\Delta C_u + \Delta C_d) - \left(\frac{c_d - c_u}{t_f}\right)$	) $\widetilde{R}$ = daily average	stations.
		k ₂ ⇒ reaeration rate	<ol> <li>The method was applied to the Charles River, Massachusetts.</li> </ol>
		t _f = travel time between t _f two stations	<ol> <li>Some important assumptions include constant temperature and symmetrical discusses</li> </ol>
		ΔC _u , ΔC _d = diurnal range of dissolved oxygen at upstream stations	
		D _u , D _d = daily average dissolved oxygen deficit at upstream and downstream stations	
		C _u , C _d ≃daily average dissolved oxygen concentration at upstream and downstream stations	
Gulliver, Mattke, Stefan	$P - R = \frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} - \frac{\partial}{\partial x} \left( D_1 \frac{\partial C}{\partial x} \right) - k_2 (C_s - C)$	U = stream velocity	1. A finite difference computer model DORM
(1982)		k ₂ = reaeration rate	was used to route dissolved oxygen changes between two stations and includes the
		C = dissolved oxygen	dissolved oxygen levels on respirations and
		C _s ≖ dissolved oxygen saturation	2. The model was applied to experimental
		D _L = longitudinal disperson coefficient	Stream reaches in the U.S. ErA's Monticello Ecological Research Station, Minnesota.
			<ol> <li>For the channels analyzed, it was found that affects of longitudinal dispersion were negligible. However the results were sensitive to reaeration, residence time between the two stations, and temperature dependent processes (saturation and respiration rates).</li> </ol>
		(continued)	

TABLE 3-31. (continued)

# TABLE 3-31. (continued)

Source	Equations	Symbols	Comments
U.S. EPA (1983)	light and dark bottle technique		<ol> <li>Light and dark bottles are suspended at various depths in water and dissolved oxygen measurements are made at regular intervals to determine P-R.</li> </ol>
			<ol> <li>This method suffers from numerous limitations which include:</li> </ol>
			<ul> <li>only photosynthetic activity of algae in water column is measured</li> <li>the estimate of R includes algal and bacterial respiration</li> <li>the P-R is a point estimate, rather than representative of a reach.</li> </ul>
U.S. EPA (1983)	benthic chamber		<ol> <li>P-R of attached algae is measured using a clear benthic chamber and a covered (dark) chamber.</li> </ol>

their applications, they used a trial and error procedure to determine P-R that best fit diurnally varying dissolved oxygen data. In the Deb and Bowers (1983) application of the same method, Erdmann's approach (1979a) was used to evaluate P-R. The method of Erdmann combines all terms which contribute to deoxygenation (algal respiration, CBOD decay and NBOD decay) into a single respiration term. To find algal respiration, CBOD and NBOD are subtracted from total community respiration.

Kelly <u>et al</u>., (1975), also shown in Table 3-31, use a Fourier series, but with a 48 hour period. The coefficients  $A_n$  are not true Fourier coefficients but are based on a best fit between predicted and observed dissolved oxygen values. Cohen and Church (1981) have more recently applied these methods to measure productivity of algae in cultures open to the atmosphere.



⁻⁻⁻⁻⁻ FINITE DIFFERENCE DATA

Figure 3-17. Diurnal variation of (P-R) in Truckee River near Station 2B (O'Connell and Thomas, 1965).

Erdmann (1979a, 1979b) has developed methods to predict time-varying P-R values and daily average values. In the time varying case the concept of the Stokes total time derivative is used (see Figure 3-18). The total derivative is the sum of the time derivative ( $\partial C/\partial t$ ) and the advective derivative ( $U\partial C/\partial x$ ). The time derivative is evaluated as the average of two times, and the advective derivative is the average between two stations.



Figure 3-18. Concept of Stokes total time derivative. Here  $DC/Dt = 0.43 \text{ mg } 0_2/1 \cdot h$  (from Erdmann, 1979a).

Gulliver <u>et al.</u>, (1982) provide a literature review of the various methods used to predict P-R in streams. They also developed a computerized model to determine P-R that includes dispersion. However, they found that effects of dispersion were negligible for their applications. Several applications of diurnal curve analyses not reported in Table 3-31 include the work of Schurr and Ruchts (1977) who used a single station method to predict monthly average P-R values, and the work of Simonsen and Harremoes (1978) who used a two station approach to predict P-R on a river in Denmark.
The final two methods shown in Table 3-31 are the light-dark bottle method and the benthic chamber method. These methods measure P-R of algae in the water column (light-dark bottles) and of attached algae (benthic chamber). The methods provide single point estimates that may not be representative of the water body as a whole.

Some models simulate daily average photosynthetic oxygen production rather than time-varing production. Erdmann (1979b) shows that, the daily average photosynthesis oxygen products rates, P, can be approximated by:

$$\overline{P} = \frac{2\Delta D0}{24} (mg/1/nr) \qquad (3-65)$$

where  $\Delta DO$  = daily maximum dissolved oxygen concentration minus daily minimum dissolved oxygen concentration, mg/l

This approximation appears to be valid only for reaeration rates less than 0.2/day (Manhattan College, 1983).

A second method of estimating P is to integrate a sinusoidal curve that represents the instantaneous photosynthetic oxygen production rate. The result is:

$$\overline{P} = \frac{2 P_m p}{\pi}$$
(3-66)

where  $P_m = maximum$  daily photosynthetic oxygen production rate, mg/l/day

p = fraction of day when algae are producing oxygen, decimal fraction

The U.S. EPA (1983) describes a third method to estimate daily average production based on light-dark bottle measurements:

$$\overline{P} = \frac{2P \Delta T}{\cos (\pi t_1 / f) - \cos(\pi t_2 f)}$$
(3-67)

where P' = observed average production rate between times  $t_2$  and  $t_1$  $\Delta T = (t_2 - t_1)/24$ 

f = number of hours in day when oxygen is being produced

Relationships between photosynthetic oxygen production and chlorophyll-a have been developed by a number of researchers. While a detailed review of these methods is outside of the scope of this section, several of the more commonly used formulations are summarized here. Megard et al. (1979) developed the following expression for daily average photosynthetic oxygen production:

$$\overline{P} = \frac{\ln \left(\frac{I_o}{I_z}\right)^C a^P m}{\varepsilon_c C_a + \varepsilon_w}$$
(3-68)

where  $I_{o}$  = light intensity at the water surface  $I_{z}$  = light intensity at depth z  $C_a = chlorophyll-a concentration$  $\varepsilon_c$  = specific attenuation of light by chlorophyll-a  $\boldsymbol{\epsilon}_{w}$  = specific attenuation of light by all causes other than chlorophyll-a  $P_m$  = maximum daily photosynthetic oxygen production rate, mq/1/dav

Demetracopoulos and Stefan (1983) modified this expression to predict hourly photosynthetic oxygen production, and used the expression in a model of the Mississippi River.

In experiments on the Sacramento-San Joaquin Estuary, Bailey (1970) correlated the daily photosynthetic oxygen production rate to a number of factors. The resulting expression was:

$$P_{av} = 3.16 C_a \frac{I^{0.677}}{k_e} + 0.16T - 0.56H$$
 (3-69)

Finally, simple relationships between chlorophyll-a and, P_m have been proposed (U.S. EPA, 1983). Figure 3-19 shows how Pm/Ca ratios are



Figure 3-19. Algal productivity and chlorophyll relationships for streams (U.S. EPA, 1983).

influenced by water temperature and algal carbon/Ca ratios. For a typical water temperature  $(20^{\circ}C)$  and a typical carbon/Ca ratio (50), Pm/Ca = 0.25. However, this ratio is likely to vary between 0.1 to 0.6 for the range of conditions present in streams.

# 3.6.3 Data

Table 3-32 summarizes data reviewed on photosynthetic oxygen production and respiration. Respiration is sometimes reported as total community respiration and at other times as algal respiration. As shown by the data, photosynthetic oxygen production can be quite variable, both over distance and time. In the Havelse River, for example, average photosynthetic oxygen production rates varied from 0.2 to 25.9 g/(m²-day). One of the primary reasons for the variability was because solar radiation intensity changed by more than an order of magnitude between measurement periods.

### 3.6.4 Summary

Most water quality models that simulate photosynthetic oxygen production and algal respiration simulate algal growth and respiration. Stoichiometric coefficients are used to convert growth and respiration to oxygen production and consumption. Tables 3-29 and 3-30 summarize these coefficients.

Some river water quality models use the approach that photosynthetic oxygen production and respiration can be modeled without the necessity of simulating algal activity. Rather, some type of curve, such as a sine curve or more generally a Fourier series, is used instead, where certain parameters must be delineated to characterize the curve.

Typically instream dissolved oxygen measurements at two stations are used to generate P-R data. Either finite difference or continuous solutions to dissolved oxygen mass balance equations are used. While light-dark bottles or benthic chambers can in principal be used to find the required information, these approaches are limited in a number of ways. The two station methods are better in that they provide an integrated estimate of algal activity.

However, two station methods should also be used cautiously. In a sense, the methods are curve fitting techniques: they are used to fit a

curve based on dissolved oxygen variation between two stations. Typically other rate constants such as reaeration rates, carbonaceous BOD decay, nitrogenous BOD decay are needed to fit the curves. Thus errors in these coefficients are propagated into P-R calculations. Also care should be taken if results are extrapolated to other situations (e.g., different temperatures, different solar intensities, and different nutrient loadings).

	· · · · · · · · · · · · · · · · · · ·	Т	Pm	Pav	R
Reference	River	°c	g/m ² -day	g/m ² -day	g/m ² -day
O'Connor and Di Toro (1970)	Grand, Michigan	28	12.7 37.6	4.4 13.0	9.3 12.7 ^a
O'Connor and Di Toro (1970)	Clinton, Michigan	21	13.2 22.9	4.2 7.3	9.3 ^a
O'Connor and Di Toro (1970)	Truckee, Nevada	28	12.9 26.	4.8 9.6	3.6 6.2 ^a
O'Connor and Di Toro (1970)	Ivel, Great Britain	16	24.	9.0	4.6 ^a
O'Connor and Di Toro (1970)	Flint, Michigan	28	4. 40.	1.3 18.	4. 20 ^a
Thomas and O'Connell (1966)	North Carolina Streams			9.8	21.5 ^b
Thomas and O'Connell (1977)	Laboratory Streams			3.4 4.0	2.4 2.9 ^b
Erdmann (1979a,b)	Charles, Massachusetts	19-25		0.0 12.	0.0 36. ^b
Deb and Bowers (1983)	Shenandoah, Virginia	23	4.8 17.4		0.9 5.9 ^a
Kelly <u>et</u> <u>al</u> . (1975)	Baker, Virginia			0.45	1.9 ^b
Kelly <u>et</u> <u>al</u> . (1975)	Rappahannock, Virginia			6.1	7.3 ^b
Kelly <u>et</u> <u>al</u> . (1975)	S. Fork Rivanna, Virgin	ia		2.1	3.4 ^b
Kelly <u>et al</u> . (1975)	Rivanna, Virginia			2.3	5.4 ^b
Kelly <u>et</u> <u>al</u> . (1975)	South, Virginia			2.0	5.3 ^b
Kelly <u>et al</u> . (1975)	Mechums, Virginia			1.3	2.6 ^b
Simonsen and Harremoes (1978)	Havelse, Denmark			0.2 25.9 ^C	4.8 22.9 ^b
Gulliver <u>et al</u> . (1982)	Experimental Channels	9-24	5. 45.	1.5 14.8	2.6 10.7 ^b

TABLE 3-32. PHOTOSYNTHETIC OXYGEN PRODUCTION AND RESPIRATION RATES IN RIVERS

^aAlgal respiration only

^bTotal community respiration

^CMeasurements were made over the period of one year, and solar radiation varied by more than a factor of 10.

In cases where diurnal water temperature changes are great, diurnal curve analyses should include temperature correction effects.

All of the approaches reviewed in Table 3-31 have apparently been successfully applied. However, no comprehensive comparison of the approaches against the same data set were found. In cases where a significant amount of data is available for analysis, a computerized approach such as Kelly <u>et al</u>. (1975) or Gulliver <u>et al</u>. (1982) appears to be better than trial and error procedures. The method that has been most rigorously tested is the DORM model of Gulliver <u>et al</u>. (1982). Also these methods can be used when the distance between stream stations is great, because the models do not assume that P-R remains constant over the travel time between the stations.

Under the appropriate conditions the simpler approach of Erdmann (1979a,b) can be used. One restriction on using approaches where P-R is assumed constant over the time increment is that the travel time between stations must be short (i.e., 1 to 3 hours) so that the constant P-R assumption is not violated.

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## Chapter 4

#### pH AND ALKALINITY

## 4.1 INTRODUCTION

The subjects of pH and alkalinity are becoming increasingly important as society begins to deal with acidic precipitation. New models developed to analyze effects of alternative controls on inputs of acidity to sensitive aquatic environments use alkalinity as a state variable, then predict pH from alkalinity (Gherini <u>et al.</u>, 1984). Earlier models did not contain many of the processes that affect pH, and their predictive capability was adequate for some, but not all, environments (e.g. Henriksen, 1979). More elaborate models now exist which take into account a more complete picture of the constituents that comprise alkalinity in the dilute systems that are at risk from acidic precipitation (organic acids, other non-carbonate weak acids, etc.) and which compute other source-sinks of alkalinity and factors that affect pH (Chen <u>et al.</u>, 1984).

# 4.2 CARBONATE ALKALINITY SYSTEM

The carbonate system is of great importance in lakes, rivers, and estuaries. Carbonate chemistry of natural waters has been described in detail elsewhere (Stumm and Morgan, 1970, 1981; Trussell and Thomas, 1971; Park, 1969; Butler, 1982; Chen and Orlob, 1972, 1975). The carbon dioxide  $(CO_2)$  - bicarbonate  $(HCO_3^-)$  - carbonate  $(CO_3^{2^-})$  equilibrium is the major buffer system in aquatic environments. This equilibrium directly affects the pH, which in turn can affect the biological and chemical constituents of the system. For example, it may become necessary to simulate pH and alkalinity in order to compute the toxicant, un-ionized ammonia (see Chapter 5), or to determine available concentrations of metals (e.g., Gherini et al., 1984).

Since algae use carbon dioxide as a carbon source during photosynthesis, this is a nutrient which can reduce the growth rate when alkalinity is low and other nutrients are high (Goldman, <u>et al.</u>, 1972). Most models include a carbonate system representation which calculates the total inorganic carbon (TIC) as the sum of bicarbonate, carbonate, and carbon dioxide. Carbon dioxide is assumed to be produced by respiration and consumed by algal growth. The major source is atmospheric exchange.

The major chemical species considered to constitute alkalinity are dissolved carbon dioxide, bicarbonate, and carbonate ion, together with the hydrogen and hydroxyl ions. Mass balance equations assume that ionic equilibrium exists and calculate carbon inputs and outputs from a pool of total inorganic carbon (TIC). Conversions between different carbon forms are based on stoichiometric equivalents. The carbon dioxide form is involved in most of the important processes, including surface reaeration, respiration, excretion, algal uptake, and organic decay reactions. However, dissolved carbon dioxide combines with water to form carbonic acid, which, in turn, dissociates to bicarbonate ion, carbonate ion, and hydrogen ion. Since the dissociation reactions occur very rapidly in comparison to the other biological and chemical processes, dissolved carbon is modeled as the sum of  $CO_2 + HCO_3^2 + CO_3^{2-}$ , and is referred to as total inorganic carbon (TIC).

Dissolved inorganic carbon is derived from several sources. These include surface reaeration; respiration by fish, zooplankton, benthic animals, and algae; soluble excretion by fish, zooplankton, and benthic animals; and the decay of organic matter in the form of detritus, sediment, and sewage BOD. Dissolved carbon is removed by assimilation during algal photosynthesis.

Conceptually, the mass balance equation defining these relationships for the EAM model (Tetra Tech, 1980) is expressed as follows:

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= detritus decay + sediment decay + fish respiration + benthic animal respiration + zooplankton respiration + algal respiration + fish excretion + zooplankton excretion + benthic animal excretion - algal assimilation + BOD decay + surface reaeration.

Although Equation (4-1) is a substantially complete picture of TIC dynamics in an aquatic system, most models do not contain the same degree of complexity. However, whether multi-compartmented or few compartments, the general aspects of the process are modeled similarly. Also, the inputs and outputs can be based on  $CO_2$  with suitable stoichiometric conversions (e.g., Di Toro and Connolly, 1980) rather than TIC.

Surface reaeration of  $CO_2$  from atmospheric sources is done in a way similar to oxygen (Section 3.2). However, only minimal effort to measure

 $\rm CO_2$  reaeration is necessary and literature values have been used (Emerson, 1975; Liss, 1973). Reaeration occurs only at the surface of the water body, and is a function of the carbon dioxide saturation level. The saturation concentration is a function of the water temperature as it affects the Henry's law constant (K_H) for computing  $\rm CO_{2sat}$ :

$$CO_{2sat} = K_{H} pCO_{2}$$
(4-2)

where  $pCO_2$  is the partial pressure of  $CO_2$  in the atmosphere (generally 0.00033 atmospheres is used) and

$$K_{\rm H} = M_{\rm CO_2} \log \left[ \frac{2385.73}{T_{\rm K}} - 14.0184 + 0.0152642 T_{\rm K} \right]$$
(4-3)

where 
$$M_{CO_2} = 44,000 \text{ mg/mole}, CO_2$$
  
 $T_K = \text{temperature in } K = 273.15 + {}^{O}C$   
 $K_H = \text{Henry's law constant, mg/(liter.atm)}$ 

After computing the total inorganic carbon according to the mass balance in Equation (4-1), the dissolved carbon dioxide concentration is calculated using relationships derived from the equilibrium constants of the dissociation reactions. The reactions involved are:

$$H_2CO_3 \stackrel{-}{\longleftrightarrow} HCO_3^- + H^+ \qquad K_1 \qquad (4-4)$$

$$HCO_{3}^{-} \xrightarrow{} CO_{3}^{-} + H^{+} \qquad K_{2} \qquad (4-5)$$

$$H_2 0 \xrightarrow{} H^+ + 0H^- \qquad K_w \qquad (4-6)$$

where the equilibrium constants are defined as

$$\kappa_{1} = \left[ \frac{HCO_{3}}{\left[ H_{2}CO_{3} \right]} \right] \left[ H^{+} \right]$$
(4-7)

$$\kappa_{2} = \begin{bmatrix} CO_{3}^{*} \end{bmatrix} \begin{bmatrix} H^{+} \end{bmatrix}$$

$$(4-8)$$

$$\kappa_{w} = \begin{bmatrix} H^{+} \end{bmatrix} \begin{bmatrix} OH^{-} \end{bmatrix}$$

$$(4-9)$$

The equilibrium constants  $K_1$ ,  $K_2$ , and  $K_w$  vary with temperature according to the following relationships (Tetra Tech, 1979):

$$\kappa_{1} = 10 \begin{bmatrix} 14.8435 - 0.032786 \ T_{K} - (3404.71/T_{K}) \end{bmatrix}$$
(4-10)  

$$\kappa_{2} = 10 \begin{bmatrix} 6.498 - 0.02379 \ T_{K} - (2902.39/T_{K}) \end{bmatrix}$$
(4-11)  

$$\begin{bmatrix} 35.3944 - 0.00835 \ T_{K} - (5242.4/T_{K} - 11.826 \ \log (T_{K}) \end{bmatrix}$$

$$K_{\rm w} = 10$$
 (4-12)

In a carbonate system, the alkalinity (alk) is calculated according to the mass balance equation:

alk = alkalinity = 
$$\begin{bmatrix} HCO_3^- \end{bmatrix}$$
 + 2  $\begin{bmatrix} CO_3^- \end{bmatrix}$  +  $\begin{bmatrix} OH^- \end{bmatrix}$  -  $\begin{bmatrix} H^+ \end{bmatrix}$  (4-13)

Other processes can affect alkalinity in aquatic systems. Addition of acids and nitrification reduce alkalinity, and uptake of nitrate by algae increases alkalinity. Because of the magnitude of the ammonia concentration in waters receiving municipal effluents, nitrification can affect alkalinity substantially, generating 2 equivalents of acid  $(H^+)$  per equivalent of ammonia oxidized (see Section 3.4). Similarly in eutrophic waters, nitrate uptake can increase alkalinity by the production of approximately 1 equivalent of base  $(OH^-)$  per equivalent of nitrate taken up by plant cells. These corrections would be of consequence in low alkalinity waters (less than 200  $\mu$ eq/1), and would be applied to Equation (4-13).

Once the total inorganic carbon and alkalinity have been determined using the mass balance equations (4-1, 4-13), the hydrogen ion concentration
can be calculated by trial and error solution of the following relationship:

alk = [TIC] 
$$\frac{1 + \frac{2K_2}{[H^+]}}{1 + \frac{[H^+]}{K_1} + \frac{K_2}{[H^+]}} + \frac{K_w_s}{[H^+]} - [H^+]$$
 (4-14)

After  $[H^+]$  is determined, it is substituted into the expression for  $CO_2$ , which can then be solved directly for the dissolved  $CO_2$  concentration:

$$CO_{2} = \frac{[TIC]}{1 + \frac{K_{1}}{[H^{+}]^{+}} + \frac{K_{1} \cdot K_{2}}{[H^{+}]^{2}}}$$
(4-15)

Not all models compute inorganic carbon species or pH. Generally these computations have been made primarily in lake systems where they are of significance in acid precipitation or are used for additional model verification as in Di Toro and Connolly (1980). In all cases, the formulations are based on the above derivations, although the computation details may differ from model to model. Water quality models that contain the  $CO_2$ , alkalinity, pH formulations include those discussed in the following references:

Smith, 1978	WQRRS
Thomann <u>et al</u> ., 1974	LAKE-3
Di Toro and Connolly, 1980	Lake Erie Model
Scavia, <u>et</u> <u>al</u> ., 1976	Lake Ontario Model
Tetra Tech, 1980	EAM
WES, 1982	CE-QUAL-R1

### 4.3 EXTENDED ALKALINITY APPROACH

### 4.3.1 <u>Definition of Extended Alkalinity</u>

The mass balance equation (4-13) has ignored several  $\text{H}^+$ -ion acceptors, and is appropriate in many instances. In very low alkalinity waters,

however, the concentration of these neglected  $H^+$ -ion acceptors can be significantly large. The neglected  $H^+$ -ion acceptors include organic substances with carboxyl and phenolic hydroxyl groups, for example:

$$R-COO^{-} + H^{+} \longrightarrow R-COOH (organic acids)$$
 (4-16)

and the monomeric aluminum species and their complexes, for example,

$$A1(OH)_{2}^{+} + 2H^{+} \Longrightarrow A1^{3+} + 2H_{2}^{0}$$
 (4-17)

and

$$A1 \cdot R + 3H^{+} = A1^{3+} + H_{3}R.$$
 (4-18)

An extended alkalinity relationship would include the alkalinity associated with water itself, the carbonate system, the monomeric aluminum system and its organic complexes, and dissolved organic acid anions. The dissolved organic carbon alkalinity can be represented by a triprotic  $(H_3R_1)$  and/or monoprotic  $(HR_1)$  model organic acid with fixed dissociation constants and a fixed number of acid-base functional groups per unit mass of carbon (eq/mgC). The components of the total alkalinity, as represented by the H⁺-ion acceptors, are given below:

$$Alk = Alk_{H_20} + Alk_{C} + Alk_{R_1} + Alk_{R_2} + Alk_{A1} + Alk_{A1 \cdot 0}$$
(4-19)  
water carbonate organic aluminum system  
system acids

where

$$A1k_{H_20} = [0H^-] - [H^+]$$
 (4-20)

$$A1k_{C} = [HCO_{3}] + 2[CO_{3}^{2-}]$$
(4-21)

$$A1k_{R_{1}} = [H_{2}R_{1}] + 2[HR_{1}^{2}] + 3[R_{1}^{3}]$$
(4-22)

$$A1k_{R_2} = [R_2]$$
(4-23)

$$A1k_{A1} = [A1(OH)^{2+}] + 2[A1(OH)^{+}_{2}] + 3[A1(OH)^{0}_{3}] + 4[A1(OH)^{-}_{4}]$$
(4-24)

$$A1k_{A1\cdot 0} = 3[A1 R_1] + [A1R_2^{2+}] + 2[A1(R_2)_2^{+}] + 3[A1(R_2)_3]$$
(4-25)

An alternative representation of solution-phase alkalinity, which is mathematically equivalent to the above is given as follows,

$$A1k = \Sigma_{k} Z_{k} N_{k} = \Sigma C_{B} - \Sigma C_{A}$$
(4-26)

where  $\Sigma C_{R} =$  the sum of the base cations

$$= 2\left[C_{a}^{2+}\right] + 2\left[Mg^{2+}\right] + \left[Na^{+}\right] + \left[K^{+}\right] + \left[NH_{4}^{+}\right]$$
(4-27)

 $\Sigma C_{\Delta}$  = the sum of the strong acid anions

$$= 2 \left[ SO_4^{2^-} \right] + \left[ NO_3^- \right] + \left[ C1^- \right]$$
(4-28)

The derivation is based on the mass balance equation and the solution electroneutrality condition. Figure (4-1) shows the equivalence for lakes in the State of Washington.

### 4.3.2 Modeling Extended Alkalinity

The concept of extended alkalinity has been incorporated in a model called PHCALC. This model was developed primarily for the ILWAS model (Tetra Tech, 1983), and was later modified into an interactive FORTRAN program to compute any one of the following options: pH, alkalinity, total inorganic carbon (TIC) and "solution equilibration". The solution equilibration approach is similar to the approach for pH, except that alkalinity can be adjusted for gibbsite precipitation or dissolution. Table 4-1 shows the list of required parameters for any given option.

All the concentrations on the left-hand-side of Equations (4-20) through (4-25) can be expressed in terms of ionization fractions and



Figure 4-1.  $[\Sigma C_B - \Sigma C_A]$  plotted against reported alkalinity (from Gherini et al., 1984).

temperature-dependent dissociation constants. Fluoride and sulfate concentrations are required for the determination of their complexations with aluminum.

# 4.3.3 Equilibrium Constants and Solubility Products

The equilibrium constants used in PHCALC are obtained by first expressing a thermodynamic temperature dependence for a related constant,  $K_i$ : 239

Options*	Parameters Required to be Specified
рН	Alk, TIC or EQ ₁ , Al _T , OAC ₁ , OAC ₂ , F, SO ₄ ²⁻ , T
Alk	pH, TIC or EQ ₁ , A1 _T or EQ ₂ , OAC ₁ , OAC ₂ , F, SO ₄ ²⁻ , T
TIC	pH, Alk, Al _T , or EQ ₂ , OAC ₁ , OAC ₂ , F, SO ₄ ²⁻ , T
EQ	Alk, TIC or EQ ₁ , Al _T , EQ ₂ , OAC ₁ , OAC ₂ , F, SO ₄ ²⁻ , T
Definition o	of Parameters:
Alk	alkalinity
TIC	total inorganic carbon
EQ	equilibration of a solution with Al(OH)
Al _T	total aluminum
oaċ ₁	total organic acid (1)
	total organic acid (2)
F	fluoride concentration
so ₄ ²⁻	sulfate concentration
Т	temperature, ^O C
EQ ₁	ratio of TIC to air-equilibrated TIC (specified for open
	system)
EQ2	-log (Ksp) for Al(OH) ₃ mineral or one of the following minerals
	for the equilibration with gibbsite
	AG - amorphous gibbsite (pK _{sp} = 31.19)
	MG - microcrystalline gibbsite (pK _{sp} = 32.64)
	NG - natural gibbsite (pK _{sp} = 33.22)
	SG - synthetic gibbsite (pK _{sp} = 33.88)

TABLE 4-1. OPTIONS AND THEIR REQUIRED INPUT PARAMETERS FOR PHCALC

*Options are the parameters to be computed

$$\log_{10} K_{i} = a + \frac{b}{T} + cT + d\log_{10} T$$
 (4-29)

The constants a, b, c and d are given as follows:

	<u> </u>	b	С	d	Reference
ĸw	6.0875	-4470.99	-0.01706	0	Stumm & Morgan, 1981
к ₁	545.56	-17052	0.12675	-215.21	Loewenthal & Marais, 1978
к ₂	-6.498	2902.39	0.02379	0	Loewenthal & Marais, 1978
к _н	-14.0184	2385.73	0.0152642	0	Stumm & Morgan, 1981

 $K_w$ ,  $K_1$ , and  $K_2$  are dimensionless while  $K_H$  is in moles liter⁻¹ atm⁻¹.  $K_H$  has to be multiplied by RT to convert to a dimensionless form. R is the universal gas constant and T is the absolute temperature in degrees Kelvin in the range of 273 K to 313 K.

The solubility products used in the equilibration with gibbsite were shown earlier in Table 4-1.

### 4.4 SUMMARY

Two approaches have been presented for the relationship of total inorganic carbon, alkalinity and pH. For waters with low dissolved organic carbon (with little color) and high alkalinity (alk  $\geq 200\mu eq/1$ ), the conventional alkalinity definition is recommended. For waters with high dissolved organic carbon and waters with alk <200  $\mu eq/1$  where the alkalinities contributed by aluminum and organic acids are no longer negligible, the extended alkalinity approach is recommended. The equivalence between the expression Alk =  $\Sigma C_{\rm B} - \Sigma C_{\rm A}$  and the extended alkalinity definition for alkalinity evaluation.

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# Chapter 5

#### NUTRIENTS

#### 5.1 INTRODUCTION

Certain elements are referred to as nutrients because they are essential to the life processes of aquatic organisms. The major nutrients of concern are carbon, nitrogen, phosphorus, and silicon. Silicon is important only for diatoms, one of the major components of the algal community. Other micronutrients such as iron, manganese, sulphur, zinc, copper, cobalt, and molybdenum are also important. However, these latter nutrients are not considered in water quality models because they are required only in trace amounts and they are usually present in quantities adequate to meet the biochemical requirements of the organisms.

Nutrients are important in water quality modeling for several reasons. For example, nutrient dynamics are critical components of eutrophication models since nutrient availablility is usually the main factor controlling algal blooms. Algal growth is typically limited by either phosphorus or nitrogen, with the exception of diatoms which are often silicon limited. Some blue-green algae can fix nitrogen and are therefore not limited by nitrogen. Carbon is usually available in excess although in some cases it may also be limiting. Carbon is also important because of its role in the pH-carbonate system, as discussed in Chapter 4.

Nitrogen is important in water quality modeling for reasons other than its role as a nutrient. For example, the oxidation of ammonia to nitrate during the nitrification process consumes oxygen and may represent a significant portion of the total BOD. Also, high concentrations of unionized ammonia can be toxic to fish and other aquatic organisms.

## 5.2 NUTRIENT CYCLES

Nutrients are present in several different forms in aquatic systems:

- dissolved inorganic nutrients
- dissolved organic nutrients
- particulate organic (detrital) nutrients
- sediment nutrients
- biotic nutrients (algae, aquatic plants, zooplankton, fish, benthic organisms)

Only the dissolved inorganic forms are available for algal growth. These include dissolved CO₂, ammonia, nitrite, and nitrate nitrogen, orthophosphate, and dissolved silica.

Each nutrient undergoes continuous recycling between the major forms listed above. For example, dissolved inorganic nutrients are removed from the water column by algae and aquatic plants during photosynthesis. These nutrients are distributed to the other aquatic organisms through the food web. Dissolved inorganic nutrients are returned to the water through the soluble excretions of all organisms, the decomposition of organic detritus and sediments, and the hydrolysis of dissolved organic nutrients. In addition, dissolved  $CO_2$  and  $N_2$  gases exchange with the atmosphere. Suspended particulate nutrients are generated through the particulate excretions of aquatic animals and the death of planktonic organisms. Organic detritus and phytoplankton which settle to the bottom contribute to the sediment nutrients. Decomposition of suspended organic detritus and organic sediment releases both dissolved organic and dissolved inorganic nutrients to the water.

Many of the above interactions are shown in Figure 5-1 for carbon, nitrogen, and phosphorus and in Figure 5-2 for silicon. Figures 5-3 and 5-4 present more detailed descriptions of the nitrogen and phosphorus cycles.

In addition to the internal recycling of nutrients within the waterbody, nutrients are also introduced through wasteloads (both point and nonpoint sources), river or tributary inflows, runoff, and atmospheric precipitation.



Figure 5-1. Nutrient interactions for carbon, nitrogen, and phosphorus (from Tetra Tech, 1979).

# 5.3 GENERAL MODELING APPROACH FOR ALL NUTRIENTS

Nutrient dynamics are governed by the following processes:

- dissolved inorganic nutrients
  - photosynthetic uptake
  - excretion
  - chemical transformations (e.g., oxidation of NH₂)
  - hydrolysis of dissolved organic nutrients
  - detritus decomposition
  - sediment decomposition and release
  - external loading







Figure 5-3. Nitrogen cycle (from Baca and Arnett, 1976).



Figure 5-4. Phosphorus cycle (from Baca and Arnett, 1976).

- dissolved organic nutrients
  - excretion
  - hydrolysis
  - detritus decomposition
  - sediment decomposition and release
  - external loading

# particulate organic nutrients

- particulate excretions
- plankton mortality
- decomposition
- settling
- zooplankton grazing
- external loading
- sediment nutrients
  - detritus settling
  - algal settling
  - sediment decomposition and release

Only processes affecting the abiotic forms of nutrients are discussed in this chapter since the biotic components of water quality models are discussed in Chapters 6 (Algae) and 7 (Zooplankton).

Nutrients are modeled by using a system of coupled mass balance equations describing each nutrient compartment and each process listed above, plus the transport processes of advection and dispersion discussed in Chapter 2. The general equations for each nutrient, omitting the transport and external loading terms, can be expressed as follows:

## dissolved inorganic nutrients:

$$\frac{dS}{dt} = -V_{s} + f_{1} e_{s} + K_{1} S' - K_{2} S + K_{org} S_{org} + f_{2} K_{det} S_{det}$$

$$+ f_{3} K_{sed} S_{sed}$$
(5-1)

$$\frac{dS_{org}}{dt} = (1 - f_1) e_s - K_{org} S_{org} + (1 - f_2) K_{det} S_{det} + (1 - f_3) K_{sed} S_{sed}$$
(5-2)

particulate organic nutrients:

$$\frac{dS_{det}}{dt} = e_p + M_p - K_{det} S_{det} - K_s S_{det} - G_z \qquad (5-3)$$

sediment nutrients:

$$\frac{dS_{sed}}{dt} = K_s S_{det} + A_s - K_{sed} S_{sed}$$
(5-4)

where S = dissolved inorganic nutrient concentration, mass/volume S' = another inorganic form of the nutrient which decays to the form S (e.g., NH₂ NO₂), mass/volume Sora = dissolved organic nutrient concentration, mass/volume S_{det} = suspended particulate organic nutrient concentration, mass/volume S_{sed} = organic sediment nutrient concentration, mass/volume = transformation rate of S' into S, 1/time Κ1 = transformation rate of S into some other dissolved Κ2 inorganic form of the nutrient, 1/time = hydrolysis rate of dissolved organic nutrient, 1/time Kora = decomposition rate of particulate organic nutrient, 1/time Kdet K_{sed} = decomposition rate of organic sediment nutrient, 1/time = settling rate for particulate organic nutrient, 1/time κ = photosynthetic uptake rate for nutrient S, mass/volume-٧ time = soluble excretion rate of nutrient by all organisms, e, mass/volume-time = fraction of soluble excretions which are inorganic f₁

- f₂ = fraction of detritus decomposition products which are immediately available for algal uptake
- e = particulate excretion rate of nutrient by all animals, mass/volume-time
- M = total rate of plankton mortality, mass/volume-time
- $G_{z}$  = detritus grazing rate by zooplankton, mass/volume-time
- A_s = algal settling rate to sediment, mass/volume-time

Note that all of the transformations between the various abiotic nutrient compartments are described by first-order kinetics. This approach is used in almost all water quality models. Nutrient models differ primarily in the specific nutrients simulated (i.e., C, N, P, and Si) and in the number of compartments used to describe each nutrient cycle (i.e., dissolved inorganic forms such as  $NH_3$ ,  $NO_2$ , and  $NO_3$ ; dissolved organic components; particulate organic components; sediments; and biotic components such as algae and zooplankton).

For example, many models omit carbon since it does not limit algal growth in most situations. Silicon is generally modeled only when diatoms are simulated as a separate phytoplankton group.

The nutrient cycles are often simplified by combining or omitting some of the forms described above. For example, many models do not simulate sediment nutrients explicitly with a mass balance equation such as Equation (5-4). Instead, user-specified sediment fluxes are specified in Equations (5-1) and (5-2). Dissolved organic nutrients are also left out of most models. In these cases, the decomposition products of the detritus and sediments as well as all soluble excretions go directly to the dissolved inorganic nutrient compartments. This in effect combines the suspended particulate and dissolved organic compartments into a single "unavailable" nutrient compartment which decays to produce available inorganic forms.

Nitrogen models also differ in the forms of inorganic nitrogen which are included, as well as in some of the processes modeled. For example, some models include only ammonia and nitrate, rather than the full oxidation sequence of ammonia to nitrite to nitrate. While most models include the nitrification reactions, only a few include denitrification. Also, only a few models include nitrogen-fixation by blue-green algae.

Sediments and particulate organic detritus are often modeled as single compartments, rather than having a separate compartment for each nutrient. In this case, the corresponding compartments for each nutrient are determined from the product of the total sediment and detritus concentrations and the stoichiometric ratios for each nutrient. The stoichiometric ratios are generally the same as those used for algae (see Section 6.3 of Chapter 6) so that mass is conserved during nutrient recycling.

Table 5-1 presents a comparison of the various nutrient forms included in several models. Transformation processes and the corresponding rate coefficients for each specific nutrient are discussed below, along with model formulations for nutrient uptake, excretion, and sediment release. Formulations for plankton mortality and zooplankton grazing are discussed in Chapters 6 and 7. Settling formulations for particulate organic detritus are essentially the same as the simplest formulations used for phytoplankton settling described in Chapter 6 (i.e., the settling rate equals the userspecified settling velocity divided by the depth of the model segment).

## 5.4 TEMPERATURE EFFECTS

Temperature influences the rates of all of the nutrient transformation processes discussed above. All of the first-order rate coefficients in Equations (5-1) through (5-4) are therefore temperature dependent. Almost all models use the exponential Arrhenius or van't Hoff relationship to describe these effects. A reference temperature of  $20^{\circ}$ C is usually assumed when specifying each rate coefficient, resulting in the following equation:

	Nu	itrients	Modele	ď	1			Nutrient	Forms			Ino	rganic Ni	trogen F	orms	
Mødel (Author)	с	N	F	Si	Dislvd. Inorg.	Dislvd. Organic	Partic. Organic	Sedi- ments	Algae	Zoo- plankton	Other Organisms	NH 3	NO2	NO3	Total Avail	References
AQUA-IV		X	X		X	N	X	X	X	X		X	X	X		Baca & Arnett (1976)
CE-QUAL-R1	X	X	X		x		x	X	X	x	X	x	λ	X		WES (EWQOS) (1982)
CLEAN	x	X	X		x	X	x	X	X	X	X				x	Bloomfield <u>et al</u> . (1973)
CLEANER	x	X	x		x	x	x	X	X	X	x				x	Scavia & Park (1976)
MS.CLEANER	x	X	x	X	x	X	X	X	X	X	X				x	Park <u>et</u> <u>al</u> . (1980)
DEM		X	x		x			х*	X			x	X	X		Feigner & Harris (1970)
DOSAG3		X	X		x			x*	X			x	X	X		Duke & Masch (1973)
EAM	х	X	x	X	x		x	X	X	X	X	x	X	X		Tetra Tech (1979, 1980)
ESTECO	x	X	X		x		x	X	X	x	X	x	X	X		Brandes & Masch (1977)
EXPLORE-1	x	X	X		x		X	P	X	X		x	X	X		Baca <u>et</u> <u>al</u> . (1973)
HSP <i>F</i>	x	X	x		x		X	х*	X	X		x	X	X		Johanson <u>et al</u> . (1980)
LAKECO	x	X	X		x		X	X	X	X	X	x	X	X		Chen & Orlob (1975)
MIT Network		X			x	N	X		X	X		x	X	X		Harleman <u>et</u> <u>al</u> . (1977)
QUAL - I I		X	X		x			x*	X			x	X	X		Roesner <u>et al</u> . (1981)
RECEIV-II		X	X	-	x				X			x	X	X		Raytheon (1974)
SSAM IV		X	X		x				X			x		X		Grenney & Kraszewski (1981)
WASP	x	X	X	x	x	x	×	X	X	X		x		x		Di Toro <u>et</u> <u>al</u> . (1981)
WORRS	x	X	X		X		X	X	X	X	X	x	x	x		Smith (1978)
Bierman		х	X	x	x		X		X	x					x	Bierman <u>et al</u> . (1980)
Canale		X	X	x	x	x	X		X	X		x		X		Canale <u>et al</u> . (1975, 1976)
Jorgensen		X	X		x		X	X	X	x	X				x	Jorgensen (1976)
Lehman	X	X	x		x				X						x	Lehman <u>et al</u> . (1975)
Nyholm		x	x		x		x	X	X						X	Nyholm (1978)
Scavia	x	x	X		X	N	x	х	x	X		x		X		Scavia et al. (1976)

TABLE 5-1. COMPARISON OF NUTRIENT MODELS

*Specify flux.

$$K_{T} = K_{20} \qquad 5-5$$
  
here  $K_{T}$  = rate coefficient at temperature T, 1/time  
T = temperature, ^OC  
 $K_{20}$  = rate coefficient at 20^OC, 1/time  
 $\theta$  = temperature adjustment coefficient

 $\rho(T_{-20})$ 

This relationship is derived in Section 3.3 of Chapter 3.

A few models use different temperature adjustment formulations. For example, Canale (1976) uses a linear relationship and Grenney and Kraszweski (1981) use a logistic equation as a temperature adjustment function.

#### 5.5 CARBON TRANSFORMATIONS

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Table 5-2 presents rate coefficients for carbon decay processes along with the corresponding temperature adjustment factors. As shown in the table, these coefficients have a broad range, indicating a lack of detailed process characterization. Process characterization has been neglected in carbon models since the relationship of carbon dynamics to water quality modeling has not been considered essential. In fact, most water quality models do not include carbon since it is not usually a limiting nutrient. In the Lake Erie version of WASP (Di Toro and Connolly, 1980), the rate of decay of particulate organic carbon to  $CO_2$  has been further reduced by using a saturation relationship (Di Toro and Connolly, 1980). However, the decay rates in all other models are computed according to the first-order kinetics discussed above.

Most of the temperature adjustment factors in Table 5-2 range from 1.02 to 1.047, corresponding to  $Q_{10}$  values ranging between 1.2 and 1.6. The exception is the Lake Erie WASP model (Di Toro and Connolly, 1980), which uses a temperature correction factor of 1.08 ( $Q_{10} = 2.16$ ) for decay of settled algae and sediment organic matter. Also, the decay rate constants for these compartments are generally higher than those used in other models.

POC → CO ₂		SOC → C	0 ₂	SA +	<b>SO</b> C	SA →	C02	References
K	θ	K	θ	к	θ	к	θ	
0.1**	1.04	0.00025	1.08	0.02	1.08	0.02	1.08	Di Toro & Connolly (1980)
0.05	1.045							O'Connor <u>et al</u> . (1981)
0.001	1.02	0.001	1.02					Chen & Orlob (1972, 1975)
0.003	1.020	0.0015	1.047					Tetra Tech (1980)
0.02	1.020	0.001	1.020					Bowie <u>et al</u> . (1980)
0.1	1.047	0.0015	1.047					Porcella <u>et al</u> . (1983)
0.005-0.05***	1.02-1.04***	0.001-0.01***	1.02-1.04***					Smith (1978)
0.001-0.02***	1.040***	0.001-0.02***	1.040***					Brandes (1976)

TABLE 5-2. RATE COEFFICIENTS FOR CARBON TRANSFORMATIONS

*Abbreviations are defined as follows:

POC - Particulate Organic Carbon  $\operatorname{CO}_2$  - Carbon Dioxide

SOC - Sediment Organic Carbon

SA - Settled Algae

SA - Settled Algae **This rate is multiplied by an oxygen limitation factor,  $\frac{0_2}{K_1+0_2}$ , where  $K_1$  is a half-saturation constant for oxygen. ***Model documentation values.

### 5.6 NITROGEN TRANSFORMATIONS

Nitrogen dynamics are modeled in a considerably more complex manner than carbon because of their substantial biogeochemical role, important oxidation-reduction reactions, and because other important water quality variables such as oxygen are affected by nitrogen. The processes that are simulated in water quality models include:

- Ammonification release of ammonia due to decay processes (deamination, hydrolysis).
- Nitrification oxidation of ammonia to nitrate (NO₃) directly (one-stage process) or to nitrite (NO₂) and then to nitrate (two-stage process). Nitrification is discussed in detail in Section 3.4 of Chapter 3 in reference to its effects on dissolved oxygen.
- Denitrification reduction of nitrate to  $N_2$  under anaerobic conditions. This process also produces  $N_2^0$  (10 percent of total reduced), but since  $N_2^0$  has not been shown to have an appreciable effect on water quality,  $N_2^0$  production has not been modeled.
- Uptake accumulation of inorganic nitrogen by plants during photosynthetic growth. Both ammonia and nitrate are accumulated, with preference for ammonia over oxidized forms, although not all models include this preference.
- Nitrogen fixation reduction of N₂ to ammoniated compounds. Nitrogen fixation by blue-green algae is an important external input of nitrogen accumulation in waterbodies that materially affects nitrogen dynamics. However, uptake of inorganic ions takes precedence over nitrogen fixation.

In addition to the above processes, unionized ammonia can play a significant role as a toxicant depending on the ammonia concentration, pH, and temperature.

Table 5-3 presents rate coefficients for the major nitrogen decay and abiotic transformation processes along with the corresponding temperature ajdustment factors. The decay processes shown include breakdown of complex organic compounds (particulate organic nitrogen, PON) to simpler organics (dissolved organic nitrogen, DON) or to ammonia, the breakdown of sediment nitrogen to ammonia, and the oxidation of ammonia to nitrate. Rate constants for ammonia decay to nitrite and then to nitrate or from ammonia to nitrate directly are approximately commensurate as an overall rate process. The rate coefficients for some of the decay processes in some versions of WASP are further reduced by saturation kinetics (Di Toro and Connolly, 1980; Di Toro and Matystik, 1980; Thomann and Fitzpatrick, 1982; O'Connor et al., 1981). For example, the decay of particulate organic nitrogen to ammonia is reduced as chlorophyll a decreases, and the nitrification rate is reduced as dissolved oxygen decreases, according to saturation kinetics.

The temperature adjustment factors have a wide range of values, indicating some uncertainty in this coefficient. The  $Q_{10}$  values generally range from 1.2 to 2.4, but with one value as high as 3.7.

#### 5.6.1 Denitrification and Nitrogen Fixation

Both of these processes affect the mass balance of nitrogen because nitrogen is transported to (denitrification) or from (nitrogen fixation) the atmosphere rather than recycling within the water. Although both processes have been shown to be important in certain aquatic environments, denitrification is not commonly included in models. HSPF (Johanson <u>et al.</u>, 1980), CE-QUAL-R1 (WES, 1982), Jorgensen (1976), AQUA-IV (Baca and Arnett, 1976), and some versions of WASP (Di Toro and Connolly, 1980; Thomann and Fitzpatrick, 1982; O'Connor <u>et al.</u>, 1981) include denitrification.

						-								
PON	→ DON	DON →	NH3	PON	+ NH3	NH3 +	NO2	NH ₃ ⊣	· NO ₃	NO ₂	+ NO ₃	SEDN +	NH3	References
<u> </u>	θ	K	θ	K	θ	К	θ	ĸ	θ	ĸ	θ	K	θ	
				0.025	(14)		Cal	ibration Values						TI I I (1070)
				0.035	(linear)			0.04	(linear)					(nomann <u>et al</u> . (1975)
				0.03**	1.08									Thomann <u>et al</u> . (1979)
				0.03***	1.08			0.12***	1.08			0.0025	1.08	Di Toro & Connolly (1980)
				0.03***	1.08			0.20	1.08					Di Toro & Matystik (1980)
				0.075	1.08			0.09-0.13***	1.08			0.0004	1.08	Thomann & Fitzpatrick (198
								0.025***	1.08					O'Connor <u>et al</u> . (1981)
				0.14	(linear)									Salas & Thomann (1978)
				0.001	1.02	0.003-0.03	1.02			0.09	1.02	0.001	1.02	Chen & Orlob (1972, 1975)
0.020	(linear)	0.020	(linear)					0.060	(linear)					Scavia <u>et</u> <u>al</u> . (1976)
0.020	(line <b>ar)</b>	0.020	(linear)					0.1	(linear)					Scavia (1980)
0.02	1.020	0.02	1.020					0.1	1.020					Bowie <u>et al</u> . (1980)
0.02	(linear)	0.024	(linear)					0.16	(linear)					Canale <u>et al</u> . (1976)
				0.003	1.020	0.02	1.047			0.25	1.047	0.0015	1.047	Tetra Tech (1980)
				0.1	1.047	0.02	1.047			0.25	1.047	0.0015	1.047	Porcella <u>et</u> <u>al</u> . (1983)
				0.01**	NI							0.95-1.8***	1.14	Nyholm (1978)
				0.005**	1.08									Bierman <u>et</u> <u>al</u> . (1980)
				0.1**	1.02									Jorgensen (1976)
				0.2**	1.072									Jorgensen <u>et al</u> . (1978)

TABLE 5-3. RATE COEFFICIENTS FOR NITROGEN TRANSFORMATIONS

(continued)

PON + DON	DON - NH3	PON → NH	3	NH3 + N	⁰ 2	NH3 + NO3		N0 ₂ + N	0 ₃	SEDN + NI	H ₃	References
Kθ	K 0	К	θ	K	θ	K Ø		ĸ	θ	K	θ	
					Model Do	cumentation Values	<u>i</u>					
		0.1-0.4	NI	0.1-0.5	NI			510.	NI			Baca <u>et al</u> . (1973)
		0.02-0.04	1.02-1.09	0.1-0.5	1.02-1.09			310.	1.02-1.09	0.01-0.1	1.02-1.09	Baca & Arnett (1976)
				0.1-0.5	1.047			0.5-2.0	1.047			Duke & Masch (1973)
				0.1-0.5	1.047			0.5-20	1.047			Roesner <u>et</u> <u>al</u> . (1978)
		0.005-0.05	1.02-1.04	0.05-0.2	1.02-1.03			0.2-0.5	1.02-1.03	0.001-0.01	1.02-1.04	Smith (1978)
		0.001-0.02	1.040	0.05-0.2	1.02			0.2-0.5	1.02	0.001-0.02	1.040	Brandes (1976)
						0.04-3.0 (log	gistic)					Grenney & Kraszewski (198
						0.001-1.3****	NI					Collins & Wlosinski (1983

TABLE 5-3. (continued)

*Abbreviations are defined as follows:

NI - No Information

PON - Particulate Organic Nitrogen

DON - Dissolved Organic Nitrogen

SEDN - Sediment Organic Nitrogen

**Unavailable nitrogen decaying to algal-available nitrogen.

***Di Toro & Connolly (1980) and Di Toro & Matystik (1980) multiply the PON NH₃ rate by a chlorophyll limitation factor,  $\frac{Chl a}{K_1 + CHl a}$ , where K₁ is half-saturation constant = 5.0 µg CHa a/1. Di Toro & Connolly (1980) and Thomann & Fitzpatrick (1982) multiply the NH₃ NO₃ rate by an oxygen limitation factor,  $\frac{O_2}{K_2 + O_2}$ , where K₂ is a half-saturation constant = 2.0 mgO₂/1. O'Connor et al. (1981) multiply the NH₃ NO₃ rate by an oxygen limitation factor,  $\frac{O_2}{K_3 + O_2}$ , where K₃ is a half-saturation constant = 0.5 mgO₂/1.

Nyholm (1978) uses a sediment release constant which is multiplied by the total sedimentation rate of algae and detritus.

****Literature value.

Denitrification rates and the corresponding temperature adjustment coefficients are listed in Table 5-4. The decay rates for the WASP model are further modified according to a saturation type relationship based on the dissolved oxygen concentration. The rate decreases rapidly as  $0_2$  increases above 0.01 mg/l. This rate would be equivalent to that of Jorgensen (1976) when  $0_2 = 5$  mg/l. This indicates disagreement in conceptualization of the process or in its quantitative response between the two models. Sediment nitrate denitrification helps decrease the gradient of the sediment oxygen demand (SOD) and may lead to a reduced requirement for SOD (see Chapter 3.5; also, Di Toro, 1984).

Nitrogen fixation by blue-green algae is modeled by assuming that growth is not limited by nitrogen and that nitrogen fixation makes up for all nitrogen requirements which cannot be satisfied by ammonia and nitrate. Some type of saturation relationship is typically used to partition the nitrogen requirements between nitrogen fixation and uptake of ammonia and nitrate. The major features of these relationships are as follows: 1) no fixation occurs when ammonia plus nitrate are above some critical threshold concentration; 2) for concentrations below the threshold, nitrogen fixation increases as ammonia and nitrate decrease; and 3) when ammonia and nitrate become very low, all of the nitrogen requirements are supplied by fixation. Nitrogen fixation is included in the EAM (Tetra Tech, 1979), Scavia <u>et al</u>. (1976), Canale <u>et al</u>. (1976), and Bierman <u>et al</u>. (1980) models.

### 5.6.2 Unionized Ammonia

Although nitrogen is an important nutrient required by microorganisms, plants, and animals, certain forms such as unionized ammonia  $(NH_3)$  can be toxic. Unionized ammonia is toxic to fish at fairly low concentrations. For example, water quality criteria ranging from 0.0015 to 0.12 mg N/l for the 30-day average concentration have been suggested (USEPA, 1984). This range exists because the biological response varies at different temperature and pH values.

Both analytical measurement techniques and most model formulations for ammonia are based on total ammonia:

Nitrate →	Nitrogen Gas	References
K	θ	
0.1*	1.045	Di Toro & Connolly (1980)
0.1**	1.045	Di Toro & Connolly (1980)
0.09*	1.045	Thomann & Fitzpatrick (1982)
0.1*	1.045	0'Connor <u>et al</u> . (1981)
0.002	No Information	Jorgensen (1976)
0.02-0.03	No Information	Jorgensen <u>et</u> al. (1978)
01.0***	1.02-1.09***	Baca & Arnett (1976)

TABLE 5-4. RATE COEFFICIENTS FOR DENITRIFICATION

*This rate is multiplied by an oxygen limitation factor,  $\frac{K_1}{K_1+O_2}$ , where  $K_1$  is a half-saturation constant = 0.1mgO₂/1.

**The same rate applies to sediment  $NO_3$  dentrification.

***Model documentation values.

$$X = \text{total ammonia} = \text{NH}_3 + \text{NH}_4^+$$
 (5-6)

The concentrations of  $NH_3$  and  $NH_4^+$  vary considerably over the range of pH and temperature found in natural waters. but each can be readily calculated assuming that equilibrium conditions exist (Stumm and Morgan, 1981). Unionized ammonia exists in equilibrium with ammonia ion and hydroxide ion (Emerson, et al., 1975):

$$NH_3(g) + nH_20 = NH_3:nH_20 = NH_4^+ + 0H^- + (n-1) H_20$$
 (5-7)

The reaction occurs rapidly and is controlled largely by pH and temperature. Thus, unionized ammonia is calculated from the equilibrium expression:

$$K_{i} = \frac{(NH_{4}^{+})(OH^{-})}{(NH_{3})(H_{2}O)} = \frac{(NH_{4}^{+})K_{w}}{(NH_{3})(H^{+})}$$
(5-8)

Rearranging and taking the negative logarithm:

$$\log \frac{(NH_4^+)}{(NH_3)} = pK_w - pK_i - pH$$
 (5-9)

The quantity  $pK_h$  is called the hydrolysis constant. Substituting and taking the inverse logarithms,

$$\left(\frac{X - NH_3}{NH_3}\right) = 10^{\left(pK_h - pH\right)} = R$$
(5-10)

and solving for NH₂,

$$\mathsf{NH}_3 = \frac{\mathsf{X}}{\mathsf{1} + \mathsf{R}} \tag{5-11}$$

Thurston <u>et al</u>., (1974) determined the temperature correction for the hydrolysis constant as follows:

$$pK_{h} = 0.09018 + 2729.92/T$$
 (5-12)

where  $T = absolute temperature, {}^{O}K$ 

Substituting this relationship into Equation 5-7, unionized ammonia in moles/liter becomes a function of measured ammonia, temperature, and pH. Most water quality models predict the concentration of measured ammonia (X) in units of weight/volume as a resultant of processes of nitrification, ammonification, respiration, and assimilation. For  $NH_3-N$ , there are 14,000 mg/mole and

$$NH_3 - N, mg/1 = \frac{14000(X)}{1 + R}$$
 (5-13)

Although more cumbersome, a table of equilibrium values for unionized ammonia can be used in a model (e.g., USEPA, 1984). Figure 5-5 illustrates the relationship between pH, water temperature, and unionized ammonia.



Figure 5-5. Effect of pH and temperature on unionized ammonia (from Willingham, 1976).

## 5.7 PHOSPHORUS TRANSFORMATIONS

Table 5-5 presents rate coefficients and temperature correction factors for the various phosphorus transformation processes included in water quality models. The transformations include the decay of particulate organic phosphorus (POP), sediment phosphorus (SEDP), and settled algae (SA) directly to  $PO_A - P$  or into intermediate forms (dissolved organic phosphorus, DOP) before decaying to  $PO_A - P$ . The decay rates have a broad range, indicating some uncertainty in quantifying these processes. Similarly. there is a broad range in temperature coefficients, with a  $Q_{10}$  range from 1.2 to 2.4, except for a  $Q_{10}$  value of 3.7 for Nyholm (1978). Several of the WASP models adjust the phosphorus decay rates using a saturation equation based on algal biomass (Di Toro and Connolly, 1980; Di Toro and Matystik, 1980; Salisbury et al., 1983; Thomann and Fitzpatrick, 1982). In the case where chlorophyll a is used to estimate algal biomass, the halfsaturation constant is 5.0 g/l, and where carbon is used to estimate algal biomass, the value is 1.0 mgC/l.

#### 5.8 SILICON TRANSFORMATIONS

Silicon can be limiting only for diatoms, so its biogeochemical cycle is simulated only when diatoms are modeled as a separate algal group. Diatoms are important because of their role in phytoplankton succession, their role in aquatic food chains, and their potential effects on water treatment plants. Table 5-6 presents decay rates and temperature adjustment coefficients for silicon. In contrast to the other nutrients, particulate and sediment silicon decay directly to dissolved inorganic silicon rather than passing through a dissolved organic phase. The range of the firstorder decay rates for particulate silica decay is 0.003-0.1 (1/day). The temperature adjustment factor varies between 1.02 and 1.08, corresponding to a  $Q_{10}$  range of 1.2 to 2.2.

POP	• DOP	P0P -	• P04	DOP	- P04	SEDP	+ 00P	SEDÞ →	P0 <b>4</b>	Sedimer DOP	nt • P04	sa →	ed im <b>en t</b> DOP	sa →	PO ₄	References
<u>k</u>	0	ĸ –	θ	<u> </u>	θ	ĸ	θ	ĸ	Ø	ĸ	θ	K	A	ĸ	8	
		D.14	(linear)													Thomann <u>et al</u> . (1975)
		0.03	1.08													Thomann <u>et al</u> . (1979)
		0.03**	1.08													Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
0.22**	1.08			0.22**	1.08	0.0004	1.08	0.0004	1.08	0.0004	1.08	0.02	1.08	0.02	1.08	Thomann & Fitzpatrick (1982)
		0.14	(linear)													Salas & Thomann (1978)
		0.001	1.02					0.001	1.02							Chen & Orlob (1972, 1975)
		0.02	(linear)													Scavia et al. (1976) Scavia (1980)
0.2	(linear)			0.2	(linear)	)										Canale et al. (1976)
		0.003	1.020					0.0015	1.047							Tetra Tech (1980)
		0.02	1.020					0.001	1.020							Bowie <u>et al</u> . (1980)
		0.1	1.047					0.0015	1.047							Porcella <u>et al</u> . (1983)
		0.1	1.14					1.0-1.7	1.14**							Nyholm (1978)
		0.005	1.08													Bierman <u>et al</u> . (1980)
		0.1	1.02					0.0018	1.02							Jorgensen (1976)
		0.5-0.8	1.072													Jorgensen <u>et al</u> . (1978)
		0.1-0.7***	1.02-1.09***					0.1-0.7***	1.02-1.09**	•						Baca <u>et al</u> . (1973)
		0.1-0.7***	1.02-1.09***													Baca & Arnett (1976)
		0.005-0.05***	1.02-1.04***					0.001-0.01***	1.02-1.04**	•						Smith (1978)
		0.001-0.02***	1.040***													Brandes (1976)

		COFFETCIENTS	FOD		TDANCEODMATIONS
IABLE 5-5.	RAIE	CUEFFICIENIS	FUK	PHOSPHOKOS	TRANSFURMATIONS

Abbreviations are defined as follows:

POP - Particulate Organic Phosphorus DOP - Dissolved Organic Phosphorus PO4 - Phosphate

SEOP - Sediment Organic Phosphorus SA ~ Settled Algae

Chl a**Di Toro & Connolly (1980), Di Toro & Matystik (1980) and Salisbury <u>et al</u>. (1983) multiply this rate by a chlorophyll limitation factor,  $K_1^+CHl a$ , where  $K_1$  is a half-saturation constant = 5.0 µg Chl a/1. Thomann & Fitzpatrick (1982) multiply this rate by an algal carbon limitation factor,  $K_2^+Algal-C$ , where  $K_2$  is a half-saturation constant = 1.0mgC/1. Nyholm (1978) utilizes a sediment release constant which is multiplied by total sedimentation of algae and detritus. ***Model documentation values.

***Model documentation values.

Particulate Silica	→ Dissolved Silica	Sediment Silica	→ Dissolved Silica	References
K	θ	K	θ	
0.0175	1.08			Thomann <u>et al</u> . (1979)
0.1	1.08			Di Toro & Connolly (1980)
0.04	(linear)			Scavia (1980)
0.03	(linear)			Canale <u>et al</u> . (1976)
0.003	1.020	0.005	1.047	Tetra Tech (1980)
0.01	1.020	0.001	1.020	Bowie <u>et al</u> . (1980)
0.04	1.047	0.0015	1.047	Porcella <u>et</u> <u>al</u> . (1983)
0.005	1.08			Bierman <u>et al</u> . (1980)

TABLE 5-6. RATE COEFFICIENTS FOR SILICA TRANSFORMATIONS

#### 5.9 ALGAL UPTAKE

Two major approaches are used to simulate nutrient uptake by algae in water quality models. The most common method is the fixed stoichiometry approach in which the nutrient composition of the algae is assumed to remain constant. Under this assumption, the nutrient uptake rates are equal to the algal gross growth rate times the corresponding nutrient fractions of the algal cells:

$$V_{\rm s} = a_{\rm s} \mu \, A \tag{5-14}$$

where  $V_s$  = uptake rate for nutrient S, mass/volume-time  $a_s$  = nutrient fraction of algal cells, mass nutrient/mass algae  $\mu$  = gross growth rate of algae, 1/time A = algal concentration, mass/volume

This formulation is used in all fixed stoichiometry models. Typical values of the nutrient compositions of algae are given in Tables 6-2 to 6-4 of Chapter 6. Algal growth formulations and the corresponding model coefficients are discussed in Section 6.4 of Chapter 6.

The second approach to modeling nutrient uptake is the variable stoichiometry approach. In this method, the internal nutrient composition of the algal cells varies with time depending on the external nutrient concentrations in the water column and the relative rates of nutrient uptake and algal growth. The uptake rate depends on the difference between the internal nutrient concentration in the algal cells and the external concentration in the water. The internal concentration of each nutrient is assumed to range between a minimum stoichiometric requirement (called the minimum cell quota or subsistence quota) and some maximum internal concentration. In general, the uptake rate increases both as the external nutrient concentration approaches the maximum internal level, regardless of the external concentration in the water.

In contrast to fixed stoichiometry models, the uptake formulations used in variable stoichiometry models vary from model to model. Some models even use different formulations for different nutrients. Variable stoichiometry formulations for nutrient uptake are discussed in Section 6.4.4.3 of Chapter 6, since nutrient uptake is an integral part of the algal growth formulations in variable stoichiometry models. The major formulations are given in Equations (6-63) to (6-67).

### 5.9.1 Ammonia Preference Factors

Since algae use two forms of nitrogen, ammonia and nitrate, during uptake and growth, many models use ammonia preference factors in the uptake formulations to account for the fact that algae tend to preferentially uptake ammonia over nitrate. Ammonia preference factors are generally used in fixed stoichiometry models when both ammonia and nitrate are simulated. In this case, the uptake equations for ammonia and nitrate become:

$$\Psi_{\rm NH_3} = \beta_{\rm NH_3} \alpha_{\rm N} \mu A \qquad (5-15)$$

and

$$V_{NO_3} = (1 - \beta_{NH_3}) a_N \mu A$$
 (5-16)

where 
$$V_{\rm NH_3}$$
 = ammonia uptake rate, mass/volume-time  
 $V_{\rm NH_3}$  = nitrate uptake rate, mass/volume-time  
 $\beta_{\rm NH_3}$  = ammonia preference factor  
 $\alpha_{\rm N}$  = nitrogen fraction of algal cells

Ammonia preference factors are generally not needed in variable stoichiometry models since separate formulations with different coefficients can be used to distinguish between ammonia and nitrate uptake rates.

The ammonia preference factor  $_{\rm NH_3}$  partitions the nitrogen uptake required for a given amount of algal growth between ammonia and nitrate. The preference factor can range from 0 to 1, with 1 corresponding to a

situation in which all the nitrogen requirements are obtained from ammonia uptake, and 0 corresponding to a situation in which all the nitrogen is obtained from nitrate. The value of the preference factor is generally a function of the ammonia and nitrate concentrations in the water.

The simplest form of the ammonia preference factor assumes there is no preference for either form of nitrogen and partitions the uptake according to the relative proportions of ammonia and nitrate in the water:

$$NH_{3} = \frac{NH_{3}}{NH_{3} + NO_{3}}$$
(5-17)

where  $NH_3$  = ammonia concentration, mass/volume  $NO_3$  = nitrate concentration, mass/volume

This approach is used in EXPLORE-1 (Baca <u>et al.</u>, 1973), LAKECO (Chen and Orlob. 1975), WQRRS (Smith, 1978), CE-QUAL-R1 (WES, 1982), EAM (Tetra Tech, 1979), ESTECO (Brandes, 1976). and earlier versions of WASP (Thomann <u>et al.</u>, 1975).

Other models which assume there is a preference for ammonia uptake have used the following formulations for the preference factor:

$$\beta_{\rm NH_3} = \frac{\gamma_1^{\rm NH_3}}{\gamma_1^{\rm NH_3} + NO_3}$$
(5-18)

$$\beta_{\rm NH_3} = \frac{\rm NH_3}{\rm \gamma_2 + \rm NH_3}$$
(5-19)

$$\beta_{\rm NH_3} = \frac{\gamma_3 \, {\rm NH_3}}{\gamma_3 \, {\rm NH_3} + (1 - \gamma_3) \, {\rm NO_3}}$$
(5-20)

$$\beta_{\mathrm{NH}_{3}} = \left(\frac{\mathrm{NH}_{3}}{\mathrm{NH}_{3} + \gamma_{4}}\right)\left(\frac{\mathrm{NO}_{3}}{\mathrm{NO}_{3} + \gamma_{4}}\right) + \left(\frac{\mathrm{NH}_{3}}{\mathrm{NH}_{3} + \mathrm{NO}_{3}}\right)\left(\frac{\gamma_{4}}{\gamma_{4} + \mathrm{NO}_{3}}\right)$$
(5-21)

where  $\gamma_1$ ,  $\gamma_2$ ,  $\gamma_3$ ,  $\gamma_4$  = coefficients in ammonia preference factor formulations

Equation (5-18) is used in SSAM IV (Grenney and Kraszewski, 1981) and Scavia <u>et al.</u> (1976), Equation (5-19) in an early Lake Erie WASP model by Di Toro <u>et al.</u> (1975), Equation (5-20) in AQUA-IV (Baca and Arnett, 1976) and Canale <u>et al</u>. (1976), and Equation (5-21) in more recent versions of WASP by Thomann and Fitzpatrick (1982) and O'Connor et al. (1981).

#### 5.10 EXCRETION

Nutrient excretion by algae and zooplankton is one of the major components of nutrient recycling. In almost all models, nutrient excretion is modeled as the product of the respiration mass flux and the nutrient stoichiometry of the organisms. The equations for algal excretion and zooplankton excretion are:

 $e_{sa} = a_{sa} r_a A \qquad (5-22)$ 

and

$$e_{sz} = a_{sz} r_z Z \qquad (5-23)$$

where  $e_{sa} = algal excretion rate of nutrient S, mass/volume-time$  $<math>e_{sz} = zooplankton excretion rate of nutrient S, mass/volume-time$  $<math>a_{sa} = nutrient fraction of algal cells, mass nutrient/mass algae$   $a_{sz} = nutrient fraction of zooplankton, mass nutrient/mass$ zooplankton $<math>r_{a} = algal respiration rate, 1/time$ 

r_z = zooplankton respiration rate, 1/time

- A = algal concentration, mass/volume
- Z = zooplankton concentration, mass/volume

The excretion formulations for other organisms such as fish or benthic animals is the same as for zooplankton. Respiration rate formulations for algae and zooplankton are discussed in Section 6.5 (Chapter 6) and 7.4 (Chapter 7), respectively. The nutrient compositions of algae are presented in Tables 6-2 to 6-4 of Chapter 6. The nutrient compositions of zooplankton are typically assumed to be the same as for algae in fixed stoichiometry models so that nutrient mass is conserved as biomass cycles through the food web.
#### 5.11 SEDIMENT RELEASE

Three major approaches have been used to simulate nutrient release from the sediments in water quality models. The simplest approach is to specify an areal flux from the bottom in the mass balance equations for dissolved nutrients. This technique is commonly used in river models and in models which do not dynamically simulate sediments as a separate constituent (e.g., QUAL-II (Roesner <u>et al.</u>, 1981), DOSAG3 (Duke and Masch, 1973), and HSPF (Johanson <u>et al.</u>, 1980)). Sediment release rates are highly site-specific, and are determined largely by model calibration of the dissolved nutrients.

The second approach is to model sediment nutrients as a dynamic pool using a mass balance equation such as Equation (5-4). In this method, nutrients are released according to a first-order decay rate:

$$R_{s} = \alpha_{s} K_{sed} Sed$$
 (5-24)

The organic sediment pool increases as algae and suspended organic detritus settle to the bottom, and decreases as the sediment decomposes. This approach is used in LAKECO (Chen and Orlob, 1975), Chen <u>et al.</u> (1975), WQRRS (Smith, 1978), CE-QUAL-R1 (WES, 1982), EAM (Tetra Tech, 1979), and ESTECO (Brandes, 1976). In some models, a fraction of the settled particulates is assumed to be refractory and unavailable for mineralization.

The third approach to modeling sediment release uses a more complex mechanistic approach in which: 1) organic sediments undergo the same decay sequences as particulate organics in the water column but with the decay products going to the interstitial water rather than the overlying water, and 2) the nutrients in the interstitial waters diffuse to the overlying water at a rate depending on the concentration gradient between the interstitial water and overlying water. This approach is used in some versions of WASP (e.g., Di Toro and Connolly, 1980; Thomann and Fitzpatrick, 1982). A few models also include denitrification in the transformation reactions.

Nyholm (1978) simulates sediment release dynamically without actually modeling sediments by assuming the release rates equal the product of a temperature dependent coefficient times the sedimentation rates of algal and detrital nutrients to the bottom.

#### 5.12 SUMMARY

Carbon, nitrogen, phosphorus. and silicon are the major growth limiting nutrients included in water quality models. Nitrogen is also important because of the effects of nitrification on dissolved oxygen dynamics and because of ammonia toxicity. All nutrients recycle continuously in the water column between particulate and sediment forms, dissolved organic forms, dissolved inorganic forms, and biotic forms. The important processes are decomposition of organic particulates and sediments, decay of dissolved organic to inorganic forms, chemical transformations such as nitrification, photosynthetic uptake of dissolved inorganic forms, and soluble and particulate excretion by aquatic organisms. Denitrification and nitrogen fixation are also important in some situations.

First-order kinetics are used in almost all models to describe the various decay processes and transformations. The exponential Arrhenius or van't Hoff relationship is used to adjust the rate coefficients for temperature effects. Some of the processes are modified by Michaelis-Menten type saturation kinetics in a few models. Uptake and excretion are based on algal growth rates and algal and zooplankton respiration rates combined with the nutrient stoichiometries of the organisms. More complex formulations are used for nutrient uptake in variable stoichiometry models. Sediment release rates are usually modeled either by specifying a nutrient flux or modeling sediments as a nutrient pool subject to first-order decay. A few models use more complex formulations which include decay reactions in the

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interstitial waters and diffusion between the interstitial waters in the sediment and the overlying water column.

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# Chapter 6

### ALGAE

## 6.1 INTRODUCTION

Algae are important components of water quality models for several reasons. For example:

- Algal dynamics and nutrient dynamics are closely linked together since nutrient uptake during algal growth is the main process which removes dissolved nutrients from the water, and algal respiration and decay are major components of nutrient recycling.
- Algal processes can cause diurnal variations in dissolved oxygen due to photosynthetic oxygen production during the daylight combined with oxygen consumption due to algal respiration during the night. Seasonal oxygen dynamics may also be closely tied to algal dynamics, particularly in highly productive stratified systems, since the respiration and decomposition of algae which settles below the photic zone is often a major source of oxygen depletion.
- Algae can affect pH through the uptake of dissolved CO₂ during photosynthesis and the recycling of CO₂ during respiration.
- Algae are the dominant component of the primary producers in many systems, particularly in lakes and estuaries. Since

they form the base of the food chain, they play a major role in the dynamics of all successive trophic levels.

- Suspended algae are often a major component of turbidity.
- Algal blooms can restrict recreational uses of water, sometimes resulting in fish kills under severe conditions.
- Algae can cause taste and odor problems in water supplies, and filter clogging problems at water treatment facilities.

Two general approaches have been used to simulate algae in water quality models: 1) aggregating all algae into a single constituent (for example, total algae or chlorophyll  $\underline{a}$ ), or 2) aggregating the algae into a few dominant functional groups (for example, green algae, diatoms, blue-greens, dinoflagellates, etc.).

The first approach is commonly used in river models since the major focus is on short term simulations (days to weeks) where the primary interest is the effects of algae on general water quality parameters such as dissolved oxygen, nutrients, and turbidity. Typical examples include QUAL-II (Roesner et al., 1981; NCASI, 1982, 1983), DOSAG3 (Duke and Masch, 1973), and RECEIV-II (Raytheon, 1974). In contrast, lake and reservior models tend to use the second approach since the focus is on long term simulations (months to years) of eutrophication problems where seasonal variations in different types of algae are important (Bierman, 1976; Bierman et al., 1973, 1980; Canale et al., 1975, 1976; Chen et al., 1975; Tetra Tech, 1979, 1980; Park et al., 1974, 1975, 1979, 1980; Scavia et al., 1976; Scavia, 1980; Lehman et al., 1975). Species-specific differences in nutrient requirements, nutrient uptake rates, growth rates, and temperature preference ranges result in a seasonal succession of dominance by different phytoplankton groups. It is often important to distinguish these differences in order to realistically model both nutrient dynamics and phytoplankton dynamics, and to predict the occurrence of specific problems such as blue-green algal blooms. Multi-group models typically use the same

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general model formulations for all groups, but provide different coefficient values to characterize the differences between groups.

## 6.2 MODELING APPROACHES

Phytoplankton dynamics are governed by the following processes: growth, respiration and excretion, settling, grazing losses, and nonpredatory mortality (or decomposition). A general equation which includes all of these processes and forms the basis for almost all phytoplankton models can be expressed as:

$$\frac{dA}{dt} = (\mu - r - e_{\chi} - s - m) A - G$$
(6-1)

- $\mu$  = gross growth rate, 1/time
- r = respiration rate, 1/time
- $e_x = excretion rate, 1/time$
- s = settling rate, 1/time
- m =, nonpredatory mortality (or decomposition) rate, 1/time
- G = loss rate due to grazing, mass/time or mass/volume-time

This equation is appropriate when phytoplankton are modeled in terms of either biomass or nutrient equivalents (carbon, nitrogen, phosphorous, etc.). However, if phytoplankton are expressed in terms of cell numbers, the growth rate is replaced with the cell division rate, and the respiration and excretion terms are omitted since they pertain to changes in biomass rather than cell numbers. The resulting equation is:

$$\frac{dA_{n}}{dt} = (\mu_{n} - s - m) A_{n} - G_{n}$$
(6-2)

where  $A_n$  = phytoplankton cell numbers, numbers or numbers/volume  $\mu_n$  = cell division rate, 1/time

# G = loss rate due to grazing, numbers/time or numbers/volume-time

The cell division rate in Equation (6-2) is assumed to be a continuous process although in reality cell division is a discrete event which is often expressed in terms of the number of divisions per day,  $n_d$ . The continuous division rate  $\mu_n$  is related to the discrete rate  $n_d$  by  $\mu_n = n_d \ln 2$ .

Most models express phytoplankton in terms of biomass (or nutrient or chlorophyll <u>a</u> equivalents) rather than cell numbers. This facilitates the modeling of both nutrient cycles and food web dynamics since it allows a more direct linkage between the phytoplankton equations and the mass balance equations for both nutrients and higher trophic levels such as zooplankton and fish. Phytoplankton cell numbers are used in a few models whose focus is restricted to phytoplankton dynamics (e.g., Lehman <u>et al.</u>, 1975; Cloern, 1978).

The major differences between different phytoplankton models are: 1) the number of phytoplankton groups modeled, 2) the specific formulations used for each process, and 3) the manner in which the various processes and corresponding terms in Equations (6-1) or (6-2) are combined. Some of the basic features of different phytoplankton models are compared in Table 6-1. The specific process formulations are discussed in later sections.

Many models combine several of the processes in Equation (6-1) into a single term, thereby simplifying the equation. For example, respiration and excretion are usually combined into a single respiration term. Respiration is often combined with growth so that the growth rate  $\mu$  represents the net growth rate, rather than the gross growth rate as in Equation (6-1). This is consistent with net growth rates typically reported in the literature from laboratory cultures. Some models combine respiration and mortality. Other models combine grazing and nonpredatory mortality into a single mortality term, particularly when algal grazers are not modeled explicitly.

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	Nurr	iber of Gro	ups	F	rocesses	Computed	Separately in I	fode1		Algal U	nits		
Model (Author)	Phyto- plankton	Attached Algae	Zoo- plankton	Growth	Respir- ation	Settling	Nonpredatory Mortality	Predatory Mortality	Dry Wt. Biomass	Ch1 <u>a</u> Carbon	Other Nutrient	Cell Numbers	Reference
AQUA-IV	1		1	x	x	X	x	x		X			Baca & Arnett (1976)
CE-QUAL-R1	2		1	x	X	x		x	x				WES (EWQOS) (1982)
CLEAN	2	1	3	x	X	X	X	x	X				Bloomfield <u>et al</u> . (1973)
CLEANER	3	1	3	x	X	x	x	x	x				Scavia & Park (1976)
MS.CLEANER	4	1	5	x	X	x	X	x	X				Park <u>et al</u> . (1980)
DEM	1			x	X	x				X			Feigner & Harris (1970)
DOSAG3	1			x	X	x				X			Duke & Masch (1973)
EAM	4	1	3	x	X	x		X	X				Tetra Tech (1979, 1980)
ESTEC0	2		1	x	X	x		X	X				Brandes & Masch (1977)
EXPLORE-1	1		1	X	X			X		X			Baca <u>et al</u> . (1973)
HSPF	1	1	1	X	X	х	X	X	X				<b>Johanso</b> n <u>et al</u> . (1980)
LAKEC0	2		1	X	X	x		X	X				C <b>hen &amp; O</b> rlob (1975)
NIT Network	1		1	X	X		X	X			N		Harleman <u>et al</u> . (1977)
QUAL-11	1			x	X	x				X			Roesner <u>et</u> <u>al</u> . (1981)
RECEIV-II	1			x	X		X			X			Raytheon (1974)
SSAM IV	1	1		X			X		X				Grenney & Kraszewski (1981)
WASP	2		2	X	X	X	X	X		X X			Di Toro <u>et al</u> . (1981)
WQRRS	2	2	1	X	X	X		X	X				Smith <b>(1978)</b>
Bierman	5		2	x	X	x	X	X	x				Bierman <u>et</u> <u>al</u> . (1980)
Canale	4		9	X	X	x		X		X			Canale <u>et al</u> . (1975, 1976)
Jorgensen	1		1	x	X	x	X	X	x			1	Jorgensen (1976)
Lehman	5			x	X	x	X					X	Lehman <u>et al</u> . (1975)
Nyholm	1			X		x	X		X				Nyholm (1978)
Scavia	5		6	x	x	X	x	X		X			Scavia <u>et al</u> . (1976)

# TABLE 6-1. GENERAL COMPARISON OF ALGAL MODELS

Because of these variations, it is very important to understand the assumptions of a particular model when selecting coefficients. Care must be taken both when extracting values from one model and applying them to another, or when using experimental measurements reported in the literature. For the latter case, the experimental conditions should be checked to make sure they are consistent with the assumptions of the model. If they are different, the appropriate adjustments should be made.

Attached algae (periphyton) and aquatic macrophytes have the same growth requirements as phytoplankton (light and nutrients) and are subject to the same basic processes of growth, respiration and excretion, grazing, and nonpredatory mortality. Therefore, they are usually modeled using the same general approach and process formulations as phytoplankton, although the specific values of the model coefficients will vary. The major differences are: 1) periphyton and macrophytes are associated with the bottom substrate and are expressed in terms of areal densities rather than volumetric densities or concentrations; 2) periphyton and macrophytes do not have settling losses, but instead they have additional losses due to sloughing or scouring from the bottom substrate; 3) periphyton and macrophytes are not subject to hydrodynamic transport; and 4) macrophytes use nutrients from the sediments and interstitial waters rather than nutrients in the water column. The general model equation for attached algae and macrophytes can be expressed as:

$$\frac{dA_{b}}{dt} = (\mu - r - e_{x} - s_{1} - m) A_{b} - G_{b}$$
(6-3)

S₁ = sloughing or scouring rate, 1/time

G_b = loss rate due to grazing, mass/time or mass/area-time

Benthic algae or macrophytes are included in only a few models such as CLEAN (Park <u>et al</u>., 1974), CLEANER (Park <u>et al</u>., 1975), MS_CLEANER

(Park <u>et al.</u>, 1980), EAM (Tetra Tech, 1979, 1980), WQRRS (Smith, 1978), HSPF (Johanson <u>et al.</u>, 1980), SSAM IV (Grenney and Kraszewski, 1981), and in Canale and Auer (1982) and Scavia <u>et al.</u> (1975).

## 6.3 CELL COMPOSITION

The majority of models express algae and other biological constituents as either dry weight biomass (Chen and Orlob, 1972; Chen <u>et al.</u>, 1975; Park <u>et al.</u>, 1974, 1975, 1979, 1980; Tetra Tech, 1979, 1980; Brandes and Masch, 1977; Smith, 1978; Johanson <u>et al.</u>, 1980; Grenney and Kraszewski, 1981; Bierman <u>et al.</u>, 1973, 1980; Jorgensen, 1976; Jorgensen <u>et al.</u>, 1978; Nyholm, 1977, 1978) or carbon (Baca and Arnett, 1976; Baca <u>et al.</u>, 1973, 1974; Canale <u>et al.</u>, 1975, 1976; Scavia <u>et al.</u>, 1976; Scavia, 1980). Nitrogen or phosphorus have also been used in a few models which focus on a single nutrient cycle and assume that particular nutrient always limits algal growth (Najarian and Harleman, 1975; Harleman <u>et al.</u>, 1977). Some models express phytoplankton as chlorophyll <u>a</u> since both field measurements and water quality standards are often reported in these units (Roesner <u>et al.</u>, 1981; Duke and Masch, 1973; Raytheon, 1974; Di Toro <u>et al.</u>, 1971, 1977; Di Toro and Matystik, 1980; Di Toro and Connolly, 1980; O'Connor <u>et al.</u>, 1975; Thomann <u>et al.</u>, 1975, 1979).

Dry weight biomass is related to the major nutrients (carbon, nitrogen, and phosphorus) and chlorophyll <u>a</u> through stoichiometric ratios which give the ratios of each nutrient to the total biomass. Typical algal nutrient compositions are summarized in Tables 6-2 to 6-4. Algae expressed as carbon, nitrogen, phosphorus, or chlorophyll <u>a</u> can be converted to dry weight biomass or any of the other units by using the stoichiometric ratios presented in the tables.

Most conventional water quality models assume the nutrient compositions of the cells and the resulting stoichiometric ratios are constant. In reality, cell stoichiometry varies with species, cell size, physiological condition, and recent environmental conditions (external nutrient concentrations, light, and temperature), although it is often assumed

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	Percent of Dry Weight Biomass								
Algal Type	C	N	Р	Si	Chl <u>a</u>	References			
Total Phytoplankton	4050.	89.	1.5			Tetra Tech (1976) Chen & Wells (1975, 1976)			
	40.	7.2	1.0			Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)			
					2.	Bierman (1976)			
	60.					Nyholm (1978)			
		6.1	0.88			Jorgensen (1976)			
	4050.*	79.*	11.2*			Smith (1978)			
		89.*	1.2-1.5*		510.*	Roesner <u>et al</u> . (1980) Duke & Masch (1973)			
	50.*	9.*	1.2*			Brandes (1976)			
	42.9-70.2**	0.6-16.**	0.16-5.**			Baca & Arnett (1976)			
		1.5-9.3**	0.08-1.17**			Jorgensen (1979)			
Diatoms	40.	7.2	1.0	2024.		Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et</u> al. (1983)			
				50.		Bierman <u>et al</u> . (1976)			
	1950.**	2.7-5.9**	0.4-2.0**			Di Toro <u>et al</u> . (1971)			
	2053**					Bierman <u>et al</u> . (1980)			
Green Algae	40.	7.2	1.0			Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)			
	3548.**	6.6-9.1**	2.4-3.3**			Di Toro <u>et al</u> . (1971)			
	1574.**					Bierman <u>et al</u> . (1980)			
Blue-green	40	7 9	1.0			Tatua Tach (1980)			
Argue	40.	/.2	1.0			Bowie et al. $(1980)$ Porcella et al. $(1983)$			
	2845.**	4.5-5.8**	0.8-1.4**			Di Toro <u>et al</u> . (1971)			
	38 <b>39</b> .**					Bierman <u>et al</u> . (1980)			
					13.**	Baca & Arnett (1976)			
					0.25**	Jorgensen (1979)			

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# TABLE 6-2. NUTRIENT COMPOSITION OF ALGAL CELLS - PERCENT OF DRY WEIGHT BIOMASS

Algal Type	C	N	Р	Si	Chl- <u>a</u>	References
Dinoflagellates					275.	0'Connor <u>et</u> <u>al</u> . (1981)
	3747**	3.3~5.0**	0.6-1.1**			Di Toro <u>et</u> <u>al</u> . (1971)
	1043.**					Bierman <u>et al</u> . (1980)
Flagellates	40.	7.2	1.0			Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	2967.**					Bierman <u>et al</u> . (1980)
Chrysophytes	3545.**	7.8-9.0**	1.2-3.0			Jorgensen (1979)
Benthic Algae	40.	7.2	1.0			Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	4050.*	79.*	11.2*			Smith (1978)

#### *Model documentation values.

**Literature values.

constant for modeling purposes. Several of the more recent algal models, however, have included variable cell stoichiometry in their formulations to simulate processes such as luxury uptake and storage of nutrients (Bierman <u>et al.</u>, 1973, 1980; Bierman, 1976; Lehman <u>et al.</u>, 1975; Jorgensen, 1976; Jorgensen <u>et al.</u>, 1978; Nyholm, 1977, 1978; Park <u>et al.</u>, 1979, 1980; Canale and Auer, 1982). These models are discussed later with reference to phytoplankton growth and nutrient uptake formulations.

#### 6.4 GROWTH

Algal growth is a function of temperature, light, and nutrients. The major growth limiting nutrients are assumed to be phosphorus, nitrogen, and carbon, with the addition of silicon for diatoms. Other essential micronutrients such as iron, manganese, sulfur, zinc, copper, cobalt, molybdenum, and vitamin B₁₂ may also limit growth under conditions of restricted availability (particularly in oligotrophic systems). However, these effects are generally not included in models since micronutrients are usually not simulated. The algal growth rate formulations used in almost all models can be expressed in general functional form as:

$$\mu = \mu_{\max}(T_{ref}) f(T) f(L,P,N,C,Si)$$
(6-4)

where  $\mu$ 

Ρ

= algal growth rate, 1/time

# max(Tref) = maximum growth rate at a particular reference
temperature Tref under optimal conditions of
saturated light intensity and excess nutrients,
1/time

f(T) = temperature function for growth

T = temperature, ^OC

f(L,P,N,C,Si) = growth limiting function for light and nutrients
L = light intensity

= available inorganic phosphorus concentration, mass/volume

Algal Type	N C	P C	Si C	References
Total Phytopl <b>ankton</b>	0.17 - 0.25	0.025		Thomann & Fitzpatrick (1982) Di Toro <u>et al</u> . (1971)
	0.18	0.024		Scavia et al. (1976) Scavia (1980)
	0.2			Canale <u>et al</u> . (1976)
	0.05 - 0.17**	0.024 - 0.24**		Baca & Arnett (1976)
	0.05 - 0.43**	0.025 - 0.05**		Jorgensen (1979)
Diatoms	0.18	0.024	0.6	Scavia (1980)
	0.067 - 0.21**	0.003 - 0.14**	0.06-0.77**	Jorge <b>nsen (197</b> 9)

TABLE 6-3.	NUTRIENT COMPOSITION O	F ALGAL	CELLS
	- RATIO TO CARBON		

**Literature Values.

Algal Type	C Chl <u>a</u>	<u>N</u> Ch1 <u>a</u>	P Chl <u>a</u>	Si Chl <u>a</u>	References
Total Phytoplankton	50100.	715.	0.5-1.0		Thomann et al. (1975, 1979) O'Connor et al. (1981) Di Toro & Matystik (1980) Di Toro & Connolly (1980) Salas & Thomann (1978)
			0.5		Salisbury <u>et</u> <u>al</u> . (1983)
		7.2	0.63		Larsen <u>et al</u> . (1973)
	25112.**	729.**	1.0**		Jorgensen (1979)
	10100.**	2.7-9.1**			O'Connor <u>et al</u> . (1981)
Diatoms	100.	1015.	0.5-1.0	4050.	Di Toro & Connolly (1980) Di Toro & Matystik (1980) Thomann <u>et</u> <u>al</u> . (1979)
			0.5		Salisbury <u>et</u> <u>al</u> . (1983)
	50200.*				Baca & Arnett (1976)
	18500**	2.2-74.6**	0.27-19.2**	2.4-50.7**	Di Toro <u>et al</u> . (1971)
Green Algae	25100.*				Baca & Arnett (1976)
Blue-green Algae	1467.*				Baca & Arnett (1976)
Dinoflagellates	275.	19.3			0'Connor <u>et</u> <u>al</u> . (1981)

# TABLE 6-4. NUTRIENT COMPOSITION OF ALGAL CELLS - RATIO TO CHLOROPHYLL a

*Model documentation values.

**Literature values.

N	= available inorganic nitrogen concentration,
	mass/volume
С	= available inorganic carbon concentration,
	mass/volume
Si	= available inorganic silicon concentration,
	mass/volume

Note that the growth limiting function f(L,P,N,C,Si) is simplified in many models by excluding some of the nutrients. For example, silicon is

included only in models which simulate diatoms as a separate algal group (Bierman <u>et al</u>., 1973, 1980; Bierman, 1976; Canale <u>et al</u>., 1975, 1976; Scavia <u>et al</u>., 1976; Scavia, 1980; Chen <u>et al</u>., 1975; Tetra Tech, 1979, 1980; Lehman <u>et al</u>, 1975; Park <u>et al</u>., 1979, 1980; Di Toro and Connolly, 1980). Carbon is frequently omitted since it is often available in excess relative to phosphorus and nitrogen (Bierman <u>et al</u>., 1980; Scavia <u>et al</u>., 1976; Nyholm, 1978; Canale <u>et al</u>., 1975, 1976; Baca and Arnett, 1976; Di Toro and Matystik, 1980). Some models include only one nutrient, phosphorus or nitrogen, and assume that nutrient is limiting at all times for the particular system under consideration (Najarian and Harleman, 1975; Canale and Auer, 1982).

It should also be noted that the nutrient concentrations in the growth limiting function f(L,P,N,C,Si) correspond to the "external" nutrient concentrations in the water for some models, and to the "internal" nutrient concentrations in the algal cells for other models. These distinctions will be discussed in more detail below.

## 6.4.1 Temperature Effects On Maximum Growth Rates

The quantity  $\mu_{max}(T_{ref})$  f(T) in Equation (6-4) represents the effects of temperature variations on maximum algal growth rates under conditions of optimum light and nutrients. The maximum growth rate  $\mu_{max}$  must be specified at a reference temperature  $T_{ref}$  which is consistent with the particular temperature function f(T) used in the model. The reference temperature may correspond to 20^oC, optimum temperature conditions, or some other temperature, depending on the form of the temperature function. Therefore, maximum growth rate coefficients obtained from one model may have to be adjusted before using the coefficients in another model which has a different temperature adjustment function. Maximum growth rates for algae are tabulated in Table 6-5, along with the corresponding reference temperatures.

Although numerous temperature adjustment functions have been used to model algae, most of them fall into one of three major categories

Algal Type	Maximum Growth Rate (1/day)	R <b>e</b> ference Temperature ( ⁰ C)	References
Total Phytoplankton	1.3 2.5	20 ⁰ C	O'Connor <u>et al</u> . (1975, 1981) Thomann <u>et al</u> . (1974, 1975, 1979) Thomann & Fitzpatrick (1982) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Di Toro <u>et al</u> . (1971, 1977) Salas & Thomann (1978) Salisbury <u>et al</u> . (1983)
	1. 2.5	20 ⁰ C	Chen (1970) Chen & Orlob (1975) Chen & Wells (1975, 1976) Tetra Tech (1976)
	1. 2.	20 ⁰ C	Battelle (1974)
	1.5	20 ⁰ C	Grenney & Kraszewski (1981)
	1 2.7	T _{opt}	Scavia & Park (1976) Youngberg (1977)
	1.5	20 ⁰ C	Nyholm (1978)
	1.8 2.53	T _{opt}	Jorgensen (1976) Jorgensen <u>et</u> <u>al</u> . (1978)
	2.4	T _{opt}	Larsen <u>et al</u> . (1973)
	0.2 8.*	20 ⁰ C	Baca & Arnett (1976)
	1. 3.*	T _{opt}	Smith (1978)
	1. 3.*	20 ⁰ C	Roesner <u>et al</u> . (1980) Duke & Masch (1973)
	0.2 8.*	20 ⁰ C	Grenney & Kraszewski (1981)
	1.5 2.*	20 ⁰ C	Brandes (1976)
	0.58 3.**	20 ⁰ C	Jor <b>gen</b> sen (1979)
Diatoms	2.1	20 ⁰ C	<b>Di Toro &amp;</b> Connolly (1980) Thomann <u>et al</u> . (1979) Salisbury <u>et al</u> . (1983)
	2.0 2.5	Topt	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	2.0 - 2.1	20 ⁰ C	Canale <u>et al</u> . (1976)
	2.1	25 ⁰ C	Bierman (1976)
	1.6	10 ⁰ - 14 ⁰ C	Bierman <u>et al</u> . (1980)
	1.8 - 2.5	T _{opt}	Scavia <u>et al</u> . (1976) Scavia (1980)
	3.0	T _{opt}	Lehman <u>et</u> <u>al</u> . (1975)

Algal Type	Maximum Growth Rate (1/day)	Reference Temperature ( ⁰ C)	References
	1.75**	27 ⁰ C**	Di Toro <u>et</u> <u>al</u> . (1971)
	0.55 3.4**	20 ⁰ C**	Collins & Wlosinski (1983)
	1.1 5.0**	20 ⁰ C**	Jorgensen (1979)
Green Algae	1.9	25 ⁰ C	Bierman (1976)
	1.4	20 ⁰ C	Bierman <u>et</u> <u>a</u> l. (1980)
	2.0 - 2.5	T _{opt}	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	1.9	20 ⁰ C	Canale <u>et</u> <u>al</u> . (1976)
	1.8 - 2.5	^T opt	Scavia <u>et al</u> . (1976) Scavia (1980)
	1.6	25 ⁰ C	DePinto <u>et al</u> . (1976)
	3.0	T _{opt}	Lehman <u>et</u> <u>al</u> . (1975)
	1.5 3.9**	25 ⁰ C**	Di Toro <u>et al</u> . (1971)
	0.7 - 2.1**	20 ⁰ C	Collins & Wlosinski (1983)
	0.9 4.1**	25 ⁰ C**	
	9.0 9.2**	39 ⁰ C**	
	1.4 2.4**	20 ⁰ C**	Jorgensen (1979)
	1.5 3.9**	25°C**	
	5.65**	40 ⁰ C**	
		059-	
Blue-green Algae	0.8	25°C	Bierman (1976)
	0.7 - 1.0	20 ⁰ - 25 ⁰ C	Bierman <u>et al</u> . (1980)
	1.6	20 ⁰ C	Canale <u>et al</u> . (1976)
	1.4 - 1.9	^T opt	Youngberg (1977)
	1.1 - 2.0	Topt	Scavia & Park (1976) Scavia (1980)
	1.1	25 ⁰ C	DePinto <u>et al</u> . (1976)
	2.5	Topt	Lehman <u>et al</u> . (1975)
	1.6 2.5	T _{opt}	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	0.41 - 0.86**	20 ⁰ C**	Jorgensen (1979)
	0.2 4.9**	25 ⁰ C**	Collins & Wlosinski (1983)
	2.0 3.9**	35 ⁰ C**	()
	0.5 11.**	40 ⁰ C**	

TABLE 6-5. (continued)

		· · · · · · · · · · · · · · · · · · ·	
Algal Type	Maximum Growth Rate (1/day)	Reference Temperature ( ^O C)	References
	•		
Dinoflagellates	0.2 - 0.28	20 ⁰ C	O'Connor <u>et</u> <u>al</u> . (1981)
	2.16**	20 ⁰ C	Di Toro <u>et</u> <u>al</u> . (1971)
	0.2 2.1**	20 ⁰ C	Collins & Wlosinski (1983)
Flagellates	1.6	Topt	Tetra Tech (1980) Porcella <u>et al</u> . (1983)
	1.2	20 ⁰ C	Bierman <u>et</u> <u>al</u> . (1980)
	1.5	T _{opt}	Lehman <u>et al</u> . (1975)
Chrysophytes	1.5	T _{opt}	Lehman <u>et</u> <u>al</u> . (1975)
	0.4 2.9**	25°C**	Collins & Wlosinski (1983)
Coccolithophores	1.75 2.16**	25 ⁰ C**	Jorgensen (1979)
Benthic Algae	0.5 1.5	T _{opt}	Tetra Tech (1980) Porcella <u>et</u> <u>al</u> . (1983)
	1.08	T _{opt}	Auer and Canale (1982)
	1.5	20 ⁰ C	Grenney & Kraszewski (1981)
	0.2 0.8*	20 ⁰ C	Grenney & Kraszewski (1981)
	0.5 1.5*	^T opt	Smith (1978)

*Model documentation values.

**Literature values.

(Figure 6-1): 1) linear increases in growth rate with temperature, 2) exponential increases in growth rate with temperature, and 3) temperature optimum curves in which the growth rate increases with temperature up to the optimum temperature and then decreases with higher temperatures.

The simplest type of temperature adjustment function assumes a linear temperature response curve above some minimum temperature  $T_{min}$ . This relationship can be expressed in general form as:

$$f(T) = \frac{T - T_{\min}}{T_{ref} - T_{\min}}$$

$$= \left(\frac{1}{T_{ref} - T_{\min}}\right) T - \left(\frac{T_{\min}}{T_{ref} - T_{\min}}\right)$$

$$= \gamma T + \beta$$
(6-5)

where  $T_{min}$  = lower temperature limit at which the growth rate is zero,  $O_{C}$ 



Figure 6-1. Major types of temperature response curves for algal growth.

 $T_{ref}$  = reference temperature corresponding to the value of the maximum growth rate  $\mu_{max}(T_{ref})$ , ^OC

$$\gamma = \frac{1}{(T_{ref} - T_{min})}$$
 = slope of growth vs. temperature curve

$$\beta = \frac{\text{Imin}}{\text{Tref} - \text{Imin}} = y \text{-intercept of growth vs. temperature}$$

This equation is typically used in simplified form by choosing a lower temperature limit  $T_{min}$  equal to zero so that Equation (6-5) becomes:

$$f(T) = \frac{T}{T_{ref}}$$
(6-6)

Reference temperatures of either  $20^{\circ}$ C or  $1^{\circ}$ C are usually used which results in:

$$f(T) = \frac{T}{20}$$
 (6-7)

or

$$f(T) = T$$
 (6-8)

This approach is used in EXPLORE-I (Baca <u>et al.</u>, 1973) and RECEIV-II (Raytheon, 1974) and by Di Toro <u>et al</u>. (1971) in an early version of WASP.

Some models use piecewise linear functions for algal growth with different slopes over different temperature ranges (Bierman <u>et al.</u>, 1980; Canale <u>et al.</u>, 1975, 1976). HSPF (Johanson <u>et al.</u>, 1980) uses Equation (6-5) over the temperature range between  $T_{min}$  and the optimum temperature for maximum growth  $T_{opt}$ , followed by a constant temperature function above  $T_{opt}$ :

$$f(T) = \left(\frac{1}{T_{opt} - T_{min}}\right) T - \left(\frac{T_{min}}{T_{opt} - T_{min}}\right) \quad \text{for } T \leq T_{opt} \quad (6-9a)$$

$$f(T) = 1 \quad \text{for } T > T_{\text{opt}} \tag{6-9b}$$

with 
$$\mu_{\max}(T_{ref}) = \mu_{\max}(T_{opt})$$
 (6-9c)

where  $T_{opt}$  = optimum temperature at which the growth rate is maximum,

This assumes growth increases linearly with temperature until the maximum growth rate is attained, and then remains at the maximum rate as temperature increases further.

The most commonly used exponential temperature adjustment functions are based on the Arrhenius or van't Hoff equation:

$$Q_{10} = \left(\frac{\kappa_2}{\kappa_1}\right) \left(\frac{10}{\tau_2 - \tau_1}\right)$$
(6-10)

where  $K_1$  = reaction rate at temperature  $T_1$   $K_2$  = reaction rate at temperature  $T_2$  $Q_{10}$  = ratio of reaction rates at  $10^{\circ}C$  temperature increments

This equation can be rearranged into a more useful form as:

$$K_2 = K_1 Q_{10} \left( \frac{T_2 - T_1}{10} \right)$$
 (6-11)

or

$$K(T) = K(T_{ref}) Q_{10} \left( \frac{T - T_{ref}}{10} \right)$$

$$= K(T_{ref}) f(T)$$
(6-12)

where f(T) is the temperature adjustment function:

$$f(T) = Q_{10} \left( \frac{T - T_{ref}}{10} \right)$$
 (6-13)

The temperature adjustment function (Equation (6-13)) is generally expressed in a more simplified form as:

$$f(T) = Q_{10}^{(1/10)(T-T} ref)$$
(6-14)  
$$= \theta^{(T-T} ref^{)}$$
where  $\theta = Q_{10}^{(1/10)}$  = temperature adjustment coefficient

The temperature adjustment coefficient  $\theta$  typically has a value between 1.01 and 1.2, with a value of 1.072 corresponding to a doubling of the growth rate for every 10^oC increase in temperature. Eppley (1972) found that  $\theta$  equals 1.066 for an exponential envelope curve of growth rate versus temperature data compiled from a large number of studies involving many

Most models which use exponential temperature functions assume a reference temperature of  $20^{\circ}$ C which gives the familiar equation (Chen and Orlob, 1975; Baca and Arnett, 1976; Roesner <u>et al.</u>, 1981; Brandes and Masch, 1977; Duke and Masch, 1973; Thomann <u>et al.</u>, 1979; Thomann and Fitzpatrick, 1982; Di Toro and Matystik, 1980; Di Toro and Connolly, 1980; O'Connor <u>et al.</u>, 1981):

$$f(T) = \theta^{(T-20^{\circ}C)}$$
 (6-15a)

with

different species (Figure 6-2).

$$\mu_{max}(T_{ref}) = \mu_{max}(20^{\circ}C)$$
 (6-15b)

However, Thomann <u>et al</u>. (1975) and Eppley (1972) use a reference temperature of  $0^{\circ}$ C which results in:

$$f(T) = \theta^{T}$$
 (6-16a)

with

$$\mu_{\max}(T_{ref}) = \mu_{\max}(0^{\circ}C) \qquad (6-16b)$$

The above equations assume that the temperature adjustment coefficient  $\theta$  has the same value regardless of the reference temperature. However, a few models have applied Equation (6-14) in a piecewise manner assuming that the value of  $\theta$  varies over different temperature intervals.

Many formulations have been used to generate temperature optimum curves for algal growth. The reference temperature is generally set at the optimum temperature for maximum growth, and the temperature adjustment function is normalized so it has a maximum value of 1.0 at the optimum temperature and smaller values elsewhere. Most curves begin with a zero value at the lower temperature tolerance limit, increase to a maximum value of 1.0 at the optimum temperature, and then decrease back to a value of zero at the upper temperature tolerance limit. These types of curves are typically based on growth vs. temperature data for a single species. These data generally show no growth at very low temperatures followed by an exponential increase in



Figure 6-2. Envelope curve of algal growth rate versus temperature for data compiled from many studies involving many different species (adapted from Eppley, 1972; Goldman, 1981).

growth with temperature over a large part of the temperature range. However, the growth rate eventually levels off to some maximum value at the optimum temperature, and then begins to decline at very high temperatures until growth finally ceases at some upper temperature limit.

Lehman <u>et al</u>. (1975) use a skewed normal distribution as a temperature optimum curve for phytoplankton growth. The equation is:

$$f(T) = \exp\left[-2.3\left(\frac{T - T_{opt}}{T_{x} - T_{opt}}\right)^{2}\right]$$
(6-17a)

with 
$$\mu_{max}(T_{ref}) = \mu_{max}(T_{opt})$$
 (6-17b)

where  $T_{opt} = optimum$  temperature at which the growth rate is maximum,  $o_C$   $T_x = T_{min}$  for  $T \le T_{opt}$   $= T_{max}$  for  $T > T_{opt}$   $T_{min} = lower$  temperature limit at which the growth rate is zero,  $o_C$   $T_{max} = upper$  temperature tolerance limit at which growth ceases,  $o_C$ 

Jorgensen (1976) and Jorgensen <u>et al</u>. (1978) use a modified form of Equation (6-17a) which is expressed as:

$$f(T) = \exp\left(-2.3 \left| \frac{T - T_{opt}}{T_{opt} - T_{min}} \right| \right)$$
(6-18)

Several models including CLEAN (Bloomfield <u>et al</u>., 1973), CLEANER (Scavia and Park, 1976), MS.CLEANER (Park <u>et al</u>, 1979, 1980), and Scavia <u>et al</u>. (1976) use a temperature optimum function originally developed by Shugart <u>et al</u>. (1974). This formulation can be expressed as:

$$f(T) = V^{X} e^{X(1-V)}$$
 (6-19a)

$$V = \frac{T_{max} - T}{T_{max} - T_{opt}}$$
(6-19b)

$$x = \left[\frac{W(1 + \sqrt{1 + 40/W})}{20}\right]^2$$
 (6-19c)

$$W = (1n Q_{10}) (T_{max} - T_{opt})$$
 (6-19d)

with 
$$\mu_{max}(T_{ref}) = \mu_{max}(T_{opt})$$
 (6-19e)

where  $Q_{10}$  is defined as in Equations (6-10) through (6-14).

The temperature function in Equations (6-19a) through (6-19e) has been modified in the ecosystem model MS.CLEANER by adding a temperature adaption formulation which essentially shifts the whole curve by varying the values of  $T_{opt}$  and  $T_{max}$  to account for acclimation to different temperatures (Park <u>et al.</u>, 1980). This formulation was originally developed by O'Neill (1972), and can be expressed as:

$$T_{shift} = T_{smax} \left[ 1 - e^{-K_{ac} |T_{avg} - T_{opt}| } \right]$$
(6-20)

where  $T_{shift} = magnitude of acclimation (translation of <math>T_{opt}$  and  $T_{max}$ ),  $O_C$   $T_{smax} = maximum magnitude of acclimation, <math>O_C$   $K_{ac} = acclimation rate coefficient$  $T_{avg} = average temperature for previous 2 weeks, <math>O_C$ 

Lassiter and Kearns (1973) and Lassiter (1975) developed a temperature optimum equation of the form:

$$f(T) = \left( e^{K_{a}(T-T_{opt})} \right) \left( \frac{T_{max} - T}{T_{max} - T_{opt}} \right)^{K_{a}(T_{max} - T_{opt})}$$
(6-21a)

$$\mu_{\max}(T_{ref}) = \mu_{\max}(T_{opt})$$
(6-21b)

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with

where  $K_a = a$  scaling constant used in the original equation from which Equation (6-21a) was derived,

$$\frac{df(T)}{dt} = K_{a} \left( \frac{T_{max} - T}{T_{max} - T_{opt}} \right)$$
(6-21c)

These equations result in a temperature optimum curve which is always skewed to the right.

Thornton and Lessem (1978) developed a temperature optimum curve by combining two logistic equations, one describing the rising limb of the curve below the optimum temperature and one describing the falling limb of the curve above the optimum temperature. The second curve is rotated about the y-axis and shifted to the right along the x-axis until the approximate peaks of both curves coincide. The left side of the temperature curve is expressed as:

$$K_{A}(T) = \frac{K_{1} e^{\gamma_{1}(T-T_{min})}}{1 + K_{1} \left[ e^{\gamma_{1}(T-T_{min})} - 1 \right]}$$
(6-22a)

$$\gamma_{1} = \frac{1}{(T_{opt(1)} - T_{min})} \ln \left[ \frac{K_{2} (1 - K_{1})}{K_{1} (1 - K_{2})} \right]$$
(6-22b)

and the right side is expressed as:

$$K_{\rm B}(T) = \frac{K_4 e^{\gamma_2(T_{\rm max}-T)}}{1 + K_4 \left[e^{\gamma_2(T_{\rm max}-T)} - 1\right]}$$
(6-23a)

$$y_{2} = \frac{1}{(T_{max} - T_{opt}(2))} \ln \left[ \frac{K_{3} (1 - K_{4})}{K_{4} (1 - K_{3})} \right]$$
(6-23b)

where 
$$T_{opt(1)}$$
 = lower limit of optimum temperature range,  ${}^{O}C$   
 $T_{opt(2)}$  = upper limit of optimum temperature range,  ${}^{O}C$   
 $y_1$  = rate coefficient for left side of curve  
 $y_2$  = rate coefficient for right side of curve  
 $K_1$  = rate multiplier near the lower temperature limit  $T_{min}$   
 $K_4$  = rate multiplier near the upper temperature limit  $T_{max}$   
 $K_2$  = 0.98  
 $K_3$  = 0.98

The temperature curve is defined as the product of Equations (6-22a) and (6-23a):

$$f(T) = K_{A}(T) K_{B}(T)$$
 (6-24a)

with 
$$\mu_{\max}(T_{ref}) = \mu_{\max}(T_{opt})$$
 (6-24b)

By using different values of the logistic equation parameters for each side, an assymmetric growth curve can be generated. The values of  $K_2$  and  $K_3$  are set equal to 0.98 rather than 1.0 so that the peak of the combined logistic equation is close to 1.0 (since the logistic equation would otherwise only approach 1.0 assymptotically). Two values of the optimum temperature,  $T_{opt(1)}$  and  $T_{opt(2)}$ , are used to allow an optimum temperature range, rather than a single optimum temperature value. This formulation is used in CE-QUAL-R1 (WES, 1982), WQRRS (Smith, 1978), and EAM (Tetra Tech, 1979, 1980). The left side of the curve (the basic logistic equation, Equation (6-22a)) is also used as a temperature adjustment curve in SSAM IV (Grenney and Kraszewski, 1981).

The MIT one-dimensional network model (Najarian and Harleman, 1975; Harleman <u>et al.</u>, 1977) uses a temperature optimum curve which is defined as:

$$f(T) = \left(\frac{T}{T_{opt}}\right)^{n} \exp\left[1 - \left(\frac{T}{T_{opt}}\right)^{n}\right] \quad \text{for } T < T_{opt} \quad (6-25a)$$

and 
$$f(T) = 1 - \left(\frac{T - T_{opt}}{T_{max} - T_{opt}}\right)^m$$
 for  $T > T_{opt}$  (6-25b)

with

$$\mu_{\max}(T_{ref}) = \mu_{\max}(T_{opt})$$
(6-25c)

The values of the exponents n and m are 2.5 and 2.0, respectively (Najarian and Harleman, 1975).

Some type of temperature optimum curve is generally more appropriate than a linear or exponential formulation when considering a single algal species or functional group, since growth usually slows down and eventually ceases above some upper temperature limit for any given species. This approach is used in most models which simulate several algal groups (e.g., Chen et al., 1975; Tetra Tech, 1979, 1980; Park et al., 1979, 1980; Canale et al., 1975, 1976; Scavia et al., 1976; Lehman et al., 1975; Smith, 1978; WES, 1982), since seasonal variation in temperature is one of the major factors causing seasonal succession in the dominance of different groups (diatoms, greens, blue-greens, etc.). However, since many species are lumped into a few functional groups, the temperature optimum curves and maximum growth rates should be defined so that they encompass the temperature-growth curves of all dominant species in the defined groups. Canale and Vogel (1974) developed a set of temperature-growth curves for diatoms, green algae, blue-green algae, and flagellates based on a literature review of growth data for many species (Figure 6-3).

Since the temperature function includes both the effects of increasing temperature on the growth rates of many individual species as well as shifts in the species composition toward dominance by warmer water species, some modelers have preferred to use exponential or linear formulations over the whole temperature range, particularly when only one or two groups are simulated (Chen and Orlob, 1975; Thomann <u>et al.</u>, 1979; Di Toro and Matystik, 1980; Di Toro and Connolly. 1980; Nyholm, 1978). This assumes that as temperature increases, the species composition changes so that species with optimum temperatures near the ambient temperature (and with

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Figure 6-3. Temperature-growth curves for major algal groups (from Canale and Vogel, 1974).

higher maximum growth rates) tend to dominate the phytoplankton assemblage. Eppley (1972) showed that an exponential relationship describes the envelope curve of growth rate versus temperature data from a large number of studies with many different species (Figure 6-2). However, this approach may overestimate the net growth of the assemblage if the growth rates are based on the maximum growth rate of the species assumed to be dominant at any given instant, since much of the biomass will include species which predominated earlier under different temperature conditions (Swartzman and Bentley, 1979). Exponential or linear functions which increase indefinitely with temperature can also be justified in situations where the maximum water temperatures are always below the optimum temperatures for the species present. For example, Canale and Vogel (1974) assumed a linear relationship below the temperature optimum for each algal group in Figure 6-3.

The temperature formulations used in different models are compared in Table 6-6.

	Tempera	ture Formulatio	on (Equati	on No.)	Defenses	
Model (Author)	Linear	Exponential	Curve	Curve	Reference Temperature	Reference
AQUA-IV		6-14			20 ⁰ C	Baca & Arnett (1976)
CE-QUAL-R1			6-24		T _{opt}	WES (EWQOS) (1982)
CLEAN			6-19		Topt	Bloomfield <u>et</u> <u>al</u> . (1973)
CLEANER			6-19		Topt	Scavia & Park (1976)
MS.CLEANER			6-19		Topt	Park <u>et al</u> . (1980)
DEM		6-14			20 ⁰ C	Feigner & Harris (1970)
DOSAG3		6-14			20 ⁰ C	Duke & Masch (1973)
EAM			6-24		T _{opt}	Tetra Tech (1979, 1980)
ESTEC0		6-14			20 ⁰ C	Brandes & Masch (1977)
EXPLORE-1	6-6				1 ⁰ C	Baca <u>et al</u> . (1973)
HSPF				piecewise linear saturation		Johanson <u>et</u> <u>al</u> . (1980)
LAKECO		6-14			20 ⁰ C	Chen & Orlob (1975)
MIT Network			6-25		T _{opt}	Harleman <u>et al</u> . (1977)
QUAL-II		6-14			20 ⁰ C	Roesner <u>et</u> <u>al</u> . (1981)
RECEIV-II	6-6				1 ⁰ C	Raytheon (1974)
SSAM IV				logistic	20 ⁰ C	Grenney & Kraszewski (1981)
WASP		6-14			20 ⁰ C	Di Toro <u>et</u> <u>al</u> . (1981)
WQRRS			6-24		T _{opt}	Smith (1978)
Bierman	piecewise linear			piecewise linear saturation	·	Bierman <u>et al</u> . (1980)
Canale	piecewise linear				1 ⁰ C	Canale <u>et</u> <u>al</u> . (1975, 1976)
Jorgensen			6-18		Topt	Jorgensen (1976)
Lehman			6-17		Topt	Lehman <u>et al</u> . (1975)
Nyholm		6-14			20 ⁰ C	Nyholm (1978)
Scavia			6-19		T _{opt}	Scavia <u>et</u> <u>al</u> . (1976)

TABLE 6-6. COMPARISON OF TEMPERATURE ADJUSTMENT FUNCTIONS FOR ALGAL GROWTH

#### 6.4.2 Algal Growth Limitation

In addition to temperature effects, algal growth rates are limited by both light and nutrient availability. As mentioned above, only macronutrients (phosphorous, nitrogen, carbon, and silicon) are generally included in models. Growth limitation was expressed previously as the factor f(L,P,N,C,Si) in the algal growth equation:

$$\mu = \mu_{\max}(T_{ref}) f(T) f(L,P,N,C,Si)$$
(6-4)

Separate growth limiting factors are typically computed for light and each potentially limiting nutrient. The number of nutrients considered will vary between models depending on the particular system under consideration. Each growth limitation factor can range from a value of 0 to 1. A value of 1 means the factor does not limit growth (i.e., light is at optimum intensity, nutrients are available in excess, etc.) and a value of 0 means the factor is so severely limiting that growth is stopped entirely.

Four major approaches have been used to combine the limiting factors for light and each limiting nutrient:

 a multiplicative formulation in which all factors are multiplied together:

$$f(L,P,N,C,Si) = f(L) f(P) f(N) f(C) f(Si)$$
 (6-26)

where f(L) = light limitation factor f(P) = nutrient limitation factor for phosphorous f(N) = nutrient limitation factor for nitrogen f(C) = nutrient limitation factor for carbon f(Si) = nutrient limitation factor for silicon (for diatoms)

 a minimum formulation in which the most severely limiting factor alone is assumed to limit growth:

$$f(L,P,N,C,Si) = min [f(L),f(P),f(N),f(C),f(Si)]$$
 (6-27)

where min  $[x_1, x_2, x_3, ...]$  = minimum of each factor  $x_i$ 

3) a harmonic mean formulation which combines the reciprocal of each limiting factor in the following manner:

$$f(L,P,N,C,Si) = \frac{n}{\frac{1}{f(L)} + \frac{1}{f(P)} + \frac{1}{f(N)} + \frac{1}{f(C)} + \frac{1}{f(Si)}}$$
(6-28)

where n = number of limiting factors (5 in this case)

4) an arithmetic mean formulation which uses the average of each limiting factor:

$$f(L,P,N,C,Si) = \frac{f(L) + f(P) + f(N) + f(C) + f(Si)}{n}$$
(6-29)

The multiplicative formulation has been used in many models (Chen and Orlob, 1972, 1975; Di Toro <u>et al</u>., 1971, 1977; Di Toro and Matystik, 1980; Di Toro and Connolly, 1980; Thomann <u>et al</u>., 1975, 1979; O'Connor <u>et al</u>., 1975; Jorgensen, 1976; Jorgensen <u>et al</u>., 1978; Canale <u>et al</u>., 1975; Jorgensen, 1976; Roesner <u>et al</u>., 1981; Baca <u>et al</u>., 1973; Duke and Masch, 1973; Brandes and Masch, 1977). This approach assumes that several nutrients in short supply will more severely limit growth than a single nutrient in short supply. The major criticism of this approach is that the computed growth rates may be excessively low when several nutrients are limiting. Also, the severity of the reduction increases with the number of limiting nutrients considered in the model, making comparison between models difficult. Many models assume that light limitation is multiplicative, but use one of the other approaches for nutrient limitation (e.g., Bierman <u>et al</u>., 1976; Baca and Arnett, 1976; Nyholm, 1978; Raytheon, 1974).

The minimum formulation is based on "Liebig's law of the minimum" which states that the factor in shortest supply will control the growth of algae.
This approach has been popular in many recent algal models (Bierman <u>et al.</u>, 1980; Park <u>et al.</u>, 1979, 1980; Scavia, 1980; Smith 1978; Tetra Tech, 1979, 1980; WES, 1982; Johanson <u>et al.</u>, 1980; Grenney and Kraszewski, 1981; Chen <u>et al.</u>, 1975; Baca and Arnett, 1976). The minimum formulation is often used only for nutrient limitation, with a multiplicative formulation for the light limitation factor.

The harmonic mean formulation is based on an electronic analogy of several resistors in series. The rationale for this formulation is that it includes some interaction between multiple limiting nutrients, but it is not as severely limiting as the multiplicative formulation. This approach has been used in only a few models, for example, the original CLEAN (Bloomfield <u>et al</u>., 1973) and CLEANER (Scavia and Park, 1976) models and Nyholm (1978). The current version of MS.CLEANER (Park <u>et al</u>., 1980) has abandoned this formulation in favor of the minimum formulation. In fact, the harmonic mean formulation and minimum formulation produce similar growth response curves under a wide range of conditions (Swartzman and Bentley, 1979).

The rationale for the arithmetic mean formulation is the same as for the harmonic mean formulation (i.e., it considers the effects of multiple nutrient limitation, but is not as severely limiting as the multiplicative formulation). However, this formulation (e.g., Patten, 1975; Patten <u>et al.</u>, 1975) is rarely used since it does not restrict growth enough. For example, the arithmetic mean formulation allows growth even if a critical nutrient such as phosphorus is totally absent, as long as other nutrients are available.

These and other formulations for combining multiple growth limitation factors are reviewed in De Groot (1983).

#### 6.4.3 Light Limitation

Light limitation formulations consist of two components: 1) a relationship describing the attenuation of light with depth and the effect

of algae on light attenuation, and 2) a relationship defining the effect of the resulting light levels on algal growth and photosynthesis.

The attenuation of light with depth is defined in essentially all models by the Beer-Lambert law:

$$I(z) = I_0 e^{-\gamma z}$$
 (6-30)

where I(z) = light intensity at depth z below the surface

- z = depth, length
- I = light intensity at the surface
- $\gamma$  = light extinction coefficient, 1/length

The light intensity at the surface  $I_0$  is a function of location, time of year, time of day, meterological conditions, and shading from topographic features or riparian vegetation. The surface light intensity used in the algal growth formulations corresponds only to the visible range, which is typically about 50 percent of the total surface solar radiation used in the heat budget computations. Almost all radiation outside of the visible range is absorbed within the first meter below the surface (Orlob, 1977). In addition, some models (for example, MS. CLEANER) assume that only a portion of the visible radiation (about 50%) is available for photosynthesis (Park et al., 1980; Strickland, 1958).

Light attenuation in models differs primarily in the way the light extinction coefficient  $\gamma$  is formulated. The simplest approach is to assume a constant value of  $\gamma$ . This approach is reasonable for short term simulations or over periods when turbidity does not change significantly. However, in long term simulations,  $\gamma$  should be computed dynamically to account for seasonal variations in turbidity due to algal shading or variations in suspended solids loads.

The light extinction coefficient is most commonly defined as the linear sum of several extinction coefficients representing each component of light absorption. The components include all suspended particulates

(phytoplankton, zooplankton, organic and inorganic particulates) as well as dissolved organic matter. The general equation is:

$$\gamma = \gamma_0 + \sum_{i=1}^{n} \gamma_i$$
 (6-31)

$$= \gamma_{0} + \sum_{i=1}^{n} a_{i}C_{i}$$
 (6-32)

- where  $\gamma_0$  = base light extinction coefficient for water without particulates or dissolved organic matter, 1/length
  - $Y_i$  = light extinction coefficient corresponding to each component of light absorption i, 1/length
  - n = total number of absorption components considered in the formulation
  - C: = concentration of absorption component i, mass/volume
  - $a_i = coefficient$  for absorption component i relating the concentration  $C_i$  to the light extinction coefficient  $\gamma_i$

Many models include the effects of all components except phytoplankton in the base extinction coefficient  $\gamma_0$  (by assigning a higher value), and then compute the temporal variations in  $\gamma$  as a function of the algal densities only. This assumes phytoplankton blooms are the major cause of turbidity changes. Equation (6-32) then becomes:

$$\gamma = \gamma_0 + a_1 A \tag{6-33}$$

- where  $\gamma_0$  = light extinction coefficient for all absorption components but phytoplankton, 1/length
  - a₁ = coefficient relating the phytoplankton concentration A to the corresponding light extinction coefficient for phytoplankton (also called the self-shading factor), 1/(length-mass/volume)
  - A = phytoplankton concentration, mass/volume

This provides a way of incorporating self-shading effects in the light limitation portion of the algal growth formulation. Some models which use this approach use a nonlinear formulation to describe the relationship between the phytoplankton concentration and the light extinction coefficient. The general expression is:

$$\gamma = \gamma_0 + a_1 A + a_2 A^{b_2}$$
 (6-34)

concentrations to the light extinction coefficient

The second component of the light limitation formulation represents the light limitation factor f(L) in Equations (6-26) through (6-29). f(L) defines the relationship between ambient light levels and algal growth rates or rates of photosynthesis. Essentially all formulations fall into one of two major categories (Figure 6-4): 1) saturation type relationships in which the growth rate increases linearly with light at low intensities, but gradually levels off at high intensities to reach a maximum value at the optimum (or saturating) light intensity, or 2) photoinhibition relationships which are similar to the above curves below the optimum light intensity, but which predict decreases in growth rates above the optimum intensity due to photoinhibition effects.

Saturation type responses are typically described by either a Michaelis-Menten (1913) type relationship (Chen and Orlob, 1975; Jorgensen, 1976; Duke and Masch, 1973; Tetra Tech, 1979; Roesner <u>et al.</u>, 1981; Johanson <u>et al.</u>, 1980; Smith, 1978; WES, 1982):

$$f(L) = \frac{I}{K_{L} + I}$$
 (6-35)

KL = half-saturation constant defining the light level at which growth is one-half the maximum rate

or a Smith (1936) formulation (Park et al., 1980):

$$f(L) = \frac{a_1 I}{\sqrt{1 + (a_1 I)^2}}$$
(6-36)

where  $a_1 = \text{constant}$  in the Smith formulation  $(1/a_1 \text{ is the slope of the}$ linear portion of the photosynthesis vs. light curve), 1/light



#### LIGHT INTENSITY

Figure 6-4. Comparison of light response curves for algal growth.

Vollenweider (1965) modified the Smith formulation to give a more general relationship of which the Smith equation is a special case. The Vollenweider form includes photoinhibition effects, and is expressed as:

$$f(L) = \left(\frac{a_{1}I}{\sqrt{1 + (a_{1}I)^{2}}}\right) \left(\frac{1}{\sqrt{(1 + (a_{2}I)^{2})^{n}}}\right)$$
(6-37)

where a₂ = photoinhibition factor, 1/light
 n = exponent

Baca and Arnett (1976) use this formulation in AQUA-IV with the exponent n equal to 1.

The most commonly used photoinhibition relationship is the Steele (1965) formulation:

$$f(L) = \frac{I}{I_s} e^{\left(1 - \frac{I}{I_s}\right)}$$
(6-38)

where  $I_s$  = optimum (saturating) light intensity

This formulation is used in many models including Di Toro <u>et al</u>. (1971, 1977), Di Toro and Matystik (1980), Di Toro and Connolly (1980), Thomann <u>et al</u>. (1975, 1979), Thomann and Fitzpatrick (1982), O'Connor <u>et al</u>. (1981), Bloomfield <u>et al</u>. (1973), Park <u>et al</u>. (1974, 1975, 1979, 1980), Scavia <u>et al</u>. (1976), Najarian and Harleman (1975), Bierman <u>et al</u>. (1980), Canale <u>et al</u>. (1975, 1976), Lehman <u>et al</u>. (1975), and Baca <u>et al</u>. (1973).

Park <u>et al</u>. (1980) use the Steele formulation above the saturating light intensity  $I_s$  and the Smith formulation below  $I_s$ . They feel that the Steele formulation is not accurate below the inhibition threshold since the predicted photosynthesis response is partially dependent on the response above the threshold (Park <u>et al.</u>, 1979). Under non-inhibiting light conditions, this may result in a light limitation factor which is too low (Groden, 1977).

Walker (1975) found that the Steele formulation underpredicts photosynthesis rates at high light intensities (above saturation) for some algae, so he modified it by adding an additional parameter n:

$$f(L) = \left(\frac{I}{I_s}\right)^n e^{\left[1 - \left(\frac{I}{I_s}\right)^n\right]}$$
(6-39)

where n = parameter for modified Steele formulation

This parameter adjusts the rate of decline of the photosynthesis vs. light curve for light intensities above and below the optimum. The original Steele formulation assumes n=1, while Walker used n values of 0.67, 0.80, and 1.0 for three different algal groups.

A few models include light adaptation algorithms in their light limitation formulations to account for the fact that algae adapted to low light levels have a more rapid response to changing light conditions (steeper slope of photosynthesis vs. light curve) than algae adapted to high light levels. Algae adapt to changing light conditions by varying the chlorophyll content of their cells, with algae adapted to lower light intensities having more chlorophyll.

Nyholm (1978) simulates this effect by varying the value of the saturating light intensity at different times of the year to shift the peak of the light limitation function f(L). The I_s values are maximum during summer and minimum during winter. This shifts the slope of the light response curve so it is steepest during the winter when the algae are adapted to low light levels.

Groden (1977) developed a more complicated formulation for the MS.CLEANER model which dynamically computes the slope of the photosynthesis

vs. light curve as a function of light intensity, and then uses this information to compute the saturating light intensity as a function of both light and temperature. The equation for the slope of the photosynthesis vs. light curve in the light inhibited range is:

$$a = K_1 \ln(I) - K_2$$
 (6-40)

where a = slope of photosynthesis vs. light curve  $K_1, K_2$  = constants

This is based on the assumptions that 1) the slope *a* is a linear function of the chlorophyll content of the cells and 2) chlorophyll decreases exponentially with light intensity until it reaches some minimum value (Groden, 1977). The values of  $K_1$  and  $K_2$  used in MS.CLEANER are 0.1088 and 0.0704, respectively (Groden, 1977; Park <u>et al.</u>, 1980). The equation for the saturating light intensity is:

$$I_{s} = \frac{\mu_{max}(T_{ref}) f(T) e}{a}$$
(6-41)  
=  $\frac{\mu_{max}(T_{ref}) f(T) e}{K_{1} \ln(I) - K_{2}}$ 

Smith (1980) developed a formulation for computing the saturating light intensity as a function of the maximum photosynthetic quantum yield, maximum growth rate, temperature, light extinction coefficient per unit chlorophyll, and the carbon to chlorophyll ratio of the algae. The equation is:

$$I_{s} = \frac{\mu_{\max}(T_{ref}) f(T) C_{r} e}{\phi_{\max} a_{c}}$$
(6-42)

where  $C_r$  = carbon to chlorophyll ratio  $\phi_{max}$  = maximum photosynthetic quantum yield, moles carbon fixed/mole photons absorbed

The effects of light adaptation are included in the carbon to chlorophyll ratio  $C_r$ . This ratio typically ranges from 20 to 100, with 20 corresponding to low-light, high-temperature conditions, and 100 corresponding to high-light, low-temperature conditions (Smith, 1980; Eppley, 1972). Based on observations that the maximum photosynthesis rate typically occurs at the depth where the light intensity is about 30 percent of the surface value ( $I_s = 0.3 I_o$ ), Smith (1980) suggested the following relationship for estimating  $C_r$  as a function of the ambient light levels:

$$C_{r} = \frac{0.3 \overline{I}_{o} \phi_{max} a_{c}}{\mu_{max}(T_{ref}) f(T) e}$$

$$= \frac{0.11 \overline{I}_{o} \phi_{max} a_{c}}{\mu_{max}(T_{ref}) f(T)}$$
(6-43)

where  $\overline{I}_{0}$  = daily average light intensity at the surface

These formulations are used by Thomann and Fitzpatrick (1982) in the Potomac Estuary version of WASP. One advantage of this approach is that I_s and C_r are defined in terms of parameters which are well documented in the literature ( $\phi_{max}$ ,  $\mu_{max}$ ,  $a_c$ ), and which have a fairly narrow range of values over a wide range of environmental conditions.

All of the above relationships for the light limitation factor f(L) have been used to fit experimental measurements of the effects of light on photosynthesis under laboratory conditions. However, in water quality models, these expressions are generally integrated over the depth of each model segment or layer since light varies with depth due to attenuation. The light attenuation formulations (Equations (6-30) through (6-34)) are substituted for the light intensity I in the light limitation formulations (Equations (6-35) through (6-39)), and the light limitation functions are integrated and depth averaged.

Since light also varies continuously with time, most models integrate the light limitation function f(L) over 24 hours to get a daily average value for a given time of the year and set of meteorological conditions. This is generally approximated by multiplying the light limitation function by the photoperiod (expressed as the fraction of the day in which the sun is out) and by using the average light intensity during the daylight hours as  $I_0$  in the formulation. This approach is used in steady-state models and dynamic models which use daily time steps. The alternative approach when short time steps (minutes to hours) are used is to compute the light limitation and algal growth formulations dynamically throughout the day using instantaneous values of  $I_0$ . The latter method simulates the diurnal variations in algal photosynthesis.

The depth and time integrated Michaelis-Menten formulation for light limitation (Equation (6-35)) is expressed as:

$$f(L) = \frac{f_p}{\gamma d} \ln \left( \frac{\kappa_L + I_o}{\kappa_L + I_o e^{-\gamma d}} \right)$$
(6-44)

where f_p = photoperiod (expressed as a fraction of the day)
d = water depth, length
I₀ = average light intensity at the surface during the daylight
hours

when averaged over the whole water depth or as:

$$f(L) = \frac{f_{p}}{\gamma (z_{2} - z_{1})} \ln \left( \frac{K_{L} + I_{0}e^{-\gamma z_{1}}}{K_{L} + I_{0}e^{-\gamma z_{2}}} \right)$$
(6-45)

where  $z_1$  = depth at top of layer, length  $z_2$  = depth at bottom of layer, length

when averaged over a single layer (for example, in a vertically segmented lake model).

The analogous expressions for the Smith formulation (Equation (6-36)) are:

$$f(L) = \frac{f_{p}}{\gamma d} \ln \left[ \frac{a_{1}I_{0} + \sqrt{1 + (a_{1}I_{0})^{2}}}{a_{1}I_{0}e^{-\gamma d} + \sqrt{1 + (a_{1}I_{0}e^{-\gamma d})^{2}}} \right]$$
(6-46)

 $f(L) = \frac{f_p}{\gamma (z_2 - z_1)} \ln \left[ \frac{a_1 I_0 e^{-\gamma z_1} + \sqrt{1 + (a_1 I_0 e^{-\gamma z_1})^2}}{a_1 I_0 e^{-\gamma z_2} + \sqrt{1 + (a_1 I_0 e^{-\gamma z_2})^2}} \right] (6-47)$ 

and

For the Steele formulation (Equation (6-38)), the depth and time integrated expressions are:

$$f(L) = \frac{2.718 f_p}{\gamma d} \begin{pmatrix} -\frac{I_0}{I_s} e^{-\gamma d} & -\frac{I_0}{I_s} \\ e & -e \end{pmatrix}$$
(6-48)

$$f(L) = \frac{2.718 f_p}{\gamma (z_2 - z_1)} \begin{pmatrix} -\frac{I_0}{I_s} e^{-\gamma z_2} & -\frac{I_0}{I_s} e^{-\gamma z_1} \\ e^{-\gamma z_2} & -e^{-\gamma z_1} \end{pmatrix}$$
(6-49)

and

Light limitation factors are compared for several models in Table 6-7. Saturating light intensities and half-saturation constants for light limitation are presented in Tables 6-8 and 6-9.

#### 6.4.4 Nutrient Limitation

Two major approaches have been used to compute nutrient limitation factors in algal models. The first approach is based on Monod (1949) or Michaelis-Menten (1913) kinetics and assumes that the growth rates are determined by the external concentrations of available nutrients. External here refers to the nutrient concentrations in the water column as opposed to the internal concentrations in the algal cells. This approach assumes the nutrient composition of the algal cells remains constant, and is generally referred to as fixed stoichiometry models.

		Light	Limitation	Formulation		
Model (Author)	Steele	Smith	Michaelis- Menten	Vollenweide	er Other	Reference
AQUA-IV				Х		Baca & Arnett (1976)
CE-QUAL-R1			Х			WES (EWQOS) (1982)
CLEAN	Х					Bloomfield <u>et al</u> . (1973)
CLEANER	Х					Scavia & Park (1976)
MS.CLEANER	Χ*	Χ*				Park <u>et</u> <u>al</u> . (1980)
DEM			X			Feigner & Harris (1970)
DOSAG3			X			Duke & Masch (1973)
EAM			X			Tetra Tech (1979, 1980)
ESTEC0			X			Brandes & Masch (1977)
EXPLORE-1	Х					Baca <u>et al</u> . (1973)
HSPF			X			Johanson <u>et al</u> . (1980)
LAKECO			Х			Chen & Orlob (1975)
MIT Network	Х					Harleman <u>et al</u> . (1977)
QUAL-II			Х			Roesner <u>et al</u> . (1981)
RECEIV-II	Х					Raytheon (1974)
SSAM IV					none	Grenney & Kraszewski (1981)
WASP	Х					Di Toro <u>et al</u> . (1981)
WQRRS			Х			Smith (1978)
Bierman	Х					Bierman <u>et al</u> . (1980)
Canale	Х					Canale <u>et al</u> . (1975, 1976)
Jorgensen			Х			Jorgensen (1976)
Lehman	Х					Lehman <u>et al</u> . (1975)
Nyholm				s	piecewise linear aturation	Nyholm (1978)
Scavia	X					Scavia <u>et al</u> . (1976)

# TABLE 6-7. COMPARISON OF LIGHT LIMITATION FORMULATIONS

*Smith formulation used below light saturation, Steele formulation used above light saturation.

Algal Type	Saturating Light Intensity (langleys/day)	References
Total Phytoplankton	300 350	Thomann <u>et al</u> . (1975, 1979) Salas & Thomann (1978) Di Toro <u>et al</u> . (1971) Di Toro & Connolly (1980) Di Toro & Matystik (1980) O'Connor <u>et al</u> . (1975)
	250 350	Scavia <u>et al</u> . (1976) Scavia & Park (1976) Scavia (1980)
	200 300	Youngberg (1977)
	216	Desormeau (1978)
	288	Larsen <u>et</u> <u>al</u> . (1973)
Diatomś	225	Thomann <u>et al</u> . (1979) Di Toro & Connolly (1980)
	300	Scavia <u>et a</u> l. (1976) Scavia (1980)
	88 - 100	Bierman (1976) Bierman <u>et al</u> . (1980)
	225	Canale <u>et al</u> . (1976)
	144	Lehman <u>et</u> <u>al</u> . (1975)
Green Algae	88 100	Bierman (1976) Bierman <u>et al</u> . (1980)
	160	Canale <u>et</u> <u>al</u> . (1976)
	65	Lehman <u>et al</u> . (1975)
Blue-green Algae	44 50	Bierman (1976) Bierman <u>et al</u> . (1980)
	43	Lehman <u>et al</u> . (1975)
	600	Canale <u>et</u> <u>al</u> . (1976)
	300 350	Youngberg (1977)
	250	Scavia (1980)
Flagellates	288	Lehman <u>et al</u> . (1975)
	100	Bierman <u>et</u> <u>al</u> . (1980)
Chrysophytes	86	Lehman <u>et al</u> . (1975)

## TABLE 6-8. ALGAL SATURATING LIGHT INTENSITIES

На	If-Saturation	Constant	
Algal Type	(Kcal/m ² /s	sec)	References
Total Phytoplankton	0.002 - 0	0.006	Chen (1970) Chen & Orlob (1975) Chen & Wells (1975, 1976) U.S. Army Corps of Engineers (1974) Tetra Tech (1976)
	0.004	46	Jorgensen (1976) Jorgensen <u>et a</u> l. (1978)
	0.002 - 0	0.006*	Smith (1978)
	0.00	5*	Roesner <u>et al</u> . (1980) Duke & Masch (1973)
	0.003	0.005*	Brandes (1976)
	0.004	0.006**	Jorgensen (1979)
	0.004	4**	Collins & Wlosinski (1983)
Díatoms	0.00	3	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	0.00	2*	Tetra Tech (1979)
	0.00005	0.0012**	Jorgensen (1979)
	0.00005	0.0026**	Collins & Wlosinski (1983)
Green Algae	0.002 -	0.004	Tetra Tech (1980) Bowie <u>et</u> <u>al</u> . (1980) Porcella <u>et al</u> . (1983)
	0.00	2*	Tetra Tech (1979)
	0.0003 0	.0011**	Jorgensen (1979)
	0.0003 - 0	.0106**	Collins & Wlosinski (1983)
Blue-green Algae	0.002 -	0.004	Tetra Tech (1980) Bowie <u>et</u> al.(1980) Porcella <u>et</u> al. (1983)
	0.00	2*	Tetra Tech (1979)
Dinoflagellates	0.00	2*	Tetra Tech (1979)
	0.0043 - 0	.0053**	Collins & Wlosinski (1983)

## TABLE 6-9. HALF-SATURATION CONSTANTS FOR LIGHT LIMITATION

(continued)

Algal Type	Half-Satura (Kcal/	ation Constant 'm ² /sec)	References
Flagellates	0.002	0.004	Tetra Tech (1980) Porcella <u>et al</u> . (1983)
	0.00	)44**	Collins & Wlosinski (1983)
Chrysophytes	0.0	)02*	Tetra Tech (1979)
	0.0014	0.0017**	Coļlins & Wlosinski (1983)
Coccolithophores	0.0003	0.0016**	Collins & Wlosinski (1983)
Benthic Algae	0.01	0.005	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> (1983)
	0.002	0.006*	Smith (1978)

*Model documentation values.

**Literature values.

The second approach assumes that algal growth is a two-step process, the first step being nutrient uptake and the second step being cell growth or division. Cell growth depends on the internal concentrations of nutrients within the cells, rather than external concentrations in the water. The uptake rates are dependent on both the external and internal concentrations. Since uptake and growth are modeled separately, the nutrient composition of the cell may change with time, resulting in variable stoichiometry or internal pool models. These models simulate processes such as luxury uptake of nutrients which allows growth even when external nutrients are depleted.

## 6.4.4.1 Nutrient Limitation in Fixed Stoichiometry Models

The majority of water quality models are of the fixed stoichiometry type. These models are generally based on conventional Monod or Michaelis-Menten kinetics. The algal growth equation for a single limiting nutrient under conditions of optimum temperature and light can be expressed as:

$$\mu = \mu_{\max} \left( \frac{s}{K_s + s} \right)$$
(6-50)  
=  $\mu_{\max} f(s)$ 

- where s = concentration of the limiting nutrient in the water, mass/volume
  - K_s = half-saturation constant for the limiting nutrient, mass/volume

The quantity  $f(s) = (\frac{s}{K_s + s})$  is the growth limitation factor for the nutrient s. The half-saturation constant refers to the concentration of the nutrient at which the growth rate is one half of its maximum value. The above equation results in a hyperbolic growth curve (Figure 6-5) in which growth increases approximately linearly with nutrients at very low nutrient concentrations, but gradually levels off to a maximum growth rate at high nutrient levels (growth saturation). At this point, the nutrient is no longer limiting, so further increases in the external nutrient supply do not affect growth.

Fixed stoichiometry models typically compute a separate growth limitation factor f(s) for each nutrient modeled, and then combine the factors using any one of the four methods discussed above in Equations (6-26) to (6-29) (i.e., multiplicative formulation, minimum formulation, harmonic mean formulation, or arithmetic mean formulation). The specific nutrient limitation factors are:

$$f(P) = \frac{PO_4}{K_P + PO_4}$$
(6-51)

$$f(N) = \frac{(NH_3 + NO_3)}{K_N + (NH_3 + NO_3)}$$
(6-52)

$$f(C) = \frac{CO_2}{K_C + CO_2}$$
(6-53)

$$f(Si) = \frac{Si}{K_{Si} + Si}$$
(6-54)



NUTRIENT CONCENTRATION

Figure 6-5. Michaelis-Menten saturation kinetics for algal growth limitation by a single nutrient.

The number of growth limiting factors included in a given model depends on both the particular algal species present and the chemistry of the water body under consideration. For example, silicon limitation is only appropriate for diatoms. Nitrogen limitation can generally be omitted for nitrogen-fixing blue-green algae (although nitrogen kinetics for blue-greens must still be included to correctly describe the nitrogen cycle). Carbon limitation is frequently excluded from algal models since carbon is often assumed to be available in excess and is therefore not modeled as a state variable. Lake models often assume phosphorus is the only limiting nutrient, while estuary models often assume nitrogen is limiting at all times.

The way in which nitrogen limitation is computed also varies from model to model. For example, some models simulate available nitrogen as a single constituent (Bierman <u>et al.</u>, 1980; Jorgensen <u>et al.</u>, 1978; Nyholm, 1978; Thomann <u>et al.</u>, 1979), while other models simulate ammonia, nitrite, and nitrate separately and assume both ammonia and nitrate are available for algal growth (Chen and Orlob, 1975; Baca and Arnett, 1976; Baca <u>et al.</u>, 1973; Smith, 1978; Najarian and Harleman, 1975; Duke and Masch, 1973). QUAL-II simulates the various forms of nitrogen, but assumes algal growth is only limited by nitrate (Roesner <u>et al.</u>, 1981). Some models include factors to account for ammonia preference by algae in their nutrient uptake formulations (Scavia <u>et al.</u>, 1976; Canale <u>et al.</u>, 1976; Grenney and Kraszewski, 1981; Thomann and Fitzpatrick, 1982; O'Connor <u>et al.</u>, 1981; JRB, 1983). Ammonia preference factors are discussed in Chapter 5.

Values of the Michaelis-Menten half-saturation constants for each limiting nutrient are available from many sources, including both the modeling literature and the experimental literature. However, care must be taken when using this information since the values reported will depend on the particular model formulations used for the modeling literature, and on the experimental conditions for the scientific literature. For example, if a multiplicative formulation is used to compute algal growth (Equation(6-26)), the half-saturation constants should be smaller than the corresponding constants where a minimum formulation is used (Equation (6-26)).

(6-27)). In general, the more limiting nutrients that are considered with a multiplicative formulation, the smaller the value of each half-saturation constant. This is necessary in order to get the same growth response with both formulations when more than one nutrient is limiting simultaneously. This is true of both the modeling literature and the experimental literature. When the harmonic mean formulation is used (Equation (6-28)), the half-saturation constants should generally be somewhere between the values of the minimum and multiplicative formulations. Half-saturation constants for each limiting nutrient are tabulated in Table 6-10.

Table 6-11 compares the algal growth formulations used in several models, including the growth limiting factors used, the specific formulations for nutrient limitation, and the methods for combining multiple limiting factors.

#### 6.4.4.2 Nutrient Limitation In Variable Stoichiometry Models

Variable stoichiometry models assume that the growth limiting factor for nutrients, f(P,N,C,Si) in Equation (6-4), is a function of the internal levels of the nutrients in the algal cells rather than the external concentrations in the water column. The internal concentrations are generally defined as:

where q = internal nutrient concentration, mass nutrient/biomass algae

Internal nutrient levels depend on the relative magnitudes of the nutrient uptake rates and the algal growth rates. The uptake rates are functions of both the internal and external nutrient concentrations, while the growth rates depend primarily on the internal concentrations.

Variable stoichiometry models differ in 1) the specific process formulations used to simulate uptake and growth, 2) the number of nutrients considered, and 3) the ways in which multiple limiting factors are combined.

		Half-Saturatio	on Constant		
Algal Type	Nitrogen (mg/l)	Phosphorus (mg/l)	Carbon (mg/l)	Silicon (mg/l)	References
Total Phytoplankton	0.025	0.0005 0.03			0'Connor <u>et al</u> . (1975, 1985) Thomann <u>et al</u> . (1974, 1975, 1979) Thomann & Fitzpatrick (1982) Di Toro & Matystik (1980) Di Toro & Connolly (1980) Di Toro <u>et al</u> . (1971, 1977) Salas & Thomann (1978) Salisbury <u>et al</u> . (1983)
	0.01 0.4	0.004 0.08	0.03 0.8		Chen (1970) Chen & Orlob (1975) Chen & Wells (1975, 1976) U.S. Army Corps of Engineers (1974) Tetra Tech (1976)
	0.2	0.02 0.03	0.5		Jorgensen (1976) Jorgensen <u>et al</u> . (1978)
	0.025	0.006 0.025			Battelle (1974)
	0.06 0.08	0.02			Grenney & Kraszewski (1981)
	0.015	0.0025			Canale <u>et al</u> . (1976)
	0.014	0.001			Larsen <u>et al</u> . (1973)
	0.025 0.3*	0.006 0.03*			Baca & Arnett (1976)
	0.04 0.10*	0.02 0.05*	0.02 0.04*		Smith (1978)
	0.2 0.4*	0.03 0.05*			Roesner <u>et al</u> . (1980) Duke & Masch (1973)
	0.015 0.3*	0.0025 0.08*			Grenney & Kraszewski (1981)
	0.10 0.4*	0.03 0.05*	0.15*		Brandes (1976)
	0.0014 0.018	0.006**			Di Toro <u>et al</u> . (1971)
	0.025 0.2**	0.002 0.08**			Jorgensen (1979)
	0.0015 0.15*	*			0'Connor <u>et al</u> . (1981)
		0.02 0.075**			Collins & Wlosinski (1983)
Diatoms	0.015 0.03	0.002	0.03	0.08	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
	0.025	0.001 0.002		0.030 0.1	Thomann <u>et a</u> l. (1979) Di Toro & Connolly (1980) Salisbury <u>et</u> <u>al</u> . (1983)
	0.025 0.030	0.004 0.009		0.03	Scavia et al. (1976) Scavia (1980)
	0.015	0.0025		0.03	Canale <u>et</u> <u>al</u> . (1976)
				0.1	Bierman (1976)
	0.015*	0.03*	0.03*	0.08*	Tetra Tech (1979)
	0.0063 0.12**	0.01 0.025**			Di Toro <u>et al</u> . (1971)
		0.025**			Jorgensen (1979)
	0.003 0.923**	0.001 0.163**			Collins & Wlosinski (1983)

Algal Type         Mitrogen (mg/l)         Phosphorus (mg/l)         Carbon (mg/l)         Silicon (mg/l)         References           Green Algae         0.03         0.035         0.004         0.03         Tetra Tech (1980) Bowle et al. (1980) Di Toro et al. (1970)           0.15         0.01         0.15         0.01         Di Toro et al. (1976) Scavia Staria et al. (1976)           0.03         0.035         0.034         Scavia et al. (1976) Scavia (1980)         Scavia et al. (1976)           0.05         0.15         0.0025         Canale et al. (1980)         Scavia et al. (1976)           0.05         0.15**         0.01**         Jorgensen (1979)         Scavia et al. (1980)           0.066         1.236**         0.062         0.475**         0.068 - 1.5**         Collins & Wosinski (           8lue-green Algae         0.         0.010 - 0.02         0.03         Tetra Tech (1980)         Sovia et al. (1980)           0.001         0.01         0.015         Scavia et al. (1980)         Sovia et al. (1980)           0.002         0.475**         0.068 - 1.5**         Collins & Wosinski (           0.001         0.015         Scavia (1980)         Sovia et al. (1980)           0.002         0.03*         Tetra Tech (1970)         Scavia (1980)      <			Half-Saturation C	onstant		
Arigat Type         (Mg/T)         (M		Nitrogen (mg(l)	Phosphorus	Carbon (ma(1))	Silicon	Deferences
Green Algae         0.03         0.03         0.04         0.03         Tetra Tech (1980) Bowle et al. (1970) Servia & Park (1976)           0.15         0.01         01 Toro et al. (1971)         Servia & Park (1976)         Servia & Park (1976)           0.01         0.035         0.005         0.025         Ganale et al. (1970)           0.03*         0.03*         0.03*         0.03*         Ganale et al. (1976)           0.03*         0.03*         0.03*         Ganale et al. (1976)         Servia & Park (1976)           0.05         0.15**         0.01**         Jorgensen (1979)         Jorgensen (1979)           0.006         1.236**         0.002         0.475**         0.068 - 1.5**         Collins & Wlosinski (1980)           8lue-green Algae         0.         0.010-0.02         0.03         Tetra Tech (1980)         Servia & Park (1976)           0.001         0.01         0.01         0.01         Di Toro et al. (1976)         Servia & Park (1976)           0.001         0.01         0.01         0.01         Di Toro et al. (1979)         Servia & Park (1976)           0.002         0.003         0.004*         0.034         Tetra Tech (1979)         Servia & Park (1976)           0.005         0.005         0.005*         0.00		(mg/ 1)	(mg/1)	(iiig/ t )	·····	
0.15         0.01         Di Toro et al. (1970)           0.001         0.035         0.005         0.024         Scavia t al. (1976)           0.15         0.0025         Canale et al. (1976)         Scavia (1980)           0.03*         0.03*         0.03*         0.03*           0.005         0.15*         0.01**         Jorgensen (1979)           0.005         0.15**         0.01**         Jorgensen (1979)           0.006         1.26**         0.002         0.475**         0.068 - 1.5**           81we-green Algae         0.         0.010 - 0.02         0.03         Tetra Tech (1970)           0.001         0.01         0.015         Scavia (1980)         Borie et al. (1976)           0.001         0.01         0.015         Scavia (1980)         Borie et al. (1976)           0.001         0.01         0.015         Scavia (1980)         Porcella et al. (1976)           0.01         0.015         0.0025         Canale et al. (1976)         Scavia (1980)           0.015         0.0025         Canale et al. (1971)         O.064*         0.031         0.088**           Dinoflagellates         0.005         0.006*         0.031         0.088**         Collins & Wlosinski (011111)	Green Algae	0.03 0.035	0.004	0.03		Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
0.001         0.035         0.005         0.024         Scavia et al. (1976) Scavia (1976)           0.15         0.0025         Canale et al. (1976)           0.03*         0.03*         0.03*           0.005         0.15**         0.01**           0.005         0.15**         0.01**           0.005         0.15**         0.01**           0.005         0.15**         0.002           0.005         0.15**         0.002           0.005         0.15**         0.002           0.006         1.236**         0.002         0.475**           0.001         0.010-         0.02         0.03           Blue-green Algae         0.         0.010-         0.02           0.001         0.01         0.015         Scavia & Park (1976)           0.001         0.01         0.015         Scavia & Park (1976)           0.015         0.0025         Canale et al. (1971)           0.016         0.0025         Canale et al. (1971)           0.017         0.14*         0.006**         0.03*           Dinoflagellates         0.005         0.03*         O'Connor et al. (1971)           0.019         0.589**         Collins & Wosinski (Collins & W		0.15	0.01			Di Toro <u>et</u> <u>al</u> . (1971)
0.15         0.0025         Canale et al. (4976)           0.03*         0.03*         0.03*         0.03*           0.005         0.15**         0.01**         Jorgensen (1979)           0.006         1.236**         0.002         0.475**         0.068 - 1.5**         Collins & Wlosinski (           Blue-green Algae         0.         0.010 - 0.02         0.03         Tetra Tech (1980) Bowle et al. (1980) Porcetla et al. (1980)           0.001         0.010 - 0.02         0.03         Scavia & Park (1976)           0.001         0.01         0.01         Di Toro et al. (1971)           0.015         0.0025         Canale et al. (1976)           0.01         0.015         0.028*         Collins & Wlosinski (           0.015         0.006*         0.03*         Tetra Tech (1979)           0.062         4.34**         0.006**         0.03*         Tetra Tech (1979)           0.062         0.03*         0'Connor et al. (1971)         0.019         0.589**           Dinoflagellates         0.005         0.03*         O'Connor et al. (1971)           0.019         0.589**         Collins & Wlosinski (         Collins & Wlosinski (           Flagellates         0.08         0.012         0.03*         Tet		0.001 0.035	0.005 0.024			Scavia <u>et a</u> l. (1976) Scavia & Park (1976) Scavia (1980)
$\begin{array}{c c c c c c c c c c c c c c c c c c c $		0.15	0.0025			Canale <u>et</u> <u>al</u> . (1976)
0.005         0.15**         0.01**         Jorgensen (1979)           0.006         1.236**         0.002         0.475**         0.068 - 1.5**         Collins & Wlosinski (           Blue-green Algae         0.         0.010 - 0.02         0.03         Tetra Tech (1990) Bowie et al. (1990) Porcella et al. (1990)           0.001         0.01         0.015         Scavia & Park (1976)           0.01         0.015         0.0025         Canale et al. (1976)           0.015         0.0025         Canale et al. (1976)           0.062         4.34**         0.006**         0.031         O'Connor et al. (1979)           0.062         4.34**         0.006**         0.031         O'Connor et al. (1979)           0.062         0.34**         0.005         O'Connor et al. (1971)           0.007         0.13**         O'Connor et al. (1971)           0.019         0.589**         Collins & Wlosinski (1972)           0.008         0.012         0.03         Tetra Tech (1979)           0.001         0.052**         Collins & Wlosinski (1972)           0.008         0.012         0.03         Tetra Tech (1979)           0.008         0.012         0.03         Tetra Tech (1979)           0.008         0.		0.03*	0.03*	0.03*		Tetra Tech (1979)
0.006         1.236**         0.002         0.475**         0.068 - 1.5**         Collins & Wlosinski (           Blue-green Algae         0.         0.0100.02         0.03         Tetra Tech (1990) Porcella et al. (1990) Porcella et al. (1990)           0.001         0.01         0.015         Scavia (1990)           0.015         0.0025         Canale et al. (1976)           0.015         0.005*         Canale et al. (1976)           0.0162         4.34**         0.006**         0.03*           Dinoflagellates         0.005         Collins & Wlosinski (           0.007         0.13**         O'Connor et al. (1979)           0.019         0.589**         O.03*         Tetra Tech (1979)           0.019         0.589**         O.03*         O'Connor et al. (1971)           0.019         0.589**         O.03*         Tetra Tech (1979)           0.019         0.589**         Collins & Wlosinski (           Flagellates         0.08         0.012         0.03           Porcella et al. (1979)         Oolins & Wlosinski (         Dorgensen (1979)           0.001         0.052**         Collins & Wlosinski (         Collins & Wlosinski (           Chrysophytes         0.015         0.02*         0.03*		0.005 0.15**	0.01**			Jorgensen (1979)
Blue-green Algae         0.         0.0100.02         0.03         Tetra Tech (1980) Porcella et al. (1980)           0.001         0.01         0.015         Scavia & Park (1976)         Scavia (1980)         Scavia (1971)         Scavia (1972)         Scavia (1972) <td< td=""><td></td><td>0.006 1.236**</td><td>0.002 0.475** (</td><td>0.068 - 1.5**</td><td></td><td>Collins &amp; Wlosinski (1983)</td></td<>		0.006 1.236**	0.002 0.475** (	0.068 - 1.5**		Collins & Wlosinski (1983)
0.001         0.01         0.015         Scavia & Park (1976)           0.01         0.01         0.015         Scavia (1980)           0.015         0.0025         Canale et al. (1971)           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.062         4.34**         0.006**         0.03*           0.064         0.03*         Tetra Tech (1979)           0.08*         0.06*         0.03*           0.019         0.589**         Collins & Wlosinski (1974)           0.019         0.589**         Collins & Wlosinski (1974)           0.001         0.052**         Collins & Wlosinski (1979)           0.001         0.052**         Collins & Wlosinski (1979)           0.006**         0.03*         Tetra Tech (1979)           0.006**         0.03*<	Blue-green Algae	0.	0.010 0.02	0.03		Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
0.01       Di Toro et al. (1971)         0.015       0.0025         0.*       0.06*         0.062       4.34**         0.006*       0.031         0.062       4.34**         0.006*       0.031         0.062       0.06*         0.06*       0.031         0.06*       0.031         0.08*       0.06*         0.08*       0.06*         0.09*       0.06*         0.007       0.13**         0.019       0.589**         0.008       0.012         0.008       0.012         0.001       0.052**         Collins & Wlosinski (         Chrysophytes       0.015         0.006*       0.03*         Collins & Wlosinski (         Coccolithophores       0.006		0.001	0.01 0.015			Scavia & Park (1976) Scavia (1980)
0.015       0.0025       Canale et al. (1976)         0.*       0.06*       0.03*       Tetra Tech (1979)         0.062       4.34**       0.006**       0.031       0.088**         Dinoflagellates       0.005       0.06*       0.03*       O'Connor et al. (1981)         0.08*       0.06*       0.03*       Tetra Tech (1979)       0'Connor et al. (1971)         0.007       0.13**       Di Toro et al. (1971)       0.019       0.589**         0.019       0.589**       Collins & Wlosinski (1971)         0.0084       0.012       0.03       Tetra Tech (1980)         Porcella et al.       (1981)       0.0084       0.13**         0.001       0.052**       Collins & Wlosinski (1982)         Chrysophytes       0.015       0.02*       0.03*         Chrysophytes       0.015       0.02*       0.03*         Coccolithophores       0.006 0.019**       Collins & Wlosinski (1972)			0.01			Di Toro <u>et al</u> . (1971)
0.*         0.06*         0.03*         Tetra Tech (1979)           0.062         4.34**         0.006**         0.031         0.088**         Collins & Wlosinski (           Dinoflagellates         0.005         0'Connor et al. (1981)         0'Connor et al. (1981)           0.08*         0.06*         0.03*         Tetra Tech (1979)         0'Connor et al. (1981)           0.09         0.13**         Di Toro et al. (1971)         0.019         0.589**         Collins & Wlosinski (           Flagellates         0.08         0.012         0.03         Tetra Tech (1980)         Porcella et al. (1983)           0.0084         0.13**         Jorgensen (1979)         Jorgensen (1979)         Ocollins & Wlosinski (           Chrysophytes         0.015         0.02*         0.03*         Tetra Tech (1979)           0.006**         0.047         0.076**         Collins & Wlosinski (		0.015	0.0025			Canale <u>et al</u> . (1976)
0.062       4.34**       0.006**       0.031       0.088**       Collins & Wlosinski (         Dinoflagellates       0.005       0'Connor et al. (1980)       0'Connor et al. (1971)         0.007       0.13**       Di Toro et al. (1971)         0.019       0.589**       Collins & Wlosinski (         Flagellates       0.08       0.012       0.03         Flagellates       0.084       0.13**       Jorgensen (1979)         0.001       0.052**       Collins & Wlosinski (         Chrysophytes       0.015       0.02*       0.03*         Coccolithophores       0.006 0.019**       Collins & Wlosinski (		0.*	0.06*	0.03*		Tetra Tech (1979)
Dinoflagellates         0.005         0'Connor et al. (198)           0.08*         0.06*         0.03*         Tetra Tech (1979)           0.007         0.13**         Di Toro et al. (1971)           0.019         0.589**         Collins & Wlosinski (1972)           Flagellates         0.08         0.012         0.03           Flagellates         0.084         0.13**         Jorgensen (1979)           0.001         0.052**         Collins & Wlosinski (1972)           Chrysophytes         0.015         0.02*         0.03*           Chrysophytes         0.015         0.02*         0.03*           Coccolithophores         0.006 0.019**         Collins & Wlosinski (1979)		0.062 4.34**	0.006** 0.	.031 0.088**		Collins & Wlosinski (1983)
0.08*       0.06*       0.03*       Tetra Tech (1979)         0.007       0.13**       Di Toro et al. (1971)         0.019       0.589**       Collins & Wlosinski (         Flagellates       0.08       0.012       0.03         Flagellates       0.08       0.012       0.03         Chrysophytes       0.015       0.02*       0.03*         Chrysophytes       0.015       0.02*       0.03*         Coccolithophores       0.006 0.019**       Collins & Wlosinski (	Dinoflagellates	0.005				0'Connor <u>et al</u> . (1981)
0.007       0.13**       Di Toro et al. (1971)         0.019       0.589**       Collins & Wlosinski (1980)         Flagellates       0.08       0.012       0.03         0.0084       0.13**       Jorgensen (1979)         0.001       0.052**       Collins & Wlosinski (1980)         Chrysophytes       0.015       0.02*       0.03*         Chrysophytes       0.015       0.02*       0.03*         Coccolithophores       0.006 0.019**       Collins & Wlosinski (1980)		0.08*	0.06*	0.03*		Tetra Tech (1979)
0.019         0.589**         Collins & Wlosinski (           Flagellates         0.08         0.012         0.03         Tetra Tech (1980) Porcella et al. (1983)           0.0084         0.13**         Jorgensen (1979)         Jorgensen (1979)           0.001         0.052**         Collins & Wlosinski (           Chrysophytes         0.015         0.02*         0.03*           Coccolithophores         0.006 0.019**         Collins & Wlosinski (		0.007 0.13**				Di Toro <u>et al</u> . (1971)
Flagellates         0.08         0.012         0.03         Tetra Tech (1980) Porcella et al. (1980) Dorcella et al. (1980) Dorcella et al. (1980) Dorgensen (1979)           0.0084         0.13**         Jorgensen (1979)         Jorgensen (1979)           0.001         0.052**         Collins & Wlosinski ( 0.006**         Tetra Tech (1979)           Chrysophytes         0.015         0.02*         0.03*           Collins & Wlosinski ( Collins & Wlosinski (		0.019 0.589**				Collins & Wlosinski (1983)
0.0084         0.13**         Jorgensen (1979)           0.001         0.052**         Collins & Wlosinski (           Chrysophytes         0.015         0.02*         0.03*         Tetra Tech (1979)           0.006**         0.047         0.076**         Collins & Wlosinski (           Coccolithophores         0.006         0.019**         Collins & Wlosinski (	Flagellates	0.08	0.012	0.03		Tetra Tech (1980) Porcella <u>et al</u> . (1983)
0.001         0.052**         Collins & Wlosinski (           Chrysophytes         0.015         0.02*         0.03*         Tetra Tech (1979)           0.006**         0.047         0.076**         Collins & Wlosinski (           Coccolithophores         0.006         0.019**         Collins & Wlosinski (		0.0084 0.13**				Jorgensen (1979)
Chrysophytes         0.015         0.02*         0.03*         Tetra Tech (1979)           0.006**         0.047         0.076**         Collins & Wlosinski (1979)           Coccolithophores         0.006         0.019**         Collins & Wlosinski (1979)		0.001 0.052**				Collins & Wlosinski (1983)
0.006**         0.047         0.076**         Collins & Wlosinski           Coccolithophores         0.006         0.019**         Collins & Wlosinski	Chrysophytes	0.015	0.02*	0.03*		Tetra Tech (1979)
Coccolithophores 0.006 0.019** Collins & Wlosinski		0.006**	0.047 0.076**			Collins & Wlosinski (1983)
	Coccolithophores	0.006 0.019**				Collins & Wlosinski (1983)
Benthic Algae 0.05 0.1 0.004 0.008 0.03 0.1 Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983	Benthic Algae	0.05 0.1	0.004 0.008	0.03 0.1		Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)
0.06 0.08 0.02 Grenney & Kraszewski		0.06 0.08	0.02			Grenney & Kraszewski (1981)
0.04 0.10* 0.02 0.05* 0.02 0.04* Smith (1978)		0.04 0.10*	0.02 0.05*	0.02 0.04*		Smith (1978)
0.015 0.3* 0.0025 0.08* Grenney & Kraszewski		0.015 0.3*	0.0025 0.08*			Grenney & Kraszewski (1981)

*Model documentation values.

**Literature values.

	Gro	wth L	imiti	ng Fa	ictors		Stoich	niometry	Nutrient Formu	Limitation lation	Method f	or Combining	Factors	
Model (Author)	Light	P04	NO3	NH3	со ₂	Si	Fixed	Variable	Michaelis- Menten	Other	Multipl- icative	Minimum	Harmonic Mean	Reference
AQUA-IV	х	Х	X	Х			X		X		light	nutrients		Baca & Arnett (1976)
CE-QUAL-R1	x	Х	Х	Х	Х		X		х			Х		WES (EWQOS) (1982)
CLEAN	x	Х	Х	Х	Х		x		х				х	Bloomfield <u>et al</u> . (1973)
CLEANER	х	Х	Х	Х	Х		x		х				х	Scavia & Park (1976)
MS.CLEANER	х	Х	Х	Х	Х	Х	C & Si	N & F	χ*	6-51*		х		Park <u>et</u> <u>al</u> . (1980)
DEM	х	Х	Х				x		х		х			Feigner & Harris (1970)
DOSAG3	x	Х	Х				x		x		х			Duke & Masch (1973)
EAM	x	Х	Х	Х	Х	Х	x		х			Х		Tetra Tech (1979, 1980)
ESTECO	x	Х	Х	Х	Х		x		х		X			Brandes & Masch (1977)
EXPLORE-1	x	Х	Х	Х			x		х		X			Baca <u>et</u> <u>al</u> . (1973)
HSPF	х	Х	Х	Х	Х		х		x			X		Johanson <u>et al</u> . (1980)
LAKECO	x	Х	Х	Х	Х		x		x		х			Chen & Orlob (1975)
MIT Network	х		Х	Х			х		х		light			Harleman <u>et al</u> . (1977)
QUAL-II	x	Х	Х				Х		х		x			Roesner <u>et al</u> . (1981)
RECEIV-II	x	Х	Х	Х			х		х		light	nutrients		Raytheon (1974)
SSAM IV		Х	Х	X			X		х			Х		Grenney & Kraszewski (1981)
WASP	x	X	Х	X		Х	x		x		X			Di Toro <u>et al</u> . (1981)
WQRRS	x	Х	Х	X	Х		x		x			Х		Smith (1978)
Bierman	X	X	Х	Х		Х	Si	N & F	χ**	6-52**	light	nutrients		Bierman <u>et al</u> . (1980)
Canale	X	X	X	Х		Х	X		x		X			Canale <u>et al</u> . (1975, 1976)
Jorgensen	x	Х	X	Х	Х			Х		6-53	X			Jorgensen (1976)
Lehman	X	Х	Х	Х	Х	Х		Х		6-53	х			Lehman <u>et al</u> . (1975)
Nyholm	x	Х	Х	Х				х		6-54, 55	light		nutrients	Nyholm (1978)
Scavia	x	Х	Х	Х		Х	X		x			X		Scavia <u>et al</u> . (1976)
	1						1							

#### TABLE 6-11. COMPARISON OF ALGAL GROWTH FORMULATIONS

*Fixed stoichiometry Michaelis-Menten formulation used for carbon and silicon, with variable stoichiometry formulations for nitrogen and phosphorus. **Fixed stoichiometry Michaelis-Menten formulation used for silicon, with variable stoichiometry formulations for nitrogen and phosphorus. Several different formulations have been used to compute nutrient limitation factors in variable stoichiometry models. As with fixed stoichiometry models, the limitation factors may range from 0 to 1. Most models assume a minimum internal stoichiometric nutrient requirement at which growth is zero. This minimum level is often called the minimum cell quota or subsistence quota. Algal growth (and the nutrient limitation factors) are assumed to increase with increasing internal nutrient levels above the minimum cell quota until the maximum growth rate is attained. Some type of hyperbolic function is typically used to express this saturation type relationship.

The following expressions have been used to determine growth limitation factors in variable stoichiometry models:

$$f(q) = \frac{q}{K_1 + q}$$
 (6-56)

$$f(q) = \frac{(q - q_{min})}{K_2 + (q - q_{min})}$$
(6-57)

$$f(q) = \left(1 - \frac{q_{\min}}{q}\right) = \left(\frac{q - q_{\min}}{q}\right)$$
(6-58)

$$f(q) = \frac{q - q_{\min}}{q_{\max} - q_{\min}}$$
(6-59)

$$f(q) = \left[\frac{(q - q_{min})}{K_3 + (q - q_{min})}\right] \left[\frac{K_3 + (q_{max} - q_{min})}{(q_{max} - q_{min})}\right]$$
(6-60)

where f(q)

= nutrient limitation factor

q

= internal nutrient concentration, mass nutrient/biomass
algae

qmin = minimum internal stoichiometric requirement (cell
quota), mass nutrient/biomass algae

q_{max} = maximum internal nutrient concentration, mass nutrient/biomass algae

Equation (6-56) is equivalent in form to the Michaelis-Menten relationship except that the internal rather than the external nutrient concentration is the independent variable. This equation is used in MS.CLEANER for both nitrogen and phosphorus limitation (Park et al., 1980). Equation (6-57) also has the same form as the Michaelis-Menten relationship, but the independent variable is the internal nutrient concentration in excess of the minimum cell quota. This equation is used by Bierman (1976) and Bierman et al. (1973, 1980) for nitrogen and phosphorus. Equation (6-58) was originally developed by Droop (1968), and it is used in several models including Lehman et al. (1975), Jorgensen (1976), Jorgensen et al. (1978, 1981), and Canale and Auer (1982) for all nutrients simulated in these models. Equation (6-58) can be derived from Equation (6-57) by assuming  $K_2$ = q_{min}, as was demonstrated by Rhee (1973, 1978) for phosphorus and nitrogen (Bierman, 1981). Equations (6-59) and (6-60) are used by Nyholm (1978) for nitrogen and phosphorus, respectively. Note that Equation (6-59) is a linear rather than hyperbolic relationship. Also, Equation (6-60) is similar to Equation (6-57) since the second factor in Equation (6-60) is a constant once  $q_{min}$ ,  $q_{max}$ , and  $K_3$  are defined.

Since variable stoichiometry formulations have not been widely used, data for the model parameters are limited. Values for the various halfsaturation constants are presented in Table 6-12. Note that the halfsaturation constants ( $K_1, K_2$ , and  $K_3$ ) have different values since the corresponding equations are different. Minimum cell quotas and maximum internal nutrient concentrations are tabulated in Tables 6-13 and 6-14.

The ways in which variable stoichiometry formulations are used varies between different models. Some models use variable stoichiometry formulations only for phosphorus and nitrogen, combining them with conventional Michaelis-Menten kinetics for carbon and silica (Park <u>et al</u>., 1980; Bierman <u>et al</u>., 1980). while other models use variable stoichiometry formulations for all nutrients modeled (Lehman <u>et al</u>., 1975; Jorgensen, 1976). In a few cases, different internal nutrient formulations are used for different nutrients in the same model (Nyholm, 1978). In some models,

	- Half-Sa	turation Constant		
Nutrient	Туре	Value	Algal Type	Reference
Phosphorus	κ ₁	0.005 g/m ³	Total Phytoplankton	Desormeau (1978)
	к ₂	0.724x10 ⁻⁷ µmole/cell 0.0005 mg/mg (D.W.)	Diatoms	Bierman <u>et al</u> . (1980)
		0.312x10 ⁻⁸ µmole/cell 0.0005 mg/mg (D.₩.)	Green Algae	
		0.148×10 ⁻⁷ µmole/cell 0.0005 mg/mg (D.W.)	Flagellates	
		0.488x10 ⁻⁸ µmole/cell 0.0007 mg/mg (D.W.)	Blue-greens (N-fixing)	
		0.566x10 ⁻⁸ µmole/cell 0.0007 mg/mg (D.W.)	Blue-greens (non N-fixing)	
	к _з	0.003 mg/mg (D.W.)	Total Phytoplankton	Nyholm (1978)
Nitrogen	ĸ ₁	0.05 g/m ³	Total Phytoplankton	Desormeau (1978)
	К ₂	0.801x10 ⁻⁵	Diatoms	Bierman <u>et</u> <u>al</u> . (1980)
		0.345x10 ⁻⁶ µmole/cell 0.025 mg/mg (D.W.)	Green Algae	
		0.163x10 ⁻⁵ µmole/cel1 0.025 mg/mg (D.W.)	Flagellates	
		0.377x10 ⁻⁶	Blue-greens (N-fixing)	
		0.438x10 ^{−6} µmole/cell 0.025 mg/mg (D.W.)	Blue-greens (non N-fixing)	
	K ₂	0.14x10 ⁻⁷ µmole/cell	Diatoms	Bierman (1976)
		0.14x10 ⁻⁷ µmole/cell	Green Algae	
		0.23x10 ⁻⁷ µmole/cell	Blue-greens (N-fixing)	
		0.14x10 ⁻⁷ µmole/cell	Blue-greens (non N-fixing)	

TABLE 6-12. HALF-SATURATION CONSTANTS FOR VARIABLE STOICHIOMETRY FORMULATIONS

carbon and silica are not included as potentially limiting nutrients (Nyholm, 1978).

The combined effects of multiple limiting nutrients in variable stoichiometry models are dealt with in the same basic ways as in fixed stoichiometry models (i.e., multiplicative formulation (Equation (6-26)), minimum formulation (Equation (6-27)), or harmonic mean formulation (Equation (6-28)). However, when a minimum (or threshold) formulation is used, the limiting nutrient is often determined by comparing the internal

		Minimum Cell Co	ncentration			
Algal Type	Nitrogen	Phosphorus	Carbon	Silicon	Units	References
Total Phytoplankton	0.015-0.02	0.001-0.003	0.15-0.18		mg/mg (D.₩.)	Jorgensen (1976, 1983)
	0.015	0.001	0.15-0.4		mg∕mg (D.W.)	Jorgensen <u>et al</u> . (1978, 1981)
	0.04	0.00146			mg∕mg (D.W.)	Nyholm (1978)
			0.3-0.7**		mg∕mg (D.₩.)	Jorgensen (1981)
Diatoms	0.520x10 ⁻⁷	0.20×10 ⁻⁸			µmoles/cell	Bierman (1976)
	0.801×10 ⁻⁵ 0.025	0.724×10 ⁻⁷ 0.0005			µmoles/cell mg/mg (D.W.)	Bierman <u>et</u> <u>al</u> . (1980)
	6.x10 ^{-7**}	0.9-30.x10 ^{-9**}		0.2-40.x10 ^{-7**}	µmoles/cell	Lehman <u>et</u> <u>al</u> . (1975)
		0.45-0.6**			µg/mm ³ cell volume	Jorgensen (1979)
Green Algae	$0.520 \times 10^{-7}$	0.20x10 ⁻⁸			µmoles/cell	Bierman (1976)
	0.345x10 ⁻⁶ 0.025	0.312×10 ⁻⁸ 0.0005			µmoles/cell mg/mg (D.W.)	Bierman <u>et</u> <u>al</u> . (1980)
		1.7-4.5x10 ^{-9**}			µmoles/cell	Lehman <u>et</u> <u>al</u> . (1975)
		>0.5**			µg/mm ³ cell volume	Jorgensen (1979)
Blue-green Algae	0.520-0.853x10 ⁻⁷	0.583-1.34x10 ⁻⁹			µmoles/cell	Bierman (1976)
	0.377-0.438x10 ⁻⁶ 0.025	0.488-0.566x10 ⁻⁸ 0.0007			µmoles/cell mg/mg (D.W.)	Bierman <u>et</u> <u>al</u> . (1980)
	1.1×10 ^{-7**}	2.5×10 ^{-9**}			µmoles/cell	Lehman <u>et al</u> . (1975)
		>0.5**			µg/mm ³ cell volume	Jorgensen (1979)
Dinoflagellates	3.9x10 ^{-7**}	11.×10 ^{-9**}			µmoles/cell	Lehman <u>et al</u> . (1975)
Flagellates	0.163×10 ⁻⁵ 0.025	0.148x10 ⁻⁷ 0.0005			µmoles/cell mg/mg (D.W.)	Bierman <u>et al</u> . (1980)
Chrysophytes	0.18-0.3x10 ^{-7**}	0.5x10 ^{-9**}			µmoles/cell	Lehman <u>et</u> <u>al</u> . (1975)
Benthic Algae		0.0005			mg/mg (D.₩.)	Auer and Canale (1982)

## TABLE 6-13. MINIMUM CELL QUOTAS

**Literature values.

		Maximum Cell Conce	ntration			
Algal Type	Nitrogen	Phosphorus (1997)	Carbon	Silicon	Units	References
Total Phytoplankton	0.08-0.12	0.013-0.03	0.6		mg∕mg (D.₩.)	Jorgensen (1976, 1983) Jorgensen <u>et al</u> . (1978, 1981)
	0.1	0.02			mg∕mg (D.W.)	Nyholm (1978)
	0.08-0.12**	0.013-0.035**			mg∕mg (D.W.)	Jorgensen <u>et al</u> . (1981)

TABLE 6-14.	MAXIMUM	INTERNAL	NUTRIENT	CONCENTRATIONS

**Literature values.

phosphorus to internal nitrogen ratio with a threshold ratio, rather than computing the growth limitation factor for each nutrient and using the smallest value.

Table 6-11 compares the growth formulations used in several variable stoichiometry and fixed stoichiometry models. The comparisons show which limiting factors are included, which formulations are used to compute nutrient limitation, and how multiple limiting factors are combined.

#### 6.4.4.3 Nutrient Uptake In Variable Stoichiometry Models

In fixed stoichiometry models, the nutrient composition of the algal cells is assumed to remain constant, so nutrient uptake is directly related to the algal growth rate by the stoichiometric ratio of nutrient mass to cell biomass. The nutrient uptake rate can then be expressed as:

$$\mathbf{v} = \mu \mathbf{q}_{c} \tag{6-61}$$

The growth rates are assumed to be functions of the external nutrient supplies (plus temperature and light) as computed by Michaelis-Menten type relationships (Equation (6-50)).

In contrast, nutrient uptake rates in variable stoichiometry models are functions of both internal nutrient levels in the cells and external nutrient concentrations in the water. The general relationship is typically of the form:

$$v = v_{max}(T_{ref}) f(T) f(q,s) f(L)$$
 (6-62)

where  $v_{max}(T_{ref})$  = maximum nutrient uptake rate at reference

	temperature T _{ref} , mass nutrient/mass algae-time
f(T)	= temperature function for uptake
f(q,s)	= nutrient uptake limitation function
q	= internal nutrient concentration, nutrient mass/cell
	biomass
S	= external nutrient concentration, mass/water volume
f(L)	= light limitation function for uptake

The temperature and light functions for uptake are essentially the same as those used for algal growth.

Variable stoichiometry models are distinguished primarily by the specific formulations used for the uptake limitation function f(q,s). These functions define the feedback between uptake rates and both internal and external nutrient levels. Some formulations attempt a more mechanistic approach, while others tend to be empirically based. In general, the uptake rates increase with the external nutrient supplies but at the same time decrease as the internal nutrient levels approach their saturation values. Uptake rates approach zero when either external nutrients are depleted or when internal nutrients reach their maximum saturated levels. However, neither of these conditions can persist since nutrients are continually recycled and since phytoplankton growth increases the algal biomass relative to the internal nutrient mass which in effect reduces the internal nutrient concentrations under conditions of restricted uptake.

The following formulations have been used to express internal and external nutrient effects on uptake rates in variable stoichiometry models:

$$f(q,s) = (q_{max} - q) \left(\frac{s}{K_{u1} + s}\right)$$
(6-63)

$$f(q,s) = \left(\frac{q_{max} - q}{q_{max} - q_{min}}\right) \left(\frac{s}{K_{u2} + s}\right)$$
(6-64)

$$f(q,s) = \frac{1}{\left(1 + \frac{K_{u3}}{s}\right)\left(1 + \frac{C_{i}}{K_{i}}\right)}$$
$$= \left(\frac{K_{i}}{K_{i} + C_{i}}\right)\left(\frac{s}{K_{u3} + s}\right)$$
$$= \left(\frac{K_{i}}{K_{i} + q + f_{i}}\right)\left(\frac{s}{K_{u3} + s}\right)$$
(6-65)

$$f(q,s) = \left(\frac{K_{i}}{K_{i} + (q - q_{min})}\right) \left(\frac{s}{K_{u3} + s}\right)$$
(6-66)

$$f(q,s) = \left(\frac{1}{1 + K_{a} q_{d}}\right) - \left(\frac{1}{1 + K_{a} s}\right)$$
(6-67a)

with 
$$q_d = q_{dmin} e^{\left(\frac{q_m}{q_{min}} - 1\right)}$$
 (6-67b)

Equation (6-63) is used by Koonce and Hasler (1972), Equation (6-64) by Lehman <u>et al</u>. (1975) and Jorgensen (1976), Equation (6-65) by Rhee (1973) and Park <u>et al</u>. (1980), Equation (6-66) by Di Toro (1980), Auer and Canale (1982), and Canale and Auer (1982), and Equations (6-67a) and (6-67b) by Bierman et al. (1973, 1980).

Maximum nutrient uptake rates and half-saturation constants for uptake are presented in Tables 6-15 and 6-16. Minimum cell quotas and maximum internal nutrient concentrations were presented previously in Tables 6-13 and 6-14. Some of the more model specific parameters are presented in Table 6-17.

Although variable stoichiometry models more realistically represent nutrient uptake and cell growth than fixed stoichiometry models, they do it at the expense of additional model complexity and computational costs. Algal growth computations in variable stoichiometry models require shorter time steps since the time scale for nutrient uptake is on the order of hours while the time scale for algal growth is on the order of days. Also, spatial variability in external and internal nutrient concentrations complicates transport since algae with different internal stoichiometries will be transported into the same model segment, requiring some type of averaging procedure at each time step.

Another criticism of variable stoichiometry models is that more model coefficients are required than in fixed stoichiometry models. Several coefficients are required for both the uptake and growth formulations. Since these coefficients must describe the response of species assemblages rather than the single species evaluated in laboratory experiments, they must be determined largely by model calibration. This introduces additional uncertainty in the model results. Also, the data base for variable stoichiometry coefficients is much smaller than for conventional Michaelis-Menten parameters.

		Maximum Upta				
Algal Type	Nitrogen	Phosphorus	Carbon	Silicon	Units	References
Total Phytoplankton	0.15	0.0014	0.55		1/day	Jorgensen (1983)
	0.012-0.03	0.0014-0.008	0.40-1.21		1/day	Jorgensen <u>et</u> <u>al</u> . (1978, 1981)
	0.14	0.1			1/day	Desormeau (1978)
	0.01-0.035**	0.003-0.01**	0.2-0.7**		1/day	Jorgensen <u>et</u> <u>al</u> . (1978)
	0.01-0.035**	0.003-0.01**	0.2-1.4**		1/day	Jorgensen (1981)
	0.0024**	0.02-2.95**			µmoles/hr	Jorgensen (1979)
Diatoms	0.015	0.024			1/day	Bierman (1976)
	0.125	0.500			1/day	Bierman <u>et al</u> . (1980)
	0.72-4.32**				l/day	Jorgensen (1979)
	0.3-120.x10 ^{-8**}	0.7-8.×10 ^{-9**}		2.6-950.×10 ^{-9**}	µmoles/cell-hr	Lehman <u>et al</u> . (1975)
	1.52-8.33x10 ^{-6**}			0.073-26.6x10 ^{-6**}	µmoles/cell-hr	Jorgensen (1979)
Green Algae	0.060	0.133			l/day	Bierman (1976)
	0.125	0.500			l/day	Bierman <u>et al</u> . (1980)
	2.2-10.6x10 ^{-8**}	1.2-4.×10 ^{-8**}			µmoles/cell-hr	Lehman <u>et al</u> . (1975)
	2.14-5.56x10 ^{-6**}				µmoles/cell-hr	Jorgensen (1979)
Blue-green Algae	0.040	0.042-0.059			1/day	Bierman (1976)
	0.125	0.500			1/day	Bierman <u>et al</u> . (1980)
	0.042×10 ^{-6**}				µmoles/cell-hr	Jorgensen (1979)
Flagellates	0.125	0.500			l/day	Bierman <u>et</u> <u>al</u> . (1980)
Chrysophytes	1.4-3.8×10 ^{-8**}	2.4×10 ^{-7**}			µmoles/cell-hr	Lehman <u>et al</u> . (1975)
		2.01-13.9x10 ⁻⁹ **			µmoles/cell-hr	Jorgensen (1979)
Coccolithophores	49.×10 ^{-10**}				µmoles/cell-hr	Lehman <u>et al</u> . (1975)
Benthic Algae		0.045			1/day	Auer and Canale (1982)

**Literature values.

Phytoplankton Group	Nitrogen (mg/l)	Phosphorus (mg/1)	Carbon (mg/l)	Silicon (mg/l)	References
Total Phytoplankton	0.2	0.02-0.03	0.5		Jorgensen (1976, 1983)
	0.2	0.02	0.5-0.6		Jorgensen <u>et al</u> . (1978)
	0.05	0.07			Desormeau (1978)
	0.0014-0.007**	0.0028-0.053**			Jorgensen (1979)
Diatoms	0.030*	0.060*			Bierman <u>et al</u> . (1980)
	0.0028-0.105**	0.18-0.053		0.022-0.098**	Lehman <u>et al</u> . (1975)
	0.0014-0.130**				Eppley <u>et</u> <u>al</u> . (1969)
	0.0042-0.105**	0.0002-0.053**		0.0053-0.098**	Jorgensen (1979)
Green Algae	0.030*	0.020*			Bierman <u>et al</u> . (1980)
	0.0024-0.02**	0.019-0.155**			Lehman <u>et</u> <u>al</u> . (1975)
	0.0014-0.02**				Eppley <u>et</u> <u>al</u> . (1969)
	0.0024-0.02**	0.0009-1.500**			Jorgensen (1979)
Blue-green Algae	0.030*	0.015-0.060*			Bierman <u>et</u> <u>al</u> . (1980)
	0.980**				Lehman <u>et al</u> . (1975)
	0.0067-0.980**				Jorgensen (1979)
Dinoflagellates	0.0015-0.133**				Lehman <u>et</u> <u>al</u> . (1975)
	0.0015-0.144**				Eppley <u>et</u> <u>al</u> . (1969)
	0.0014-0.133*				Jorgensen (1979)
Flagellates	0.030*	0.060*			Bierman <u>et al</u> . (1980)
	0.007-0.077**				Jorgensen (1979)
Chrysophytes	0.0014-0.0084**	0.016-0.496**			Lehman <u>et al</u> . (1975)
	0.0014-0.0084**				Eppley <u>et</u> <u>al</u> . (1969)
	0.0014-0.0084**	0.009-0.496**			Jorgensen (1979)
Coccolithophores	0.0014**				Lehman <u>et al</u> . (1975)
	0.0014-0.0028**				Eppley <u>et al</u> . (1969)
	0.0014-0.0043**				Jorgensen (1979)
Bacillariophyceae	0.0063-0.120**				Jorgensen (1979)
Benthic Algae		0.125			Auer and Canale (1982)

## TABLE 6-16. HALF-SATURATION CONSTANTS FOR NUTRIENT UPTAKE

*Apparent half-saturation values under nutrient-starved conditions.
**Literature values.

		Model Parameter		
Nutrient	Туре	Value	Algal Type	Reference
Phosphorus	К _і	0.0001 g/m ³	Total Phytoplankton	Desormeau (1978)
	к _і	0.0007 mg/mg (D.W.)	Benthic Algae	Auer and Canale (1982)
	fi	0.01%	Total Phytoplankton	Desormeau (1978)
	К _а	0.518x10 ⁶ 1/mol 0.167x10 ⁷ 1/mol 0.518-2.0x10 ⁶ 1/mol 0.518 x 10 ⁶ 1/mol	Diatoms Green Algae Blue-green Algae Flagellates	Bierman <u>et al</u> . (1980)
	ĸ _a	0.50x10 ⁶ 1/mol 0.50x10 ⁶ 1/mol 0.90~1.0x10 ⁶ 1/mol	Diatoms Green Algae Blue-green Algae	Bierman (1976)
	^q dmin	0.5 μg/l 0.5 μg/l 0.5 μg/l 0.5 μg/l 0.5 μg/l	Diatoms Green Algae Blue-green Algae Flagellates	Bierman <u>et al</u> . (1980)
	^q dmin	0.215x10 ⁻⁷ mol/l cell vol. 0.215x10 ⁻⁷ mol/l cell vol. 0.107x10 ⁻⁷ mol/l cell vol.	Diatoms Green Algae Blue-green Algae	Bierman (1976)
Nitrogen	К _і	0.0005 g/m ³	Total Phytoplankton	Desormeau (1978)
	fi	0.05%	Total Phytoplankton	Desormeau (1978)
	K _a	0.100x107/1/mo1 0.100x107/1/mo1 0.100x107/1/mo1 0.100x107/1/mo1 0.100x107/1/mo1	Diatoms Green Algae Blue-green Algae Flagellates	Bierman <u>et al</u> . (1980)
	Ka	0.10x107/1/mo1 0.10x107/1/mo1 0.10x107/1/mo1	Diatoms Green Algae Blue-green Algae	Bierman (1976)
	q _{dmin}	3. μg/1 3. μg/1 3. μg/1 3. μg/1	Diatoms Green Algae Blue-green Algae Flagellates	Bierman <u>et</u> <u>al</u> . (1980)
	q _{dmin}	0.267x10 ⁻⁶ mol/l cell vol. 0.267x10 ⁻⁶ mol/l cell vol. 0.267x10 ⁻⁶ mol/l cell vol.	Diatoms Green Algal Blue-green Algae	Bierman (1976)

#### TABLE 6-17. MODEL-SPECIFIC NUTRIENT UPTAKE PARAMETERS

Di Toro (1980) and Di Toro and Connolly (1980) have shown that since the time scale for nutrient uptake is a fraction of the time scale for algal growth and is usually much smaller than the time scale for changes in external nutrient concentrations, many of the complexities of variable stoichiometry models can be avoided by assuming cellular equilibrium with external nutrient concentrations at each time step. This allows algal growth to be computed using conventional Michaelis-Menten kinetics, but at the same time allows the internal stoichiometry of the algae to vary. Since the cells are assumed to equilibrate immediately with the external nutrient concentrations during transport, both the computational difficulties associated with the rapid uptake dynamics and the problem of algae with different internal stoichiometries being transported into the same model segment are eliminated. Variable stoichiometry formulations are more important to accurately simulating nutrient recycling than to computing algal growth, so this scheme may be a reasonable compromise between the variable stoichiometry formulations.

#### 6.5 RESPIRATION AND EXCRETION

Respiration and excretion are generally combined and modeled as a single term which includes all metabolic losses and excretory processes. These losses represent the difference between gross growth and net growth. Since net growth (rather than gross growth) is typically reported in the literature, some models lump respiration, excretion, and gross growth into a single net growth term, rather than simulating each process separately. However, it is generally more appropriate to compute growth and respiration separately since growth rates are sensitive to nutrient supplies while respiration rates depend primarily on temperature. Also, respiration and excretion are important components of nutrient recycling, so these processes are usually computed separately for use in the nutrient dynamic equations.

Most models express respiration (plus excretion) as either a constant loss term or as a function of temperature. The general expression is:

$$r = r(T_{ref}) f_r(T)$$
 (6-68)

where r = rate of respiration plus excretion, l/time r(T_{ref}) = respiration rate at a particular reference temperature T_{ref}, l/time f_r(T) = temperature function for respiration The temperature functions for respiration use the same formulations discussed above for growth (Equations (6-5) through (6-25)). Most models use the same temperature function and coefficients for both processes. The major approaches are 1) linear increases in respiration with temperature, 2) exponential increases in respiration with temperature, and 3) temperature optimum curves in which respiration increases with temperature up to the optimum temperature and then decreases with higher temperatures. The most commonly used exponential formulation is the Arrhenius relationship with a reference temperature of  $20^{\circ}$ C (Equation (6-15a)). Some models, for example CE-QUAL-R1 (WES, 1982), use the left hand side of a temperature optimum curve or a logistic equation (Equation (6-22a)) to define temperature effects on respiration. This approach assumes respiration increases exponentially at low temperatures, but eventually levels off to some maximum value at higher temperatures.

A few models use formulations which relate the respiration rate to the physiological condition of the algal cells. For example, Scavia (1980) represents respiration as the sum of two components, 1) a low maintenance rate representing periods of minimal growth, and 2) a rate which is directly proportional to the photosynthesis rate (as defined by the growth limitation factor):

$$r(T_{ref}) = r_{min}(T_{ref}) + k_r(T_{ref}) f(L,P,N,C,Si)$$
(6-69)

- where r_{min}(T_{ref}) = base respiration rate under conditions of minimal growth (poor physiological condition) at reference temperature T_{ref}, 1/time

Both rates are multiplied by a temperature adjustment function.

The MS.CLEANER model uses a similar formulation which expresses respiration as the sum of endogenous respiration and photorespiration
(Groden, 1977; Park <u>et al.</u>, 1980). The endogenous respiration is defined as:

$$r_e = .0175 e^{.069T}$$
 (6-70)

where  $r_e$  = endogenous respiration rate, 1/time T = temperature, ^OC

Photorespiration is defined as a constant fraction of the temperature adjusted maximum photosynthesis rate in early versions of MS.CLEANER (Groden, 1977):

$$r_{p} = K_{p1} \mu_{max}(T_{ref}) f(T)$$
 (6-71)

and as a fraction of the actual photosynthesis rate (including temperature, light, and nutrient limitation effects) in later versions (Park <u>et al.</u>, 1980):

 $r_{p} = K_{p2} \mu$  (6-72) =  $K_{p2} \mu_{max}(T_{ref}) f(T) f(L,P,N,C,Si)$ 

where  $K_{p2}$  = fraction of actual photosynthesis rate which is oxidized by photorespiration

MS.CLEANER also considers excretion as a separate loss term, in contrast to most models which lump respiration and excretion together. Excretion is formulated similar to photorespiration. However, since the excretion of photosynthate and photorespiratory compounds relative to carbon assimilation (photosynthesis) is highest at both low light levels and inhibitory high light levels, the excretion rate is expressed as (Desormeau, 1978; Collins, 1980):

$$e_{x} = K_{e} \left( 1 - f(L) \right) \mu \qquad (6-73)$$

where e = excretion rate, 1/time

 $K_{\rho}$  = fraction of photosynthesis excreted

f(L) = light limitation factor

μ = growth (photosynthesis) rate, including effects of temperature, light, and nutrient limitation, 1/time

Lehman <u>et al</u>. (1975), Jorgensen (1976), and Jorgensen <u>et al</u>. (1978, 1981) use variable stoichiometry formulations which relate the respiration rate to the internal carbon levels of the cells. The ratio of the internal carbon level to the maximum internal carbon level is used to define the physiological state of the cells. The respiration rate increases with the internal carbon level according to the equation:

$$r(T_{ref}) = r_{max}(T_{ref}) \left(\frac{C_{int}}{C_{max}}\right)^{2/3}$$
(6-74)

where r_{max}(T_{ref}) = maximum respiration rate at reference temperature T_{ref}, 1/time C_{int} = internal carbon level, mass carbon/biomass algae C_{max} = maximum internal carbon level, mass carbon/biomass algae

Algal respiration rates are tabulated in Table 6-18.

#### 6.6 SETTLING

Phytoplankton settling rates depend on the density, size, shape, and physiological state of the phytoplankton cells, the viscosity and density of the water, and the turbulence and velocities of the flow field. The settling velocities for spherical particles in still water can be computed from Stoke's law. Stoke's law can be modified to account for non-spherical phytoplankton cells by using an "equivalent radius" and "shape factor" in the formulation (Scavia, 1980):

Algal Type	Respiration Rate (1/day)	[.] Reference Temperature ( ⁰ C)	References		
Tota] Phytoplankton	0.05 0.15	20 ⁰ C	Di Toro <u>et al</u> . (1971, 1977) O'Connor <u>et al</u> . (1975, 1981) Thomann <u>et al</u> . (1974, 1975, 1979) Di Toro & Matystik (1980) Di Toro & Connolly (1980) Thomann & Fitzpatrick (1982) Salisbury <u>et al</u> . (1983)		
	0.05 - 0.10	20 ⁰ C	Chen & Orlob (1975) Chen & Wells (1975, 1976) Tetra Tech (1976)		
	0.08	20 ⁰ C	Canale <u>et al</u> . (1976)		
	0.10	20 ⁰ C	Lombardo (1972)		
	0.088 0.6	T _{opt}	Jorgensen (1976) Jorgensen <u>et al</u> . (1978)		
	0.051	20 ⁰ C	Brandes (1976)		
	0.05	20 ⁰ C	Grenney & Kraszewski (1981)		
	0.005 0.12*	20 ⁰ C	Baca & Arnett (1976)		
	0.05 0.2*	20 ⁰ C	Smith (1978)		
	0.05 - 0.5*	20 ⁰ C	Roesner <u>et al</u> . (1980) Duke & Masch (1973)		
	0.02 0.8*	20 ⁰ C	Grenney & Kraszewski (1981)		
	0.05 0.10**	20 ⁰ C	Collins & Wlosinski (1983)		
	0.05 - 0.20**	20 ⁰ C	Jorgensen (1979)		
Diatoms	0.04 0.08	20 ⁰ C	Thomann <u>et al</u> . (1979) Di Toro & Connolly (1980) Salisbury <u>et al</u> . (1983) Di Toro <u>et al</u> . (1971)		
	0.07 0.08	20 ⁰ C	Porcella <u>et al</u> . (1983) Tetra Tech (1980)		
	0.03 0.05	20 ⁰ C	Bierman (1976) Bierman <u>et al</u> . (1980)		
	0.05 0.25	T _{opt}	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)		
	0.05 - 0.59**	20 ⁰ C	Collins & Wlosinski (1983)		
	(con	tinued)			

## TABLE 6-18. ALGAL RESPIRATION RATES

Algal Type	Respiration Rate (1/day)	Reference Temperature ( ^O C)	References			
Green Algae	0.05 0.07	20 ⁰ C	Tetra Tech (1980) Porcella <u>et</u> al. (1983)			
	0.05 0.25	T _{opt}	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et</u> al. (1980)			
	0.03 0.05	20 ⁰ C	Bierman (1976) Bierman <u>et al</u> . (1980)			
	0.01 0.46**	20 ⁰ C	Collins & Wlosinski (1983)			
Blue-green Algae	0.05 0.065	20 ⁰ C	Tetra Tech (1980) Porcella <u>et al</u> . (1983)			
	0.05 0.25	T _{opt}	Scavia et al. (1976) Scavia (1980) Bowie <u>et</u> al. (1980)			
	0.03 0.05	20 ⁰ C	Bierman (1976) Bierman <u>et al</u> . (1980)			
	0.10 0.92**	20 ⁰ C	Collins & Wlosinski (1983)			
Dinoflagellates	0.047	20 ⁰ C	0'Connor <u>et</u> <u>al</u> . (1981)			
Flagellates	0.05	20 ⁰ C	Bierman <u>et al</u> . (1980)			
	0.05 - 0.06	20 ⁰ C	Tetra Tech (1980) Porcella <u>et</u> <u>al</u> . (1983)			
Chrysophytes	0.15 0.32**	20 ⁰ C	Collins & Wlosinski (1983)			
Benthic Algae	0.02 0.1	20 ⁰ C	Tetra Tech (1980) Bowie <u>et al</u> . (1980) Porcella <u>et al</u> . (1983)			
	0.44	T _{opt}	Auer and Canale (1982)			
	0.1	20 ⁰ C	Grenney & Kraszewski (1981)			
	0.02 0.8*	20 ⁰ C	Grenney & Kraszewski (1981)			
	0.05 - 0.2*	20 ⁰ C	Smith (1978)			

TABLE 6-18. (continued)

*Model documentation values. **Literature values.

$$V_{s} = \frac{2}{9} \frac{g R^{2} (\rho_{p} - \rho_{w})}{\nu F_{s}}$$
(6-75)

where V = settling velocity, length/time

- g = acceleration of gravity, length/time²
- R = equivalent radius (based on a sphere of equivalent volume), length
- $\rho_{\rm p}$  = density of the cell, mass/length^3
- $\rho_{\rm w}$  = water density, mass/length³
- $\nu$  = kinematic viscosity
- $F_{c}$  = shape factor

The shape factor has a value  $\geq 1.0$  and accounts for all factors which reduce the settling velocities below that of an equivalent spherical particle, for example increased drag due to diatom spicules, flat or elongated cells, clusters or colonies of cells, etc. In a model of Lake Ontario, Scavia (1980) used a shape correction factor of 1.3 for small diatoms, 2.0 for large diatoms, and 1.0 for all other algal groups.

In practice, very few models use Stoke's law as a model formulation (Scavia <u>et al</u>., 1976; Scavia, 1980; Park <u>et al</u>., 1980). Most models lump many species into a few algal groups, so representative values of the cell radius, shape factor, and cell density are difficult to define, making this level of detail unnecessary. Since the shape factor is really a calibration parameter, it is more direct to simply use the settling velocity as a calibration parameter. Also, Stoke's law does not account for turbulence and flow velocities which tend to keep algae in suspension or resuspend settled algae. Additional factors which further complicate settling include the production of gas vacuoles or gelatinous sheaths which make some species buoyant, and the fact that settling velocities may vary with the nutritional state or physiological condition of the cells.

Settling rates are also partly dependent on the structure of the model. For example, one-dimensional layered lake models typically use settling velocities which are an order of magnitude lower than measured values or values used in two-or three-dimensional models which simulate hydrodynamic processes (Scavia and Bennett, 1980). This is probably because onedimensional models do not adequately represent vertical transport process such as upwelling or entrainment of phytoplankton in large-scale circulations which effectively reduce the net settling rates (Scavia and Bennett, 1980).

Because of the above factors, most models specify phytoplankton settling velocities directly as model coefficients. The settling rate in Equations (6-1) or (6-2) is generally expressed as:

$$s = \frac{V_s}{d}$$
 (6-76)

where s = settling rate, 1/time
V_s = settling velocity, length/time
d = water depth, length

In layered models, algae settling in from the above layer, as well as algae settling out of the layer, must be included in the formulation. This also requires consideration of the bottom topography, since a fraction of the algae will settle onto the bottom area associated with each layer.

Equation (6-76) is refined in some models by including a temperature function which accounts for changes in settling velocities due to temperature effects on the density and viscosity of water. The settling rate is then expressed as:

$$s = \frac{V_s(T_{ref})}{d} f_s(T)$$
 (6-77)

Ν.

.f (T) = temperature adjustment function for the settling velocity Typical examples of temperature adjustment functions include (Tetra Tech, 1980):

$$f_{s}(T) = \frac{157.5}{0.069T^{2} - 5.3T + 177.6}$$
(6-78)

where  $T = temperature in {}^{O}C$ .

or (Scavia and Park, 1976):

$$f_{c}(T) = 1 + a_{c} T$$
 (6-79)

where a_c = slope of settling velocity vs. temperature curve

Scavia <u>et al</u>. (1976) have also expanded the settling rate formulation to account for variations in settling velocities due to the physiological condition of the phytoplankton cells. The basic assumption is that the cells are healthiest and the settling rates smallest when neither light nor nutrients are limiting growth. The settling rates are therefore expressed as a function of the growth limitation factor f(L,P,N,C,Si). Potential formulations include (Scavia et al., 1976; Scavia, 1980):

$$s = \frac{V_{smax}(T_{ref})}{d} f_{s}(T) \left( \frac{K_{set_{1}}}{f(L,P,N,C,Si) + K_{set_{1}}} \right)$$
(6-80)

or 
$$s = \frac{V_{smax}(T_{ref})}{d} f_s(T) \left[ 1 - K_{set_2} f(L,P,N,C,Si) \right]$$
 (6-81)

A few models require specification of the settling rate s rather than the settling velocity  $V_{c}$  as a model calibration coefficient. When used in

this way, the settling rate may take on a wide range of values since it depends as much on the water depth as the settling velocities of the algae.

Phytoplankton settling velocities are presented in Table 6-19. Additional data are available in a review by Smayda (1970).

### 6.7 NONPREDATORY MORTALITY

Nonpredatory mortality accounts for all algal losses which are not explicitly accounted for by the grazing term or other loss processes in the model (for example, settling and respiration if they are not computed explicitly). Nonpredatory mortality includes processes such as senescence, bacterial decomposition of cells (parasitism), and stress-induced mortality due to severe nutrient deficiencies, extreme environmental conditions, or toxic substances. The nonpredatory mortality rate in Equations (6-1), (6-2), or (6-3) is generally specified as a constant model coefficient. This is in contrast to the predatory mortality or grazing rate which is computed dynamically to reflect changes in the predator densities.

In some models, a temperature adjustment function is used with nonpredatory mortality which results in:

$$m = m(T_{ref}) f_m(T)$$
(6-82)

where m = nonpredatory mortality rate, 1/time m(T_{ref}) = nonpredatory mortality rate at reference temperatur[®] T_{ref}, 1/time f_m(T) = temperature function for mortality

The temperature functions for mortality generally use the same formulations used for growth and respiration (Equations (6-5) through (6-25)). However, if a temperature optimum curve is used for growth, the temperature function for mortality will often use only the left hand portion of the curve to produce a temperature response curve in which mortality increases with temperature until some maximum mortality rate is reached.

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Algal Type	Settling Velocity (m/day)	References
Total Phytoplankton	0.05 0.5	Chen & Orlob (1975) Tetra Tech (1976) Chen (1970) Chen & Wells (1975, 1976)
	0.05 0.2	O'Connor <u>et al</u> . (1975, 1981) Thomann <u>et al</u> . (1974, 1975, 1979) Di Toro & Matystik (1980) Di Toro & Connolly (1980) Thomann & Fitzpatrick (1982)
	0.02 0.05	Canale <u>et</u> <u>al</u> . (1976)
	0.4	Lombardo (1972)
	0.03 0.05	Scavia (1980)
	0.05	Bierman <u>et</u> <u>al</u> . (1980)
	0.2 0.25	Youngberg (1977)
	0.04 0.6	Jorgensen (1976) Jorgensen <u>et al</u> . (1978, 1981)
	0.01 ~ 4.0*	Baca & Arnett (1976)
	0. 2.0*	Chen & Orlob (1975) Smith (1978)
	0.15 2.0*	Duke & Masch (1973) Roesner <u>et al</u> . (1977)
	0 0.2*	Brandes (1976)
	0 30.**	Jorgensen (1979)
Diatoms	0.05 - 0.4	Bierman (1976) Bierman <u>et al</u> . (1980)
	0.1 - 0.2	Thomann <u>et al</u> . (1979) Di Toro & Connolly (1980)
	0.1 - 0.25	Tetra Tech (1980) Porcella <u>et</u> <u>al</u> . (1983)
	0.03 - 0.05	Canale <u>et al</u> . (1976)
	0.3 - 0.5	Smayda & Boleyn (1965)
	2.5	Lehman <u>et</u> <u>al</u> . (1975)
	0.02 14.7**	Collins & Wlosinski (1983)
	0.08 - 17.1** (continued)	Jorgensen (1979) d)

# TABLE 6-19. PHYTOPLANKTON SETTLING VELOCITIES

Algal Type	Settling Velocity (m/day)	References			
Green Algae	0.05 - 0.19	Jorgensen <u>et</u> al. (1978)			
	0.05 0.4	Bierman (1976) Bierman <u>et al</u> . (1980)			
	0.02	Canale <u>et</u> <u>al</u> . (1976)			
	0.8	Lehman <u>et</u> <u>al</u> . (1975)			
	0.1 0.25	Tetra Tech (1980) Porcella <u>et</u> <u>al</u> . (1983)			
	0.3	DePinto <u>et al</u> . (1976)			
	0.08 0.18**	Collins & Wlosinski (1983)			
	0.27 - 0.89**	Jorgensen (1979)			
Blue-green Algae	0.05 0.15	Bierman (1976) Bierman <u>et</u> <u>al</u> . (1980)			
	0.	Canale <u>et</u> <u>al</u> . (1976)			
	0.2	Lehman <u>et al</u> . (1975)			
	0.1	DePinto <u>et al</u> . (1976)			
	0.08 0.2	Tetra Tech (1980) Porcella <u>et al</u> . (1983)			
	0.10 0.11**	Collins & Wlosinski (1983)			
Flagellates	0.5	Lehman <u>et al</u> . (1975)			
	0.05	Bierman <u>et al</u> . (1980)			
	0.09 - 0.2	Tetra Tech (1980) Porcella <u>et</u> al. (1983)			
	0.07 0.39**	Collins & Wlosinski (1983)			
Dinoflagellates	8.0	0'Connor <u>et</u> <u>al</u> . (1981)			
	2.8 6.0**	Collins & Wlosinski (1983)			
Chrysophytes	0.5	Lehman <u>et al</u> . (1975)			
Coccolithophores	0.25 13.6	Collins & Wlosinski (1983)			
	0.3 1.5**	Jorgensen (1979)			

*Model documentation values.

**Literature values.

A few models use more sophisticated formulations for nonpredatory mortality which try to relate the mortality rate to the physiological condition of the algal cells or to the size of the decomposer population (De Pinto, 1979). For example, Scavia <u>et al</u>. (1976) use the value of the growth limitation factor f(L,P,N,C,Si) as a measure of cell health and express the mortality rate as:

$$m(T_{ref}) = m_{max}(T_{ref}) \left[1 - f(L,P,N,C,Si)\right]$$
(6-83)

where m_{max}(T_{ref}) = maximum nonpredatory mortality under poor physiological conditions at reference temperature T_{ref}, 1/time

This assumes minimal mortality and algal decomposition when growth conditions are optimal, and maximum mortality when conditions are severely limiting.

Lehman <u>et al</u>. (1975) use a similar approach, but also include the duration of growth limiting conditions in the formulation. They define the mortality rate as:

$$m(T_{ref}) = m_{max}(T_{ref}) \left(1 - e^{-K_{so}T_{so}}\right)$$
(6-84)

where  $T_{so}$  = number of days of suboptimal conditions (defined as  $\mu/\mu_{max}$ .05), time  $K_{so}$  = coefficient defined as ln2 divided by the number of days at suboptimal conditions until m increases to  $\frac{1}{2} m_{max}$ 

MS.CLEANER expresses nonpredatory mortality as a function of both the internal nutrient concentrations and temperature such that the mortality rate increases exponentially under conditions of either nutrient starvation or critically high temperatures. The equation is (Desormeau, 1978; Park <u>et al.</u>, 1980):

$$m = K_{m} e^{K_{n}(N_{crit}-f(P,N,C,Si))} e^{(T-T_{crit})}$$
(6-85)

This assumes that when the internal nutrient levels drop below the subsistence quota, increased senescence, bacterial colonization, and cell lysis occur.

Bierman <u>et al</u>. (1980) use a nonpredatory mortality function which indirectly includes the size of the decomposer bacteria population in the formulation. Although the bacteria are not modeled explicitly, they are assumed to increase in proportion to the total algal concentration (the sum of all algal groups in the model). Therefore, increases in the bacteria associated with the bloom of one algal group will result in higher mortality rates for all other groups since a higher decomposer population is established. The equation is:

$$m(T_{ref}) = K_m(T_{ref}) \sum_{i=1}^{n} A_i$$
 (6-86)

Nyholm (1978) uses a Michaelis-Menten type saturation function of the algal concentrations in his formulation for algal mortality:

$$m(T_{ref}) = m_{max}(T_{ref}) \left(\frac{A}{K_{m1} + A}\right)$$
(6-87)

where m_{max}(T_{ref}) = maximum nonpredatory mortality rate at reference temperature T_{ref}, 1/time A = algal concentration, mass/volume K_{m1} = half-saturation constant for algal nonpredatory mortality, mass/volume

At high algal concentrations, this is equivalent to the basic first order formulation (Equation (6-82)), while at very low algal levels, the mortality rate is essentially a second order relationship analogous to Equation (6-86). However, even though the mortality rate is second order at low algal densities, the Michaelis-Menten term reduces the net rate at low densities below the maximum first-order rate at high algal densities.

The Michaelis-Menten formulation is also used by Di Toro and Matystik (1980), Di Toro and Connolly (1980), and Thomann and Fitzpatrick (1982) in their formulation for the decomposition of organic matter (dead algal cells), although a basic first-order formulation is used for algal nonpredatory mortality. These models use the Michaelis-Menten formulation to account for the effects of the bacterial population on decomposition rates, assuming that decomposers (and the resulting decomposition rates) increase in proportion to the algal densities at low concentrations, but that other factors limit decomposition rates at high algal densities (Di Toro and Matystik, 1980; Di Toro and Connolly, 1980). These mechanisms could also be assumed for nonpredatory mortality.

Rodgers and Salisbury (1981) use a modified Michaelis-Menten formulation for nonpredatory mortality which includes the effects of both bacterial activity and the physiological condition of the algal cells on algal decomposition:

$$m(T_{ref}) = m_{max}(T_{ref}) \left(\frac{A/\mu}{K_{m2} + A/\mu}\right)$$
(6-88)

where µ = algal growth rate, 1/time
 K_{m2} = half-saturation constant for algal nonpredatory mortality;
 mass-time/volume

The mortality rate is directly proportional to the algal biomass (an indicator of bacterial activity) and inversely proportional to the algal growth rate (an indicator of the physiological condition of the cells), both through a saturation type relationship which limits the maximum rate.

Some models include formulations to account for stress-induced mortality due to factors such as extreme temperatures or toxic substances. Stress related mortality is typically modeled by expanding the nonpredatory mortality term to include additional terms for these effects, for example:

$$m = m(T_{ref}) f_{m}(T) + m_{T}(T_{ref}) f_{T}(T) + m_{x} f_{x}(X)$$
(6-89)

where  $m_T(T_{ref})$  = thermal mortality rate at reference temperature  $T_{ref}$ , 1/time  $f_T(T)$  = thermal mortality response curve  $m_x$  = toxic mortality rate, 1/time  $f_x(X)$  = dose-response curve for toxic mortality X = concentration of toxicant, mass/volume

Toxic effects can also be included in the growth and respiration formulations.

Algal nonpredatory mortality rates are presented in Table 6-20.

#### 6.8 GRAZING

Algal grazing losses can be modeled in several ways, depending on 1) whether predator populations are simulated in the model, and 2) whether alternate food items are available for the predators.

When predators are not explicitly modeled, predator-prey dynamics cannot be simulated, so grazing effects are typically handled by either assuming a constant grazing loss which is specified by the user as a model input parameter:

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Algal Type	Nonpredatory Mortality Rate (1/day)	References			
Total Phytoplankton	0.02	Thomann & Fitzpatrick (1982)			
	0.003 0.17	Baca & Arnett (1976)			
	0.03	Scavia <u>et al</u> . (1976)			
	0.005 0.10	Salas & Thomann (1978)			
	0.01 0.1	Jórgensen (1976) Jorgensen <u>et</u> <u>al</u> . (1978)			
Diatoms	0.03	Scavia <u>et al</u> . (1976)			
Benthic Algae	0 0.8	Tetra Tech (1980) Bowie <u>et</u> al. (1980) Porcella <u>et</u> al. (1983)			

TABLE 6-20. ALGAL NONPREDATORY MORTALITY RATES

where G = loss rate due to grazing, mass algae/time

or

or by assuming a loss rate which is directly proportional to the algal densities (e.g., RECEIV-II (Raytheon, 1974)):

$$G = e_{z} A \tag{6-91}$$

$$G = e_z(T_{ref}) f_g(T) A \qquad (6-92)$$

where 
$$e_z = grazing$$
 rate coefficient, 1/time  
A = algal biomass or density. mass or mass/volume  
 $e_z(T_{ref}) = grazing$  rate coefficient at reference temperature  
 $T_{ref}$ , 1/time  
 $f_g(T) = temperature$  function for grazing

The second formulation is equivalent to that often used for non-predatory mortality (Equation (6-82)), so both nonpredatory mortality and grazing losses are typically combined into a single total mortality term when predator populations are not directly simulated:

$$m_{tot} = \left(m(T_{ref}) + e_z(T_{ref})\right) f_m(T)$$
$$= m_{tot}(T_{ref}) f_m(T)$$
(6-93)

where  $m_{tot}$  = total mortality rate, 1/time  $m_{tot}(T_{ref}) \stackrel{:}{=} total mortality rate at reference temperature <math>T_{ref}$ , 1/time  $f_m(T)$  = temperature function for mortality

The temperature functions used for grazing are the same as those discussed previously for algal growth, respiration, and mortality (Equations (6-5) to (6-25)).

Many general water quality models include a single zooplankton group to provide a more realistic grazing formulation for algae (Baca <u>et al</u>., 1973; Johanson <u>et al</u>., 1980; Najarian and Harleman, 1975). The zooplankton are often added only to obtain better simulations of algal dynamics, rather than to evaluate the zooplankton dynamics of the system. The coupled algae and zooplankton equations provide the major features of predator-prey interactions since the algal grazing rate is defined as a function of the zooplankton density which in turn varies dynamically with the food supply (algal concentration). The algal grazing rate in these models is typically expressed either in terms of a zooplankton filtration rate:

$$G = C_f A Z$$
 (6-94)

or

$$G = C_{f}(T_{ref}) f_{q}(T) A Z \qquad (6-95)$$

where C_f = zooplankton filtration rate, water volume/mass zooplankton-time

or in terms of a zooplankton ingestion rate:

$$G = C_g Z \qquad (6-96)$$

$$G = C_{g}(T_{ref}) f_{g}(T) Z$$
 (6-97)

where C = zooplankton ingestion rate, mass algae/mass zooplankton-time C (Tref) = ingestion rate at reference temperature Tref, mass algae/mass zooplankton-time

Ingestion rates are often back-calculated from computed zooplankton growth rates based on the equation (Chen and Orlob, 1975; Smith, 1978; Tetra Tech, 1979; WES, 1982):

$$C_{g} = \frac{g_{z}}{E}$$
 (6-98)

where g_z = zooplankton growth rate, 1/time E = zooplankton assimilation efficiency

In this approach, zooplankton growth rates are first computed as a function of food supply and temperature, and then the amount of algae which would have to be consumed to produce the growth is computed from Equation (6-98). The alternative approach is to specify or compute the ingestion rates directly, and then calculate the zooplankton growth rates based on the amount of food consumed and the assimilation efficiencies. Specific formulations for zooplankton filtration rates, ingestion rates, growth rates, and assimilation efficiencies are discussed in detail in Chapter 7. Models which simulate only a single algal and zooplankton group tend to oversimplify predator-prey dynamics since a single constituent represents all primary producers and another single constituent represents all consumers. This ignores the complexities of the food web, as well as differences in foraging strategies, grazing rates, and food preferences between different types of predator organisms. This approach may be adequate in short term simulations where one group of phytoplankton and zooplankton are dominant. However, in long term simulations, more than one group of algae and zooplankton should be used to adequately simulate predator-prey interactions and population dynamics.

Algal grazing rates in multi-group models are functions of alternative food sources and food preferences, as well as predator densities, algal densities, and temperature. The basic grazing formulations are essentially the same as those mentioned above for a single zooplankton group, except that 1) grazing losses must be considered for each potential predator which grazes the algae, and 2) total grazing rates calculated for a given predator must be partitioned among the various food items which it consumes. Some models also consider differences in the ingestion or assimilation efficiencies between different food items (Scavia <u>et al</u>., 1976; Park <u>et al</u>., 1980), and differences in the feeding behavior of different zooplankton groups (e.g., non-selective filterers, selective filterers, carnivorous raptors, omnivores, etc.) (Canale et al., 1975, 1976; Park et al., 1980).

Grazing losses for non-selective feeders can be partitioned between different algal groups by distributing them in proportion to the algal concentrations:

$$G_{ij} = C_j \frac{A_i}{\sum_{k=1}^{n} F_k} Z_j$$
 (6-99)

- where G_{ij} = loss rate of algal group i due to grazing by zooplankton group j, mass algae/time
  - C_j = total ingestion rate of zooplankton group j on all food items, mass food/mass zooplankton-time
  - A_i = biomass or concentration of algal group i, mass or mass/volume
  - F = biomass or concentration of potential food item k consumed by zooplankton group j, mass or mass/volume
  - n = number of potential food items
  - Z = biomass or concentration of zooplankton group j, mass or mass/volume

When grazing is expressed in terms of a filtration rate this partitioning is done automatically since the grazing losses are simply the algal concentrations times the volumetric filtration rates.

The above expression can be modified to account for selective feeding behavior by using food preference factors. These are weighting factors which reflect the probability that a given food will be consumed relative to the others when all foods are present in equal concentrations. The preference factors account for feeding differences due to factors like food particle size and shape, desirability and quality of food, and zooplankton feeding behavior. The grazing losses for each algal group subject to selective feeding can be expressed as:

$$G_{ij} = C_{j} \frac{P_{ij}A_{i}}{\sum_{k=1}^{n} P_{kj}F_{k}} Z_{j}$$
(6-100)

where P_{ij} = preference factor for zooplankton j grazing on algal group i P_{kj} = preference factor for zooplankton j grazing on food item k

The total ingestion rates  $C_j$  for each predator are the same as discussed above for a single zooplankton group (Equations (6-94) through (6-98)).

When several predators are modeled, the total grazing loss for a given algal group is the sum of the grazing losses from each predator:

$$G_{i} = \sum_{j=1}^{n} G_{ij}$$
 (6-101)

where G_i = loss rate for algal group i due to grazing by all predators, mass algae/time

 $n_p$  = total number of predators grazing on algal group i

Any of the previous formulations can be used to define the incremental grazing rates  $G_{ii}$  associated with each predator.

Zooplankton grazing rates are tabulated in Chapter 7, along with more detailed descriptions of the grazing formulations for zooplankton.

6.9 SUMMARY

Phytoplankton and attached algae are generally modeled as a biomass pool using the same mass balance approach used for nutrients and other constituents. The simpler models lump all algae into a single group, while more complex models distinguish between different functional groups such as green algae, diatoms, and blue-green algae. Single-group models are commonly used in rivers, while multi-group models are more common in lakes where long-term simulations of the seasonal succession of different types of phytoplankton are important.

Algal dynamics depend on growth, respiration, excretion, settling, nonpredatory mortality, and predation. Although some of these processes can be measured in the field or laboratory, most of the coefficients defining the process rates are usually determined by model calibration. This is necessary since the rates will vary with environmental conditions such as temperature, light, nutrient concentrations, and predator densities as well as with the species composition of the algae, all of which change continually with time. Literature values from laboratory experiments are useful for establishing reasonable ranges for the coefficients. However, specific experimental results are difficult to apply directly since experiments typically use a single species rather than the species assemblages represented in models, and since experimental conditions may not represent conditions in the field. Model constructs must be relied upon to describe the effects of changing environmental and ecological conditions on the process rates.

Most processes in algal models are assumed to be temperature dependent. Three major approaches have been used to describe these effects: linear temperature response curves, exponential curves, and temperature optimum curves. The exponential Arrhenius relationship is commonly used when only one algal group is simulated, while temperature optimum curves are more common in multi-group models.

The most important and complex formulations in algal models are the growth formulations. Growth is a function of temperature, light, and nutrients. Light limitation is typically defined by either a saturation type relationship or a photoinhibition relationship in which growth decreases at light intensities above the optimum. Most models use Michaelis-Menten kinetics to describe nutrient limitation effects and assume the nutrient composition of the algal cells remains constant. More sophisticated models allow the internal stoichiometry of the algae to vary with changes in the external nutrient concentrations. These models simulate nutrient uptake and algal growth as two separate steps. Nutrient uptake is first computed as a function of both the internal nutrient levels in the cells and the external concentrations in the water. Algal growth is then computed based on the internal nutrient concentrations in the cells. Various formulations have been used to describe uptake and growth kinetics in variable stoichiometry models. These formulations are more complex and involve more model coefficients than fixed stoichiometry models.

Most models use simple temperature-dependent first-order relationships to describe respiration, settling, and nonpredatory mortality. A few models include the effects of the physiological condition of the algae on these processes by making them a function of the growth rate, growth limitation factor, or internal nutrient level (in variable stoichiometry models). Some models also include the effects of the decomposer bacteria population on nonpredatory mortality. These latter effects are modeled indirectly by assuming the decomposers increase in proportion to the algal densities and using algal concentrations as an indicator of the bacterial population, rather than by simulating the decomposers directly. Both second-order mortality formulations and Michaelis-Menten type saturation relationships have been used to describe these effects.

Algal grazing is usually modeled as a first-order loss when zooplankton are not simulated. When zooplankton are modeled, algal grazing is a function of the algal densities, zooplankton densities, and the zooplankton filtration rates or consumption rates. In multi-group models which include several algal and zooplankton groups, selective feeding behavior can be simulated by including food preference factors in the grazing formulations.

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#### Chapter 7

### ZOOPLANKTON

#### 7.1 INTRODUCTION

Zooplankton are included in water quality models primarily because of their effects on algae and nutrients. Algal dynamics and zooplankton dynamics are closely tied through predator-prey interactions. Nutrient dynamics are also influenced by zooplankton since zooplankton excretion is an important component of nutrient recycling, and because of the effects zooplankton have on algal dynamics. These interrelationships are particularly important for long-term simulations in lakes and estuaries since both zooplankton and algal densities may change by orders of magnitude over periods of several months.

As with phytoplankton, zooplankton have been modeled both as a single constituent representing total zooplankton and as several functional groups. The functional groups may represent different feeding types (e.g., herbivores, carnivores, omnivores, non-selective filter feeders, selective filter feeders, etc.) or different taxonomic groups (cladocerans, copepods, rotifers, etc.). While many models use only one group, multiple-group models more realistically represent trophic interactions since, for example, herbivorous zooplankton can be distinguished from carnivorous species. However, multi-group models require more coefficients and model parameters, as well as more detailed information for model calibration.

Zooplankton dynamics are governed by the same general processes as phytoplankton: growth, respiration and excretion, predation, and nonpredatory mortality. The major difference is that zooplankton are not subject to settling losses since they are motile and migrate vertically in the water column, typically in a diurnal pattern. As a result, zooplankton are usually simulated using the same types of equations and formulations as used for phytoplankton. The general zooplankton equation which forms the basis of almost all models is:

$$\frac{dZ}{dt} = (g_z - r_z - m_z) Z - G_z$$
(7-1)

where Z = zooplankton biomass or equivalent nutrient mass, mass or mass/volume

- g_ = gross growth rate, 1/time
- r, = respiration and excretion rate, 1/time
- m_ = nonpredatory mortality rate, 1/time
- G_z = loss rate due to predation, mass/time or mass/volume-time

The above equation treats zooplankton populations as a biomass pool. Zooplankton population models have also been developed which partition the population into a series of age classes, including all important developmental stages from eggs to adults. Growth, respiration, mortality, and reproduction are computed separately for each life stage. Both changes in numbers and changes in the average weights of each age class are typically included in the model structure. While this approach may give a more realistic representation of zooplankton population dynamics, it is generally too detailed to be used in general water quality modeling. As a result, most models use the biomass pool approach, both because it is simpler and because it is consistent with the phytoplankton and nutrient formulations typically used.

As with phytoplankton models, the major differences between zooplankton models are the number of zooplankton groups, the formulations used for each process, and the way in which various processes are combined. Some of these features are compared in Table 7-1 for several zooplankton models. Process formulations are discussed in the following sections.

## 7.2 TEMPERATURE EFFECTS

Most models include temperature response relationships for essentially all processes affecting zooplankton. Growth, consumption, respiration, and

<u> </u>	Number of Groups			Zooplankton Processes Computed Separately in Model			Zooplankton Units				
Model (Author)	Zoo- plankton	Phyto- plankton	Fish	Growth	Respiration	Nonpredatory Mortality	Predatory Mortality	Dry Wt. Biomass	Carbon	Other Nutrient	Reference
AQUA-IV	1	1		X	x	X			x		Baca & Arnett (1976)
CE-QUAL-R1	1	2	3	x	X	x	x	x			WES (EWQOS) (1982)
CLEAN	3	2	3	x	x	x	X	x			Bloomfield <u>et al</u> . (1973)
CLEANER	3	3	3	x	x	x	x	х			Scavia & Park (1976)
MS.CLEANER	5	4	8	х	X	x	x	х			Park <u>et al</u> . (1980)
EAM	3	4	20	х	x	x	x	х			Tetra Tech (1979, 1980)
ESTEC0	1	2	3	х	x	x	x	x			Brandes & Masch (1977)
EXPLORE-1	1	1		х	x	x			x		Baca <u>et al</u> . (1973)
HSPF	1	1		х	x	x		x			Johanson <u>et al</u> . (1980)
LAKECO	1	2	3	х	x	X	x	х			Chen & Orlob (1975)
MIT Network	1	1		x	х	X				N	Harleman <u>et al</u> . (1977)
WASP	2	2		X	X	X	x		x		Di Toro <u>et al</u> . (1981)
WQRRS	1	2	3	x	x	X	x	x			Smith (1978)
Bierman	2	5		x	X	Х		х			Bierman <u>et al</u> . (1980)
Салаје	9	4		x	x	x	x		X		Canale <u>et al</u> . (1975, 1976)
Jorgensen	1	1	1	x	X	x	x	x			Jorgensen (1976)
Scavia	6	5		x	X	X	X		X		Scavia <u>et al</u> . (1976)

# TABLE 7-1. GENERAL COMPARISON OF ZOOPLANKTON MODELS

nonpredatory mortality are generally direct functions of temperature, and predation is indirectly related through temperature effects on the consumption rates of zooplankton predators. In most models, the temperature response formulations used for zooplankton are identical to those used for phytoplankton, and the same temperature function is generally used for all processes affecting a given zooplankton group. The major differences in the response functions between different organisms are the particular coefficient values used to define the shapes and slopes of the response curves, the optimum temperatures, and the upper and lower lethal limits. A few models use different formulations for each process. For example, CE-QUAL-R1 (WES, 1982) uses an optimum curve for growth, a logistic equation for respiration, and a reverse logistic equation for nonpredatory mortality.

The various formulations used to define temperature effects are described in detail in the algal growth section of the report (Section 6.3.1), and they will not be repeated here. In general, all formulations can be classified as either linear response curves, exponential response curves, or temperature optimum curves which exhibit maximum process rates at the optimum temperature and decreasing rates as the temperature moves away from the optimum.

#### 7.3 GROWTH

Zooplankton growth formulations represent increases in the biomass of the population due to both reproduction and the growth of individuals. The growth rate depends on the amount of food which is ingested and assimilated, and is therefore a function of food densities, ingestion rates, and assimilation efficiencies. Part of the assimilated food goes into individual growth and metabolic losses, and part goes into reproduction.

Both ingestion rates and assimilation efficiencies vary according to many factors, including (Leidy and Ploskey, 1980):

 Zooplankton factors such as species, age, size, feeding type, sex, reproductive state, and physiological or nutritional state

- Food related factors such as food concentration, type, particle size, quality, and desirability of the food
- Temperature

Ingestion rates also vary on a diurnal basis, with maximum feeding rates typically occurring at night. Peak nighttime grazing rates have been shown to range from 2 to 27 times the minimum daytime rates (Leidy and Ploskey, 1980).

Almost all zooplankton growth formulations are based on the following fundamental relationship:

$$g_z = C_q E \tag{7-2}$$

where  $g_{z} = zooplankton growth rate, 1/time$ 

 $C_g$  = ingestion or grazing rate, mass food/mass zooplankton-time

E = assimilation efficiency, fraction

Since most zooplankton are filter feeders, the ingestion rate is often expressed in terms of a volumetric filtration rate multiplied times the total available food concentration. In this case, the above equation becomes:

$$g_{T} = C_{f} F_{T} E$$
 (7-3)

where C_f = zooplankton filtration rate, water volume/mass zooplanktontime F_T = total available food concentration, mass/volume

For raptorial feeders, the previous equation (Equation (7-2)) is generally used.

The simplest growth formulations assume constant filtration rates and assimilation efficiencies (Figure 7-1). For this situation, the growth rate


#### FOOD CONCENTRATION, FT

Figure 7-1. Growth rate and grazing rate as a function of food supply for zooplankton with constant filtration rates and assimilation efficiencies (adapted from Leidy and Ploskey, 1980).

is directly proportional to the food supply. More sophisticated models include more complex formulations for the ingestion (or filtration) rates and the assimilation efficiencies to account for variability due to factors like food densities, food types, different feeding methods, and temperature effects on feeding and growth (Canale <u>et al.</u>, 1975, 1976; Scavia <u>et al.</u>, 1976; Scavia, 1980; Scavia and Park, 1976; Park <u>et al.</u>, 1975, 1979, 1980). The effects of food density and temperature on zooplankton growth rates can be expressed in general functional form as:

$$g_z = C_{gmax}(T_{ref}) E_{max}(T_{ref}) f(T) f_g(F_1, F_2, \dots F_n)$$
 (7-4)

or

$$g_z = C_{fmax}(T_{ref}) E_{max}(T_{ref}) f(T) F_T f_f(F_1, F_2, \dots F_n)$$
 (7-5)

where  $C_{gmax}(T_{ref})$  = maximum ingestion rate at reference temperature  $T_{ref}$  under conditions of saturated feeding (excess food supply), mass food/mass zooplankton-time

- C_{fmax}(T_{ref}) = maximum filtration rate at reference temperature T_{ref}, water volume/mass zooplankton-time
- E_{max}(T_{ref}) = maximum assimilation efficiency at reference temperature T_{ref}, fraction
- f(T) = temperature function for ingestion or filtration and assimilation
- $f_g(F_1, F_2, \dots, F_n) =$  growth limitation factor for ingestion formulation (Equation (7-2)) accounting for food density effects on ingestion rates and/or assimilation rates (where  $F_1, F_2, \dots, F_n$  are the concentrations of the potential food items)
- $f_f(F_1, F_2, \dots, F_n)$  = growth limitation factor for filtration formulation (Equation (7-3)) accounting for food density effects on filtration rates and/or assimilation rates

In some models, the maximum ingestion rate and the maximum assimilation efficiency are combined into a single parameter representing the maximum growth (or assimilation) rate (Chen and Orlob, 1972, 1975; Chen <u>et al.</u>, 1975; Jorgensen, 1976; Jorgensen <u>et al.</u>, 1978, 1981, 1983; Najarian and Harleman, 1975; Smith, 1978; WES, 1982; Tetra Tech, 1979). In this case, Equation (7-4) becomes:

$$g_{z} = g_{max}(T_{ref}) f(T) f_{g}(F_{1}, F_{2}, \dots F_{n})$$
 (7-6)

where  $g_{max}(T_{ref})$  = maximum zooplankton growth rate at reference temperature  $T_{ref}$ , 1/time

Maximum consumption rates, filtration rates, and growth rates are presented in Tables 7-2, 7-3, and 7-4, respectively.

Zooplankton Group	Maximum Consumption Rate (1/day)	References
Total Zooplankton	0.8	Scavia & Park (1976)
2007 14	0.35 - 0.50	Bierman (1976)
	0.24 1.2**	Collins & Wlosinski (1983)
Omnivores	1.4	Scavia (1980) Bowie <u>et al</u> . (1980)
	0.43	Canale <u>et</u> <u>al</u> . (1976)
Carnivores	1.6	Scavia <u>et</u> <u>al</u> . (1976)
	0.7	Canale <u>et</u> <u>al</u> . (1976)
Fast Ingesters	0.7	Bierman <u>et al</u> . (1980)
Slow Ingesters	0.1	Bierman <u>et al</u> . (1980)
Cladocerans	1.6 1.9	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.045 13.8**	Leidy & Ploskey (1980)
	0.045 2.3**	Collins & Wlosinski (1983)
Copeods	1.7 1.8	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.10 0.47**	Collins & Wlosinski (1983)
Rotifers	1.8 2.2	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	3.44**	Leidy & Ploskey (1980)
	3.44**	Collins & Wlosinski (1983)
Mysids	1.0 - 1.2	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)

# TABLE 7-2. ZOOPLANKTON MAXIMUM CONSUMPTION RATES

**Literature values.

Zooplankton Group	Maximum Filtration Rate	Units	References
Total Zooplankton	0.13 1.2	1/mgC-day	Di Toro <u>et al</u> . (1971) O'Connor <u>et al</u> . (1975, 1981)
	0.05 - 0.2*	l/mgC-day	<b>Baca &amp; Arnett</b> (1976)
	0.8 1.10**	l/mg(D.W.)-day	Di Toro <u>et</u> <u>al</u> . (1971)
Herbivores	0.7 - 1.4	1/mgC-day	Thomann <u>et al</u> . (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et</u> <u>al</u> . (1983)
Carnívores	1.0 3.9	1/mgC-day	Thomann <u>et al</u> . (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
Cl <b>adoc</b> erans	3.5 4.0	l/mg(D.W.)-day	Canale <u>et</u> <u>al</u> . (1976)
	0.2 1.6**	1/mg(D.W.)-day	Di Toro <u>et al</u> . (1971)
	0.192 0.682**	1/mg(D.₩.)-day	Lombardo (1972)
	0.2 1.6**	1/mg(D.W.)-day	Jorgensen (1979)
	0.009 177**	ml/animal-day	Leidy & Ploskey (1980)
	0.18 9.4**	ml/animal-day	Wetzel (1975)
	0.18 9.4**	ml/animal-day	Jorgensen (1979)
Copepods	1.0 6.5	1/mg(D.W.)-day	Canale <u>et</u> <u>al</u> . (1976)
	0.05 - 2.2**	1/mg(D.₩.)-day	Di Toro <u>et al</u> . (1971)
	0.161 2.21**	l/mg(D.W.)-day	Lombardo (1972)
	0.05 2.2**	l/mg(D.W.)-day	Jorgensen (1979)
	0.02 - 4.1**	ml/animal-day	Wetzel (1975)
	0.02 - 5.28**	ml/animal-day	Jorgensen (1979)
	0.006 35.**	ml/animal-day	Leidy & Ploskey (1980)
Rotifers	0.6 1.5**	1/mg(D.₩.)-day	Di Toro <u>et al</u> . (1971)
	0.6 - 1.5**	ml/animal-day	Jorgensen (1979)
	0.007 0.576**	ml/animal-day	Leidy & Ploskey (1980)

### TABLE 7-3. ZOOPLANKTON MAXIMUM FILTRATION RATES

*Model documentation values.

**Literature values.

The temperature function f(T) in the above equations uses the same types of formulations discussed previously for phytoplankton. Experimental results suggest optimum type response curves for short term changes in temperature, but more of a linear response curve when acclimation has time to occur (Leidy and Ploskey, 1980). Work by Geller (1975) indicates acclimation times may range from 4 to 6 weeks, which is short enough for zooplankton to acclimate to the typical seasonal variations in temperature, but not to rapid changes (for example, thermal plume effects). However, since feeding is expected to slow down or cease as the temperature approaches the upper lethal limit, an optimum type response curve is appropriate if it is skewed so that the optimum occurs near the upper lethal limit. Table 7-5 presents a comparison of the temperature adjustment functions used in several zooplankton models.

Zooplankton Group	Maximum Growth Rate (1/day)	References
Total Zooplankton	0.15 0.25	Chen (1970) Chen & Orlob (1975) Chen & Wells (1975, 1976)
	0.175 0.2	Jorgensen (1976) Jorgensen <u>et al</u> . (1978)
	0.1 0.3*	U.S. Army Corps of Engineers (1974) Brandes (1976) Smith (1978)
	0.15 0.30**	Jorgensen (1979)
Cladocerans	0.35 0.5	Tetra Tech (1980) Porcella <u>et al</u> . (1983)
	0.27 0.74**	Jorgensen (1979)
Copepods	0.5	Tetra Tech (1980)
Rotifers	0.44 0.45	Porcella <u>et al</u> . (1983)
	0.24 - 0.76**	Jorgensen (1979)
Mysids	0.14	Tetra Tech (1980)

#### TABLE 7-4. ZOOPLANKTON MAXIMUM GROWTH RATES

*Model documentation values.

**Literature values.

#### TABLE 7-5. COMPARISON OF TEMPERATURE ADJUSTMENT FUNCTIONS FOR ZOOPLANKTON GROWTH AND CONSUMPTION

	Tempera	ature Formulation	n (Equation	No.)		
Model (Author)	Linear	Exponential	Optimum Curve	Other Curve	Reference Temperature	Reference
AQUA-IV				none		Baca & Arnett (1976)
CE-QUAL-R1			6-24		T _{opt}	WES (EWQOS) (1982)
CLEAN			6-19		Topt	Bloomfield <u>et al</u> . (1973)
CLEANER			6-19		T _{opt}	Scavia & Park (1976)
MS.CLEANER			6-19		T _{opt}	Park <u>et</u> <u>al</u> . (1983)
EAM			6-24		T _{opt}	Tetra Tech (1979, 1980)
ESTECO		6-14			20 ⁰ C	Brandes & Masch (1977)
EXPLORE-1	X				1 ⁰ C	Baca <u>et al</u> . (1973)
HSPF		6-14			20 ⁰ C	Johanson <u>et al</u> . (1980)
LAKECO		6-14			20 ⁰ C	Chen & Orlob (1975)
MIT Network			6-25		T _{opt}	Harleman <u>et al</u> . (1977)
WASP	Х				1°C	Di Toro <u>et al</u> . (1981)
WQRRS			6-24		T _{opt}	Smith (1978)
Bierman		х			20 ⁰ C	Bierman <u>et al</u> . (1980)
Canale	piecewise linear				1 ⁰ C	Canale <u>et</u> <u>al</u> . (1975, 1976)
Jorgensen			6-18		T _{opt}	Jorgensen (1976)
Scavia			6-19		T _{opt}	Scavia <u>et al</u> . (1976)

#### 7.3.1 Growth Limitation

The growth limitation functions used in the above equations,  $f_g(F_1, F_2, \dots F_n)$  and  $f_f(F_1, F_2, \dots F_n)$ , are somewhat different since the latter function is multiplied times the total available food concentration  $F_T$  to give the net grazing rate. Therefore:

$$f_{g}(F_{1},F_{2},...F_{n}) \approx f_{f}(F_{1},F_{2},...F_{n}) F_{T}$$
 (7-7)

Both functions typically represent some type of saturation response to feeding, assimilation, and growth. Experimental observations show that at low food concentrations, zooplankton ingestion rates increase with increases in the food supply. For filter feeders which are filtering water at a constant rate, the grazing rate is directly proportional to the food concentration (Figure 7-1). Grazing rates for predatory zooplankton also increase with the food supply at low food concentrations since less energy and time are required to find and capture prey items as the prey density increases. However, as food becomes more abundant, the grazing rates eventually become saturated and level off at some maximum value after which the grazing rate becomes independent of the food supply. Filter feeders can regulate their ingestion rates at high food levels by reducing their filtering rates as the food concentration increases. At low concentrations, the feeding rate is limited by the ability of the zooplankton to filter water, while at high concentrations, it is limited by the ability to ingest and digest the food (Leidy and Ploskey, 1980). Similarly, the feeding rates for carnivorous zooplankton are limited at low prey densities by the ability of the zooplankton to find and capture prey items, while at high prey densities, they are limited by the ability to process, ingest, and digest the prey. Also, at very high ingestion rates, zooplankton growth may be limited by assimilation rates since ingested food remains in the gut for less time, resulting in only partial digestion and reduced assimilation efficiencies.

While the saturation type feeding response has been demonstrated in numerous studies, work by Mayzaud and Poulet (1978) indicates that zooplankton may be able to acclimate to changing food concentrations by adjusting their digestive enzyme levels, allowing them to filter at maximum rates over a much wider range than suggested by the saturation response curves of short term experiments (Leidy and Ploskey, 1980). This results in a linear response curve with ingestion rates directly proportional to the food supply. However, some upper limit on feeding and growth must exist based on theoretical arguments, so a saturation response curve is probably appropriate, even though the saturating food levels may be much higher than

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typically experienced in the field except perhaps during phytoplankton blooms.

Two major approaches are used to simulate saturation responses in zooplankton models, the Michaelis-Menten (1913) formulation and the Ivlev (1966) formulation. The Michaelis-Menten formulation is a hyperbolic function analagous to that used in phytoplankton growth calculations, and is probably the most common approach used in water quality models (Chen and Orlob, 1972, 1975; Di Toro and Connolly, 1980; Di Toro and Matystik, 1980; Bloomfield <u>et al</u>., 1973; Park <u>et al</u>., 1974, 1975, 1979, 1980; Scavia <u>et al</u>., 1976; Scavia, 1980; Canale <u>et al</u>., 1975, 1976; Bierman, 1976; Bierman and Harleman, 1975). The basic equation is:

$$f_{g}(F_{1}, F_{2}, \dots F_{n}) = \frac{F_{T}}{K_{z} + F_{T}}$$
 (7-8)

where F_T = total available food supply, mass/volume
K_z = half-saturation constant for zooplankton feeding and
growth, mass/volume

The Ivlev formulation is an exponential function which is more popular in biologically oriented models (Kremer and Nixon, 1978). The general equation is:

$$f_g(F_1, F_2, \dots F_n) = 1 - e^{-K F_T}$$
 (7-9)

where K = proportionality constant for Ivlev formulation

Figure 7-2 shows a comparison of the Michaelis-Menten and Ivlev functions where both functions have the same half-saturation value (i.e.,  $K = -\ln(\frac{1}{2})/K_z$ ). Both response functions range from minimum values of 0 at very low food concentrations to maximum values of 1 at food saturation. However, for food concentrations below the half-saturation constant ( $K_z$ ), the Ivlev function is slightly lower than the Michaelis-Menten function. For food concentrations above  $K_z$ , the Ivlev function is higher and approaches saturation sooner than the Michaelis-Menten function. Note that both functions are used with the total ingestion form of the growth equation (Equation (7-4)) rather than with the filtration form (Equation (7-5)), since the growth limitation function in the filtration form must always be multiplied times the total food supply to get the net response.

Both the Michaelis-Menten and Ivlev formulations can be modified to allow for threshold food concentrations below which zooplankton do not feed. This provides a refuge for prey organisms when they are present in very low concentrations. The resulting equations are:



Figure 7-2. Comparison of the Ivlev and Michaelis-Menten functions with the same half-saturation value (i.e.,  $K = -\ln(\frac{1}{2})/K_Z$ ) (adapted from Swartzman and Bentley, 1977, and Leidy and Ploskey, 1980).

$$f_{g}(F_{1},F_{2},...F_{n}) = \frac{F_{T} - F_{o}}{K_{z} + (F_{T} - F_{o})}$$
 (7-10)

$$f_{g}(F_{1},F_{2},...F_{n}) = \frac{F_{T} - F_{o}}{K_{z} + F_{T}}$$
 (7-11)

and 
$$f_g(F_1, F_2, \dots, F_n) = 1 - e^{-K(F_T - F_0)}$$
 (7-12)

Zooplankton half-saturation constants and threshold feeding levels are presented in Tables 7-6 and 7-7.

A few models, for example CLEAN, CLEANER, and MS.CLEANER (Bloomfield et al., 1973; Park et al., 1974, 1975, 1979, 1980; Scavia and Park, 1976), use a modified Michaelis-Menten formulation in which the half-saturation constant varies as a function of zooplankton densities to account for competition and feeding interference effects. The equation is:

$$K_{z} = K_{z1} + K_{z2} Z$$
 (7-13)

where  $K_{z1}$  = feeding area coefficient, mass/volume  $K_{z2}$  = competition or interference coefficient

Other saturation response functions besides the Michaelis-Menten and Ivlev formulations have been used in some models. For example, rectilinear saturation curves have been constructed by assuming feeding increases linearly with food concentration until a critical food density is reached, and then levels off at a maximum rate for all concentrations above the critical density. This is expressed as:

$$f_{g}(F_{1},F_{2},...F_{n}) = \frac{F_{T}}{F_{sat}} \quad \text{for } F_{T} < F_{sat} \quad (7-14)$$
$$= 1 \quad \text{for } F_{T} \ge F_{sat}$$

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Zooplankton Group	Half-Saturation Constant***	Units	References
Total Zooplankton	0.010 0.060	mg(Chl <u>a</u> )/]	Di Toro <u>et al</u> . (1971) O'Connor <u>et al</u> . (1975, 1981)
	0.5 (growth)	mg/l	Chen (1970) Chen & Orlob (1975) Chen & Wells (1975, 1976)
	0.5 - 2.0	mg/l	Jorgensen (1976) Jorgensen <u>et</u> <u>al</u> . (1978)
	1.0	mg/l	Bierman <u>et al</u> . (1980)
	0.2 0.6* (growth)	mg/1	U.S. Army Corps of Engineers (1974) Brandes (1976) Smith (1978)
	0.06 0.6*	mg/l	Baca & Arnett (1976)
Herbivores	0.010 0.015	mg(Chl <u>a</u> )/l	Thomann <u>et al</u> . (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
Carnivores	0.010	mg(Chl <u>a</u> )/l	Thomann <u>et al</u> . (1975)
	0.02	mgC/l	Scavia <u>et al</u> . (1976)
	0.2	mgC/l	Canale <u>et al</u> (1976)
Omnivores	0.2	mgC/l	Canale <u>et</u> <u>al</u> . (1976)
	0.15	mgC/1	Scavia (1980)
	0.375	mg/1	Bowie <u>et</u> <u>al</u> . (1980)
Cladocerans	0.16 0.2	mgC/l	Scavia <u>et al</u> . (1976) Scavia (1980)
	0.5	mg/l	Bowie <u>et al</u> . (1980)
	0.8 (growth)	mg/l	Tetra Tech (1980)
	1.8 (growth)	mg/1	Porcella <u>et al</u> . (1983)
Copepods	0.16 0.4	mgC/1	Scavia <u>et al</u> . (1976) Scavia (1980)
	1.0	mg/l	Bowie <u>et al</u> . (1980)
	1.2 (growth)	mg/l	Tetra Tech (1980)
Rotifers	0.2 0.6	mgC/l	Scavia <u>et al</u> . (1976) Scavia <u>(1980</u> )

# TABLE 7-6. MICHAELIS-MENTEN HALF-SATURATION CONSTANTS FOR ZOOPLANKTON CONSUMPTION AND GROWTH

Zooplankton Group	Half-Saturation Constant***	Units	References
	0.5	mg/l	Bowie <u>et al</u> . (1980)
	2.0 (growth)	mg/l	Porcella <u>et</u> <u>al</u> . (1983)
Mysids	0.10 0.20	mgC/1	Scavia <u>et a</u> l. (1976) Scavia (1980)
	0.5	mg/l	Bowie <u>et al</u> . (1980)
	2.0 (growth)	mg/l	Tetra Tech (1980)

*Model documentation values.

***Half-saturation constants are for consumption unless specified for growth.

## 

or

$$f_{g}(F_{1},F_{2},\ldots F_{n}) = \frac{F_{T} - F_{o}}{F_{sat} - F_{o}} \quad \text{for } F_{T} < F_{sat} \quad (7-15)$$

= 1 for  $F_T \ge F_{sat}$ 

when a threshold feeding concentration  ${\rm F}_{\rm O}$  is used.

The growth limitation functions used with the filtration form of the growth equation (Equation (7-5)) are different than the saturation response functions discussed above since they must be multiplied by the available food concentration to get the total response. In contrast to the previous functions, these functions generally decrease with increases in the food supply to account for factors like reduced filtering rates, adjustments in particle size selectivity, and reduced assimilation efficiencies which occur at high food concentrations. These types of functions generally have maximum values of 1 at low food densities and decrease assymptotically toward some minimum value as the food density increases.

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Di Toro and Matystik (1980) and Di Toro and Connolly (1980) use a reverse Michaelis-Menten formulation to simulate reductions in filtration rates as food concentration increases:

$$f_{f}(F_{1}, F_{2}, \dots F_{n}) = 1 - \frac{F_{T}}{F_{T} + K_{f}}$$

$$= \frac{K_{f}}{F_{T} + K_{f}}$$
(7-16)

where K_f = food concentration at which the filtration rate is 1/2 of
 its maximum value, mass/volume

Zooplankton Group	Threshold Feeding Level	References
Total Zooplankton	0.028 mg/1	Scavia & Park (1976)
	0.01 mg/1	Youngberg (1977)
	0.20 mg/1	Bierman <u>et</u> <u>al</u> . (1980)
Carnivores	0.01 mgC/1	Scavia <u>et al</u> . (1976)
Omnivores	0.001 mgC/1	Scavia (1980)
	0.025 mg/1	Bowie <u>et al</u> . (1980)
Cladocerans	0.02 0.05 mgC/1	Scavia <u>et a</u> l. (1976) Scavia (1980)
	0.05 mg/1	Bowie <u>et</u> <u>al</u> . (1980)
Copepods	0.02 0.05 mgC/1	Scavia <u>et al</u> . (1976) Scavia (1980)
	0.05 mg/1	Bowie <u>et</u> <u>al</u> . (1980)
Rotifers	0.02 - 0.05 mgC/1	Scavia <u>et al</u> . (1976) Scavia (1980)
	0.05 mg/1	Bowie <u>et</u> <u>al</u> . (1980)
Mysids	0.02 0.05 mgC/1	Scavia <u>et al</u> . (1976) Scavia (1980)
	0.05 mg/1	Bowie <u>et al</u> . (1980)

TABLE 7-7. THRESHOLD FEEDING LEVELS FOR ZOOPLANKTON

This function approaches O assymptotically at high food densities, resulting in a saturation response for total consumption (Figure 7-3a).

Canale <u>et al</u>. (1975, 1976) use a slightly different formulation to account for reductions in filtering rates and changes in particle size selectivity at high food levels:

$$f_f(F_1, F_2, \dots, F_n) = \frac{K_1 F_T + K_2}{F_T + K_2}$$
 (7-17)

where  $K_1$  = multiplier for minimum filtering rate (minimum value of  $f_f$ )  $K_2$  = food concentration at which the filtering rate is half way between its minimum and maximum value,  $f_f = 1/2$  ( $K_1 + 1$ ), mass/volume

This function approaches  $K_1$  assymptotically at high food levels rather than O. As a result, the total consumption rate continues to increase in proportion to the food supply at high food concentrations since the volumetric filtration rate remains at a constant minimum level (Figure 7-3b). However, a saturation type response can be generated by setting the minimum multiplier  $K_1$  equal to 0, in which case this formulation is identical to Equation (7-16).

A reverse Michaelis-Menten formulation has also been used to simulate reductions in the assimilation efficiencies of filter feeders at high food concentrations (Di Toro <u>et al.</u>, 1971, 1977; Di Toro and Matystik, 1980; Di Toro and Connolly, 1980; Thomann <u>et al.</u>, 1975, 1979; Canale <u>et al.</u>, 1975, 1976). The equation is:

$$f_{f}(F_{1}, F_{2}, \dots, F_{n}) = \frac{K_{a}}{F_{T} + K_{a}}$$
 (7-18)

where  $K_a$  = food concentration at which the assimilation efficiency is 1/2 of its maximum value, mass/volume





FOOD CONCENTRATION, F_T (b)

Figure 7-3. Comparison of reverse Michaelis-Menten formulation (a) and Canale et al.'s (1975, 1976) formulation (b) for filtration rate as a function of food concentration.

If a constant volumetric filtration rate is used (Di Toro <u>et al.</u>, 1971, 1977; Canale <u>et al.</u>, 1975, 1976), this results in a Michaelis-Menten type relationship for total consumption in which the maximum assimilation rate (growth rate) equals the product of the constant filtration rate, maximum assimilation efficiency, and the food concentration at half-maximum assimilation efficiency  $K_a$  (ignoring temperature effects):

$$g_{z} = C_{fmax} E_{max} F_{T} \left( \frac{K_{a}}{F_{T} + K_{a}} \right)$$
$$= C_{fmax} E_{max} K_{a} \left( \frac{F_{T}}{K_{a} + F_{T}} \right)$$
(7-19)

However, Di Toro and Matystik (1980) and Di Toro and Connolly (1980) also use this formulation with a reverse Michaelis-Menten formulation for the filtration rate, which results in a more complicated expression for total consumption involving the product of a Michaelis-Menten term and a reverse Michaelis-Menten term:

$$g_z = C_{fmax} E_{max} K_a \left( \frac{F_T}{K_a + F_T} \right) \left( \frac{K_f}{K_f + F_T} \right)$$
 (7-20)

Zooplankton growth and consumption formulations are compared for several models in Table 7-8.

#### 7.3.2 Food Supply

The total available food concentration  $F_T$  used in all of the above growth formulations can be defined in several ways. The simplest approach is to assume all potential food items can be consumed with equal efficiency and define  $F_T$  as the sum of the available food concentrations:

$$F_{T} = \sum_{k=1}^{n} F_{K}$$
 (7-21)

		Food	Sources			Basic Approa	ch		Growt	h Limitation Fo	ormulation		Assimi	lation Effic	iency
Model (Author)	Phyto- plankton	Detritus	Zoo- plankton	Preference Factors Used	Growth Computed Directly	Total Ingestion Computed	Filtration Rate Computed	Michaelis- Menten	Ivlev	Variable Assimilation Efficiency	Variable Filtration Rate	Threshold Feeding Included	Constant	Varies with Food Type	Varies with Food Conc.
AQUA-IV	1					x		X					X		
CE-QUAL-R1	2	1		x		x		x					x		
CLEAN	2	1	3	x		x		x				x		x	
CLEANER	3	1	3	x		x		x				x		x	
MS.CLEANER	4	2	5	x		raptorial feeders	filter feeders	raptors & saturation filterers		X*		x		X	
EAM	4	1	3	x				x					X		
ESTEC0	2	1		x	x	~		x					x		
EXPLORE-1	1				ŀ	x		x					x		
HSPF	1						x			x					X
LAKECO	2	ı		x	l			x					x		
MIT Network	<b>(</b> 1				x			x					x		
WASP	2		1				x			x	x		1		X
WQRRS	2	1		x	x			x					X		
Bierman	5			X		x		x				x	x		
Canale	4		9	x		carnivores	filter feeders	carnivores		nonselective filterers	selective filterers		carnivores & se tive filterer	ec-	nonselective filterers
Jorgensen	1				x			x				x	x		
Scavia	5	1	6	x		X		X				x		X	

## TABLE 7-8. COMPARISON OF ZOOPLANKTON GROWTH FORMULATIONS

"Maximum assimilation rate used for constant rate filters, with excess consumption egested as pseudofeces.

where  $F_k$  = concentration of potential food item k, mass/volume n = total number of potential food items

A more realistic approach recognizes that food items vary in the efficiency and frequency at which they are utilized by zooplankton, even if all food items are present in equal concentrations. This is due to factors such as food particle size and shape, desirability and quality of different types of food, ease of capture, and zooplankton feeding behavior. For example, many filter feeders are able to selectively filter different food items with different efficiencies, varying their selectivity according to the abundance and desirability of the various food items present. Food particle shape and size are important distinguishing features since, for example, filamentous algae are often actively rejected or avoided while individual cells of the same species in suspension may be consumed (Leidy and Ploskey, 1980). However, the quality and desirability of the food are also important, since senescent cells are less likely to be consumed than healthy cells of the same species. For raptorial feeders, particle size and shape are not quite as critical since they are able to tear large prey items into smaller pieces before consuming them. Prey desirability and ease of capture then become more important.

The above factors are accounted for in models by assigning feeding preference factors to each potential food item. Preference factors can have values ranging from 1 to 0, with 1 corresponding to a food item which is desirable and easily captured and consumed (or filtered), and 0 corresponding to a food item which is never consumed. Food preference factors have been called selectivity coefficients, electivities, ingestion efficiencies, and several other names in different models, but they all basically represent the same thing--weighting factors which reflect the probability that a given food item will be consumed relative to the others when all foods are present in equal concentrations. They account for the fact that some food items may be less available for consumption than indicated by their concentrations alone. When food preference factors are specified, the total available food concentration  $F_T$  is defined as:

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$$F_{T} = \sum_{k=1}^{n} P_{k} F_{k}$$
 (7-22)

where  $P_{i_k}$  = food preference factor for food item k

F_L = concentration of food item K, mass/volume

n = total number of potential food items

Vanderploeg and Scavia (1979) show how preference factors can be derived from the different forms of data reported in zooplankton feeding experiments. In field situations, preference factors may change as the composition of the food supply changes. However, this level of sophistication is generally not included in current ecological models.

#### 7.3.3 Assimilation Efficiencies

In addition to differences in food preferences or ingestion efficiencies for different food types, food items may also differ in their assimilation efficiency by zooplankton. The assimilation efficiencies for different food types varies with the energy content, digestibility, and quality of the food (Leidy and Ploskey, 1980). For example, the assimilation efficiencies for algae are typically higher than for detritus and bacteria, although the assimilation efficiencies for blue-green algae are also generally low. Algae with gelatinous sheaths or resistant cell walls and masses of colonial cells may pass through a zooplankton gut intact and in viable condition (Wetzel, 1975), indicating minimal assimilation efficiencies for these food items. The animal foods of raptorial feeders are assimilated more efficiently than plant foods. Also, since the energy content and digestibility of algae and detritus vary much more widely than animal foods, the assimilation efficiencies for herbivores and detritivores typically cover a much wider range than for carnivorous zooplankton (Leidy and Ploskey, 1980).

Variations in the assimilation efficiencies of different food items can be modeled in several ways. One approach is to incorporate these effects in the food preference factors, for example, by assigning a low value to the preference factor for blue-green algae relative to the other algal groups. This in effect lowers the amount of blue-green algae available for zooplankton assimilation and growth. Another approach is to define different maximum assimilation efficiencies for different food items, to compute net assimilation separately for each food item, and then to sum the individual assimilation terms to get the total zooplankton growth rate (Scavia <u>et al</u>., 1976; Scavia, 1980). This can be expressed for the total consumption formulation (Equation (7-4)) as (ignoring temperature effects):

$$g_{z} = C_{gmax} \sum_{k=1}^{n} \left[ E_{max_{k}} f_{g_{k}}(F_{1}, F_{2}, \dots F_{n}) \right]$$
 (7-23)

where 
$$C_{gmax}$$
 = maximum total consumption rate, mass food/mass  
zooplankton-time  
= maximum assimilation efficiency for food item  
k  
 $f_{g_k}(F_1, F_2, \dots F_n)$  = growth limitation factor for food item k  
n = total number of potential food items

and for the filtration formulation (Equation (7-5)) as:

$$g_{z} = C_{fmax} f_{f}(F_{1}, F_{2}, \dots F_{n}) \sum_{k=1}^{n} \left[ E_{max_{k}} P_{k} F_{k} \right]$$
 (7-24)

where  $C_{fmax}$  = maximum volumetric filtration, volume/mass zooplankton-time  $f_f(F_1, F_2, \dots F_n)$  = growth limitation function for filtration formulation  $P_k$  = food preference factor for food item k  $F_k$  = concentration of food item k, mass/volume

Note that growth limitation factors must be computed separately for each food item in the total consumption formulation since the quantities which are summed must reflect both the assimilation efficiencies and the amounts of food consumed for each different food item. For the Michaelis-Menten formulation, the individual growth limitation factor may be defined as:

$$f_{g_k}(F_1, F_2, \dots F_n) = \frac{\frac{P_k F_k}{K_z + \sum_{k=1}^{n} P_k F_k}}{K_z + \sum_{k=1}^{n} P_k F_k}$$
 (7-25)

n

This is equivalent to the total Michaelis-Menten factor when summed over all food items:

$$\sum_{k=1}^{n} f_{g_{k}}(F_{1}, F_{2}, \dots, F_{n}) = \sum_{k=1}^{n} \frac{P_{k} F_{k}}{K_{z} + \sum_{k=1}^{n} P_{k} F_{k}} = \frac{\sum_{k=1}^{n} P_{k} F_{k}}{K_{z} + \sum_{k=1}^{n} P_{k} F_{k}}$$
(7-26)

Analogous expressions for the Ivlev formulation are more difficult to formulate, since the individual terms are not consistent with the total growth limitation function, even under conditions of equal assimilation efficiencies.

As discussed previously, assimilation efficiencies may decrease with increases in ingestion rate at high food concentrations since the retention time in the gut decreases resulting in incomplete digestion and reduced assimilation. Model formulations to describe these effects have already been discussed in the growth limitation section (Equation (7-18)).

Zooplankton average assimilation efficiencies are presented in Table 7-9. Figures 7-4 and 7-5 present frequency histograms of assimilation efficiency data compiled by Leidy and Plosky (1980).

#### 7.4 RESPIRATION AND MORTALITY

Zooplankton respiration and mortality are modeled using the same general formulations as phytoplankton. Almost all models represent both respiration and nonpredatory mortality rates as either constant coefficients or simple functions of temperature. The basic equations are:

Zooplankton Group	Assimilation Efficiency	References
Total Zooplankton	0.60 - 0.75	Di Toro <u>et al</u> . (1971) O'Connor <u>et al</u> . (1975, 1981)
	0.63	Jorgensen (1976) Jorgensen <u>et al</u> . (1978)
	0.7	Tetra Tech (1976) Chen & Wells (1975, 1976)
	0.6	Bierman <u>et al</u> . (1980)
	0.5 0.8*	Brandes (1976) Smith (1978)
	0.5 0.7*	Baca & Arnett (1976)
<b>Herbivore</b> s	0.6 (max.)	Thomann <u>et al</u> . (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
Carnivores	0.6 (max.)	Thomann <u>et al</u> . (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
	0.5	Scavia <u>et al</u> . (1976)
	0.4 (Cladocerans)	Canale <u>et</u> <u>al</u> . (1976)
Omnivores	0.5 (0.2 for detritus, blue-green algae)	Scavia (1980) Bowie <u>et al</u> . (1980)
	0.4	Canale <u>et</u> <u>al</u> . (1976)
Cladocerans	0.5 (0.2 for detritus, blue-green algae)	Scavia <u>et a</u> l. (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.5	Tetra Tech (1980) Porcella <u>et al</u> . (1983)
	0.8 (max.)	Canale <u>et</u> <u>al</u> . (1976)
Copepo <b>ds</b>	0.5 (0.2 for detritus, blue-green algae)	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie et al. (1980)
	0.7	Canale <u>et al</u> . (1976)

## TABLE 7-9. ZOOPLANKTON ASSIMILATION EFFICIENCIES

Zooplankton Group	Assimilation Efficiency	References
Rotifers	0.5 (0.2 for detritus, blue-green algae)	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et</u> al. (1980)
	0.5	Tetra Tech (1980) Porcella <u>et</u> <u>al</u> . (1983)
Mysids	0.5 (0.2 for detritus, blue-green algae)	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.5	Tetra Tech (1980)

*Model documentation values.

$$r_z = r_z(T_{ref}) f_r(T)$$
 (7-27)

and

$$m_z = m_z(T_{ref}) f_m(T)$$
 (7-28)

where  $r_z = zooplankton respiration rate, 1/time$   $r_z(T_{ref}) = respiration rate at reference temperature T_{ref}, 1/time$   $f_r(T) = temperature function for respiration$   $m_z = zooplankton nonpredatory mortality rate, 1/time$   $m_z(T_{ref}) = nonpredatory mortality at reference temperature T_{ref}, 1/time$  $f_m(T) = temperature function for nonpredatory mortality$ 

Since the respiration and nonpredatory mortality rate equations have the same basic form and typically use the same temperature functions, many models combine both processes into a single loss term:

$$r_{z} + m_{z} = d_{z}(T_{ref}) f_{r}(T)$$
 (7-29)

where  $d_z(T_{ref})$  = total loss rate due to both respiration and nonpredatory mortality at reference temperature  $T_{ref}$ , 1/time 402



Figure 7-4. Frequency histograms for zooplankton assimilation efficiencies (from Leidy and Ploskey, 1980).

In a few models, the respiration rate is partitioned into two components, 1) the standard respiration rate representing the combined basal metabolism and digestion energetics and 2) the active respiration rate which represents the additional respiration associated with zooplankton activity. These two components can be distinguished by using different temperature response functions for each component. For example, standard respiration is



Figure 7-5. Frequency histograms showing variations in zooplankton assimilation efficiencies with different food types (from Leidy and Ploskey, 1980)

typically associated with an exponential temperature curve which increases until the upper lethal limit is approached, while the active respiration rate may be associated with a temperature optimum curve:

$$r = r_{std}(T_{ref}) f_s(T) + r_{act}(T_{ref}) f_a(T)$$
(7-30)

where  $r_{std}(T_{ref})$  = standard respiration rate at reference temperature  $T_{ref}$ , 1/day  $f_s(T)$  = temperature function for standard respiration  $r_{act}(T_{ref})$  = active respiration rate at reference temperature  $T_{ref}$ , 1/day  $f_a(T)$  = temperature function for active respiration

Another approach is to assume that the activity level (and active respiration) is proportional to the feeding level by using a Michaelis-Menten or Ivlev function:

$$r = r_{std}(T_{ref}) f_{s}(T) + r_{act}(T_{ref}) f_{a}(T) f(F_{1}, F_{2}, \dots, F_{n})$$
(7-31)

where  $f(F_1, F_2, \dots, F_n) = growth limitation factor as a function of food supply$ 

This approach is used by Scavia <u>et al</u>. (1976) and Scavia (1980) where the first term represents the minimum endogenous respiration rate under starvation conditions and the second term represents the increase in respiration associated with feeding.

A similar formulation is used in CLEANER (Scavia and Park, 1976) and MS.CLEANER (Park <u>et al.</u>, 1979, 1980) where the active respiration rate is expressed as a fraction of the total consumption rate:

$$r = \left[r_{min}(T_{ref}) + K_r C_g\right] f(T)$$
 (7-32)

where  $r_{min}(T_{ref})$  = minimum endogenous respiration under starvation conditions at reference temperature  $T_{ref}$ , 1/time K_r = fraction of ingested food which is respired C_g = ingestion rate, 1/time

The CLEANER and MS.CLEANER models also include additional factors to account for crowding effects and population age effects on both respiration and nonpredatory mortality rates. The crowding factor is expressed as:

$$f_{crd} = 1 + \frac{K_c Z}{Z_{cap}}$$
 (7-33)

- where  $f_{crd} = crowding factor$ 
  - K = crowding coefficient

Z_{cap} = zooplankton carrying capacity, mass or mass/volume

This factor increases the respiration and mortality rates as zooplankton density increases. The age factor accounts for the effects of the population age structure on the net respiration and mortality rates since these rates generally vary with age. The basic assumption is that the population consists primarily of immature individuals at low zooplankton densities and of adults at high population densities (Scavia and Park, 1976). The age factor represents the difference between adult and juvenile rates. The age factor for respiration is expressed as:

$$f_{rage} = 1 + K_{rx} \left( \frac{Z_{cap} - Z}{Z_{cap}} \right)$$
(7-34)

where f
rage = age factor for respiration
K
rx = fractional increase in respiration rate between young
zooplankton and adults

and the age factor for mortality is expressed as:

$$f_{mage} = 1 - K_{mx} \left( \frac{Z_{cap} - Z}{Z_{cap}} \right)$$
(7-35)

where  $f_{mage}$  = age factor for nonpredatory mortality

Both the crowding and age structure factors are multiplied with the respiration and nonpredatory mortality rates defined in Equations (7-32) and (7-28) to incorporate these effects into the rates.

Some versions of CLEANER (Youngberg, 1977) also include an oxygen reduction factor in the respiration equation to account for decreases in respiration at low dissolved oxygen levels. The equation is:

$$f_{ox} = \frac{0_2 - 0_{min}}{K_{ox} + (0_2 - 0_{min})}$$
(7-36)

where f_{ox} = oxygen reduction factor 0₂ = ambient oxygen concentration, mg/l 0_{min} = minimum oxygen requirement, mg/l K_{ox} = half-saturation constant for oxygen limitation (set at 0.9 mg/l)

Bierman <u>et al</u>. (1980) use a second order formulation for zooplankton mortality when the zooplankton density exceeds a critical level. This accounts for density dependent effects on both natural mortality and predatory mortality (which is not directly simulated in this model) at high densities. The equation is:

$$m = \left[ m_1(T_{ref}) + K_m(T_{ref}) Z \right] f(T)$$
 (7-37)

where  $m_1(T_{ref})$  = mortality rate below the critical zooplankton density at reference temperature  $T_{ref}$ , 1/time

 $K_m(T_{ref})$  = density dependent mortality coefficient for increased mortality above the critical zooplankton density at reference temperature  $T_{ref}$ , 1/mass zooplankton-time The nonpredatory mortality rate can also be partitioned into several components which account for specific types of mortality such as natural senescence, thermally-induced mortality, toxic mortality, and stress-induced mortality due to low dissolved oxygen, pH extremes, starvation, etc. The general equation is:

$$m_{z} = m_{z}(T_{ref}) f_{m}(T) + m_{T}(T_{ref}) f_{T}(T) + m_{x}(T_{ref}) f_{1}(T) f_{x}(X) + m_{s}(T_{ref}) f_{2}(T) f(0_{2}, pH, ...) + m_{f}(T_{ref}) f_{3}(T) + f_{f}(F_{T})$$
(7-38)

where	m _z (T _{ref} )	=	mortality rate due to senescence at reference
	2 0		temperature T _{ref} , 1/time
	f _m (T)	=	temperature function for senescent mortality
	m _T (T _{ref} )	=	thermal mortality rate at reference temperature
			T _{ref} , 1/time
	f _T (T)	=	thermal mortality response curve
	m _x (T _{ref} )	Ξ	toxic mortality rate at reference temperature
			T _{ref} , 1/time
	f ₁ (T)	Ξ	temperature function for toxic mortality
	$f_{x}(X)$	=	dose-response curve for toxic mortality
	X	Ξ	concentration of toxicant, mass/volume
	m _c (T _{rof} )	=	stress-induced mortality rate for low dissolved
	5 10		oxygen, pH extremes. etc., at reference temperature
			T _{ref} , 1/time
	f ₂ (T)	=	temperature function for stress-induced mortality
	f(0 ₂ ,pH)	Ξ	stress-induced mortality function for low dissolved
	L.		oxygen, pH extremes, etc.
	m _f (T _{ref} )	=	starvation-induced mortality rate at reference
			temperature T _{ref} , 1/time
	f ₃ (T)	=	temperature function for starvation mortality
	$f_{f}(F_{T})$	=	starvation mortality function

Various formulations could be used to define these effects, although most current models deal only with natural mortality and sometimes thermal effects. Zooplankton respiration rates and mortality rates are presented in Tables 7-10 and 7-11. Figures 7-6 and 7-7 present frequency histograms of respiration rates and nonpredatory mortality rates from data compiled by Leidy and Ploskey (1980).

#### 7.5 PRE DATORY MORTALITY

Zooplankton predatory mortality is modeled using the same formulations described previously for phytoplankton. However, since zooplankton are often the highest trophic level included in water quality models, predatorprey dynamics between zooplankton and higher trophic levels cannot usually be simulated. Therefore, predation by fish and carnivorous zooplankton is modeled by either assuming a constant predation loss which is specified as a model input parameter:

$$G_{z} = constant$$
 (7-39)

or by assuming a loss rate which is directly proportional to the zooplankton densities:

$$G_{7} = e_{7} Z$$
 (7-40)

or

$$G_z = e_z(T_{ref}) f_e(T) Z$$
 (7-41)

Since these formulations are essentially the same as those used for nonpredatory mortality, nonpredatory mortality and predation losses are

Zooplankton Group	Respiration Rate	Units	Temperature	References
Total Zooplankton	0.01	1/day	20 ⁰ C	Chen (1970) Chen & Orlob (1975) Chen & Wells (1975, 1976)
	0.02 - 0.035	1/day	20 ⁰ C	Jorgensen (1976) Jorgensen <u>et</u> <u>al</u> . (1978)
	0.36	1/day	20 ⁰ C	Lombardo (1972)
	0.02 0.16	1/day	20 ⁰ C	0'Connor <u>et al</u> . (1975)
	0.005 0.02	1/day	20 ⁰ C	Tetra Tech (1976)
	0.001 - 0.11*	1/day	20 ⁰ C	U.S. Army Corps of Engineers (1974) Brandes (1976) Smith (1978)
	0.005 0.3*	1/day	20 ⁰ C	Baca & Arnett (1976)
Herbivores	0.02 - 0.03	1/day	20 ⁰ C	Thomann et al. (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
Carnivores	0.007 - 0.02	l/day	20 ⁰ C	Thomann <u>et al</u> . (1975, 1979) Di Toro & Connolly (1980) Di Toro & Matystik (1980) Salisbury <u>et al</u> . (1983)
	0.30	1/day	Topt	Scavia <u>et</u> <u>al</u> . (1976)
	0.04 - 0.06	1/day	20 ⁰ C	Canale <u>et</u> <u>al</u> . (1976)
Omnivores	0.08 0.33	l/day	T _{opt}	Scavia (1980) Bowie <u>et</u> al. (1980)
	0.04 - 0.06	1/day	20 ⁰ C	Canale <u>et</u> <u>al</u> . (1976) [.]
Cladocerans	0.1 0.36	l/day	T _{opt}	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et</u> <u>al</u> . (1980)
	0.017 - 0.10	l/day	20 ⁰ C	Tetra Tech (1980) Porcella <u>et al</u> . (1983)
	0.04 - 0.06	1/day	20 ⁰ C	Canale <u>et al</u> . (1976)
	0.157 - 0.413**	1/day	20 ⁰ C	Lombardo (1972)
	0.090 0.216**	1/day	20 ⁰ C	Leidy & Ploskey (1980)
	0.006 0.772**	1/day	Topt	Collins & Wlosinski (1983)
	8.5 - 14.2**	m1 0 ₂ mg(D.W.)-day	18 ⁰ C	Di Toro <u>et</u> <u>al</u> . (1971)

## TABLE 7-10. ZOOPLANKTON RESPIRATION RATES

Zooplankton			<b>T</b>	Deference
Group	Respiration Rate	Units	Temperature	References
	5.4 14.2**	ml O ₂ mg(D.W.)-day	20 ⁰ C	Lombardo (1972)
	14.2**	m1 0 ₂ mg(D.W.)-day	20 ⁰ C	Jorgensen (1979)
Copepods	0.1 0.35	l/day	T _{opt}	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.04 0 <b>.06</b>	1/day	20 ⁰ C	Canale <u>et al</u> . (1976)
	0.017	1/day	20 ⁰ C	Tetra Tech (1980)
	0.085 - 0.550**	1/day	20 ⁰ C	Lombardo (1972)
	0.064 - 0.738**	1/day	20 ⁰ C	Leidy & Ploskey (1980)
	0.043 - 0.695**	1/day	T _{opt}	Collins & Wlosinski (1983
	3.0 12.2**	m1 0 ₂ mg(D.W.)-day	20 ⁰ C	Di Toro <u>et al</u> . (1971)
	2.93 - 18.9**	m1 0 ₂ mg(D.W.)-day	20 ⁰ C	Lombardo (1972)
	3.0 - 13.5**	m1 0 ₂ mg(D.W.)-day	20 ⁰ C	Jorgensen (1979)
Rotifers	0.12 0.40	l/day	T _{opt}	Scavia <u>et a</u> l. (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.15	1/day	20 ⁰ C	Porc <b>ella <u>et al</u>. (198</b> 3)
	0.163 0.677**	l/day	20 ⁰ C	Leidy & Ploskey (1980)
Mysids	0.05 0.28	l/day	T _{opt}	Scavia <u>et al</u> . (1976) Scavia (1980) Bowie <u>et al</u> . (1980)
	0.022	l/day	20 ⁰ C	Tetra Tech (1980)

*Model documentation values.

**Literature values.

often combined into a single total mortality term when higher trophic levels are not directly simulated:

$$m_{tot} = \left[ m_{z}(T_{ref}) + e_{z}(T_{ref}) \right] f_{m}(T)$$

$$= m_{tot}(T_{ref}) f_{m}(T)$$
(7-42)

In ecologically oriented models where long term seasonal changes in population dynamics are important, zooplankton are often separated into several functional groups based on general feeding types (filter feeders, carnivorous raptors, omnivores, etc.) or on major taxonomic groups (cladocerans, copepods, rotifers) (Canale <u>et al</u>., 1975, 1976; Scavia <u>et al</u>., 1976; Scavia, 1980; Park <u>et al</u>., 1974, 1975, 1979, 1980; Chen <u>et al</u>., 1975; Tetra Tech, 1979). Although several species must be lumped into each functional group, this approach recognizes the importance of complexities in the food web, different foraging strategies, and predator population dynamics in evaluating both zooplankton and phytoplankton dynamics. Several planktivorous fish groups are also sometimes provided for the same reasons. (Chen <u>et al.</u>, 1975; Tetra Tech, 1979; Park et al., 1979, 1980).

In these situations, zooplankton predation rates are computed as the sum of the consumption rates by all potential predators, including carnivorous or omnivorous zooplankton and planktivorous fish. The general relationship for predatory mortality can be expressed as:

$$G_{z_{i}} = \sum_{j=1}^{n_{p}} \left[ C_{j} X_{j} \frac{P_{ij} Z_{i}}{n_{j}} \right]$$
(7-43)  
$$\sum_{k=1}^{n_{p}} P_{kj} F_{kj}$$

P ij = food preference factor for predator group j feeding on zooplankton group i

Zooplankton Group	Mortality Rate (1/day)	Mortality Type	References
Tota] Zeeplankton	0.075	total	$\mathbf{D}$ i Toro et al (1971)
ZoopTankton	0.075	nonnadatony	$\frac{1}{1000} \frac{1}{20} \frac{1}{1000} $
	0.025 0.022	nonpredatory	$\frac{1970}{1970}$
	0.025 0.035	nonpredatory	$\frac{1}{2} \frac{1}{2} \frac{1}$
	0.005	nonpredatory	Chen and wells (1975, 1976)
	0.02	nonpredatory	
	0.015	total	0.00000  et al. (1981)
	0.005*	nonpredatory	U.S. Army Corps of Engineers (1974)
	0.001 - 0.005*	nonpredatory	Brandes (1976)
	0.005 - 0.02*	nonpredatory	Smith (1978)
	0.003 - 0.075**	total	Jorgensen (1979)
Carnivores	0.01	nonpredatory	Scavia <u>et al</u> . (1976)
	0.01	fish grazing	Scavia <u>et al</u> . (1976)
Omnivores	0.005	fish grazing	Scavia (1980)
Fast Ingesters	0.05	nonpredatory	Bierman <u>et al</u> . (1980)
Slow Ingesters	0.01	nonpredatory	Bierman <u>et al</u> . (1980)
Cladocerans	0.01	nonpredatory	Scavia <u>et al</u> . (1976)
	0.04 - 0.05	fish grazing	Scavia <u>et al</u> . (1976)
	0.001 - 0.005	fish grazing	Scavia (1980)
	0.01	nonpredatory	Tetra Tech (1980)
	0.1	nonpredatory	Porcella <u>et al</u> . (1983)
	0.0007 - 0.027**	nonpredatory	Leidy & Ploskey (1980)
	0.001 - 0.027**	nonpredatory	Collins & Wlosinski (1983)
Copepods	0.01	nonpredatory	Scavia <u>et</u> <u>al</u> . (1976)
	0.05	fish grazing	Scavia <u>et</u> <u>al</u> . (1976)
	0.002	fish grazing	Scavia (1980)
	0.003 - 0.005	nonpredatory	Canale <u>et</u> <u>al</u> . (1976)
	0.01	nonpredatory	Tetra Tech (1980)

## TABLE 7-11. ZOOPLANKTON MORTALITY RATES

Zooplankton Group	Mortality Rate (1/day)	Mortality Type	References
	0.0005 0.153**	nonpredatory	Leidy & Ploskey (1980)
	0.003 - 0.155**	nonpredatory	Collins & Wlosinski (1983
Rotifers	0.01	nonpredatory	Scavia <u>et al</u> . (1976)
	0.12	nonpredatory	Porcella <u>et al</u> . (1983)
Mysids	0.01	nonpredatory	Scavia <u>et al</u> . (1976)
	0.1	fish grazing	Scavia <u>et al</u> . (1976)
	0.08	fish grazing	Scavia (1980)
	0.01	nonpredatory	Tetra Tech (1980)

*Model documentation values.

**Literature values.

- Z = biomass or concentration of zooplankton group i, mass or mass/volume
- $n_{j}$  = total number of potential food items for predator group j
- F_{kj} = biomass or concentration of potential food item k consumed by predator group j, mass or mass/volume

The quantity  $(P_{ij} Z_i / \sum_{k=1}^{n_j} P_{kj} F_{kj})$  in Equation (7-43) represents the fraction of the total food consumption by predator group j which is provided by zooplankton group i. The quantity  $C_j X_j$  represents the total rate of food ingestion by predator group j. Ingestion rate formulations for carnivorous zooplankton were discussed in the previous section. Consumption rates for planktivorous fish are generally modeled in the same way. As discussed in the algae chapter, consumption rates are sometimes back-calculated from computed growth rates and known assimilation efficiencies using the equation:



FIGURE 7-6. Frequency histograms of zooplankton respiration rates (from Leidy and Ploskey, 1980).
$$C_{j} = \frac{g_{j}}{E_{j}}$$
(7-44)  
where  $C_{j}$  = total consumption rate for predator group j, 1/time  
 $g_{j}$  = growth rate for predator group j, 1/time  
 $E_{j}$  = assimilation efficiency for predator group j

When different assimilation efficiencies are used for different food items, consumption rates are generally calculated directly for each food item and combined with the food specific assimilation efficiencies to determine net growth (as discussed in Section 7.3.3).

### 7.6 SUMMARY

Zooplankton are typically modeled as a biomass pool using the same mass balance approach used for nutrients, phytoplankton, and other constituents.



NONPREDATORY MORTALITY RATE (1/day)

Figure 7-7. Frequency histogram of nonpredatory mortality rates for zooplankton (from Leidy and Ploskey, 1980).

The simplest models lump all zooplankton into a single group, while more complex models distinguish between different feeding types or different taxonomic groups.

Zooplankton dynamics depend on growth, reproduction, respiration, excretion, predation, and nonpredatory mortality. However, these processes are not generally measured in the field for a specific model application since: 1) many of them are difficult or impossible to measure directly; 2) the rates depend on environmental conditions (e.g., temperature), ecological conditions (e.g., food supply and predator densities), and the species composition of the zooplankton, all of which change continually with time; and 3) the fluxes depend largely on the zooplankton densities, which may vary by orders of magnitude over a seasonal cycle.

As a result, many of the model coefficients must be determined by model calibration rather than by measurement. Model constructs must be relied upon to describe the effects of different factors on these processes. Literature values from laboratory experiments are useful for establishing reasonable ranges of the process rates and coefficients. However, specific experimental results are difficult to apply directly since experiments typically use a single species rather than the species assemblages represented in models, and since experimental conditions may not represent conditions in the field.

Most models include formulations to describe the effects of temperature on all process rates. Food density effects on growth and consumption are typically modeled using saturation kinetics similar to those used for phytoplankton. Respiration and mortality rates are most commonly modeled as first-order losses, although a few models use more complicated formulations which include the effects of other factors, for example, crowding effects. Since few models include higher trophic levels such as fish, predatory mortality is typically treated in a simplistic manner.

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# CHAPTER 8

# COLIFORM BACTERIA

## 8.1 INTRODUCTION

Coliform concentrations in natural waters have been used as an indicator of potential pathogen contamination since at least the 1890's (Whipple, 1917). Until recently, coliforms have been considered to be less sensitive to environmental stresses than enteric pathogens. Accordingly, coliforms were believed to be more persistent in natural waters and, therefore, a "safe" or conservative index of potential pathogen levels.

However, recent evidence about enteric viruses, opportunistic pathogens, and pathogenic Escherichia coli have raised doubts that coliforms are the "ideal indicator" (Sobsey and Olson, 1983). First, enteric viruses appear to generally have both lower decay rates than coliforms and also a lower ID-50 (i.e., the dose required to infect 50 percent of the persons exposed) than most bacterial enteric pathogens. Second, opportunistic pathogens (e.g., <u>Pseudomonas aeruginosa</u>, <u>Aeromonas hydrophila</u>, and <u>Legionella pneumophila</u>) often have major non-fecal sources and are able to grow in natural waters. These pathogens generally have a high ID-50, threatening primarily immunologically compromised persons such as hospital patients who are being given immunological suppressants. Finally, some strains of <u>E</u>. coli produce an enteric toxin that results in gastroenteritis.

In the context of drinking water, Olivieri (1983) has recommended that different indicators be used when different aspects of pathogen behavior are of interest, e.g., indicator of feces, treatment efficiency, or post-treatment contamination. Chamberlin (1982) has compared coliform (combining Total Coliform, Fecal Coliform, and <u>E. coli</u>) decay rates with pathogen and

virus decay rates measured simultaneously and has found that the respective decay rates were highly correlated ( $r^2 = 0.73$ ) and that within-species variability was as great as pathogen-to-coliform variation (see Figure 8-1). At low decay rates, coliform decay rates were approximately equal to pathogen decay rates while at the highest decay rates, pathogen decay was slower.



COLIFORM DECAY RATE (1/HR)



In addition, epidemiological studies have revealed that enterococci levels are more closely associated with enteric disease than are coliforms (Cabelli <u>et al</u>. 1982). This work has in part motivated a proposed revision of the contact recreation bacterial water quality criteria: switching from fecal coliforms to <u>E</u>. <u>coli</u> and/or enterococci (U.S. Environmental Protection Agency, 1984).

Taken as a whole, these issues may serve to motivate modelers to include additional indicators as state variables and to use coliforms as <u>an</u> indicator rather than as the indicator.

### 8.2 COMPOSITION AND ASSAY

The coliform group consists of both fecal and non-fecal components. The fecal component includes mainly the <u>Escherichia</u> and <u>Klebsiella</u> genera while the non-fecal component includes mainly the <u>Enterobacter</u> and <u>Citrobacter</u> genera commonly associated with soils and plants (Dufour, 1977).

Neither the multiple tube (MPN) nor the membrane filter (MF) techniques for Total Coliforms (TC) effectively differentiates between the fecal and non-fecal components. The Fecal Coliform (FC) tests (either MPN or MF) provide a better differentiation at the cost of additional labor and time plus more exacting equipment requirements. The tests require either supplemental tests run on TC or incubation at elevated temperatures within precise limits (i.e.,  $44.5^{\circ}C \pm 0.2^{\circ}C$ ). These more stringent conditions eliminate most of the non-fecal component while still permitting the fecal component to survive. FC represents from 15 to 90 percent of the TC, depending on sample source. Unfortunately, there are major non-fecal sources of FC, most commonly of <u>Klebsiella</u> species (Hendry <u>et al</u>. 1982). Pulp mill wastewater provides a frequent example. Tests for <u>E. coli</u> are even more specific to fecal sources, but again incur further costs for labor and time.

The non-fecal components of the coliforms, especially the <u>Enterobacter</u> and <u>Citrobacter</u> genera, are of limited use in indicating fecal contamination but do indicate prior contact with soil or plant material. In addition, these genera are capable of regrowth in nutrient-rich natural waters or where surfaces are available for growth.

Fecal streptococci (FS) provide another common indicator of fecal contamination (Clausen et al. 1977). Although all FS belong to the single genus Streptococcus, there are again fecal and non-fecal components. Enterococci and S. faecalis are more specific to fecal sources than the nonenterococcal streptococci. FS and particularly the enterococci are often considered to be able to survive longer in natural waters than either TC or FC. Chamberlin (1982) compared FS (combining TC, FC, and E. coli results) decay rates in cases where the rates were measured in the same experiments and found a high correlation  $(r^2 = 0.80)$  between the logarithm of the respective rates. In addition, the relationship between the logarithms of the rates had a slope estimated by linear regression that was not significantly different (p = 0.05) from 1.0. The intercept was marginally distinguishable from 0.0 at p = 0.01 and was estimated as -0.31. This suggests that coliform decay rates were generally twice as large as FS decay rates but that the rates changed generally by equal amounts from one environment to another. According to Geldreich and Kenner (1969), the FC/FS ratio is useful in discriminating between recent human versus animal fecal contamination. If the ratio exceeds approximately 1 (although 4 is often cited as the cut-off value), the source is presumptively human fecal material while if the ratio is less than 1, the source is assumed to be animal feces. But as Dutka and Kwan (1980) have observed, the ratio can change dramatically once the material enters natural waters. They monitored changes from an initial ratio of 2.7 to a low of 0.07 and a high of 22.5 in a single experimental run.

Other proposed fecal indicators have been discussed by Olivieri (1983) and include <u>Clostridium perfringens</u>, yeasts, and RNA coliphages. None of these novel indicators has become generally accepted.

Beyond the selections of a particular indicator or set of indicators, recent work has shown the importance of sublethal stress or injury of influencing observed concentrations in decay studies (Rose <u>et al</u>. 1975; Bissonette <u>et al</u>. 1977). Rhodes and Kator (1982) and Kapuscinski and Mitchell (1981) have, among others, substantiated these results and have suggested particular mechanisms of injury. Consequently, the decision to use or not use a resuscitation step (e.g., incubation at  $35^{\circ}$ C in less selective medium for two hours) can have a major impact on the observed decay rates.

## 8.3 MODELING COLIFORMS

Modeling of coliforms is done for one main reason--establishing the level of fecal and/or soil pollution and potential pathogen contamination. The usual approach is simply to simulate disappearance and to estimate coliform levels as a function of initial loading and the disappearance rate which, in turn, is a function of time or distance of travel from the source and of environmental conditions such as temperatures, salinity, and light intensity.

# 8.3.1 Factors Affecting Disappearance Rates

Upon discharge to a water body, environmental conditions determine the extent to which coliform regrowth and death occur. Fecal coliforms and streptococci are occasionally observed to increase in numbers, although this may be due to disaggregation of clumps of organisms. Non-fecal organisms may, in fact, increase in numbers in natural waters where conditions are adequate (Lombardo, 1972; Mitchell and Chamberlin, 1978).

Factors can be conveniently classified into three categories: physical, physicochemical, and biochemical-biological. However, note that synergisms (e.g., osmotic effects and photo-oxidation) and interferences (e.g., sedimentation versus photo-oxidation) may exist. Kapuscinski and Mitchell (1980) and Bitton (1980) have reviewed factors that govern virus inactivation in natural waters and present essentially a parallel list to the one given below.

Physical factors that can affect the coliform population in natural waters, resulting in an apparent increase or decrease in the coliform disappearance rate include:

- Photo-oxidation
- Adsorption
- Flocculation
- Coagulation
- Sedimentation
- Temperature

Physicochemical factors include

- Osmotic effects
- pH
- Chemical toxicity
- Redox potential

Biochemical-biological factors include:

- Nutrient levels
- Presence of organic substances
- Predators
- Bacteriophages (viruses)
- Algae
- Presence of fecal matter

# 8.3.1.1 Physical Factors

Chamberlin and Mitchell (1978) have noted that, although many data have been collected on coliform disappearance rates, mechanisms mediating the rates have historically been poorly understood. According to Chamberlin and Mitchell, however, light is one of the most important factors. They observe that it is difficult to show statistically significant relationships between coliform disappearance rates and many factors usually hypothesized as influencing those rates. In contrast, significant relationships between light intensity and coliform disappearance rates can be demonstrated. Chamberlin and Mitchell (1978) have shown that field data statistically support the photo-oxidation model (to be discussed), and data presented by Wallis <u>et al</u>. (1977) also appear to implicate incident light. Subsequent work by Sieracki (1980), Kapuscinski and Mitchell (1983), Lantrip (1983), and others has demonstrated that viruses and enteric bacterial pathogens are also sensitive to light but that viruses are generally less sensitive than coliforms.

Chamberlin and Mitchell (1978) have elaborated upon possible mechanisms by which light may increase coliform disappearance rates. They point out that although in many cases of light induced mortality, one or more photosensitizing substances are involved, visible and near ultraviolet (UV) light can kill <u>E</u>. <u>coli</u> in the absence of exogenous photosensitizers. Grigsby and Calkins (1980) have confirmed the significance of the near UV.

One suggested mechanism is that light quanta drive some exogenous or endogenous chromophore to an electronically excited state. The chromophore, in the process of returning to the ground state, transfers its absorbed light energy to another substance to form superoxides  $\binom{n}{2}$ , which, in turn, cause damage to cellular components. Alternatively, the activated chromophore may cause damage directly, without the agency of a superoxygenated intermediate. Kapuscinski and Mitchell (1981) observed that injury to the catalase system is the most likely site of damage in <u>E</u>. <u>coli</u> and that the damage can be repaired if the coliforms are transferred to an appropriate recovery medium. Krinsky (1977) has, on the other hand, argued that the "cause of death" may be division-inhibition, mutation, and/or membrane damage.

Substances within coliform and other bacterial cells are effective, near-UV chromophores, including ubiquinones, porphyrins, and tryptophan (Krinsky 1977). Exogenous sources of photo-oxidants include algal pigments, lignins, and humic and fulvic acids. More highly colored and turbid waters have been shown to produce peroxides, singlet oxygen, and hydroxide radicals at greater rates than well waters (for example, Zepp <u>et al</u>. 1977; Cooper and Zika, 1983).

Adsorption, coagulation, and flocculation may affect coliform disappearance rates, although few quantitative data are available. Adsorption refers to the attachment of coliform organisms to suspended particles. Coagulation refers to the coalescence of bacteria into clumps, and flocculation refers to the formation of soft, loose aggregates incorporating much water.

According to Mitchell and Chamberlin (1978), early investigations by several workers have demonstrated that clays tend to adsorb coliforms more than do silts or sands. This is, of course, commonly the case with sorbed substances. As Mitchell and Chamberlin point out, the nature and stability of coliform aggregates incorporating other particulate matter depends to a very large extent upon the physicochemical nature of the particles. Gannon <u>et al</u>. (1983) found that 90 to 96 percent of the coliforms entering a lake from upland watersheds were associated with 0.45 to  $5 \,\mu$ m particles.

Sedimentation involves the settling out of bacterial particles and aggregates. The rate of disappearance may be materially influenced by aggregation and sedimentation, but the magnitude and direction of the change in rate is not well understood. The mechanism of apparent disappearance due to sedimentation is actually simple removal of cells from the water column--that is, transfer of matter from one physical compartment (the water column) to another (the benthos). However simple, sedimentation may sometimes be the predominant mechanism of removal as Gannon <u>et al.</u> (1983) demonstrated in a field study of coliform survival in a lake. Accordingly, modeling coliform disappearance in the water column may give misleading results, particularly where shellfish are harvested for human consumption. Reduction in coliform levels in the water column may simply mean increased numbers in the benthos.

Temperature influences most, if not all, of the the other factors. Bitton (1980) and Lantrip (1983) argue that temperature is the single most important modifier of decay rates, especially in freshwater and in the dark.

# 8.3.1.2 Physicochemical Factors

Mitchell and Chamberlin (1978) report that physicochemical factors may have significant effects on disappearance rates. Survival rates of <u>E</u>. <u>coli</u>, for example, are inversely proportional to salinity both in natural seawater (due to osmotic and other effects) and in artificial salt solutions. In addition, Sieracki (1980) has observed a synergism with light effects. Work by Zafiriou and True (1979) suggest that nitrite photolysis in seawater may be a partial cause. In general, <u>E. coli</u> have been found to survive longer in lower pH salt solutions (pH < 8) than under alkaline conditions.

Heavy metal toxicity toward microorganisms has been known since the late nineteenth century. A great number of studies have been done on the "oliogodynamic action" of silver and copper salts. According to Mitchell and Chamberlin (1978), heavy metals have been implicated as important mediators of <u>E</u>. <u>coli</u> disappearance rates, and the heavy metal effects may be reduced by addition of chelating agents. Redox potential, through its effect on heavy metals solubilities, also affects disappearance rates. In addition to this, redox may influence disappearance rates in other ways, although data on this are not extensive.

Finally, Kott (1982) has presented evidence that when coliforms undergo the transition from the generally low oxygen environment of sewage to the higher oxygen levels found in seawater, the oxygen shock promotes rapid decay.

# 8.3.1.3 Biochemical and Biological Factors

Nutrient concentrations may be important in determining disappearance rates under some conditions. In many nutrient studies, the apparent impact of nutrient addition to the coliform culture is due to chelation of heavy metal ions (Mitchell and Chamberlin, 1978). Thus, the apparent decrease in disappearance rate in many cases may not be due to the additional nutrient, but instead to reduce toxicity of the culture medium. Mitchell and Chamberlin (1978) cite the work of Jones (1964) who found that  $\underline{E}$ . coli would

not grow at  $37^{\circ}$ C in either filter-sterilized natural or synthetic seawater supplemented with glucose, ammonium chloride, and potassium phosphate. Inhibition could be reversed by autoclaving, by addition of very small amount of organic matter, or by addition of metal chelating or complexing agents. Jones demonstrated that two levels of toxic metals would produce the inhibitory effect, and concluded that the apparent influence on disappearance rates was due to naturally occurring trace heavy metals in solution. Furthermore, as Mitchell and Chamberlin (1978) note, other researchers have obtained experimental results implicating heavy metals, and their chelation upon addition of nutrients, in apparent changes in disappearance rates.

In some situations, it appears that nutrient levels influence disappearance rates in ways unrelated to toxic metals availability. Sayage and Hanes (1971) and Chamberlin (1977), for example, have reported growthlimiting effects of available BOD or organic matter. Recent work by Dutka and Kwan (1983) indicates that after-growth and long-term persistence is particularly sensitive to nutrient levels. Further, it is possible that the level of nutrients affects coliform predators, thereby influencing rates of grazing on coliforms. Mitchell and Chamberlin (1978) report that predators in natural waters may be significant in reducing coliform populations given high predator levels. They cite three groups of micro-organisms which may be importantly in seawater. These are cell wall-lytic marine bacteria, certain marine amoebae, and marine bacterial parasites similar to Bdellovibrio bacteriovorus. Experiments performed by a number of researchers have implicated predators in disappearance of coliforms in both fresh and seawater, although Lantrip (1983) did not observe a significant predator influence in chamber experiments using freshwater. Bacteriophages, on the other hand, are apparently of minor importance, despite their demonstrated presence in sea water. The relative insignificance of phages, according to Mitchell and Chamberlin (1978), stems from their ineffectiveness in killing E. coli where the bacterial cells are not actively growing and multiplying, and the rapid inactivation of the phages by seawater.

Some forms of phytoplankton produce antibacterial agents which are excreted into the water column. These substances are heat-liable macromolecules, and according to Mitchell and Chamberlin (1978) at least one, a chlorophyllide, is active only if the system is illuminated. The fact that at least one antibacterial agent is activated by light suggests that algae may play a mediating role in the effect of light on disappearance rates. Other mechanisms of algal anti-coliform activity have been suggested. One is that during algal blooms, other organisms which prey on both algae and coliforms may also increase in numbers.

Table 8-1 is a summary of factors influencing coliform disappearance rates.

# 8.3.2 Modeling Formulations

Traditionally, coliform modeling has only taken into account disappearance, and a simple first-order kinetics approach has been used (Baca and Arnett,1976; Chen, <u>et al</u>., 1975; Chen <u>et al</u>., 1976; U.S. Army Corps of Engineers,1974; Chen and Orlob, 1975; Lombardo, 1973; Lombardo, 1972; Smith, 1978; Anderson <u>et al</u>. 1976; Huber, <u>et al</u>. 1972; Hydroscience, 1971; Chen and Wells, 1975; Tetra Tech, 1976b):

$$\frac{dC}{dt} = -kC \tag{8-1}$$

or

$$C_t = C_0 e^{-kt}$$
(8-2)

where C = coliform concentration, MPN or count/100 ml  $C_0$  = initial coliform concentration, MPN or count/100 ml  $C_t$  = coliform concentration at time t, MPN or count/100 ml k = disappearance rate constant, day⁻¹ or hr⁻¹ t = exposure time, days or hours. A summarized listing of values for k is presented in Table 8-2. The data summarize 30 studies of rates measured <u>in situ</u>. Table 8-3 shows values for k from a number of modeling studies. The median rate for the <u>in situ</u> studies is .04  $hr^{-1}$  with 60 percent of the values less than .05  $hr^{-1}$  and 90 percent less than .22  $hr^{-1}$ .

THE CALL OF THE THE COLLEGE ON DISATERNANCE NAT	TABLE 8-1.	FACTORS	AFFECTING	COLIFORM	DISAPPEARANCE	RATES
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Factor	Effects
Sedimentation	Important with regard to water column coliform levels, particularly where untreated or primary sewage effluent or stormwater is involved, and under low vertical mixing conditions. May adversely affect shellfish beds by depositing coliforms and fecal matter into benthos.
Temperature	Probably the most generally influential factor modifying all other factors.
Adsorption, Coagulation, Flocculation	Inconclusive.
Solar Radiation	Important; high levels may cause more than 10-fold increase in disappearance rate over corresponding rate in the dark in seawater. Rates also materially increased in freshwater.
Nutrient Deficiencies	Appear to accelerate disappearance. Numerous studies have indicated that increasing nutrient levels of seawater decrease disappearance rates.
Predation	Several species of organisms (bacteria, amoebae) have been shown to attack and destroy <u>E. coli</u> . Importance of predation depends strongly on the concentration of predators.
Bacteriophages	Apparently not important.
Algae	Bactericidal substances are known to be produced by planktonic algae. Substances may be photoactivators, mediating the influence of light on coliform disappearance. This might account for variability of data in studies of light-induced disappearance rates. Another hypothesis is that algal predators with blooms concomitant with algal blooms may produce substances toxic to <u>E. coli</u> or may prey upon them.
Bacterial Toxins	Antibiotic substances produced by indigenous bacteria are not believed important in coliform disappearance.
Physiochemical Factors	Apparently, pH, heavy metals content, and the presence of organic chelating substances mediate coliform disappearance rates. Importance of each, however, is poorly understood at present. Salinity strongly enhances the effect of solar radiation.

A number of researchers have determined values for the half saturation constant ( $K_s$ ) for <u>E</u>. <u>coli</u> growth, using the Monod expression:

System	Temperature	k(1/hr)	Reference
Ohio River	Summer (20 ⁰ C) Winter (5 ⁰ C	0.049 0.045	Frost and Streeter (1924)
Upper Illinois River	June-September October and May December-March April and November	0.085 0.105 0.024 0.043	Hoskins <u>et al</u> . (1927)
Lower Illinois River	June-September October and May December-March April and November	0.085 0.037 0.026 0.029	Hoskins <u>et</u> <u>al</u> . (1927)
"Shallow Turbulent Stream"		0.63	Kittrell and Kochtitzky (1947)
Missouri River	Winter	0.020	Kittrell and Furfari (1963)
Tennessee River (Knoxville)	Summer	0.043	Kittrell and Furfari (1963)
Tennessee River (Chattanooga)	Summer	0.005	Kittrell and Furfari (1963)
Sacramento River	Summer	0.072	Kittrell and Furfari (1963)
Cumberland River	Summer	0.23	Kittrell and Furfari (1963)
Glatt River		1.1	Wasser et al. (1934)
Groundwater Stream	10 ⁰ C	0.021	Wuhrmann (1972)
Leaf River (Mississippi)		0.017	Mahloch (1974)
Wastewater Lagoon	7.9~25.5 ⁰ C	0.00833-0.029	Klock (1971)
Maturation Ponds		0.083	Marais (1974)
	19 ⁰ C	0.07	
Oxidation Ponds	"Т"	k = 0.108 $(1.19)^{T-20}$	Marais (1974)
Lake Michigan	10-17 ⁰ C	0.36	Zanoni et al. (1978)
Ford Lake (Ypsilanti, Michigan)	August	0.4	Gannon <u>et al</u> . (1983)
DeGray Reservoir	October 1976 (15 ⁰ C)	0.052	Thornton et al. (1980)
(Arkansas)	March 1977 (10 ⁰ C)	0.109 and 0.016	<u></u> <u></u> , (1990)
	June 1977 (20 ⁰ C)	0.138 and 0.114	

# TABLE 8-2.COLIFORM BACTERIA FRESHWATER DISAPPEARANCE RATES MEASUREDIN SITU (AFTER MITCHELL AND CHAMBERLIN, 1978)

Modified from Mitchell and Chamberlin (1978).

$$\mu = \frac{\mu_{\rm M}S}{K_{\rm s} + S} \tag{8-3}$$

where  $\mu$  = growth rate at nutrient concentrations, day⁻¹

- S = concentration of growth limiting nutrient, mg/l
- $\mu_{\rm M}$  = maximum growth rate, day⁻¹
- $K_s$  = half-saturation constant producing the half-maximal value of  $\mu$ , mg/l

Table 8-4 shows some reported values for  $K_s$ .

However, Gaudy <u>et al</u>. (1971) have shown that the Monod expression (Equation 8-3) is not adequate to describe transient coliform growth behavior. Accordingly, as suggested by Mitchell and Chamberlin (1978), the utility of the K_s value is in evaluating which nutrient may be growth limiting rather than in estimating a growth rate,  $\mu$ .

		an a
System	k @20 ⁰ C, 1/hr	Reference
North Fork Kings River, California	.042	Chen, <u>et al</u> . (1976)
Various Streams	.0004146	Baca and Arnett (1976)
Lake Ontario	.02083	U.S. Army Corps of Engineers (1974)
Lake Washington	.02	Chen and Orlob (1975)
Various Streams	.042125	Hydroscience (1971)
Boise River, Idaho	.02	Chen and Wells (1975)
San Francisco Bay Estuary	.02	Chen (1970)
Long Island Estuaries, New York	.02333	Tetra Tech (1976)

TABLE 8-3. VALUES FOR COLIFORM-SPECIFIC DISAPPEARANCE RATES USED IN SEVERAL MODELING STUDIES

Nutrient	Medium	т ос	K _s Micromoles	Remarks	Reference
Glucose	minimal medium		22.		Monod (1942)
			19.4 41.7		Moser (1958)
		30	405.		Schultz and Lipe (1964)
	seawater	30 20	550. 44		Jannasch (1968)
	Scawater	20			
Lactose	seawater	20	50.		Jannasch (1968)
	minimal medium		111.		Monod (1942)
<b>D</b> I I I			0.7		M I I I I I I I I I I I I I I I I I I I
Phosphate	minimal medium minimal medium	30	0.7 17.35	uptake study	Shehata and Marr (1970)
Glucose		30	0.378		Shehata and Marr (1971)

# TABLE 8-4. NUTRIENT K_s VALUES FOR <u>ESCHERICHIA</u> <u>COLI</u> (AFTER MITCHELL AND CHAMBERLIN, 1978)

Work on coliforms in the Ohio River by Frost and Streeter (1924) revealed that the log decay rate for coliforms is nonlinear with time. Accordingly, use of a simple decay expression such as Equation (8-1) with a single value of k is only an approximation to the actual disappearance process. Such an approach must, to some extent as a function of time, overestimate and/or underestimate dC/dt. One approach to solving the problem of a time-variable decay rate is to decompose the death curve into two components, each having its own decay rate (Velz, 1970). This approach is predicated upon typical death rate curves such as those shown in Figure 8-2. These curves have essentially two regions, each with its own characteristic slope, and the coliform concentration as a function of time may be defined as:

$$C_{t} = C_{o}e^{-kt} + C_{o}e^{-k't}$$
 (8-4)

Table 8-5 shows values for  $C_0$ ,  $C'_0$ , k, and k' for <u>E</u>. <u>coli</u> as estimated by Phelps (1944).

Lombardo (1972), in an effort to more meaningfully model coliforms, has formulated the dynamics of the coliform population plus streptococci with three separate first-order expressions:

$$C_{T_t} = C_{T_o} e^{-k_t t}$$
(8-5)

$$C_{F_t} = C_{F_o} e^{-k_f t}$$
(8-6)

$$C_{S_{t}} = C_{S_{0}} e^{-k_{s}t}$$
(8-7)



Figure 8-2. Typical mortality curves for coliforms as a function of time. Curve A is for cool weather while curve B represents warm weather decay (redrawn from Velz, 1970).

Parameter	Warm Weather	Cold Weather
C _o (percent)	99.51	97
k (1/day)	1.075	1.165
Half-life (day)	.64	.59
C <mark>'</mark> (percent)	.49	3.0
k' (1/day)	.1338	.0599
Half-life (day)	5.16	11.5

TABLE 8-5. VALUES OF Co, C', k, AND k' FROM THE OHIO RIVER PHELPS (1944)

where  $C_t$  = organism concentration at time t, MPN or count/100 ml  $C_c$  = organism concentration at time zero, MPN or count/100 ml

Table 8-6 provides data for  $k_{\rm T}^{},\ k_{\rm S}^{}$  and  $k_{\rm F}^{}$  as summarized from Lombardo (1972).

As discussed earlier, recent studies have suggested that incident light levels strongly affect coliform disappearance rates. Chamberlin and Mitchell (1978) have defined a light level-dependent disappearance rate coefficient as

$$k' = k_{\rho} \ell_{0} e^{-\alpha z} \qquad (8-8)$$

where k' = the light dependent coliform disappearance rate, 1/hr.  $k_{l}$  = proportionality constant for the specific organism, cm²/cal  $l_{o}$  = incident light energy at the surface, cal/cm²-hr  $\alpha$  = light attenuation coefficient per unit depth z = depth in units consistent with  $\alpha$ .

Indicator	n	Median k (1/hr)	Minimum k (1/hr)	Maximum k (1/hr)
тс	16	0.038	0.010	0.105
FC	13	0.048	0.008	0.130
FS	5	0.007	0.002	0.063

TABLE 8-6. SUMMARY OF DECAY RATES OF TC, FC, AND FS, REPORTED BY LOMBARDO (1972)

Then, incorporating the vertical dispersion of bacterial cells,

$$\frac{\partial C(z,t)}{\partial t} - V_z \frac{\partial C(z,t)}{\partial z} = E_z \frac{\partial^2 C(z,t)}{\partial z^2} - k'C(z,t)$$
(8-9)

where  $E_z$  = the vertical dispersion coefficient,  $cm^2/hr$  $V_z$  = the vertical settling velocity, cm/hr

An expression of this kind is useful where the vertical distribution of coliforms is nonuniform over depth and where disappearance is assumed to be solely a function of light intensity. Chamberlin (1977) has presented solutions of Equation 8-2 for various ranges of  $V_z$ ,  $E_z$ ,  $k_\ell$ ,  $\alpha$ , and H (depth of water column) using dimensionless variables.

According to an independent development by Mancini (1978) and Chamberlin and Mitchell (1978), if the bacterial cells can be assumed uniform over depth (i.e., the water column is vertically mixed), then the depth-averaged light intensity and the depth-averaged decay rate, respectively, may be computed:

$$\bar{\ell} = \ell_0 \left( \frac{1 - e^{-\alpha H}}{\alpha H} \right)$$
(8-10)

and

$$\bar{k} = k_{\ell} \bar{\ell}$$
 (8-11)

where  $\bar{\ell}$  = the depth-averaged light intensity, cal/cm²/hr

H = the depth of the water column in units consistent with  $\alpha$ 

 $\bar{k}$  = the depth-averaged light-dependent disappearance rate, hr⁻¹

The depth-averaged, light-dependent, disappearance rate,  $\bar{k}$ , may be used in the first order disappearance expression for a vertically mixed water body so that:

$$\frac{dC}{dt} = -\bar{k}C \qquad (8-12)$$

It is clear that the use of such a model (Equation (8-12)) might be further refined by computing  $\bar{k}$  using a sinusoidal function to estimate light levels and incorporating the influence of such factors as latitude, day of the year, time of day, and atmospheric conditions including cloud cover and dust effects. Table 8-7 presents some values for  $k_p$ .

Since coliforms and other indicators are known to decay in the dark, Mancini (1978) and Lantrip (1983) have developed decay rate models combining light-dependent and light-independent (i.e., dark) components. The model proposed by Mancini expresses k' as a function of temperature, percent seawater, and depth-averaged light intensity:

$$k' = \frac{(0.8 + 0.006(\% SW))}{24} 1.07^{T-20} + k \rho^{\bar{\ell}}$$
(8-13)

where  $T = water temperature in {}^{O}C.$ 

The model coefficients were estimated based on a combination of laboratory, chamber, and field studies. Note that  $k_{f}$  is not expressed as a function of either salinity or temperature.

Organism	Study	kg (cm²/cal)	Data Source
Coliform Group	14 field studies Mean 5′ percentile 95 percentile	0.481 0.163 1.25	Gameson and Gould (1975)
	24 field studies Mean 5 percentile 95 percentile	0.168 0.068 0.352	Foxworthy and Kneeling (1969)
	61 laboratory studies Mean 5 percentile 95 percentile	0.136 0.062 0.244	Gameson and Gould (1975)
	Estimated from diurnal field experiments in SW	0.18 at I = 1.0 cal/cm ² hr 0.07 at I = 0.1 cal/cm ² hr	Bellair <u>et al</u> . (1977)
Fecal Coliform	Estimated from compilation of field and laboratory studies, both SW and FW.	0.042	Mancini (1978)
Doth Sw and Fw. Total Coliforms 22 chamber studies in FW Mean Minimum Maximum		0.004 0.000 0.013	Lantrip (1982)
Fecal Coliforms	22 chamber studies in FW Mean Minimum Maximum	0.005 0.000 0.011	Lantrip 91982)
<u>Escherichia</u> <u>coli</u>	4 field studies Mean Minimum Maximum	0.362 0.321 0.385	Gameson and Gould (1975)
	4 laboratory studies Mean	0.354	Gameson and Gould (1975)
<u>Seratia</u> <u>marcescens</u>	4 field studies Mean Minimum Maximum	0.192 0.093 0.360	Gameson and Gould (1975)
Bacillus subtilis var. niger	1 laboratory study	0.002	Gameson and Gould (1975)
Fecal Streptococci	3 laboratory studies Minimum Maximum	0.048 0.123	Gameson and Gould (1975)
	3 field studies 1 field study	0.000 0.007	Gameson and Gould (1975)
	12 field studies, initial rates Mean Minimum Maximum	0.091 0.004 0.184	Foxworthy and Kneeling (1969)
	23 chamber studies in FW Mean Minimum Maximum	0.008 0.001 0.028	Lantrip (1982)
Salmonella <u>typhimurium</u>	2 laboratory studies	1.48 6.40	Eisenstark (1970)

# TABLE 8-7. COMPARISON OF $k_{f}$ ESTIMATES BASED ON CHAMBERLIN AND MITCHELL (1978) WITH ADDITIONAL VALUES

Lantrip (1983) developed a set of temperature and light-dependent models based on a series of chamber studies conducted in freshwater. Separate models were determined for TC, FC, and FS. He used nonlinear regression methods to determine the "best" coefficient values and reported both the "best" estimates and associated standard deviations. The three models have the same form:

$$k' = k_{d,20} \theta^{T-20} + k_{\ell} \bar{\ell}$$
(8-14)

where  $k_{d,20} = "dark"$  decay rate at 20⁰C (1/hr)

 $\theta$  = temperature correction term

The coefficients for the three models are summarized in Table 8-8. Note that Lantrip also considers  $k\rho$  to be independent of temperature.

Finally, many investigators have noted an initially very low decay rate in laboratory and field studies. For example, see Mitchell and Chamberlin (1978), Mancini (1978), and others. Kapuscinski and Mitchell (1983) and Severin <u>et al</u>. (1978) have argued that this "shoulder" in the decay curve is not the consequence of growth or particle breakup but is instead due to the nature of the photo-oxidation process. Severin <u>et al</u>. present two mechanistic models that would produce a "shoulder":

 Multi-target model based on assumption that several targets or sites in the organism must be hit before the organism will be killed:

$$C_{t} = C_{o} \left( 1 - \left[ (1 - e^{-k} \ell^{\cdot \ell \cdot t})^{j} \right] \right)$$
(8-15)

where j = number of critical sites,

• A series-event model that assumes that the same target must be hit a series of times before inactivation occurs:

$$C_{t} = C_{0} e^{-k \boldsymbol{\ell} \cdot \boldsymbol{\ell} \cdot t} \left( \sum_{i=0}^{n} \frac{(k_{\boldsymbol{\ell}} \cdot \boldsymbol{\ell} \cdot t)^{i}}{i!} \right)$$
(8-16)

where n = event threshold for inactivation

Such models are still novel in engineering applications and have not yet been incorporated into water quality models.

# 8.3.3 Methods of Measurement

Estimates of the coliform disappearance rate, k, may be obtained in a number of ways in the laboratory chamber studies, or, preferably, <u>in situ</u>. For laboratory estimates, samples of effluent may be taken along with samples of receiving water. Then, under controlled conditions of light, temperature, and dilution, the time rate of disappearance may be determined for various combinations of conditions. Unfortunately "bottle effects" often distort laboratory results as shown by Zanoni and Fleissner (1982),

]	Indicator	n	Standard Error Regression	^k d,20 (1/hr)	θ	k <b>ę</b> (cm ² /cal)
тс	Estimate	38	0.0151	0.0301	1.0893	0.0022
	Standard Error			0.0044	0.0208	0.00065
FC	Estimate	41	0.020	0.0305	1.0978	0.00377
	Standard Error			0.0057	0.0280	0.00081
FS	Estimate	38	0.0183	0.0294	1.0859	0.00502
	Standard Error			0.0050	0.0234	0.00076
		_				

TABLE 8-8. PARAMETER ESTIMATES FOR LANTRIP (1983) MULTI-FACTOR DECAY MODELS

since enteric bacterial growth is promoted by availability of surfaces for attachment.

In situ k values can be determined whether the flow regime is well defined or not, although there are inherent errors involved in each method. Where there are no flow regime data, or where flows are of a transient nature, a commonly used method (e.g., Zanoni et al. 1978 and Gannon et al. 1983 provide recent examples) is to add a slug of a conservative tracer substance (a dye, rare element, or radioisotope) to the steady-state discharge. Then the discharge plume is sampled, dilution is estimated from concentrations of tracer, and the dilution corrected coliform counts permit k to be estimated. It should be recognized that this technique may give misleading results where the dilution of the tracer is due to mixing with water heavily contaminated with the same discharge. Since the tracer had been introduced as a slug, there is no way to know how much of the surviving coliforms originated in the tracer-dosed effluent and how much came from pre-dosing or post-dosing effluent. However, where the flow regime is sufficiently predictable and stable to assure that dilution occurs essentially with ambient water, and where coliform levels in the ambient water are known, this should not be a problem.

Another method, which is particularly useful where discharge is to a channel, is as follows. First, a base sampling site is established below the discharge where the water column is fully mixed normal to the direction of flow. Then samples are taken at the base site and at several points downstream. Based upon known velocities and the change in coliform concentration with distance (time), k values may be estimated. Clearly, errors will be introduced to the extent that there is incomplete lateral mixing of the stream, nonuniform longitudinal velocities laterally and vertically across the channel, and unknown inflows causing dilution or introducing additional coliforms between sampling sites.

Also, sampling can be done so that the same "parcel" or water is sampled, in case the discharge is not at steady-state. For example, if the first sampling site is one mile below the base site, and the channel flow

has a mean velocity of 2 ft per second, then the first sampling site should be sampled:

$$\frac{5280 \text{ ft}}{\text{mile}} \times \frac{1 \text{ second}}{2 \text{ ft}} \times \frac{1 \text{ hr}}{3600 \text{ seconds}} = .73 \text{ hr}$$

or 44 minutes after sampling at the base site. Clearly, however, this does not account for dispersion, and the 44 minutes is an average figure corresponding to the peak loading. Where possible, dye studies or other techniques should be used to characterize stream dispersion at the sampling location. Then, by integrating under the curve, total surviving coliforms can be estimated. If, on the other hand, discharge and stream conditions are clearly at steady-state, sampling times are of no consequence.

Equation (8-17) may be used to estimate k where a slug dose of tracer has been introduced into the discharge (assuming first-order decay):

$$k = -\ln (C_{+}F_{0}/F_{+}C_{0})/t$$
 (8-17)

where  $F_0$  = discharge concentration of tracer, mg/l  $F_+$  = observed concentration of tracer, mg/l

If no tracer is used and conditions approximating plug flow exist, then:

$$k = -\ln(C_{+}/C_{0})/t$$
 (8-18)

where  $C_0 = \text{concentration of coliforms at the base sampling site, MPN}$ or count/100 ml

Regardless of the technique used for estimating k, it is important to concurrently quantify, to the extent possible, those variables which influence k. For example, light levels should be measured or at least estimated over the period for which k is estimated. If this is not done, and if the effects of the important parameters are not taken into account in modeling coliforms, serious errors will result. Table 8-9 shows how serious such errors can be. The data show T-90 values for coliforms as a function

Time of Day	T-90 (hours)	Time of Day	T-90 (hours)	Time of Day	T-90 (hours)
0100	40	0900	3.2	1700	5.3
0200	40	1000	2.5	1800	6.7
0300	40	1100	2.3	1900	8.5
0400	40	1200	2.5	2000	11
0500	40	1300	2.9	2100	14
0600	19	1400	3.3	2200	20
0700	8.0	1500	3.9	2300	27
0800	4.6	1600	4.6	2400	34

# TABLE 8-9. EXPERIMENTAL HOURLY T-90 VALUES (AFTER WALLIS, ET AL., 1977)

of incident light. T-90 values are the times required for 90 percent mortality. The associated k values are .058  $hr^{-1}$  in the dark and .1  $hr^{-1}$  at midday. It is clear that estimating a single value for a k could result in greater than order-of-magnitude errors.

# 8.4 SUMMARY

The coliform group is of interest as an index of potential pathogen contamination in surface waters and has become one of the more commonly modeled water quality parameters. Modeling coliforms usually involves the use of a simple first-order decay expression to describe disappearance. Since regrowth is generally neglected, no growth terms are normally included in the model.

The disappearance rate, k, is a function of a number of variables, the effects of all of which are not well understood. It now appears that light (in the near-UV and visible range) is important as are a number of

physicochemical factors. Rates of disappearance are also sensitive to the salinity of the water which also affects the influence of light on disappearance rates.

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